

# LINEAR TRANSFORMATION OF DATA

OLD DATA

+5

NEW DATA

$x$

$x+5$

3

8

4

9

4

9

8

13

$\sum x = 19$

+nd

+4(5)

$\sum (x+5) = 39$

$$\text{Mean}(x) = \frac{\sum x}{n} = \frac{19}{4} = 4.75$$

$$\text{Mean}(x+5) = \frac{\sum (x+5)}{n} = \frac{39}{4} = 9.75$$

1 New Mean = Old mean  $\pm d$

$$\text{Mean}(x \pm d) = \text{Mean}(x) \pm d$$

2 New Sum = old Sum  $\pm nd$

$$\sum (x \pm d) = \sum (x) \pm nd$$

3 NEW SD = OLD SD

NEW VARIANCE = OLD VARIANCE

$$\text{SD}(x \pm d) = \text{SD}(x)$$

$$\text{VAR}(x \pm d) = \text{VAR}(x)$$

NOTE: WE CANNOT CONVERT  $\sum x^2$  to  $\sum (x \pm d)^2$  DIRECTLY. FOR THIS WE USE SD FORMULA TWICE AND EQUATE.

- 19 The length of time,  $t$  minutes, taken to do the crossword in a certain newspaper was observed on 12 occasions. The results are summarised below.

$$\Sigma(t - 35) = -15 \quad \Sigma(t - 35)^2 = 82.23$$

Calculate the mean and standard deviation of these times taken to do the crossword  $t$  [4]

$$n = 12$$

OLD

$$t$$

$$-35$$

NEW

$$t - 35$$

This is not possible directly to predict  $\Sigma x^2$

$$\Sigma(t - 35)^2 = 82.23$$

$$\Sigma(t) \xrightarrow[-n d]{-12(35)} \Sigma(t - 35) = -15$$

$$\Sigma(t) = -15 + 12(35)$$

$$\Sigma t = 405$$

$$\text{Mean}(t) = \frac{405}{12} \xrightarrow{-35} \text{New Mean} : \frac{\Sigma(t - 35)}{n}$$

$$= 33.75$$

$$= \frac{-15}{12}$$

$$= -1.25$$

$$\xrightarrow{+35}$$

$$\text{new data} = \text{old data} - 35$$

$$\text{new mean} = \text{old mean} - 35$$

$$-1.25 = \text{old mean} - 35$$

$$\text{old mean} = 33.75$$

$$SD(t) = SD(t - 35)$$

$$= \sqrt{\frac{\sum (t - 35)^2}{n} - \left(\frac{\sum (t - 35)}{n}\right)^2}$$

$$= \sqrt{\frac{82.23}{12} - \left(\frac{-15}{12}\right)^2}$$

$$SD(t) = 2.3180$$

35 Esme noted the test marks,  $x$ , of 16 people in a class. She found that  $\Sigma x = 824$  and that the standard deviation of  $x$  was 6.5.

(i) Calculate  $\Sigma(x - 50)$  and  $\Sigma(x - 50)^2$ .

[3]

$$\begin{array}{ccc}
 \text{OLD} & \boxed{n=16} & \text{NEW} \\
 \boxed{x} & \xrightarrow{-50} & \boxed{x-50} \\
 \text{OLD DATA} & -50 & = \text{NEW DATA} \\
 \Sigma x = 824 & \xrightarrow[\begin{smallmatrix} -nd \\ -(16)(50) \end{smallmatrix}]{-50} & \Sigma(x-50) = ?? \\
 & & \Sigma(x-50) = 24 \\
 SD(x) = SD(x-50) \\
 6.5 = \sqrt{\frac{\Sigma(x-50)^2}{n} - \left(\frac{\Sigma(x-50)}{n}\right)^2} \\
 6.5 = \sqrt{\frac{\Sigma(x-50)^2}{16} - \left(\frac{24}{16}\right)^2} \\
 6.5^2 = \frac{\Sigma(x-50)^2}{16} - \left(\frac{24}{16}\right)^2 \\
 \Sigma(x-50)^2 = 712
 \end{array}$$

40 A sample of 36 data values,  $x$ , gave  $\Sigma(x - 45) = -148$  and  $\Sigma(x - 45)^2 = 3089$ .

(i) Find the mean and standard deviation of the 36 values.

[3]

(ii) One extra data value of 29 was added to the sample. Find the standard deviation of all 37 values.

[4]



**44** The values,  $x$ , in a particular set of data are summarised by

$$\Sigma(x - 25) = 133, \quad \Sigma(x - 25)^2 = 3762.$$

The mean,  $\bar{x}$ , is 28.325.

**(i)** Find the standard deviation of  $x$ . [4]

**(ii)** Find  $\Sigma x^2$ . [2]