

# D1 Stationary Point

## P3

- 1 The equation of a curve is  $y = x + \cos 2x$ . Find the  $x$ -coordinates of the stationary points of the curve for which  $0 \leq x \leq \pi$ , and determine the nature of each of these stationary points. [7]

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- 2 The curve with equation  $y = 6e^x - e^{3x}$  has one stationary point.

(i) Find the  $x$ -coordinate of this point. [4]

(ii) Determine whether this point is a maximum or a minimum point. [2]

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- 3 The curve with equation  $y = e^{-x} \sin x$  has one stationary point for which  $0 \leq x \leq \pi$ .

(i) Find the  $x$ -coordinate of this point. [4]

(ii) Determine whether this point is a maximum or a minimum point. [2]

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- 4 The curve  $y = \frac{e^x}{\cos x}$ , for  $-\frac{1}{2}\pi < x < \frac{1}{2}\pi$ , has one stationary point. Find the  $x$ -coordinate of this point. [5]

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- 5 The curve  $y = \frac{\ln x}{x^3}$  has one stationary point. Find the  $x$ -coordinate of this point. [4]

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- 6 The equation of a curve is  $y = 3 \sin x + 4 \cos^3 x$ .

(i) Find the  $x$ -coordinates of the stationary points of the curve in the interval  $0 < x < \pi$ . [6]

(ii) Determine the nature of the stationary point in this interval for which  $x$  is least. [2]

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7 The curve with equation  $y = \frac{e^{2x}}{x^3}$  has one stationary point.

(i) Find the  $x$ -coordinate of this point. [4]

(ii) Determine whether this point is a maximum or a minimum point. [2]

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8 The equation of a curve is

$$y = 3 \cos 2x + 7 \sin x + 2.$$

Find the  $x$ -coordinates of the stationary points in the interval  $0 \leq x \leq \pi$ . Give each answer correct to 3 significant figures. [7]

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9 A curve has equation  $y = \cos x \cos 2x$ . Find the  $x$ -coordinate of the stationary point on the curve in the interval  $0 < x < \frac{1}{2}\pi$ , giving your answer correct to 3 significant figures. [6]

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10 The curve with equation  $y = \frac{e^{2x}}{4 + e^{3x}}$  has one stationary point. Find the exact values of the coordinates of this point. [6]

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11 The curve with equation  $y = \sin x \cos 2x$  has one stationary point in the interval  $0 < x < \frac{1}{2}\pi$ . Find the  $x$ -coordinate of this point, giving your answer correct to 3 significant figures. [6]

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12 The curve with equation  $y = \frac{(\ln x)^2}{x}$  has two stationary points. Find the exact values of the coordinates of these points. [6]

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13 The curve with equation  $y = \frac{2 - \sin x}{\cos x}$  has one stationary point in the interval  $-\frac{1}{2}\pi < x < \frac{1}{2}\pi$ .

(i) Find the exact coordinates of this point. [5]

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14 A curve has equation  $y = \frac{e^{3x}}{\tan \frac{1}{2}x}$ . Find the  $x$ -coordinates of the stationary points of the curve in the interval  $0 < x < \pi$ . Give your answers correct to 3 decimal places. [6]

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15 The curve  $y = \sin \left(x + \frac{1}{3}\pi\right) \cos x$  has two stationary points in the interval  $0 \leq x \leq \pi$ .

(i) Find  $\frac{dy}{dx}$ . [2]

(ii) By considering the formula for  $\cos(A + B)$ , show that, at the stationary points on the curve,  $\cos\left(2x + \frac{1}{3}\pi\right) = 0$ . [2]

(iii) Hence find the exact  $x$ -coordinates of the stationary points. [3]

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16 The curve with equation  $y = \frac{e^{-2x}}{1 - x^2}$  has a stationary point in the interval  $-1 < x < 1$ . Find  $\frac{dy}{dx}$  and hence find the  $x$ -coordinate of this stationary point, giving the answer correct to 3 decimal places. [5]

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