

CASE 1: When σ is known

- Interval Estimate of population mean

$$\rightarrow \bar{x} \pm z_{\alpha/2} \frac{\sigma}{\sqrt{n}} \times \boxed{}$$

$(1-\alpha)$: confidence coefficient
 α : margin of Error
 \bar{x} : sample mean
 σ : pop std
 n : sample size

- 5% margin of error assumed if not given
- If N given then use FPC also " $\frac{N-n}{N-1}$ "

- $z_{\alpha/2} \rightarrow$ resembles left area
- $t_{\alpha/2} \rightarrow //$
- \rightarrow Ignore sign

CASE 2: when σ unknown

$$\rightarrow \bar{x} \pm t_{\alpha/2, v} \frac{s}{\sqrt{n}} \times \boxed{}$$

$(1-\alpha)$: confidence coefficient / level
 α : margin of Error
 \bar{x} : sample mean
 s : sample std
 n : sample size
 v : degree of freedom

- In Q's margin of error equals either

$$\rightarrow t_{\alpha/2, v} \frac{s}{\sqrt{n}}$$

$$\rightarrow z_{\alpha} \times \frac{\sigma}{\sqrt{n}}$$

Expectation Properties

- $E(a) = a$
- $E(ax+b) = a(E(x)) + b$
- $E(xy) = E(x)E(y)$
- $E(a^2x) = a^2(E(x))$

- $cov = \text{co-variance}$

$$cov = \sigma_{xy} = E(xy) - E(x)E(y)$$

Properties Variance

- $Var(a) = 0$
- $Var(ax+b) = a^2 Var(x) + \underbrace{Var(b)}_0$
 $= a^2 Var(x)$
- $Var(x \pm y) = Var(x) \pm Var(y) + 2cov(xy)$

- $corr = \text{correlation}$, range $-1 \text{ --- } 1$

$$corr = r_{xy} = \frac{cov(x,y)}{SD(x)SD(y)}$$

-ve : variables inversely proportional

+ve : variables directly proportional

0 : no relation

- If $E(xy) = E(x)E(y)$, then dependant otherwise independant