Linear regression

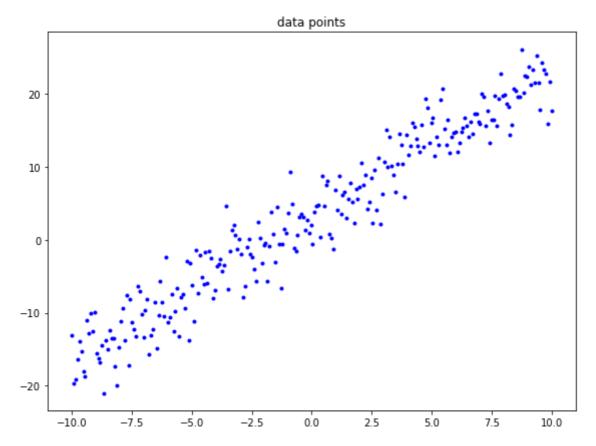
import library

```
In [ ]:
```

```
import numpy as np
import matplotlib.image as img
import matplotlib.pyplot as plt
import matplotlib.colors as colors
from mpl_toolkits.mplot3d import Axes3D
```

load data points

```
• \{(x_i, y_i)\}_{i=1}^n
```



compute the residual

In []:

compute the loss

• useful functions: np.inner

In []:

compute the gradient with respect to $heta_0$

• useful functions: np.inner

In []:

compute the gradient with respect to $heta_1$

• useful functions: np.inner

```
In [ ]:
```

gradient descent for the optimization

In []:

```
number_iteration
                = 500
learning_rate
                = 0.01
theta0
                = 0
theta1
list_theta0
                = np.zeros(number_iteration)
list_theta1
                = np.zeros(number_iteration)
list_loss
                = np.zeros(number_iteration)
for i in range(number_iteration):
   # complete the blanks
   theta0 = theta0 - learning_rate * compute_gradient_theta0(x, y, theta0, theta1)
   theta1 = theta1 - learning_rate * compute_gradient_theta1(x, y, theta0, theta1)
         = compute_loss(x, y, theta0, theta1)
   list_theta0[i] = theta0
   list_theta1[i] = theta1
   list_loss[i]
                = loss
```

functions for presenting the results

```
In [ ]:
```

```
def function_result_01():
    plt.figure(figsize=(8,6))
    plt.plot(x, y, '.', color='blue')
    plt.title('data points')
    plt.show()
```

In []:

```
def function_result_02():

    plt.figure(figsize=(8,6))
    ax = plt.gca()
    plt.plot(list_theta0, '-', color='blue', label=r'$\theta_0$')
    plt.plot(list_theta1, '-', color='red', label=r'$\theta_1$')
    plt.title('model parameters')
    ax.legend()
    plt.show()
```

In []:

```
def function_result_03():

   plt.figure(figsize=(8,6))
   plt.plot(list_loss, '-', color='blue')
   plt.title('loss curve')
   plt.show()
```

```
def function_result_04():
    f = theta0 + theta1 * x

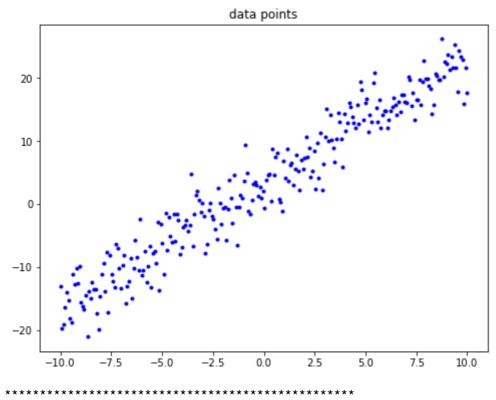
    plt.figure(figsize=(8,6))
    ax = plt.gca()
    plt.plot(x, y, '.', color='blue', label='data point')
    plt.plot(x, f, '-', color='red', label='regression')
    plt.title('regression')
    ax.legend()
    plt.show()
```

In []:

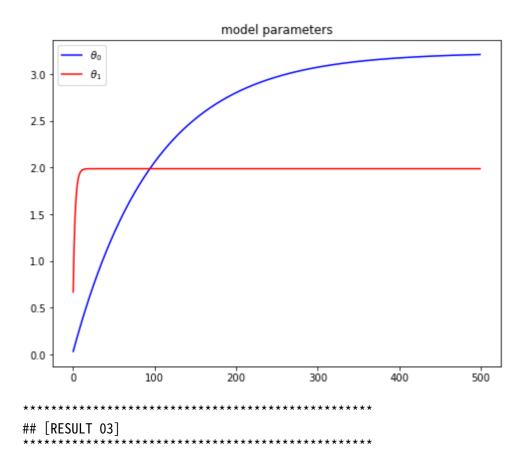
```
def function_result_05():
    X0 = np.arange(-10, 10, 0.1)
    X1 = np.arange(-10, 10, 0.1)
    grid_theta0, grid_theta1 = np.meshgrid(X0, X1)
    grid_loss = np.zeros(grid_theta0.shape)
    for i, t0 in enumerate(X0):
        for j, t1 in enumerate(X1):
            grid_loss[j, i] = compute_loss(x, y, t0, t1)
    fig = plt.figure(figsize=(8,6))
    ax = fig.add_subplot(111, projection='3d')
    plt.title('loss surface')
    ax = plt.axes(projection='3d')
    ax.set_xlabel(r'$\theta_0$')
ax.set_ylabel(r'$\theta_1$')
    ax.set_zlabel('loss')
    ax.plot_surface(grid_theta0, grid_theta1, grid_loss, rstride=1, cstride=1, cmap='viridis',
edgecolor='none')
    plt.tight_layout()
    plt.show()
```

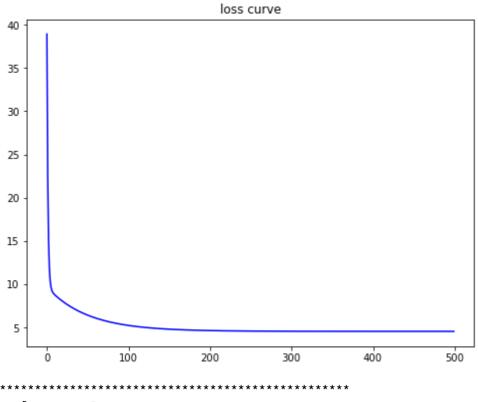
results



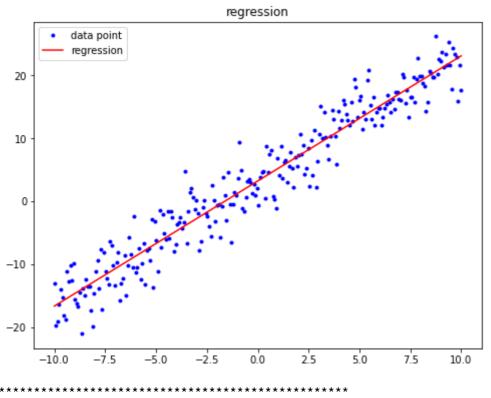


[RESULT 02]





[RESULT 04]



loss surface

