

# Assignment 2 - Report

Q1: Time Complexity:  $O(n^2)$  – Space Complexity:  $O(n^2)$

Pseudocode:

**Start:**

- Initialize an empty Sudoku board.
- Fill the main diagonal of the board with random numbers from 1 to 9.
- Solve the Sudoku puzzle.
- Remove some numbers from the board to create a puzzle.
- Display the puzzle.

**Solve the Sudoku puzzle:**

- Find an empty cell in the Sudoku board.
- If there are no empty cells:
  - The puzzle is solved.
  - Return true.
- For each number from 1 to 9:
  - If the number is valid to be placed in the empty cell:
    - Place the number in the cell.
    - If solving the puzzle with this number leads to a solution:
      - Return true.
    - Remove the number from the cell (backtrack).
- Return false (no solution found).

**Remove some numbers from the board to create a puzzle:**

- Randomly select cells in the board.
- If the selected cell is not empty:
  - Remove the number from the cell.
  - Decrease the count of numbers to remove.
- Repeat until the desired number of numbers is removed.

**Display the puzzle:**

- Print the Sudoku board with some numbers hidden.

Output:

One solution found:

```
[[6 7 8 2 9 1 3 5 4]
 [5 2 1 3 8 4 6 9 7]
 [9 4 3 5 6 7 1 2 8]
 [2 3 7 1 5 9 4 8 6]
 [8 1 5 6 4 2 7 3 9]
 [4 9 6 7 3 8 5 1 2]
 [3 8 9 4 7 5 2 6 1]
 [7 6 2 9 1 3 8 4 5]
 [1 5 4 8 2 6 9 7 3]]
```

Multiple solutions found:

```
[[1 9 2 3 5 4 6 7 8]
 [8 6 4 7 9 2 3 5 1]
 [7 5 3 1 6 8 4 2 9]
 [2 1 5 4 8 3 7 9 6]
 [9 7 6 2 1 5 8 3 4]
 [3 4 8 6 7 9 5 1 2]
 [4 3 1 5 2 6 9 8 7]
 [5 2 9 8 4 7 1 6 3]
 [6 8 7 9 3 1 2 4 5]]
```

```
[[1 9 2 3 5 4 6 7 8]
 [8 6 4 7 9 2 3 5 1]
 [7 5 3 1 6 8 2 4 9]
 [2 1 5 4 8 3 7 9 6]
 [9 7 6 2 1 5 8 3 4]
 [3 4 8 6 7 9 5 1 2]
 [4 3 1 5 2 6 9 8 7]
 [5 2 9 8 4 7 1 6 3]
 [6 8 7 9 3 1 4 2 5]]
```

## Q2: Time Complexity: $O(n)$ – Space Complexity: $O(n)$

### Pseudocode:

#### Start:

1. Set the size of the population to 50, number of generations to 1000, and mutation rate to 0.3.
2. Generate an initial population of matrices filled with random numbers from 1 to 9.
3. Display the initial population.

#### Evolution loop:

For each generation:

- a. Sort the population based on how close each matrix is to a magic square.
- b. If a perfect magic square is found, return it.
- c. Create a new generation by selecting the top half of the current population.
- d. Breed and mutate to fill the new generation.
- e. Replace the old generation with the new one.

#### Check if a given matrix is a magic square:

Check if the sums of all rows, columns, and diagonals equal 15.

#### Calculate fitness of a matrix:

Calculate how much each row, column, and diagonal deviates from a magic square.

#### Generate a population:

Create a population of matrices with numbers 1 to 9 in random order.

#### Select parents:

Randomly choose two matrices from the population to be parents for breeding.

#### Crossover:

Mix parts of two parent matrices to create children.

#### Mutate:

Randomly swap two numbers in a child matrix to maintain uniqueness.

#### Display population:

Show all matrices in the population.

#### Main function to run the genetic algorithm:

Run the genetic algorithm and display the solution if found.

End.

### Output:

```
Matrix 48:  
[[7 8 2]  
 [5 6 1]  
 [4 3 9]]
```

```
Matrix 49:  
[[7 8 1]  
 [4 3 2]  
 [5 9 6]]
```

No solution found.

```
A solution was found:  
[[2 8 5]  
 [8 5 2]  
 [5 2 8]]
```