# Isotropic smoothing of image via Heat equation

## import library

```
In [ ]:
```

```
import numpy as np
import matplotlib.image as img
import matplotlib.pyplot as plt
from matplotlib import cm
import matplotlib.colors as colors
from skimage import color
from skimage import io
```

## load input image

filename for the input image is 'barbara\_color.jpeg'

```
In [ ]:
```

```
I0 = io.imread('barbara_color.jpeg')
```

## check the size of the input image

```
In [ ]:
```

```
# complete the blanks
        = np.shape(I0)[0]
num_row
num\_column = np.shape(I0)[1]
num channel = np.shape(I0)[2]
print('number of rows of I0 = ', num_row)
print('number of columns of I0 = ', num_column)
print('number of channels of I0 = ', num_channel)
number of rows of I0 = 512
```

```
number of columns of I0 = 512
number of channels of I0 = 3
```

## convert the color image into a grey image

In [ ]:

```
number of rows of I = 512
number of columns of I = 512
```

## normalize the converted image

• normalize the converted grey scale image so that its maximum value is 1 and its minimum value is 0

## In [ ]:

```
maximum value of I = 1.0 minimum value of I = 0.0
```

# define a function to compute the derivative of input matrix in x(row)-direction

- forward difference : I[x+1,y]-I[x,y]

In [ ]:

- backward difference : I[x,y]-I[x-1,y]

### In [ ]:

# define a function to compute the derivative of input matrix in y(column)-direction

- forward difference : I[x,y+1]-I[x,y]

In [ ]:

- backward difference : I[x,y]-I[x,y-1]

### In [ ]:

## define a function to compute the laplacian of input matrix

- $\Delta I = 
  abla^2 I = rac{\partial^2 I}{\partial x^2} + rac{\partial^2 I}{\partial y^2}$
- $ullet \Delta I = I[x+1,y] + I[x-1,y] + I[x,y+1] + I[x,y-1] 4*I[x,y]$
- $\Delta I$  = derivative x forward derivative x backward + derivative y forward derivative y backward

In [ ]:

# define a function to compute the heat equation of data $\boldsymbol{I}$ with a time step

```
• I = I + \delta t * \Delta I
```

```
In [ ]:
```

## run the heat equation over iterations

In [ ]:

# functions for presenting the results

```
In [ ]:
```

```
def function_result_01():
    plt.figure(figsize=(8,6))
    plt.imshow(I0)
    plt.show()
```

```
In [ ]:
```

```
def function_result_02():
    plt.figure(figsize=(8,6))
    plt.imshow(I, cmap='gray', vmin=0, vmax=1, interpolation='none')
    plt.show()
```

#### In [ ]:

```
def function_result_03():
    L = compute_laplace(I)

plt.figure(figsize=(8,6))
plt.imshow(L, cmap='gray')
plt.show()
```

#### In [ ]:

```
def function_result_04():
    time_step = 0.25
    I_update = heat_equation(I, time_step)

plt.figure(figsize=(8,6))
    plt.imshow(I_update, vmin=0, vmax=1, cmap='gray')
    plt.show()
```

#### In [ ]:

#### In [ ]:

#### In [ ]:

```
def function_result_07():
    L = compute_laplace(I)

    value1 = L[0, 0]
    value2 = L[-1, -1]
    value3 = L[100, 100]
    value4 = L[200, 200]

    print('value1 = ', value1)
    print('value2 = ', value2)
    print('value3 = ', value3)
    print('value4 = ', value4)
```

#### In [ ]:

```
def function_result_08():
    time_step = 0.25
    I_update = heat_equation(I, time_step)

value1 = I_update[0, 0]
    value2 = I_update[-1, -1]
    value3 = I_update[100, 100]
    value4 = I_update[200, 200]

print('value1 = ', value1)
    print('value2 = ', value2)
    print('value3 = ', value3)
    print('value4 = ', value4)
```

### In [ ]:

In [ ]:

## results

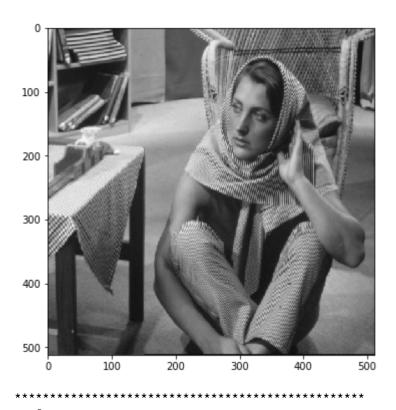
In [ ]:

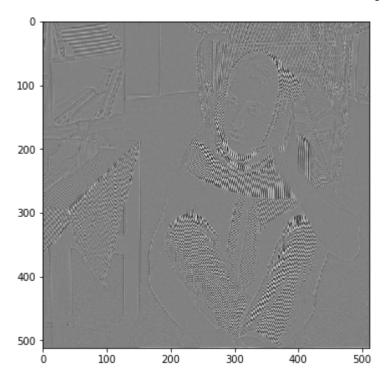
\*\*\*\*\*\*\*\*\*\*

## [RESULT 01]

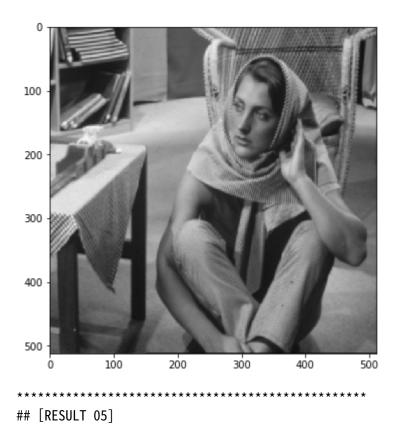


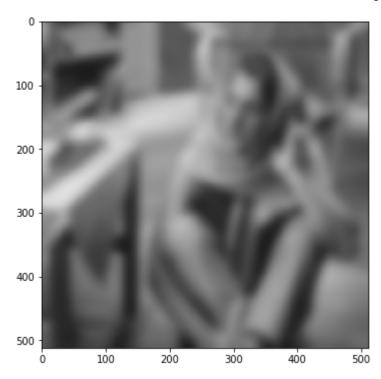
## ## [RESULT 02]

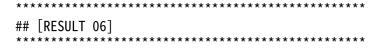


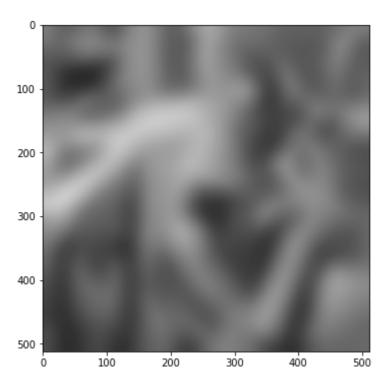


# ## [RESULT 04]









## [RESULT 07] value1 = 0.3842307424134238 value2 = 0.3473015945865081 value3 = -0.11096969959074021 value4 = -0.057368751329410106 ## [RESULT 08] value1 = 0.1205466403535327 value2 = 0.16065986420375264 value3 = 0.5126456173363071 value4 = 0.5929656202312226 ## [RESULT 09] value1 = 0.588913112688924 value2 = 0.4010963411433222 value3 = 0.3678389043817923 value4 = 0.6014962322332662 ## [RESULT 10] value1 = 0.4905270260686319 value2 = 0.4088943172743327 value3 = 0.351276787536652 value4 = 0.6310803621724141 In [ ]: In [ ]: