

ASSIGNMENT-3

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Exercise 16.3

17) A and B are events such that $P(A) = 0.42$, $P(B) = 0.48$ and $P(A \text{ and } B) = 0.16$. Determine

- (i) $P(\text{not } A)$
- (ii) $P(\text{not } B)$
- (iii) $P(A \text{ or } B)$

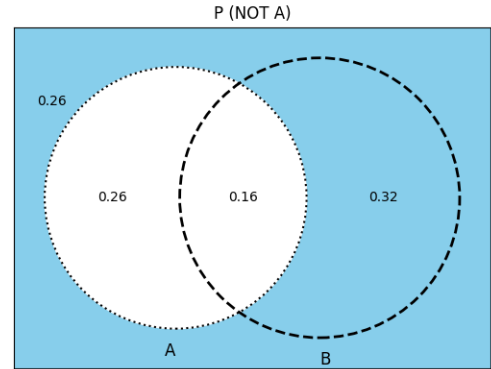


Figure 1: $P(\text{not } A)$

Solution

There are two discrete groups A,B.let Y be discrete random variable such that

$$Y = \begin{cases} 1, & \text{if A is chosen} \\ 2, & \text{if B is chosen} \end{cases}$$

(i) Determine $p(\text{not } A)$

Given $P(A) = 0.42$ so we have $P(X = 1) = 0.42$

$$\begin{aligned} P(A^c) &= 1 - P(X = 1) \\ &= 1 - 0.42 \\ &= 0.58 \end{aligned}$$

$$\therefore P(\text{not } A) = 0.58 \quad (1)$$

(ii) Determine $p(\text{not } B)$

Given $P(B) = 0.48$ so we have $P(X = 2) = 0.48$

$$\begin{aligned} P(B^c) &= 1 - P(X = 2) \\ &= 1 - 0.48 \\ &= 0.52 \end{aligned}$$

$$\therefore P(\text{not } B) = 0.52 \quad (2)$$

Verification

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Enter the value of P(A) =0.42
Enter the value of P(B) =0.48
Enter the value of p(A and B) =0.16
P(NOT A) = 0.58
P(NOT B) = 0.52
P(A OR B) = 0.74
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python code

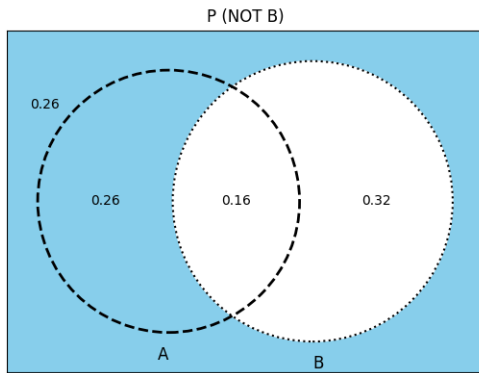


Figure 2: $P(\text{not } B)$

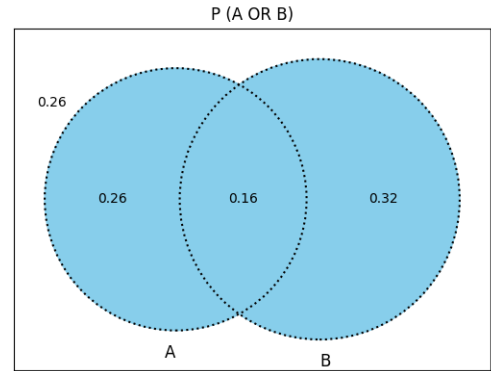


Figure 3: $P(A \cup B)$

(iii) Determine $p(A \text{ or } B)$

Given $P(A \cap B) = 0.16$, $P(A) = 0.42$
 $P(B) = 0.48$ so we have

$$P\left(\bigcap_{i=1}^2 (X = i)\right) = 0.16$$

$$\begin{aligned} P\left(\bigcup_{i=1}^2 (X = i)\right) &= P(X = 1) + P(X = 2) \\ &\quad - P\left(\bigcap_{i=1}^2 (X = i)\right) \\ &= 0.42 + 0.48 - 0.16 \\ &= 0.74 \end{aligned}$$

$$\therefore P(A \text{ or } B) = 0.74 \quad (3)$$