Linear Regression

import library

```
In [ ]:
```

```
import numpy as np
import matplotlib.image as img
import matplotlib.pyplot as plt
import matplotlib.colors as colors
from mpl_toolkits.mplot3d import Axes3D
```

load point data for training and testing

```
In [ ]:
```

```
data type of x = float64
data type of y = float64
data type of z = float64
```

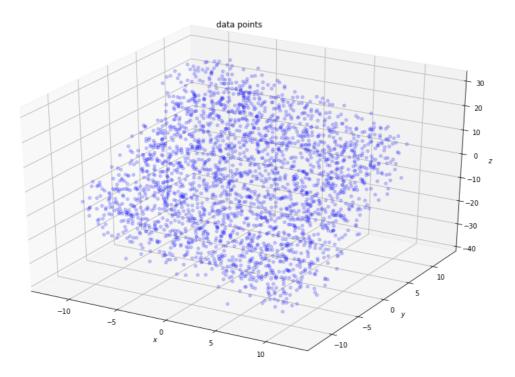
plot the data in the three dimensional space

In []:

```
fig = plt.figure(figsize=(12, 8))
ax1 = plt.subplot(111, projection='3d')

ax1.set_xlabel('$x$')
ax1.set_ylabel('$y$')
ax1.set_zlabel('$z$')
ax1.scatter(x, y, z, marker='o', color='blue', alpha=0.2)

plt.title('data points')
plt.tight_layout()
plt.show()
```



compute the prediction function

```
• 	heta=(	heta_0,	heta_1,	heta_2)\in\mathbb{R}^3
```

• $x,y\in\mathbb{R}$

compute the loss function

```
• 	heta=(	heta_0,	heta_1,	heta_2)\in\mathbb{R}^3
• x,y,z\in\mathbb{R}
```

In []:

• useful functions: np.inner

In []:

compute the gradient for the model parameters heta

• useful functions: np.matmul

In []:

gradient descent for the optimization

```
In [ ]:
```

```
number_iteration
               = 1000
learning_rate
               = 0.01
theta
            = np.array((0, 0, 0))
theta_iteration = np.zeros((number_iteration, len(theta)))
loss_iteration = np.zeros(number_iteration)
for i in range(number_iteration):
   # complete the blanks
   theta
         = theta - learning_rate * compute_gradient(theta, x, y, z)
         = compute_loss(theta, x, y, z)
   loss
   theta_iteration[i, :] = theta
   loss_iteration[i]
                      = loss
```

functions for presenting the results

In []:

```
def function_result_01():
    plt.figure(figsize=(8,6))
    plt.title('loss')

plt.plot(loss_iteration, '-', color='red')
    plt.xlabel('iteration')
    plt.ylabel('loss')

plt.tight_layout()
    plt.show()
```

In []:

```
def function_result_02():
    plt.figure(figsize=(8,6))
    plt.title('model parameters')

plt.plot(theta_iteration[:, 0], '-', color='red', label=r'$\theta_0$')
    plt.plot(theta_iteration[:, 1], '-', color='green', label=r'$\theta_1$')
    plt.plot(theta_iteration[:, 2], '-', color='blue', label=r'$\theta_2$')

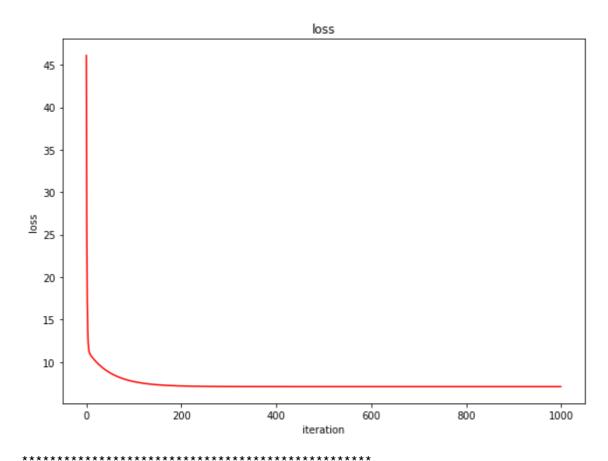
plt.xlabel('iteration')
    plt.ylabel('model parameter')
    plt.legend()

plt.tight_layout()
    plt.show()
```

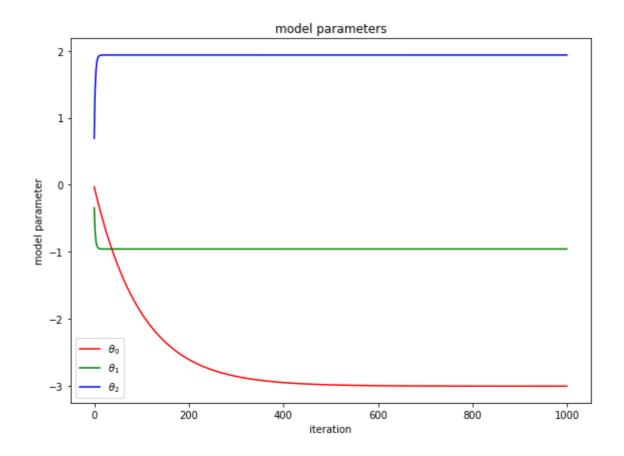
```
def function_result_03():
   xx = np.arange(-10, 10, 0.1)
   yy = np.arange(-10, 10, 0.1)
    (grid_x, grid_y) = np.meshgrid(xx,yy)
    zz = theta[0] + theta[1] * grid_x + theta[2] * grid_y
   fig = plt.figure(figsize=(8,8))
    ax = fig.add_subplot(111, projection='3d')
   plt.title('regression surface')
    ax = plt.axes(projection='3d')
    ax.set_xlabel(r'$x$')
    ax.set_ylabel(r'$y$')
    ax.set_zlabel(r'$z$')
    ax.plot_surface(grid_x, grid_y, zz, rstride=1, cstride=1, cmap='viridis', edgecolor='none'
, alpha=0.5)
    ax.scatter(x, y, z, marker='o', color='blue', alpha=0.5)
    plt.tight_layout()
    plt.show()
```

results

[RESULT 01]



[RESULT 02]



[RESULT 03]

