

Multiple-criteria decision analysis

```
In [1]: 1 from urllib import request
2 from bs4 import BeautifulSoup
3 import re
4 import statistics
5 import urllib
6 import numpy as np
7 import pandas as pd
8 import os
9 import matplotlib.pyplot as plt
10 import seaborn as sns
11 import time
12 import math
13 from tabula import read_pdf
14 from matplotlib.colors import ListedColormap
15 from IPython.display import set_matplotlib_formats
16 set_matplotlib_formats('png', 'pdf')
17 import networkx as nx
18 from tabulate import tabulate
19 from IPython.display import Image, display
20 from pymcdm import methods as mcdm_methods
21 from pymcdm import weights as mcdm_weights
22 from pymcdm import normalizations as norm
23 from pymcdm import correlations as corr
24 from pymcdm.helpers import rankdata, rrankdata
```

```
In [2]: 1 os.getcwd()
```

```
Out[2]: 'D:\\mcdm'
```

```
In [3]: 1 ls
```

Volume in drive D is Data
Volume Serial Number is 125B-8C1E

Directory of D:\mcdm

18-Sep-22	10:47 AM	<DIR>	.
25-Aug-22	07:16 PM	<DIR>	.ipynb_checkpoints
18-Sep-22	10:44 AM		821 am.txt
17-Sep-22	11:56 AM		10,370 final.xlsx
18-Sep-22	10:47 AM		803 final1
25-Aug-22	07:11 PM		99,738 matrix_image.jpeg
08-Sep-22	10:13 PM		1,360,338 mcdm_models - Jupyter Notebook.pdf
18-Sep-22	10:46 AM		385,709 mcdm_models.ipynb
28-Aug-22	04:41 PM		1,402 weights.csv
25-Aug-22	07:11 PM		66,825 weights_image.jpeg
		8 File(s)	1,926,006 bytes
		2 Dir(s)	988,194,381,824 bytes free

```
In [4]: 1 display(Image("matrix_image.jpeg"))
```

Table 1. Indicator Data Set

States	West Bengal	Maharashtra	Gujarat	Karnataka	Andhra Pradesh	Punjab	Uttar Pradesh	Rajasthan	Tamil Nadu
Growth Rate of Carbon Emissions	0.0741	-0.0053	0.0473	0.0156	0.0386	-0.04975	-0.0028	0.0789	0.0187
Carbon Emissions Intensity	0.0342	0.0196	0.0083	0.0142	0.0086	0.0193	0.0076	0.0102	0.0173
Per Capita Carbon Emissions	0.1974	0.0467	0.0442	0.0631	0.0493	0.0743	0.0365	0.0394	0.0693
Forest Area (Sq. Km.)	16,901.51	50,777.56	14,857.33	38,575.48	29,137.40	1,848.63	14,805.65	16,629.51	26,364.02
Forest Coverage	19.04%	16.50%	7.57%	20.11%	17.88%	3.67%	6.15%	4.86%	20.27%
Energy consumption per capita(KWh)	703	1424	2378	1396	1480	2046	606	1282	1866
Energy consumption intensity	0.0046	0.00061	0.15002	0.008671	0.02151	0.0105	0.00909	0.0104	0.0092
The proportion of renewable energy power generation	4%	14%	21%	49.60%	51%	15%	7%	43.50%	14.30%
Per capita GDP (in INR)	1,26,121	2,16,375	2,22,486	2,46,880	1,88,371	1,85,282	74,141	1,23,343	2,15,784
GDP Index	8%	9.26%	9.30%	9.50%	9.33%	4%	6.50%	8.38%	13.23%
Number of patents granted (patents filed in 2017-18)	538	3820	712	2022	276	247	721	189	2742
Investment in R&D per capita(in INR)	28.178	18.152	115.685	57.5276	61.872	186.451	21.306	24.968	84.802
Ownership of vehicles per capita	0.043	0.171	0.2883	0.22773	0.08973	0.324	0.101	0.1605	0.291

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description of the data set

```
In [5]: 1 df = pd.read_excel(r"D:\mcdm\final.xlsx")
```

```
In [6]: 1 df1 = pd.read_csv(r"D:\mcdm\weights.csv")
```

In [7]:

1 df1

Out[7]:

	INDICATORS	STATES	WEST BENGAL	MAHARASHTRA	GUJARAT	KARNATAKA	AND PRAD
0	A1	Growth rate of carbon emissions	5.0000	8.0000	14.0000	8.0000	7.
1	A2	Carbon emissions intensity	0.0342	0.0196	0.0083	0.0142	0.
2	A3	Per capita carbon emissions	0.1974	0.0467	0.0442	0.0631	0.
3	A4	Forest area(sq. km)	16901.5100	50777.5600	14875.3300	38575.4800	29137.
4	A5	Forest coverage rate	0.1904	0.1650	0.0757	0.2011	0.
5	A6	Energy consumptopn per capita(KWh)	703.0000	1424.0000	2378.0000	1396.0000	1480.
6	A7	Energy consumptioin intensity	0.0046	0.0006	0.1500	0.0087	0.
7	A8	The proportion of renewable energy power gener...	0.0400	0.1400	0.2100	0.4960	0.
8	A9	per capita GDP(in INR)	126121.0000	216375.0000	222486.0000	246880.0000	188371.
9	A10	GDP index	0.0800	0.0926	0.0930	0.0950	0.
10	A11	Number of patents granted(patents filled in 20...	538.0000	3820.0000	712.0000	2022.0000	276.
11	A12	Investment in R&D per capita(in INR)	28.1780	18.1520	115.6850	57.5276	61.
12	A13	Ownership of vehicles per capita	0.0430	0.1710	0.2883	0.2277	0.

```
In [10]: 1 df = df.T
2 df.drop(index=df.index[0],
3         axis=0,
4         inplace=True)
5 df
```

Out[10]:

	W.B	Mah	Guj	Kar	A.P.	Pun	U.P.	Rajasthan	T.N.
1	49.5	27.5	48.3	42.7	92.6	35	63.2	50.2	31.3
2	197.04	0.0467	0.0442	0.0631	0.0493	0.0743	0.0365	0.0394	0.0693
3	16,901.51	50,777.56	14857.33	38575.48	29137.40	1848.63	14,805.65	16629.51	26,364.02
4	19.04	16.5	7.57	20.19	17.88	3.67	6.15	4.86	20.27
5	703	1424	2378	1396	1480	2046	606	1282	1866
6	0.0046	0.00061	0.15002	0.008671	0.02151	0.0105	0.00909	0.0104	0.0092
7	12.33	32.73	44.75	65.57	39.78	33.66	15.92	60.65	52.11
8	121463	202130	213936	223175	168480	151491	65431	116492	213396
9	7.5	6.2	13.1	8.4	4.8	3.83	8.9	5.1	9.1
10	538	3820	712	2022	276	247	721	189	2742
11	278.41	221.77	789.52	373.48	543.49	551.44	471.02	192.56	688.34
12	31.9	50.45	44.45	41.12	39.13	37.5	22.3	24.9	42.54
13	31.3	62.6	72	70.2	49.8	97.5	56.6	74.6	70.4

```
In [11]: 1 df.shape
```

Out[11]: (13, 9)

```
In [12]: 1 weights = list(df1["subjective_weights"])
```

```
In [13]: 1 weights.insert(12,0.0358)
2 print(weights)
```

[0.0327, 0.0412, 0.0426, 0.0902, 0.0419, 0.0336, 0.040999999999999995, 0.0886, 0.0325, 0.0334, 0.1007, 0.0704, 0.0358, 0.0377]

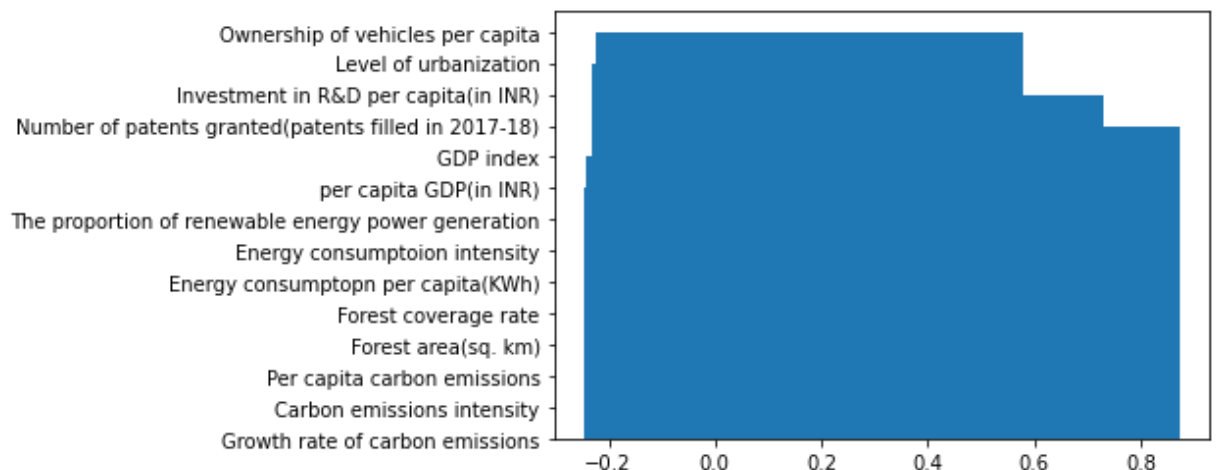
```
In [14]: 1 sum =0
2 for i in weights:
3     t = i**2
4     sum = sum + t
5 root = sum**0.5
6 for i in range(len(weights)):
7     weights[i] = weights[i]/root
8 print(weights)
9 subjective_weights = weights
```

```
[0.15397069032917832, 0.19399365264716045, 0.2005856699701222, 0.42471425895082
215, 0.1972896613086413, 0.1582084157510823, 0.1930519358867373, 0.417180524867
43723, 0.1530289735687552, 0.15726669899065918, 0.47415438887303535, 0.33148429
96689344, 0.16856730011573648, 0.17751360933975602]
```

```
In [15]: 1 states = list(df1["STATES"])
2 states.insert(12,"Level of urbanization")
3 print(states)
```

```
['Growth rate of carbon emissions', 'Carbon emissions intensity', 'Per capita c
arbon emissions', 'Forest area(sq. km)', 'Forest coverage rate', 'Energy consum
ptopn per capita(KWh)', 'Energy consumptoion intensity', 'The proportion of ren
ewable energy power generation', 'per capita GDP(in INR)', 'GDP index', 'Number
of patents granted(patents filled in 2017-18)', 'Investment in R&D per capita(i
n INR)', 'Level of urbanization', 'Ownership of vehicles per capita']
```

```
In [16]: 1 x = weights
2 y = states
3 plt.bar(x,y)
4 plt.show()
```



setting types based on the Criteria types profit = +1 and cost = -1

```
In [17]: 1 types = np.array([-1,-1,-1,+1,+1,-1,-1,+1,+1,+1,+1,+1,-1,-1])
```

```
In [42]: 1 df.to_csv("final1")
```

```
In [43]: 1 df = pd.read_csv("am.txt")
2 df
```

Out[43]:

	Unnamed: 0	W.B	Mah	Guj	Kar	A.P	Pun
0	0	5.0000	8.00000	14.00000	8.000000	7.00000	19.0000
1	1	49.5000	27.50000	48.30000	42.700000	92.60000	35.0000
2	2	197.0400	0.04670	0.04420	0.063100	0.04930	0.0743
3	3	16901.5100	50777.56000	14857.33000	38575.480000	29137.40000	1848.6300
4	4	19.0400	16.50000	7.57000	20.190000	17.88000	3.6700
5	5	703.0000	1424.00000	2378.00000	1396.000000	1480.00000	2046.0000
6	6	0.0046	0.00061	0.15002	0.008671	0.02151	0.0105
7	7	12.3300	32.73000	44.75000	65.570000	39.78000	33.6600
8	8	121463.0000	202130.00000	213936.00000	223175.000000	168480.00000	151491.0000
9	9	7.5000	6.20000	13.10000	8.400000	4.80000	3.8300
10	10	538.0000	3820.00000	712.00000	2022.000000	276.00000	247.0000
11	11	278.4100	221.77000	789.52000	373.480000	543.49000	551.4400
12	12	31.9000	50.45000	44.45000	41.120000	39.13000	37.5000
13	13	31.3000	62.60000	72.00000	70.200000	49.80000	97.5000

final matrix

```
In [44]: 1 matrix = df[df.columns[1:]].to_numpy()
2 matrix
3 matrix = matrix.astype(float)
```

```
In [45]: 1 matrix = matrix.T
```

```
In [46]: 1 df.columns
```

Out[46]: Index(['Unnamed: 0', 'W.B', 'Mah', 'Guj', 'Kar', 'A.P', 'Pun', 'U.P',
 'Rajasthan', 'T.N'],
 dtype='object')

normalization of the matrix

```
In [47]: 1 normalization_methods = [
2         norm.minmax_normalization,
3         norm.max_normalization,
4         norm.sum_normalization,
5         norm.vector_normalization,
6         norm.logarithmic_normalization
7     ]
8     norm_list = []
9     for method in normalization_methods:
10         nmatrix = norm.normalize_matrix(matrix, method, types)
11         norm_list.append(nmatrix)
```

```
In [54]: 1 norm_list[3]
```

```
Out[54]: array([[0.16874355, 0.04023754, 0.03053517, 0.08051594, 0.16427955,
0.19243148, 0.08829305, 0.01823154, 0.07888563, 0.10322581,
0.04763591, 0.04704491, 0.32862625],
[0.10546472, 0.0702104 , 0.12907158, 0.24189571, 0.14236411,
0.09499953, 0.67691338, 0.06381039, 0.13533732, 0.11948387,
0.33823269, 0.03030588, 0.08263701],
[0.06026556, 0.16579805, 0.136372 , 0.07086356, 0.06531493,
0.05688786, 0.00270765, 0.09571559, 0.1391596 , 0.12 ,
0.06304232, 0.19314324, 0.04901467],
[0.10546472, 0.09691013, 0.09552524, 0.18376707, 0.17351165,
0.09690496, 0.04668368, 0.2260711 , 0.15441745, 0.12258065,
0.17903311, 0.09604588, 0.06205941],
[0.12053111, 0.16001439, 0.12226456, 0.13880565, 0.15427092,
0.09140495, 0.01889061, 0.23245214, 0.11782149, 0.1203871 ,
0.02443775, 0.10329912, 0.15753544],
[0.14061963, 0.07130175, 0.08112574, 0.00880656, 0.03166523,
0.06611893, 0.03868076, 0.06836828, 0.1158894 , 0.0516129 ,
0.02426067, 0.31129145, 0.04361398],
[0.03835081, 0.18106892, 0.16514089, 0.07053161, 0.05176877,
0.22323322, 0.04463165, 0.0319052 , 0.0463734 , 0.08387097,
0.06383921, 0.03557168, 0.13991018],
[0.04963046, 0.1349141 , 0.15298585, 0.07922017, 0.0419327 ,
0.1055221 , 0.03905269, 0.198268 , 0.07714806, 0.10812903,
0.01673455, 0.04171567, 0.08804317],
[0.21092944, 0.07954473, 0.08697897, 0.12559373, 0.17489215,
0.07249696, 0.04414652, 0.06517776, 0.13496766, 0.17070968,
0.24278378, 0.14158217, 0.04855989]])
```

```
In [ ]: 1
```

Calculating the objective_weights using the standard deviation method

non normalized

```
In [48]: 1 objective_stdv0 = mcdm_weights.standard_deviation_weights(matrix)
2         objective_stdv0
```

```
Out[48]: array([9.20037475e-05, 2.76009274e-04, 9.18310800e-04, 2.05115756e-01,
9.97193508e-05, 8.11060856e-03, 6.60539213e-07, 2.56324038e-04,
7.63578231e-01, 3.98222591e-05, 1.82236223e-02, 2.90349276e-03,
1.28671117e-04, 2.56768145e-04])
```

norm.minmax_normalization,

norm.max_normalization,

norm.sum_normalization,

norm.vector_normalization,

norm.logarithmic_normalization

```
In [49]: 1 objective_stdv1 = mcdm_weights.standard_deviation_weights(norm_list[0])
2         objective_stdv1
```

```
Out[49]: array([0.07804365, 0.0647362 , 0.07117382, 0.06400853, 0.0917225 ,
0.06988666, 0.06750306, 0.07351159, 0.07391034, 0.06559197,
0.0766325 , 0.07426429, 0.06979225, 0.05922263])
```

```
In [50]: 1 objective_stdv2 = mcdm_weights.standard_deviation_weights(norm_list[1])
2         objective_stdv2
```

```
Out[50]: array([0.07950775, 0.05666819, 0.08860576, 0.0767987 , 0.0935303 ,
0.06484377, 0.08370976, 0.07432087, 0.0650481 , 0.0577938 ,
0.09069806, 0.06991724, 0.04848937, 0.05006834])
```

```
In [51]: 1 objective_stdv3 = mcdm_weights.standard_deviation_weights(norm_list[2])
2         objective_stdv3
```

```
Out[51]: array([0.07118403, 0.04152524, 0.05517877, 0.07529295, 0.06616019,
0.06204167, 0.22849562, 0.05524271, 0.03985939, 0.04584234,
0.12462011, 0.05442989, 0.03535316, 0.04477394])
```

```
In [52]: 1 objective_stdv4 = mcdm_weights.standard_deviation_weights(norm_list[3])
2         objective_stdv4
```

```
Out[52]: array([0.07184938, 0.05400845, 0.14319839, 0.07748235, 0.07019613,
0.05313678, 0.13253183, 0.06060421, 0.04549767, 0.05158571,
0.1064112 , 0.05985176, 0.03455021, 0.03909592])
```



```
In [53]: 1 objective_stdv5 = mcdm_weights.standard_deviation_weights(norm_list[4])
          2 objective_stdv5
```

```
Out[53]: array([0.02545093, 0.00925847, 0.1285619 , 0.07465679, 0.22163115,
                 0.00608004, 0.02945866, 0.12366206, 0.02582013, 0.15112951,
                 0.12627431, 0.06337073, 0.00725759, 0.00738774])
```

```
In [54]: 1 dict1 = {"non normalized":objective_stdv0,"minmax_normalization":objective_s
          2         "max_normalization":objective_stdv2,
          3         "sum_normalization":objective_stdv3,
          4         "vector_normalization":objective_stdv4,
          5         "logarithmic_normalization":objective_stdv5}
          6 stdv_df = pd.DataFrame(dict1)
```

objective weights for standard deviation

In [55]:

```
1 stdv_df
```

Out[55]:

	non normalized	minmax_normalization	max_normalization	sum_normalization	vector_normalization
0	9.200375e-05	0.078044	0.079508	0.071184	0.071849
1	2.760093e-04	0.064736	0.056668	0.041525	0.054008
2	9.183108e-04	0.071174	0.088606	0.055179	0.143198
3	2.051158e-01	0.064009	0.076799	0.075293	0.077482
4	9.971935e-05	0.091723	0.093530	0.066160	0.070196
5	8.110609e-03	0.069887	0.064844	0.062042	0.053137
6	6.605392e-07	0.067503	0.083710	0.228496	0.132532
7	2.563240e-04	0.073512	0.074321	0.055243	0.060604
8	7.635782e-01	0.073910	0.065048	0.039859	0.045498
9	3.982226e-05	0.065592	0.057794	0.045842	0.051586
10	1.822362e-02	0.076632	0.090698	0.124620	0.106411
11	2.903493e-03	0.074264	0.069917	0.054430	0.059852
12	1.286711e-04	0.069792	0.048489	0.035353	0.034550
13	2.567681e-04	0.059223	0.050068	0.044774	0.039096

In [57]:

```
1 for i in stdv_df:  
2     stdv_df[i] = (stdv_df[i]+weights)/2
```

In [58]:

```
1 stdv_df
```

Out[58]:

	non normalized	minmax_normalization	max_normalization	sum_normalization	vector_normalization
0	0.077031	0.116007	0.116739	0.112577	0.112910
1	0.097135	0.129365	0.125331	0.117759	0.124001
2	0.100752	0.135880	0.144596	0.127882	0.171892
3	0.314915	0.244361	0.250756	0.250004	0.251098
4	0.098695	0.144506	0.145410	0.131725	0.133743
5	0.083160	0.114048	0.111526	0.110125	0.105673
6	0.096526	0.130277	0.138381	0.210774	0.162792
7	0.208718	0.245346	0.245751	0.236212	0.238892
8	0.458304	0.113470	0.109039	0.096444	0.099263
9	0.078653	0.111429	0.107530	0.101555	0.104426
10	0.246189	0.275393	0.282426	0.299387	0.290283
11	0.167194	0.202874	0.200701	0.192957	0.195668
12	0.084348	0.119180	0.108528	0.101960	0.101559
13	0.088885	0.118368	0.113791	0.111144	0.108305

Calculating the objective_weights using the entropy method

In [59]:

```
1 h = 1/math.log(9)
2 h
```

Out[59]: 0.45511961331341866

non normalized

In [60]:

```
1 objective_entropy0 = mcdm_weights.entropy_weights(matrix)
```

In [61]:

```
1 objective_entropy0
```

Out[61]: array([0.03171869, 0.01453517, 0.47765957, 0.04123877, 0.03312549,
0.01624145, 0.20522134, 0.02281071, 0.01191184, 0.01391356,
0.09639667, 0.02073328, 0.0062934 , 0.00820006])

normalization - minmax normalization

```
In [62]: 1 objective_entropy1 = mcdm_weights.entropy_weights(norm_list[0])
```

```
In [63]: 1 objective_entropy1
```

```
Out[63]: array([0.07142857, 0.07142857, 0.07142857, 0.07142857, 0.07142857,
                0.07142857, 0.07142857, 0.07142857, 0.07142857, 0.07142857,
                0.07142857, 0.07142857, 0.07142857])
```

normalization - max normalization

```
In [64]: 1 objective_entropy2 = mcdm_weights.entropy_weights(norm_list[1])
```

```
In [65]: 1 objective_entropy2
```

```
Out[65]: array([0.13336501, 0.13336501, 0.13336501, 0.01141092, 0.00916595,
                0.13336501, 0.13336501, 0.00631181, 0.00329605, 0.00384993,
                0.02667331, 0.00573698, 0.13336501, 0.13336501])
```

normalization - sum normalization

```
In [66]: 1 objective_entropy3 = mcdm_weights.entropy_weights(norm_list[2])
```

```
In [67]: 1 objective_entropy3
```

```
Out[67]: array([0.0587459 , 0.02095732, 0.05648031, 0.0725612 , 0.05828558,
                0.04116053, 0.36508986, 0.04013633, 0.02095935, 0.02448144,
                0.16961365, 0.03648101, 0.01401327, 0.02103425])
```

normalization - vector_normalization

```
In [68]: 1 objective_entropy4 = mcdm_weights.entropy_weights(norm_list[3])
```

```
In [69]: 1 objective_entropy4
```

```
Out[69]: array([0.0187327 , 0.01163798, 0.08480304, 0.13535804, 0.10872783,
                0.01043164, 0.07594827, 0.07487162, 0.03909826, 0.04566848,
                0.31640288, 0.06805287, 0.00448869, 0.0057777 ])
```

normalization - logarithmic normalization

```
In [70]: 1 objective_entropy5 = mcdm_weights.entropy_weights(norm_list[4])
```

```
In [71]: 1 objective_entropy5
```

```
Out[71]: array([4.81887842e-03, 6.39081017e-04, 1.10041907e-01, 4.36840910e-02,
                3.88220231e-01, 2.74670809e-04, 6.46511519e-03, 1.19636151e-01,
                5.01987815e-03, 1.72297665e-01, 1.17932624e-01, 3.01734670e-02,
                3.91210219e-04, 4.05030274e-04])
```

```
In [72]: 1 dict2 = {"non normalized":objective_entropy0,"minmax_normalization":objectiv
2           "max_normalization":objective_entropy2,
3           "sum_normalization":objective_entropy3,
4           "vector_normalization":objective_entropy4,
5           "logarithmic_normalization":objective_entropy5}
6 entropy_df = pd.DataFrame(dict2)
```

objective weights for entropy

```
In [73]: 1 entropy_df
```

```
Out[73]:
```

	non normalized	minmax_normalization	max_normalization	sum_normalization	vector_normalization
0	0.031719	0.071429	0.133365	0.058746	0.018733
1	0.014535	0.071429	0.133365	0.020957	0.011638
2	0.477660	0.071429	0.133365	0.056480	0.084803
3	0.041239	0.071429	0.011411	0.072561	0.135358
4	0.033125	0.071429	0.009166	0.058286	0.108728
5	0.016241	0.071429	0.133365	0.041161	0.010432
6	0.205221	0.071429	0.133365	0.365090	0.075948
7	0.022811	0.071429	0.006312	0.040136	0.074872
8	0.011912	0.071429	0.003296	0.020959	0.039098
9	0.013914	0.071429	0.003850	0.024481	0.045668
10	0.096397	0.071429	0.026673	0.169614	0.316403
11	0.020733	0.071429	0.005737	0.036481	0.068053
12	0.006293	0.071429	0.133365	0.014013	0.004489
13	0.008200	0.071429	0.133365	0.021034	0.005778

```
In [75]: 1 for i in entropy_df:
2         entropy_df[i] = (entropy_df[i]+weights)/2
```

combined weights using entropy

```
In [76]: 1 entropy_df
```

Out[76]:

	non normalized	minmax_normalization	max_normalization	sum_normalization	vector_normalization
0	0.092845	0.112700	0.143668	0.106358	0.086352
1	0.104264	0.132711	0.163679	0.107475	0.102816
2	0.339123	0.136007	0.166975	0.128533	0.142694
3	0.232977	0.248071	0.218063	0.248638	0.280036
4	0.115208	0.134359	0.103228	0.127788	0.153009
5	0.087225	0.114818	0.145787	0.099684	0.084320
6	0.199137	0.132240	0.163208	0.279071	0.134500
7	0.219996	0.244305	0.211746	0.228658	0.246026
8	0.082470	0.112229	0.078163	0.086994	0.096064
9	0.085590	0.114348	0.080558	0.090874	0.101468
10	0.285276	0.272791	0.250414	0.321884	0.395279
11	0.176109	0.201456	0.168611	0.183983	0.199769
12	0.087430	0.119998	0.150966	0.091290	0.086528
13	0.092857	0.124471	0.155439	0.099274	0.091646

```
In [77]: 1 print(dir(mcdm_weights))
```

```
['__all__', '__builtins__', '__cached__', '__doc__', '__file__', '__loader__',  
'__name__', '__package__', '__spec__', '_fake_normalization', 'angle_weights',  
'cilos_weights', 'correlation_matrix', 'critic_weights', 'entropy_weights', 'eq  
ual_weights', 'gini_weights', 'idocriw_weights', 'linear_normalization', 'merek  
_weights', 'minmax_normalization', 'normalize_matrix', 'np', 'null_space', 'pea  
rson', 'standard_deviation_weights', 'sum_normalization']
```

Topsis method

```
In [93]: 1 col = list(df.columns)  
2 col.remove('Unnamed: 0')
```

```
In [94]: 1 topsis = mcdm_methods.TOPSIS()
```

```
In [95]: 1 topsis_methods = {
2         'minmax': mcdm_methods.TOPSIS(norm.minmax_normalization),
3         'max': mcdm_methods.TOPSIS(norm.max_normalization),
4         'sum': mcdm_methods.TOPSIS(norm.sum_normalization),
5         'vector': mcdm_methods.TOPSIS(norm.vector_normalization),
6         'log': mcdm_methods.TOPSIS(norm.logarithmic_normalization),
7     }
```

```
In [96]: 1 results = {}
2     for name, function in topsis_methods.items():
3         results[name] = function(matrix, vec, types)
```

```
In [97]: 1 print(tabulate([[name, *np.round(pref, 2)] for name, pref in results.items()
2                  headers=['Method'] + [f'A{i+1}' for i in range(10)]]))
```

Method	A1	A2	A3	A4	A5	A6	A7	A8	A9
minmax	0.36	0.64	0.45	0.65	0.45	0.34	0.37	0.41	0.68
max	0.34	0.69	0.42	0.66	0.45	0.33	0.36	0.4	0.68
sum	0.22	0.78	0.27	0.46	0.27	0.16	0.23	0.24	0.5
vector	0.34	0.76	0.41	0.67	0.46	0.39	0.43	0.43	0.71
log	0.47	0.67	0.55	0.73	0.48	0.27	0.39	0.4	0.75

```
In [98]: 1 top = tabulate([[name, *rankdata(pref, reverse=True)] for name, pref in resu
2                  headers=['Method'] + [f'A{i+1}' for i in range(10)]])
```

```
In [99]: 1 print(col)

['W.B', 'Mah', 'Guj', 'Kar', 'A.P', 'Pun', 'U.P', 'Rajasthan', 'T.N']
```

```
In [100]: 1 norm_list.insert(0,matrix)
```

```
In [101]: 1 entropy_df["subjective"] = weights
```

```
In [102]: 1 vec = np.array(list((entropy_df["vector_normalization"]+entropy_df["subjecti
```

```
In [103]: 1 m = topsis(matrix, vec, types)
```

```
In [104]: 1 m = list(m)
```

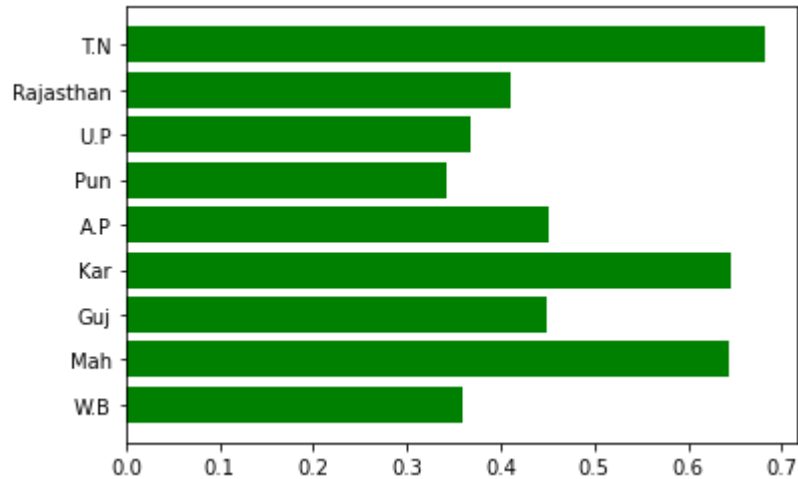
```
In [105]: 1 print(m)

[0.3586792108010278, 0.6429005650492241, 0.4486186695657274, 0.645737141353914
4, 0.4509100770400232, 0.342261727379166, 0.3674053780781845, 0.410971179132432
36, 0.6818350055960277]
```

```
In [106]: 1 print(col)
```

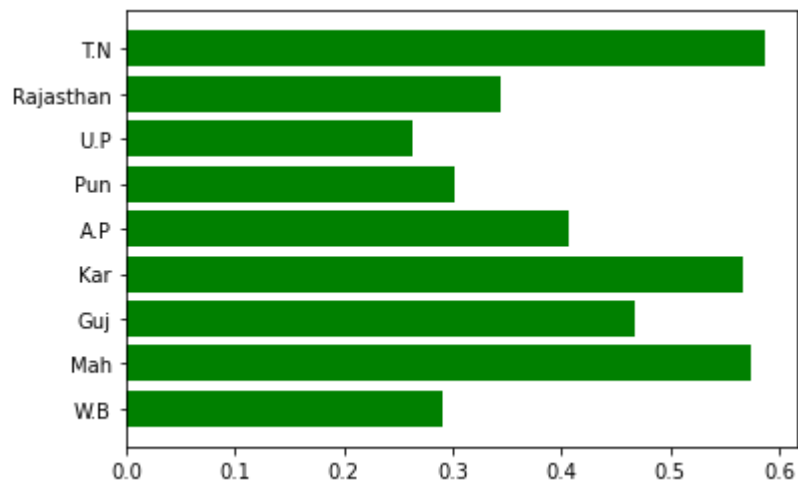
```
['W.B', 'Mah', 'Guj', 'Kar', 'A.P', 'Pun', 'U.P', 'Rajasthan', 'T.N']
```

```
In [107]: 1 plt.barh(col,m, color ='green')  
2 plt.show()
```



```
In [108]: 1 g = list(topsis(norm_list[3],vec, types))
```

```
In [109]: 1 plt.barh(col,g, color ='green')  
2 plt.show()
```



```
In [110]: 1 vikor = mcdm_methods.VIKOR()  
2 v = vikor(matrix, vec, types)
```



```
In [111]: 1 vikor_methods = {
2         'VIKOR': mcdm_methods.VIKOR(),
3         'minmax': mcdm_methods.VIKOR(norm.minmax_normalization),
4         'max': mcdm_methods.VIKOR(norm.max_normalization),
5         'sum': mcdm_methods.VIKOR(norm.sum_normalization),
6         'vector': mcdm_methods.VIKOR(norm.vector_normalization),
7         'log': mcdm_methods.VIKOR(norm.logarithmic_normalization),
8     }
```

```
In [112]: 1 results = {}
2     for name, function in vikor_methods.items():
3         results[name] = function(matrix, vec, types)
```

```
In [113]: 1 print(tabulate([[name, *np.round(pref, 2)] for name, pref in results.items()
2                 headers=['Method'] + [f'A{i+1}' for i in range(10)]]))
```

Method	A1	A2	A3	A4	A5	A6	A7	A8	A9
VIKOR	0.82	0.2	0.7	0.11	0.76	0.99	0.79	0.89	0
minmax	0.82	0.2	0.7	0.11	0.76	0.99	0.79	0.89	0
max	0.82	0.2	0.7	0.11	0.76	0.99	0.79	0.89	0
sum	0.79	0.15	0.64	0.16	0.77	0.99	0.75	0.89	0.02
vector	0.82	0.2	0.7	0.11	0.76	0.99	0.79	0.89	0
log	0.53	0.3	0.33	0.06	0.65	0.93	0.55	0.9	0

```
In [114]: 1 copras = mcdm_methods.COPRAS()
2     cop = copras(matrix, vec, types)
```

ranks by vikor method

```
In [115]: 1 print(tabulate([[name, *rankdata(pref)] for name, pref in results.items()],
2                 headers=['Method'] + [f'A{i+1}' for i in range(10)]]))
```

Method	A1	A2	A3	A4	A5	A6	A7	A8	A9
VIKOR	7	3	4	2	5	9	6	8	1
minmax	7	3	4	2	5	9	6	8	1
max	7	3	4	2	5	9	6	8	1
sum	7	2	4	3	6	9	5	8	1
vector	7	3	4	2	5	9	6	8	1
log	5	3	4	2	7	9	6	8	1

```
In [116]: 1 print(col)
```

```
['W.B', 'Mah', 'Guj', 'Kar', 'A.P', 'Pun', 'U.P', 'Rajasthan', 'T.N']
```

ranks by topsis method

In [117]: 1 print(top)

Method	A1	A2	A3	A4	A5	A6	A7	A8	A9
minmax	8	3	5	2	4	9	7	6	1
max	8	1	5	3	4	9	7	6	2
sum	8	1	4	3	5	9	7	6	2
vector	9	1	7	3	4	8	6	5	2
log	6	3	4	2	5	9	8	7	1

In [118]: 1 print(col)

['W.B', 'Mah', 'Guj', 'Kar', 'A.P', 'Pun', 'U.P', 'Rajasthan', 'T.N']

ranks by corpus method

In [119]: 1 print(tabulate([['Preference', *np.round(cop, 2)],
2 ['Rank', *rrankdata(cop)]],
3 headers=[''] + [f'A{i+1}' for i in range(10)]))

	A1	A2	A3	A4	A5	A6	A7	A8	A9
Preference	0.37	1	0.52	0.88	0.59	0.43	0.53	0.52	0.93
Rank	9	1	7	3	4	8	5	6	2

In []: 1

In []: 1