

CASE 1: When σ is known

- 5% margin of error assumed if not given
- If N given then use FPC also " $\frac{N-n}{N-1}$ "

- Interval Estimate of population mean

$$\rightarrow \bar{x} \pm z_{\alpha/2} \frac{\sigma}{\sqrt{n}} \times \boxed{(1-\alpha)}$$

$(1-\alpha)$: confidence coefficient
 α : margin of error
 \bar{x} : sample mean
 σ : pop std
 n : sample size

$z_{\alpha/2} \rightarrow$ resembles left area

$t_{\alpha/2} \rightarrow //$

→ ignore sign

- In Q's margin of error equals either

$$\rightarrow t_{\alpha/2} \cdot \sqrt{\frac{s}{\sqrt{n}}}$$

$$\rightarrow z_{\alpha} \times \frac{\sigma}{\sqrt{n}}$$

CASE 2: when σ unknown

$$\rightarrow \bar{x} \pm t_{\alpha/2, v} \frac{s}{\sqrt{n}} \times \boxed{(1-\alpha)}$$

$(1-\alpha)$: confidence coefficient / Level
 α : margin of error
 \bar{x} : sample mean
 s : sample std
 n : sample size
 v : degree of freedom

Expectation Properties

- $E(a) = a$
- $E(ax+b) = a(E(x)) + b$
- $E(xy) = E(x)E(y)$
- $E(a^2x) = a^2(E(x))$

• cov = co-variance

$$\text{cov} = \sigma_{xy} = E(xy) - E(x)E(y)$$

Properties Variance

- $\text{Var}(a) = 0$
- $\text{Var}(ax+b) = a^2 \text{Var}(x) + \text{Var}(b) = a^2 \text{Var}(x)$
- $\text{Var}(x+y) = \text{Var}(x) + \text{Var}(y) + 2\text{cov}(xy)$

• corr = correlation , range $-1 \rightarrow 1$

$$\text{corr} = r_{xy} = \frac{\text{cov}(x,y)}{\text{SD}(x)\text{SD}(y)}$$

-ve : variables inversely proportional

+ve : variables directly proportional

• 0 : no relation

• If $E(xy) = E(x)E(y)$, then dependant
otherwise independent