

Logic Gates

- Logic Gates are used in Digital electronics and are used to create electronic circuits.
- Not a physical device.

Symbols For Logic Gates



NOT



OR



AND



NAND



NOR



XOR

Truth Table

- Truth tables are used to trace the output from a logic gate or logic circuit
- The "NOT" Gate is the only logic gate with one input.
- When constructing truth tables, all possible combinations "1s" and "0s" are considered.

$2^2 = 4$

INPUTS	
A	B
0	0
0	1
1	0
1	1

$2^3 = 8$

INPUTS		
A	B	C
0	0	0
0	0	1
0	1	0
0	1	1
1	0	0
1	0	1
1	1	0
1	1	1

• Divide kartay chalay jaana
hai

NOT Gate

OR Gate



INPUT	OUTPUT
A	X
0	1
1	0



INPUT		OUTPUT
A	B	X
0	0	0
0	1	1
1	0	1
1	1	1

* Not Binary
addition

- $X = \text{NOT } A \rightarrow \text{logic Notation}$
- $X = \bar{A} \rightarrow \text{Boolean Algebra}$
- Inverses inputs

- If even one input is "1" then output is "1".
- $X = A \text{ OR } B \rightarrow \text{logic Notation}$
- $X = A + B \rightarrow \text{Boolean Algebra}$

AND Gate

NAND Gate



INPUT	OUTPUT	
A	B	X
0	0	0
0	1	0
1	0	0
1	1	1

NAND



INPUT	OUTPUT	
A	B	X
0	0	1
0	1	1
1	0	1
1	1	0



If even one input is "0" then the output is 0.

Inverses output of AND

$X = A \text{ NAND } B \rightarrow \text{logic Notation}$

$X = \overline{A \cdot B} \rightarrow \text{Boolean Algebra}$

$X = A \text{ AND } B \rightarrow \text{logic Notation}$

$X = A \cdot B \rightarrow \text{Boolean Algebra}$

NOR Gate

XOR Gate

NOR



INPUT		OUTPUT
A	B	X
0	0	1
0	1	0
1	0	0
1	1	0

XOR



INPUT		OUTPUT
A	B	X
0	0	0
0	1	1
1	0	1
1	1	0

- Inverse the output of "OR"
- $X = A \text{ NOR } B \rightarrow \text{Logic Notation}$
- $X = \overline{A + B} \rightarrow \text{Boolean Algebra}$

- Same input, the output would be "0". Different input, the output would be "1".

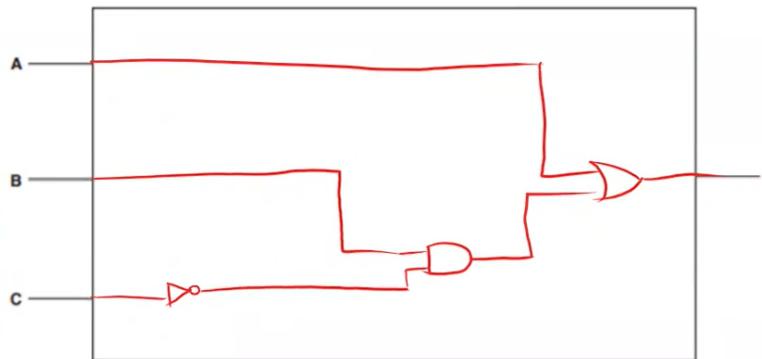
- $X = A \text{ XOR } B \rightarrow \text{logic Notation}$
- $X = A \oplus B \rightarrow \text{Boolean Algebra}$

CASE 1: Construct logic Circuit by Logic Expression.

• Solve values of Bracket first.

6 (a) Draw a logic circuit to represent the logic expression:

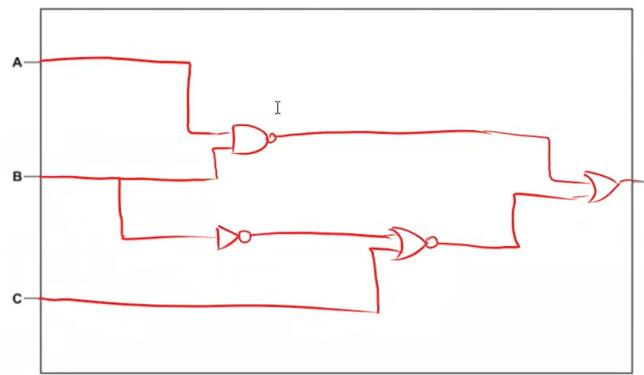
$$X = A \text{ OR } (B \text{ AND NOT } C)$$



A NAND B NOT B NOR C

$$X = \text{NOT}(A \text{ AND } B) \text{ OR } \text{NOT}(\text{NOT } B \text{ OR } C)$$

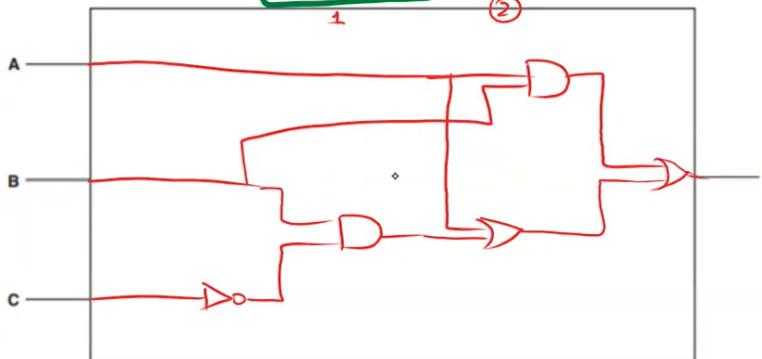
Draw the logic circuit for the given expression using a maximum of four gates.



6 (a) Draw a logic circuit to represent the logic expression:

$$X = A \text{ OR } (B \text{ AND NOT } C) \text{ OR } (A \text{ AND } B)$$

1 2

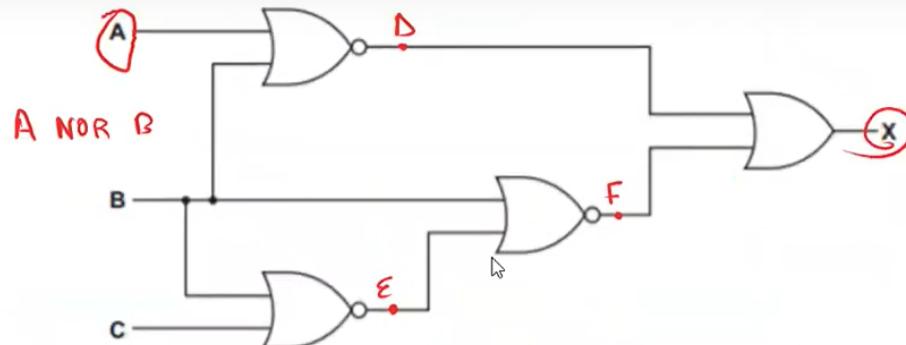


[5]

[4]

CASE 2: Construct a Truth Table by Logic Circuit

8 (a) Complete the truth table for the following logic circuit:



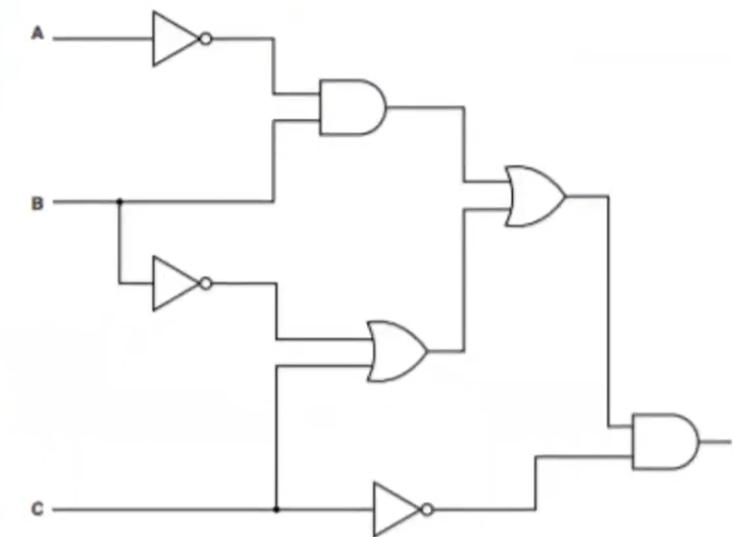
A	B	C	D	E	F	working	$\neg x$
0	0	0	1	1	0	0	1
0	0	1	1	0	0	1	1
0	1	0	0	0	1	0	0
0	1	1	0	0	1	0	0
1	0	0	0	1	0	0	0
1	0	1	0	0	0	1	1
1	1	0	0	0	1	0	0
1	1	1	0	0	1	0	0

[4]

CASE 3: Construct a logic Expression From a Logic Circuit

No steps, only
use logic

(c) Write a logic statement that describes the following logic circuit.



$$((\text{NOT } A \text{ AND } B) \text{ OR } (\text{NOT } B \text{ OR } C)) \text{ AND } \text{NOT } C$$

CASE 4: Construct a logic Expression From Truth Table

- $A = 1$
- $\bar{A} = 0$

• Row multiply

• Column add

3 (a) A Boolean algebraic expression produces the following truth table.

INPUT			OUTPUT
A	B	C	X
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	0

$$\bar{A} \cdot \bar{B} \cdot \bar{C} + \bar{A} \cdot \bar{B} \cdot C + \bar{A} \cdot B \cdot \bar{C} + \bar{A} \cdot B \cdot C + A \cdot \bar{B} \cdot \bar{C} + A \cdot B \cdot \bar{C}$$

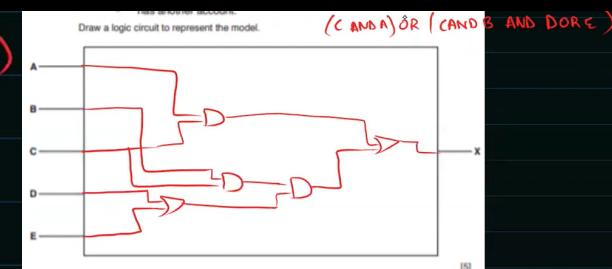
Step 1 : Mark rows with output 1

Step 2 : Now write A or \bar{A} / B or \bar{B} / C or \bar{C}

CASE 5 : Construct Logic Circuit from Problem statement

Note: Always write the expression first.

		0	False
A customer is approved ($X = 1$) if the person:			
$(C \text{ AND } A) \text{ OR } ((C \text{ AND } B) \text{ AND } D \text{ OR } E)$			
*	is over 21 and employed or	A	
*	is over 21 and self-employed and	B	
◦	either earns more than 30000 or	C	
◦	E	D	
	has another account.	E	Σ
			DORF



- Use the parameters from the table