

---

# Project Report for ECE 351

## *Lab 2: User Defined Functions*

---

Isaias Munoz

September 6, 2022

UNIVERSITY OF IDAHO

# Contents

|          |                     |           |
|----------|---------------------|-----------|
| <b>1</b> | <b>Introduction</b> | <b>1</b>  |
| <b>2</b> | <b>Methodology</b>  | <b>1</b>  |
| 2.1      | Part 1 . . . . .    | 1         |
| 2.2      | Part 2 . . . . .    | 2         |
| 2.3      | Part 3 . . . . .    | 3         |
| <b>3</b> | <b>Results</b>      | <b>7</b>  |
| 3.1      | Part 1 . . . . .    | 7         |
| 3.2      | Part 2 . . . . .    | 7         |
| 3.3      | Part 3 . . . . .    | 9         |
| <b>4</b> | <b>Questions</b>    | <b>12</b> |

# 1 Introduction

The purpose of this lab is to introduce user defined functions and then utilize these functions to time shift, scale , reverse and discrete differentiation. This lab uses Python to accomplish it. One of the main key points in this lab is to use numpy and not lists. I first began with inserting the necessary packages or a lot actually.

## 2 Methodology

### 2.1 Part 1

The first task that was assigned was to write a user defined function in order to plot:

$$y(t) = \cos(t)$$

Following code that was provided as an example of user define functions and using `numpy.cos()` I created the following user define function for  $y(t) = \cos(t)$ . making sure the axis were all visible and within range Figure 1 below shoes the code. It is important to notice that I did not need the if statement and could have achieved it by just writing a for loop without the "if". The plot is under results as Fig 7.

```
26 steps = .2e-2 # Define step size
27 #creating and plotting cosine(t)
28 #####
29 t = np . arange ( 0 , 10 + steps , steps )
30
31 def func1 ( t ) : # The only variable sent to the function is t
32     y = np.zeros ( t . shape ) # initialize y(t) as an array of zeros
33     for i in range ( len ( t ) ) : # run the loop once for each index of t
34         if i < ( len( t ) + 1 ) : #works both ways with an if or withouth an if
35             y [ i ] = np . cos ( t [ i ])
36     return y # send back the output stored in an array
37
38
39 y = func1 ( t ) # call the function we just created
40
41
42 #plotting the function I just created
43 plt . figure ( figsize = (10 , 7) )
44 plt . plot ( t , y )
45 plt . grid ()
46 plt . ylabel ( 'cos(t)' )
47 plt . xlabel ( 'time' )
48 plt . title ( 'Plotting cosine task 1' )
49 #####
```

Figure 1: Cosine user define function

## 2.2 Part 2

For part 2 the task was to create user define functions for a figure that was given and to plot the results. The derivation of the equation was pretty tough to understand but I finally manage to understand how to make equations from a graph using step and ramp functions.

$$y(t) = r(t) - r(t - 3) + 5u(t - 3) - 2u(t - 6) - 2r(t - 6)$$

The first equation created was a step and ramp function shown in Figure 2.

```
55 #creating a stepfunction and ramp function and using it to plot fig2
56 #####
57 # >>> np.arange(start=1, stop=10, step=3)
58 # array([1, 4, 7])
59
60 t = np . arange (-5 , 10 + steps , steps )
61 # q = np . arange (-1 , 14 + steps , steps )
62
63 def stepfunc ( t ) : #creating step function
64     y = np.zeros ( t.shape ) #initializing y as all zeroes
65     for i in range (len ( t ) ) : #startingforloop
66         if t [ i ]<0:
67             y[i]=0
68         else:
69             y[i]=1
70     return y
71
72 def rampfunc ( t ) :
73     y = np.zeros ( t . shape )
74     for i in range (len ( t ) ) :
75         if t [ i ]<0:
76             y[i]=0
77         else:
78             y[i]=t[i]
79     return y
80
81 tryone=stepfunc(t)
82 try2=rampfunc(t)
83
84 plt . figure ( figsize = (10 , 7) )
85 plt . plot (t , tryone )
86 plt . grid ()
87 plt . ylabel ('Y output')
88 plt . xlabel ('t')
89 plt . title ('plotting step func to make sure it works')
90
91 plt . figure ( figsize = (10 , 7) )
92 plt . plot (t , try2 )
93 plt . grid ()
94 plt . ylabel ('Y output')
95 plt . xlabel ('t')
96 plt . title ('plotting ramp func to make sure it works')
97
98 fig2=rampfunc(t)-rampfunc(t-3)+5*stepfunc(t-3)-2*stepfunc(t-6)-2*rampfunc(t-6)
99
100
101 plt . figure ( figsize = (10 , 7) )
102 plt . plot (t , fig2 )
103 plt . grid ()
104 plt . ylabel ('Y output')
105 plt . xlabel ('t')
106 plt . title ('plotting Figure 2 using step and ramp functions')
107
108 #####
109
```

Figure 2: Step and Ramp user functions Code

I began with initializing a range of my x-axis ( $t$ ) and that would be from  $(-5,10)$  incremented specific steps I declared earlier. I defined the function "stepfunc" and passed it the range of my x-axis. I began a loop for the length of my x-axis range and if the value of the position in which the range landed on was less than zero then I would make the  $y[i]$  equal to zero, if it wasn't then I would make that position in my y array as one. My 'y' array was initialized to zero earlier and is my 'output'. This gives me a step function. Figure 8 shows the plot that it works as a step function under the results section. I did something very similar with the ramp function, except that if  $t[i]$  is not less than the value zero then I would make  $y[i] = t[i]$  meaning I would make them equal with a slope of 1 which is the definition of a natural ramp function. Figure 9 shows the ramp function working. Finally it was time to put these functions to create the figure given and match it. After the functions were created then it was simply to write the function that was made from steps and ramp functions with appropriate shifts. Figure 10 can be found under the results section it shows the identical match of the figure provided using step and ramp functions.

## 2.3 Part 3

In this task the function created was to be used for time-shifting and scaling operations. Figure 3 shows the time reversal code.

```

118 #####
119 #Apply a time reversal and plot the result.
120 def timereversalfunc(temp): #Much easier when making a function!!!!!! took forever
121
122     timereverse=np.zeros(temp.shape)
123
124     for i in range (0,len(temp)-1):
125
126         timereverse[i]=temp[(len(temp)-1)-i] #imputting values into array reversed
127
128     return timereverse
129
130 reversalz=timereversalfunc(fig2) #calling timereversal and passing it original fig
131
132 plt . figure ( figsize = (10 , 7) )
133 plt . plot (t , reversalz)
134 plt . grid ()
135 plt . ylabel ('Y output' )
136 plt . xlabel ('time')
137 plt . title ('Plotting Fig 2 with timereversal')
138
139
140
141 #####

```

Figure 3: Time reversal function Code

The time reversal took me a while and made me realize making functions is much easier then what I originally was thinking. I created 'timereversalfunc' which took in a value 'temp'. I initialized 'timereverse' to zero and began a loop to from 0 to the length of temp which in this case  $temp = fig2$  or the function that was used to make the figure in part 2. I then proceeded to insert all the values into 'timereverse' but increments down or the opposite way to fill it in backwards. I return and called the function and the plot is in Figure 11 under the results sections.

The next sub-task was to time shift the figure created  $f(t - 4)$  and  $f(-t - 4)$ . Below in Figure 4 is the code.

```

146 #####
147 # apply f(t-4) and f(-t-4)
148 #this is a long way of shifting the t axis
149 #Apply time-shift operations f (t -4) and f (-t -4) and plot the results.
150 # steps = .2e-2 # Define step size
151 # q = np . arange (-1 , 14 + steps , steps ) #this also works by just chaning
152 # your range of numbers because your chaing your t shifting no need
153 # to write a functuon well maybe, not quiet a function is better tbh
154 #other way doesnt work because steeps to 14 way to long
155
156 def functminus4(temp2,shifter):
157
158     temp2= temp2 +shifter#shifting your time scale instaed of the actual fig
159     # temp2.rotate(4)
160     return temp2
161
162 tminus4=functminus4(t,4)
163 # fig2shift=rampfunc(q)-rampfunc(q-3)+5*stepfunc(q-3)-2*stepfunc(q-6)-2*rampfunc
164
165 plt . figure ( figsize = (10 , 7) )
166 plt . plot (tminus4 , fig2)
167 plt . grid ()
168 plt . ylabel ('Y output' )
169 plt . xlabel ('time shifted')
170 plt . title ('Plotting Fig 2 with f(t-4)')
171
172
173
174
175 # negtminusneg4=functminus4(-t,-4)#doesnt work cause your reverse both
176
177 plt . figure ( figsize = (10 , 7) )
178 plt . plot (tminus4 , reversalz)
179 plt . grid ()
180 plt . ylabel ('Y output' )
181 plt . xlabel ('time shifted')
182 plt . title ('Plotting Fig 2 with f(-t-4)')
183
184 # plt . figure ( figsize = (10 , 7) )
185 # plt . plot (q, fig2shift)
186 # plt . grid ()
187 # plt . ylabel ('Y output' )
188 # plt . xlabel ('time')
189 # plt . title ('Plotting Fig 2 with timereversal')
190
191
192 #####

```

Figure 4: Time Shifting function Code

In the time-shift code in Figure 4 I define 'functminus4' and passed it two values; 'temp2' and 'shifter'. One would hold the range shifted and the other was how many moves shifted. I then called 'functminus4' and passed t and 4 't' would be my range since all I am doing is shifting my range declared earlier. I then plot that with the original figure and obtain the plot which can be found under the results section under Figure 12. The other sub-task was  $f(-t - 4)$  and to plot the results. Figure 4 has the code for this shift as well. I used the reversed shift used in the previous task and the reversed figure and plotted both. No function needed to be created and this actually worked. The result is in Figure 13.

The other sub-task was to to apply a timescale operation.  $f(t/2)$  and  $f(2t)$  and plot the results. I felt like these were the easiest but took a while to think about and once figured out they were simple.

```

193 #####
194
195 # Apply time scale operations f (t/2) and f (2t) and plot the results.
196
197 # def scalefunc(temp3,scale):
198 #     # temp3/=scale
199 #     # return temp3
200
201 #     for i in range(0,len(temp3)-1):
202 #         temp3[i]=temp3[i]*scale
203
204 #     return temp3
205 t = np . arange (-5 , 10 + steps , steps )
206 #much simpler than making a function since you can divide the timescale and
207 #then simply graph your original function
208 tdivby2=t/2
209 ttimes2=t*2
210
211 # funcscale=scalefunc(t,2)
212
213
214 plt . figure ( figsize = (10 , 7) )
215 plt . plot (tdivby2 , fig2)
216 plt . grid ()
217 plt . ylabel ('Y output' )
218 plt . xlabel ('time divided by 2')
219 plt . title ('Plotting Fig 2 with f(t/2)')
220
221
222 plt . figure ( figsize = (10 , 7) )
223 plt . plot (ttimes2 , fig2)
224 plt . grid ()
225 plt . ylabel ('Y output' )
226 plt . xlabel ('time multiplied by 2')
227 plt . title ('Plotting Fig 2 with f(2t)')
228
229 #####
230

```

Figure 5: Time Shifting function Code

I was thinking of making a function but realized if I divided my x-range time-frame I could achieve the same thing. That is what I did I divided my time-frame by 2 and plotted it with the original function 'fig2'. The same scenario happen for multiplication.

I multiplied my time scale by 2. It is important to note that I rarely am making changes to the original timescale. I am making it equal to another value and that way I can mess with it and not change the original. Like in this task 'tdivby2' and 'ttimes2' are the scale changes and its those I am plotting with my original function 'fig2'. The plot results are in Figure 14 and 15 for both shifts respectively.

The last task was to differentiate the figure and plot it by hand and use python *numpy.diff()* to differentiate it. Figure 6 shows the code and the plot can be found under the results section Figure 16.

```
234 #####
235
236
237 #Calculate and plot the diritive of func2Plot
238 derivfig2 = np.diff(fig2)
239 xsize = np.arange(-5, 10, steps)
240 plt.figure(figsize=(10, 7))
241 plt.plot(xsize, derivfig2)
242 plt.ylabel('Y Output')
243 plt.xlabel('Time')
244 plt.title("Derivative of fig2")
245 plt.grid()
246
247
248
249
250 #####
251
1 252
```

Figure 6: Time Shifting function Code

I called the differentiate function and was easier then what I thought, since I thought I needed a special package included in python. After calling the *np.diff()* I proceeded to plot it which used the same structure as my previous plots.



## 3 Results

### 3.1 Part 1

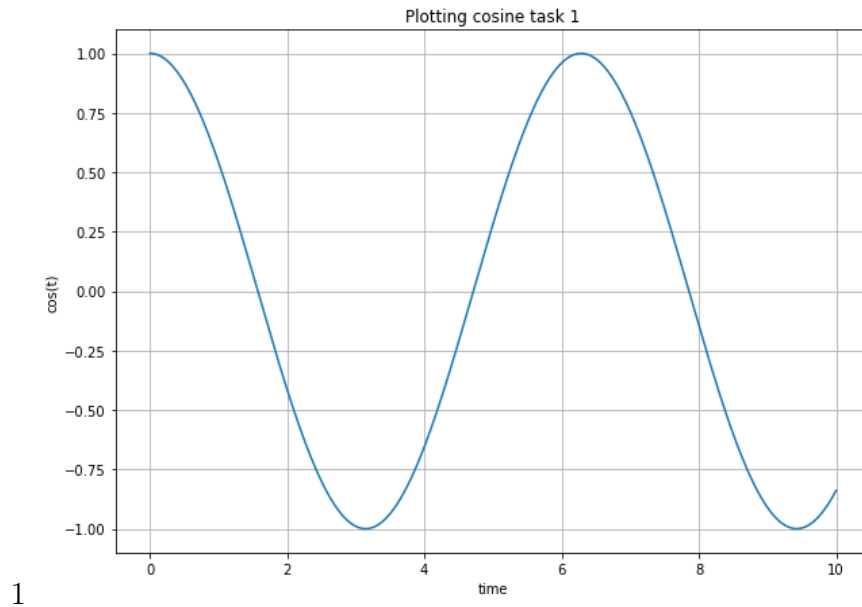


Figure 7: Cosine(x)

### 3.2 Part 2

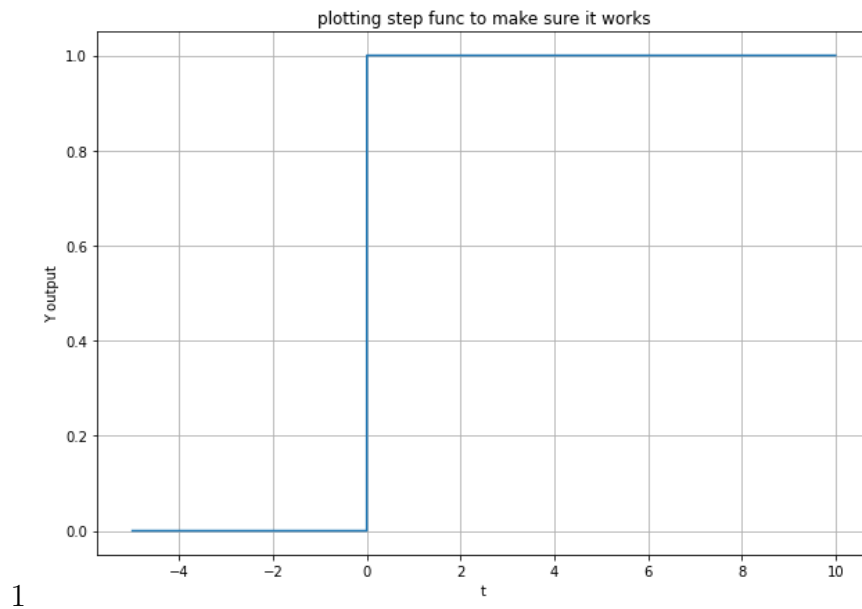


Figure 8: Step function

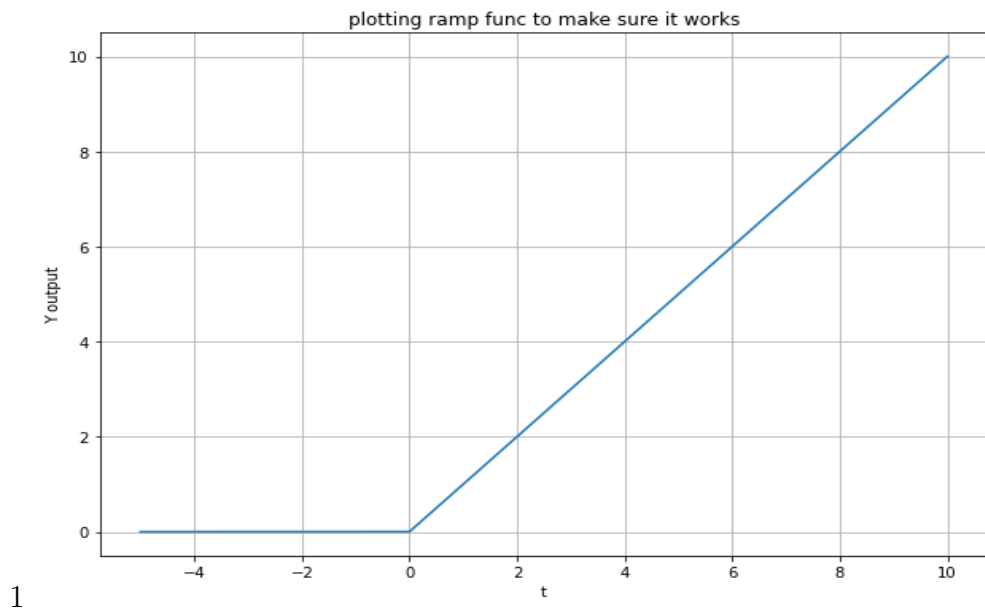


Figure 9: Ramp function

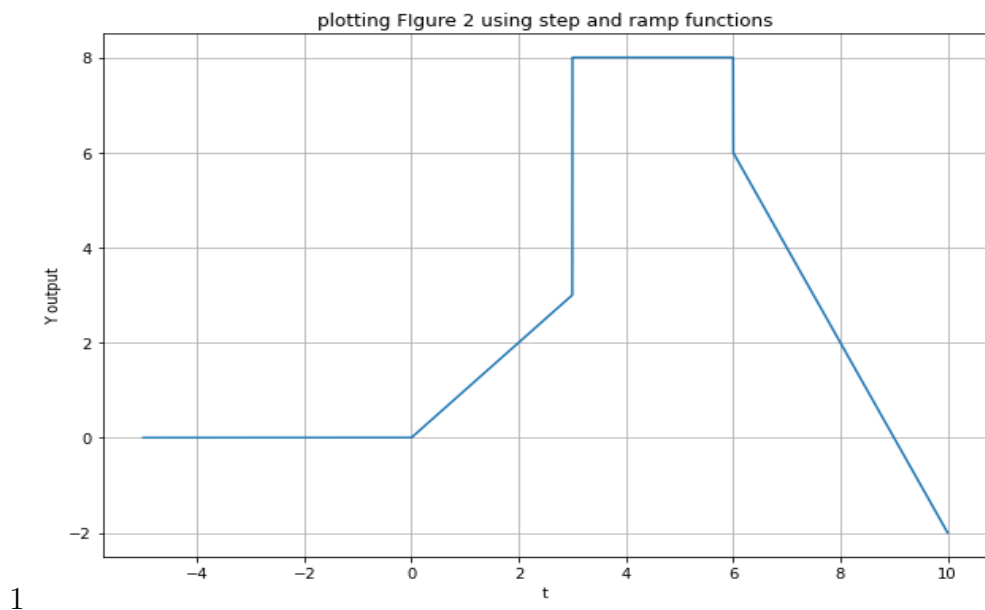


Figure 10: Imitated figure

### 3.3 Part 3

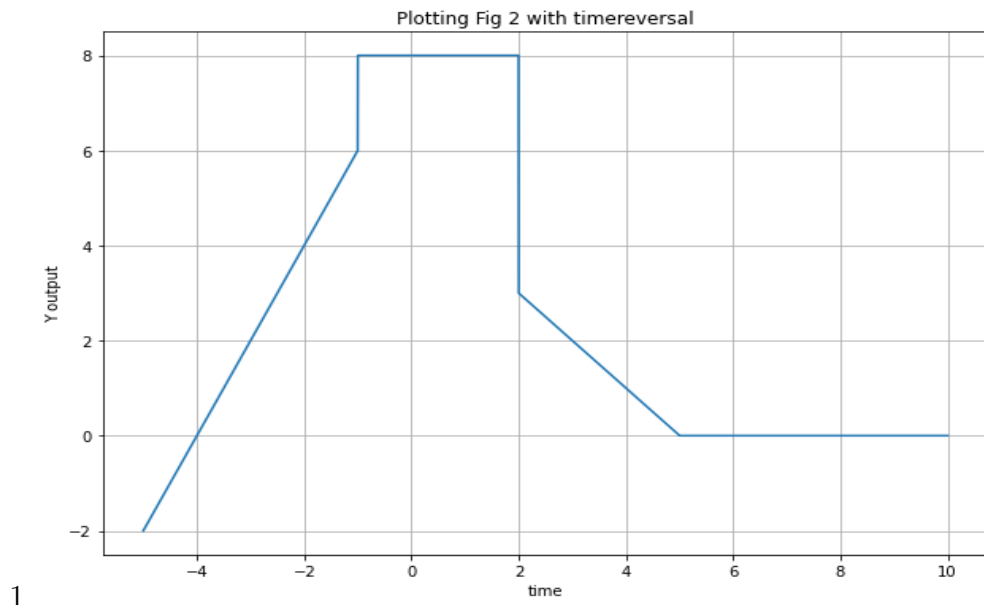


Figure 11: Time reversal figure

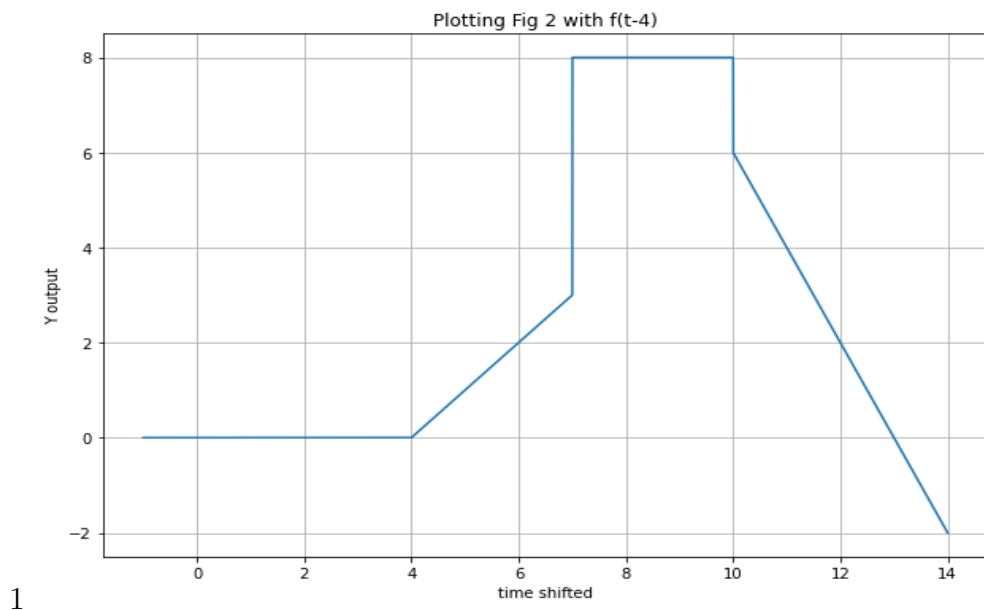


Figure 12:  $f(t-4)$  function

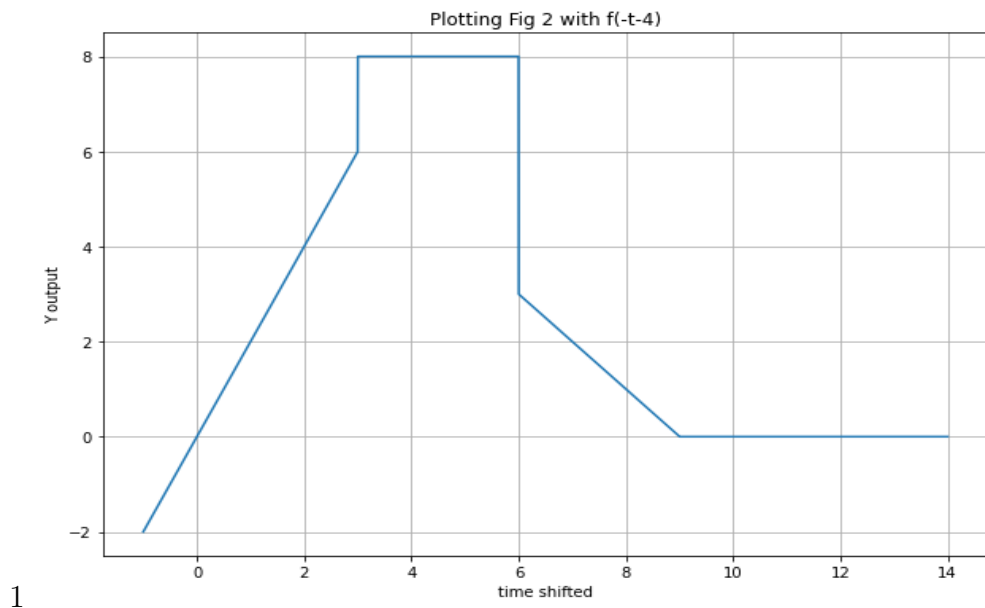


Figure 13:  $f(-t-4)$  function

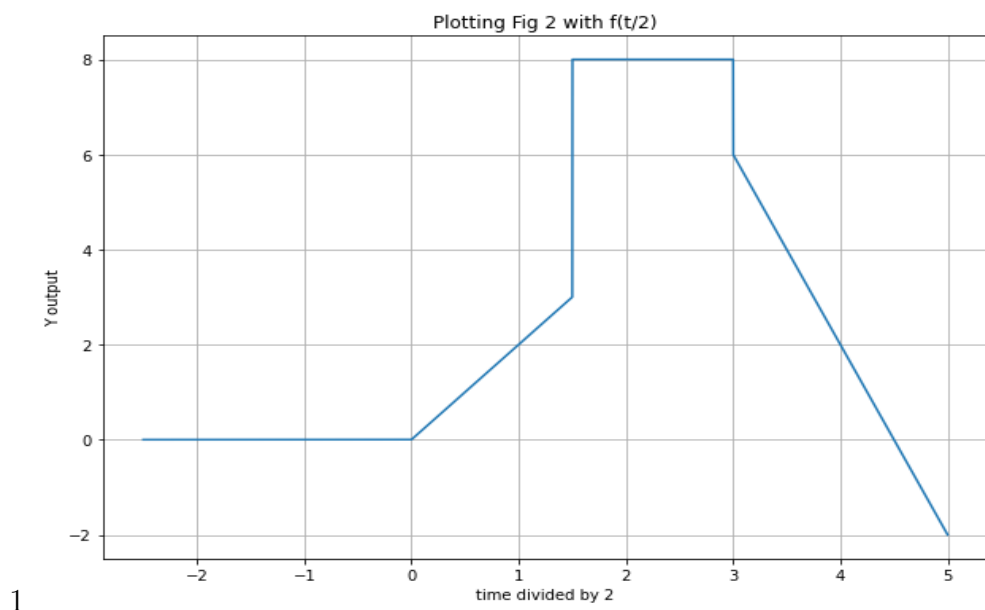
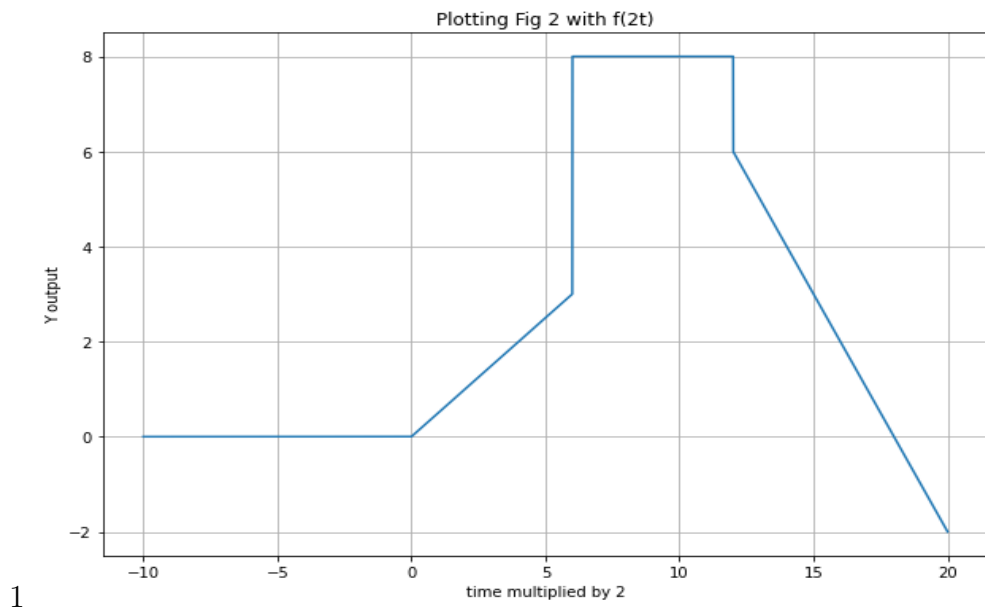
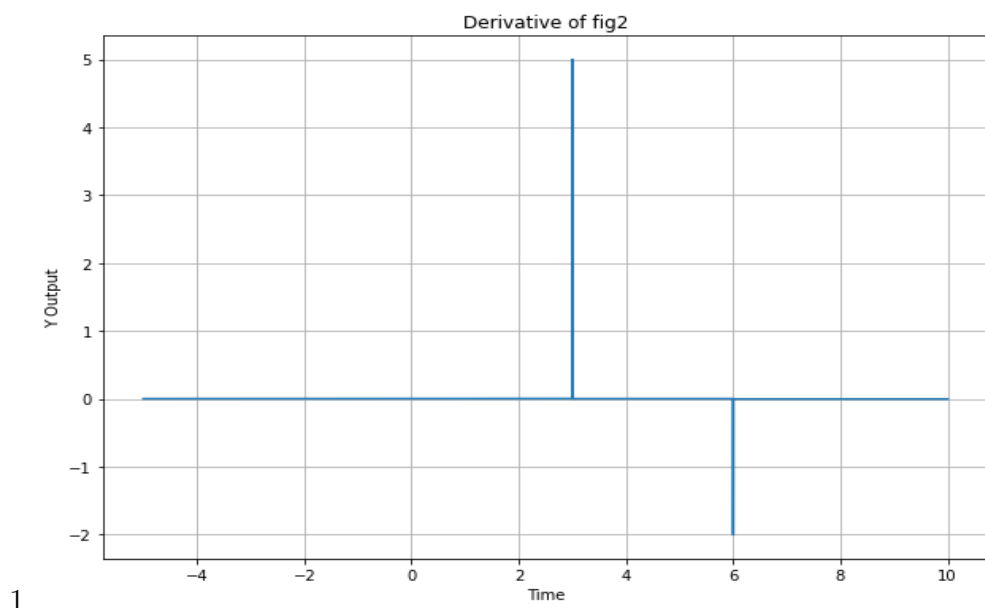


Figure 14:  $f(t/2)$  function



1

Figure 15:  $f(2t)$  function



1

Figure 16: Derivative function

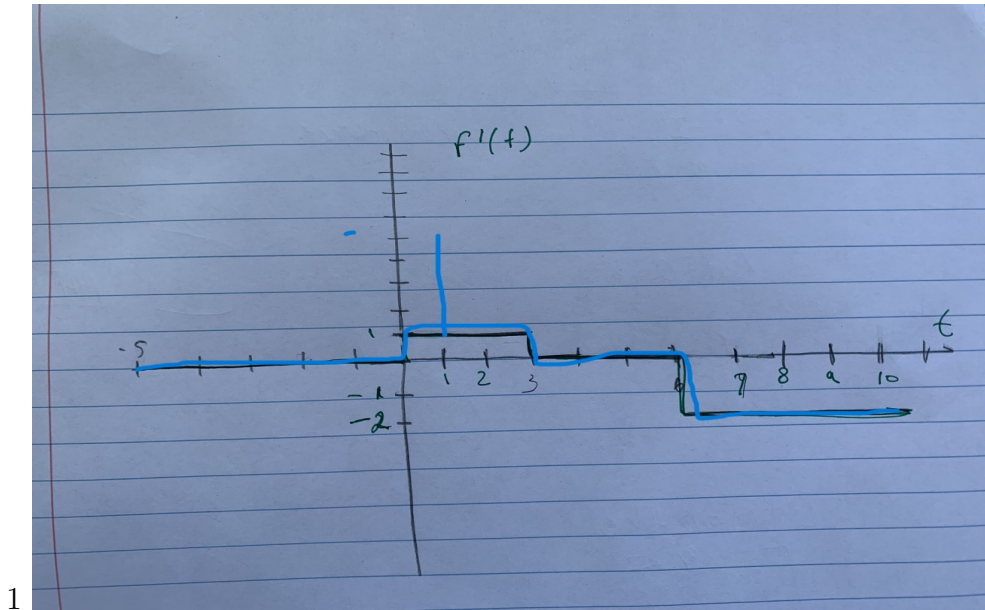


Figure 17: Derivative function

## 4 Questions

1. Are the plots from Part 3 Task 4 and Part 3 Task 5 identical? Is it possible for them to match? Explain why or why not.

They are not quite identical because python's plot shows a spike at time 3 where mine doesn't match. I think it depends on how you are taking the derivative. Maybe in python since its array values it is taking derivatives more precisely with small intervals on the function so there is a derivative at 3 seconds. Therefore I think it is possible to match maybe by messing with how you spread your time range and steps. Maybe by making a step-size of 1.

2. How does the correlation between the two plots (from Part 3 Task 4 and Part 3 Task 5) change if you were to change the step size within the time variable in Task 5? Explain why this happens.

By shifting your step-size towards 1 it makes both graphs more identical.

3. Leave any feedback on the clarity of lab tasks, expectations, and deliverables.

I was just confused if we could have made a couple subplots for Task 3 and not have a bunch of graphs. Another thing is on the time reverse it took me a while to know get it. Maybe an example shown would be helpful but that was just me. Aside from that it was straightforward but very long, hopefully because it was the first lab and figuring out latex.