

## Tutorial-3

1.) linear search in sorted arr.

```
int idx = -1
```

```
for (i = 0; i < n; i++)
```

```
{
    if (arr[i] == search)
        idx = i; break;
}
```

```
if (arr[i] > search)
    break;
}
```

```
return idx;
```

2.) iterative insertion

```
int i, temp, j;
```

```
for (i = 1 to n)
{
```

```
    temp = arr[i];
```

```
    j = i - 1;
```

```
    while (j > 0 && arr[j] > temp)
        arr[j+1] = arr[j]; j--;
```

```
    arr[j+1] = temp;
}
```

Mukul Rawat



Date: / /

recursive :-

if ( $n \leq 1$ )  
return;

insertion - sort (arr,  $n-1$ )

last = arr[n-1]

j = n-2

while ( $j > 0$  &  $arr[j] > last$ )  
arr[j+1] = arr[j]; j--;

arr[j+1] = last

insertion sort is known as  
online sorting because values  
of whole array need not to  
be known at one time while  
executing information one by one  
linearly.

Muskan Kaur



3) Name.	time	space
Selection	$B \rightarrow O(n^2)$ $w \rightarrow O(n^2)$	$O(1)$
Bubble	$B \rightarrow O(n^2)$ $w \rightarrow O(n^2)$	$O(1)$
Insertion	$B \rightarrow O(n^2)$ $w \rightarrow O(n^2)$	$O(1)$
merge	$B, w \rightarrow O(n \lg n)$	$O(n)$
Quick	$B \rightarrow O(n \lg n)$ $w \rightarrow O(n^2)$	$O(n)$ ↓ recursion stack
Heap sort	$B \rightarrow O(n \lg n)$ $w \rightarrow O(n \lg n)$	$O(1)$
Count sort	$B, w \rightarrow O(n+k)$	$O(k)$
K: max element.		

Heap sort space complexity is  $O(1)$

because heap sort use tail recursion (which uses constant space).  $\therefore$  NO stack call will cause  $O(k \lg n)$  space.



Maul Kawan

Date: / /

4) Name	inplace	stable	online.
Selection	✓		
merge		✓	
Quick	✓		
Heap	✓		
Bubble	✓		
Count-		✓	
insertion	✓	✓	✓

5) iterative Binary Search

low = 0, high = n-1

while (low <= high)

int mid = (low + high) / 2

if (arr[mid] == element)

return element;

else if (arr[mid] > element)

high = mid - 1;

else

low = mid + 1

return -1



## 5.) Recursion Binary Search

if  $(l \leq r)$

int mid =  $(l + r) / 2$

if  $(arr[mid] == x)$   
return mid

else if  $(arr[mid] > x)$   
binary search  $(arr, l, mid - 1, x)$

else  
binary search  $(arr, mid + 1, r, x)$   
return -1;

Time complexity :- Best  $O(1)$   
Worst  $O(\log n)$

6.)  $T(n) = T(n/2) + 1$

7.) Algo 1

unordered set  $j = arr[0]$

1.) run loop for  $i = 1$  to  $n$

2.) if  $(element[i] \neq arr[i])$

return  $j \cdot end()$

else

$j \cdot insert(arr[i])$

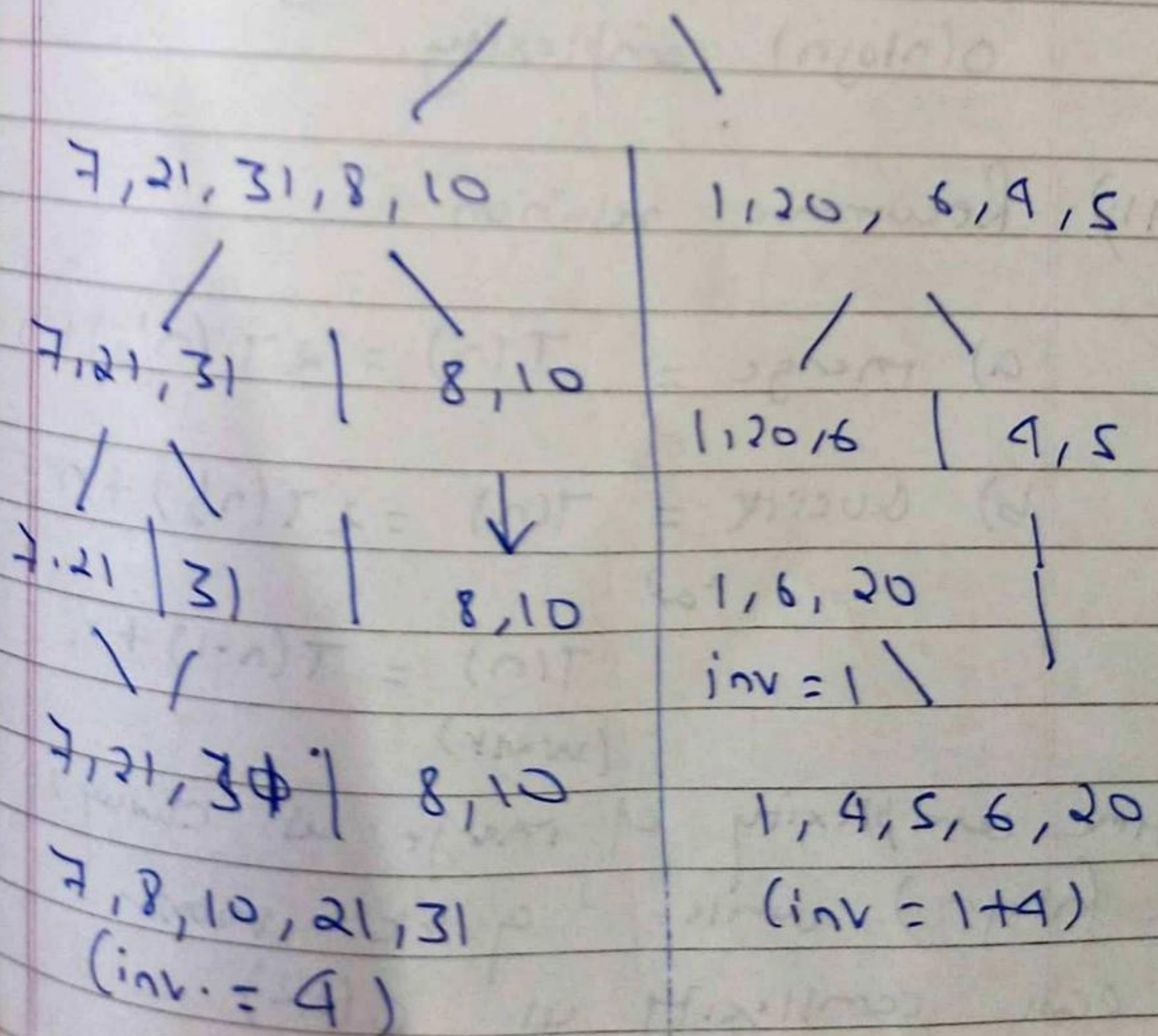


8) Quicksort is best for general purpose. Its stability is important & space is available then merge sort is best-

9) Inversion denote how far a array is from being sorted. If inversion is '0' array is sorted. Inversion is MAX if array is in descending order.

condition:- if  $i < j$ ,  $arr[i] > arr[j]$

$arr[] = \{ 7, 21, 31, 1, 10, 1, 20, 6, 4, 5 \}$





7, 8, 10, 21, 31

(inv = 4)

1, 4, 5, 6, 20

(inv = 5)

1, 4, 5, 6, 7, 8, 10, 20, 21, 31

$$\text{inv} = 4 + 5 + 3 \times 4 + 5 \times 2$$

$$= 4 + 5 + 12 + 10$$

$$= 31 \text{ inversions.}$$

==>

iv) When pivot is always on extreme quick sort will give  $O(n^2)$  time complexity.  
If pivot is always in middle it will give  $O(n \log n)$  complexity.

ii) Recurrence relation

a) Merge =  $T(n) = 2T(n/2) + n$

b) Quick =  $T(n) = 2T(n/2) + n$

$T(n) = T(n-1) + n$

(worst)

time complexity of merge is always  $O(n \log n)$  while quick worst case complexity is  $O(n^2)$



Maul Tawar

Date: / /

12) just change condition of  
getting minimum element to  
get stable selection sort  
if (arr[i] ≤ temp)  
min = i

to

if (arr[i] < temp)  
min = i;

13) bubble sort

for (i = 0; i < n-1; i++)

{  
is-sorted = false

for (j = i+1; j < n; j++)

{  
if (arr[j] > arr[j-1])  
swap(arr[j], arr[j-1])

is-sorted = false

if (is-sorted)  
break;

}