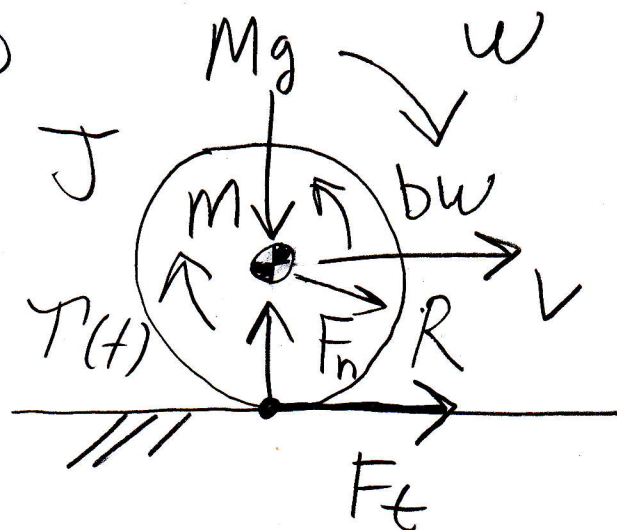
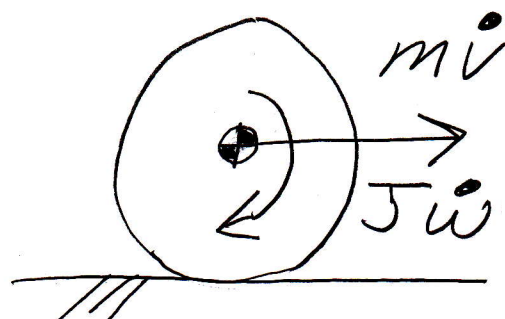


one wheel model:

FBD



=



$V_{gw}$  in  
compatible dir.

$T(t)$  - motor torque

$F_n$  - normal force on wheel

$F_t$  - tangential force on wheel.

Newton's 2nd Law:

$$J\dot{w} = T(t) - bw - RF_t \quad (1)$$

$$m\dot{v} = F_t \quad (2)$$

$$F_t = \mu F_n, \quad F_n = mg$$

Tire friction model:  $\mu = \mu(S)$   $\epsilon \ll 1$

Slip ratio  $S$  is defined by:  $S = \frac{\omega R - v}{|v| + \epsilon}$

The slip ratio is a nondimensional measure of how much the wheel is slipping

For perfect rolling with no slipping  $S = 0$

For complete slipping with no forward motion  $S = \infty$

Negative slip ratios occur when braking ( $S = -1$  locked brakes)

The friction coefficient function in general depends the road surface conditions and tires

A large number of tires are closely approximated by the semi-empirical "Magic Formula" (for tires).

A traction / braking / launch controller normally tries to achieve a good / optimal slip ratio (output  $y = S$ )