project2020

January 6, 2021

1 Higher Diploma in Science in Computing (Data Analytics)

1.1 ### Programme Module: Fundamentals of Data Analysis (COMP07084) - Project 2020

In this project we had to perform and explain simple linear regression using Python on the `powerproduction` dataset available on Moodle.

The goal was to accurately predict wind turbine `power` output from wind `speed` values using the data set as a basis. Our submission had to be in the form of a git repository containing, at a minimum, the following items:

1. Jupyter notebook that performs simple linear regression on the data set.
2. In that notebook, an explanation of your regression and an analysis of its accuracy.
3. Standard items in a git repository such as a README.

To enhance our submission, we also has to consider comparing simple linear regression to other types of regression on this data set. Rest assured, all the above concepts will be explored in lecture videos and other materials in the coming semester.

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1.2 ## 1.0 Wind Energy

1.2.1 1.1 Introduction

Energy demand across the world is increasing rapidly because of population and economic growth especially in emerging market economies. This has meant the search for new energy resources has intensified across the globe. The supply of energy is a key element in a countries social and economic development so much so that it can impact international relations. Conflicts in Iraq/Syria, South Sudan, the Crimea/Ukraine, and the South China Sea show the desire to control valuable oil and gas assets is fuelling long-standing historic tensions. Michael Klare argues that *"in a fossil-fuel world, control over oil and gas reserves is an essential component of national power".* (Klare, 2014)

These factors combined with the impact of climate change mean the world will increasingly use renewable energy instead of fossil fuels in order to meet energy demand. Wind energy is seen as a positive alternative to fossil fuels but as with all renewables it has advantages as well as disadvantges. Although the manufacturer and installation of wind turbines does involve the release of some pollution into the environment, in the long run it is a source of clean energy and does not emit any greenhouse gases. It is renewable, space efficient, low cost and promotes job creation.

However, it does have disadvantages, including its intermittent and unpredictable nature, noise issues, wildlife habitat dislocation as well as impacting tourism with some considering it an eye sore. It also faces location limitation issues, *"because to be economically viable, they need to be installed in a place where they will produce enough electricity, which means coastal areas, the tops of hills, and open planes - essentially anywhere with strong, reliable wind. Most of these suitable places tend to be in remote areas far outside of cities and towns, in more rural areas or offshore. Because of this distance, new infrastructure, such as power lines, have to be built in order to connect a wind farm to the power grid".* (Lane, 2020)

1.2.2   1.2 Facts and figures

In 2019 global direct primary energy consumption stood at 158,839 TWh with renewable energy sources (RES) accounting for 19,219 TWh or 12.1% of this figure. Within (RES) wind energy contributed 6.6% or 1,270 TWh of all renewables. In 2019 Europe had 205 GW of wind energy capacity accounting for 15% of the EU-28 consumed electricity. An additional 15.4 GW of new wind power capacity was added in 2019 an increase of 27% on the previous year.

Within Europe ten member states are achieving wind power shares above 10%. *"The highest share, and a new record, was set by Denmark where 47% of the electricity demand in 2019 was met by wind energy, followed by Ireland at 32% and Portugal at 27%"* (Windeurope.org, 2020).

In Ireland wind energy is the largest contributing resource of renewable power. According to the Sustainable Energy Authority of Ireland (SEAI) in their Wind Energy Roadmap, *"wind energy has the potential to generate enough electricity to exceed domestic demand by 2030 and for its wind market to become export driven in the 2020-2030 timeframe"* (SEAI, 2011). This could generate €15 billion in economic value and lead to the creation of 20,000 jobs in the installation, operation and maintenance of wind farms. It would also present a large carbon abatement in the range of 400 to 450 metric tonnes of CO_2 by 2050.

In order to achieve these ambitious goals significant investment is required and it is estimated that the wind industry would hit a peak annual investment of between €6 billion and €12 billion by 2040 (SEAI, 2011). Caution should be applied however when assessing investment in wind energy. One report has identified a payback period of 23 years for an investment in a wind energy project, which would be a disappointing timeframe for investors. However, this does not have to be the case if a significant feasibility assessment is carried out.

According to a study carried out by TUD, if due consideration is given to *"site selection, electricity market conditions, the quality of the control system and the competencies of the design/installation/commissioning company"* (Kealy, 2015) there should be a positive outcome for investors, consumers and the environment. Their study based on a wind farm in the North East of Ireland were an average capacity factor of 34% was returned from the wind farm's turbines a payback period of 6.7 years was set. Because of the intermittent nature of wind, turbines typically produce only 20% - 40% of their maximum possible output over the course of a year which is known as the capacity factor (Miller, 2014).

1.2.3   1.3 Location

The crucial factor in the location of wind farms is calculating the annual energy production and how the energy it produces compares to alternative sources of energy. Key to this is access to and modelling of long-term data. Data should be collected from a potential site over a two to three-

year timeframe. From this data the long-term annual variability needs to be calculated and can the renewable energy production output be predicted/forecast (Nelson, 2019). Modelling solutions at their most basic can be done through physical modelling via computational fluid dynamics or mathematical modelling via regular linear algebra.

Simple mathematical modelling on its own won't provide the accuracy but will suffice for common use cases like estimating maximum power production. This is the case with wind turbine manufacturers using power curve modelling techniques. The wind turbine power curve shows the relationship between wind speed and power generated *"for different wind speeds. A typical wind turbine power curve has three main characteristic speeds: 1) cut-in (Vc); 2) rated (Vr); and 3) cut-out (Vs) speeds. The turbine starts generating power when the wind speed reaches the cut-in value. The rated speed is the wind speed at which the generator is producing the machine's rated power. When the wind speed reaches the cut-out speed, the power generation is shut down to prevent defects and damages"* (Wadhvani, 2017).

Power curves can oversimplify reality though and can err by plus or minus 20% the actual power output. In actuality additional variables must be factored in (Miller, 2014). For example, *"wind speed at heights below and above the hub, wind shear, and turbulence are also strong predictors of power production"*. Any model used in predicting power output from wind turbines must also quantify uncertainty or confidence level associated with them. *"Such confidence levels are particularly of value to electric grid operators, who need both the predictions of output and the associated levels of confidence to determine an optimal schedule for turning various sources of power on and off. Quantifying output uncertainty is also crucial for siting wind farms"*(Miller, 2014). Outliers also need to be considered in any model, wind ramps being one of the most important. Because power output is proportional to the cube of the wind speed a wind ramp can result in a dramatic change in power production. *"Consequently, accurate wind ramp prediction is extremely important, leading some experts to refer to it as "the Holy Grail of wind forecasting."(Miller, 2014)*

1.3   2.0 Simple linear regression

For this project we had to perform a simple linear regression on a dataset relating to wind turbines with the goal of accurately predicting wind turbine power output from the wind speed values. Regression is a statistical technique which is used to investigate the relationship between variables. When we only have one input variable, in this case wind speed, it is a simple linear regression, when there is more than one input variable then a multiple linear regression would be used.

The equation for a simple linear regression is $y = w0 + w1 * x1$. In our case we know the input variable $x1$ is wind speed and y is power output.

$w0$ and $w1$ are the two coefficients, where $w0$ is the intercept (of the y-axis), and $w1$ is the slope of the line. $w1$ shows the impact of the independent variable $x1$ on y.

For example, when $w1 = 0$, there's no impact of $x1$ on y since $(0 * x1 = 0)$. (Linear Regression in Machine Learning, 2020).

Therefore simply, linear regression is an algorithm that finds the best values of w0 and w1 to fit the training dataset. (Linear Regression in Machine Learning, 2020).

1.4 3.0 Importing the required libraries

Numerical Python or NumPy is the first library we require. NumPy is the fundamental package for scientific computing in Python. It is a Python library that provides a multidimensional array object, various derived objects (such as masked arrays and matrices), and an assortment of routines for fast operations on arrays, including mathematical, logical, shape manipulation, sorting, selecting, I/O, discrete Fourier transforms, basic linear algebra, basic statistical operations, random simulation and much more.

```
[1]: import numpy as np
```

Next import the pandas library. pandas is a fast, powerful, flexible and easy to use open source data analysis and manipulation tool,built on top of the Python programming language.

```
[2]: import pandas as pd
```

Next up import statsmodels. statsmodels is a Python module that provides classes and functions for the estimation of many different statistical models, as well as for conducting statistical tests, and statistical data exploration. An extensive list of result statistics are available for each estimator. The results are tested against existing statistical packages to ensure that they are correct.

```
[3]: import statsmodels as sm
```

Finally we need to import Matplotlib a plotting library available for the Python programming language as a component of NumPy. Matplotlib embeds plots in Python applications. Seaborn is a Python data visualization library based on matplotlib. It provides a high-level interface for drawing attractive and informative statistical graphics. The `%matplotlib inline` statement will cause our matplotlib visualizations to embed themselves directly in our Jupyter Notebook, which makes them easier to access and interpret.

```
[4]: import matplotlib.pyplot as plt
     %matplotlib inline
     %config InlineBackend.figure_format = 'retina'
```

Seaborn is a Python data visualization library based on matplotlib. It provides a high-level interface for drawing attractive and informative statistical graphics.

```
[5]: import seaborn as sns
```

1.5 4.0 Create dataframe

Now let's load the data from thepowerproduction csv file provided using the pandas.read_csv function.

```
[6]: dataset = pd.read_csv('powerproduction.csv', delimiter = ',')
```

1.6 5.0 Data exploration

Having obtained the data, the next step is to perform some exploratory data analysis, looking in more detail at the dataset attributes.

1.6.1 5.1 DataFrame.info

Now lets take a quick look at the data types and if there are any null records in the dataset using the pandas.DataFrame.info function

```
[7]: dataset.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 500 entries, 0 to 499
Data columns (total 2 columns):
 #   Column  Non-Null Count  Dtype
---  ------  --------------  -----
 0   speed   500 non-null    float64
 1   power   500 non-null    float64
dtypes: float64(2)
memory usage: 7.9 KB
```

The dataset has only two columns, speed and power and both are floats. There is 500 records in the dataset and no null records.

1.6.2 5.2 DataFrame.head

First I'm going to have a look at the first 10 records of the dataset using the pandas.DataFrame.head function.

```
[8]: dataset.head(10)
```

```
[8]:    speed  power
    0  0.000  0.000
    1  0.125  0.000
    2  0.150  0.000
    3  0.225  0.000
    4  0.275  0.000
    5  0.325  4.331
    6  0.400  5.186
    7  0.450  3.826
    8  0.501  1.048
    9  0.526  5.553
```

From the results it's clear the wind turbine only begins to produce output after a certain wind speed is reached. This makes sense as the blades on wind turbines only begin to rotate once the cut-in speed is reached. The cut-in speed for most turbines is around 3-5 metres per second (m/s), or 8-12 miles per hour (mph). Around cut-in, the generator may be used as a motor to help the wind overcome inertia and start the blades turning. (Enerpower, 2020). Now lets examine the last 10 records in the dataset using the pandas.DataFrame.tail function.

1.6.3   5.3 DataFrame.tail

```
[9]: dataset.tail(10)
```

```
[9]:        speed  power
      490  24.499    0.0
      491  24.525    0.0
      492  24.575    0.0
      493  24.650    0.0
      494  24.750    0.0
      495  24.775    0.0
      496  24.850    0.0
      497  24.875    0.0
      498  24.950    0.0
      499  25.000    0.0
```

From the data displayed it appears no power is produced after a set wind speed is reached, this is called the cut-out speed which is around 24 m/s or 55 mph or greater. This is to prevent wear and tear. Since winds of this strength occur only for a handful of hours per year, very little energy is lost in high wind periods.(Enerpower, 2020)

1.7   6.0 Summary statistics

1.7.1   6.1 DataFrame.describe

DataFrame.describe produces descriptive statistics that include summaries of the central tendency, dispersion and shape of a dataset's distribution, excluding NaN values.

```
[10]: dataset.describe()
```

```
[10]:             speed        power
      count  500.000000   500.000000
      mean    12.590398    48.014584
      std      7.224991    41.614572
      min      0.000000     0.000000
      25%      6.324750     5.288000
      50%     12.550500    41.645500
      75%     18.775250    93.537000
      max     25.000000   113.556000
```

```
[11]: dataset.mean()
```

```
[11]: speed    12.590398
      power    48.014584
      dtype: float64
```

```
[12]: dataset.median()
```

```
[12]: speed    12.5505
      power    41.6455
      dtype: float64
```

```
[13]: dataset.var()
```

```
[13]: speed     52.200499
      power   1731.772627
      dtype: float64
```

```
[14]: dataset.std()
```

```
[14]: speed     7.224991
      power    41.614572
      dtype: float64
```

Now lets plot our data to see what it looks like.

```
[15]: dataset.plot(x='speed', y='power', style=('o'), markersize=1.5)
      plt.title('Wind speed vs Power output')
      plt.xlabel('Wind speed')
      plt.ylabel('Power output')
      plt.grid(b=True, which='major', color='#666666', linestyle='-')
      plt.minorticks_on()
      plt.grid(b=True, which='minor', color='#999999', linestyle='-', alpha=0.2);
```
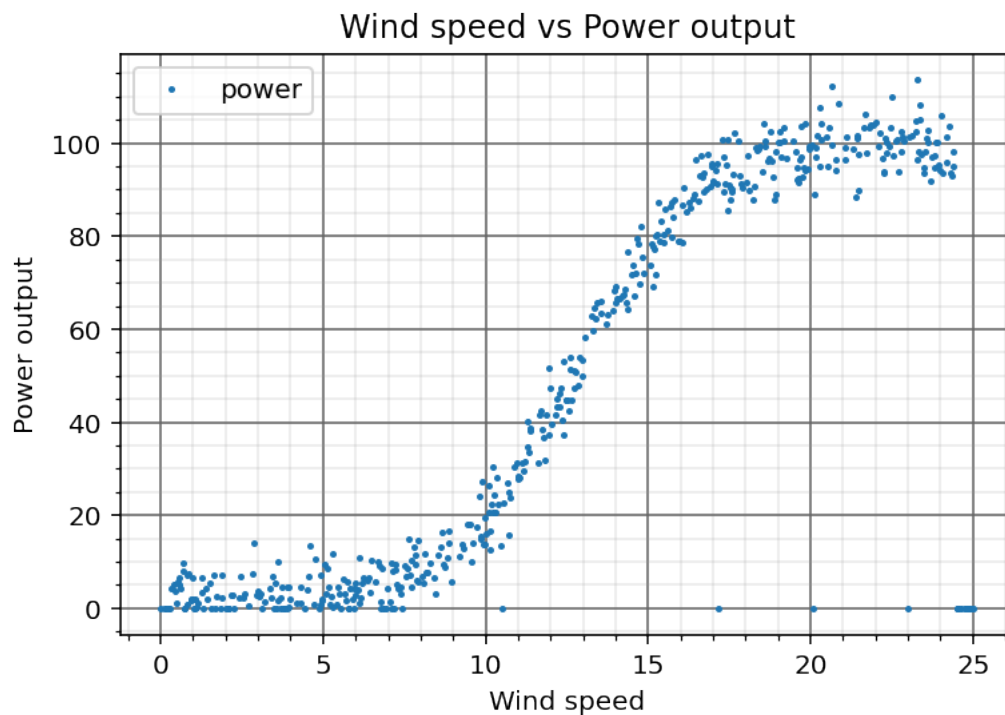
1.8 7.0 Simple linear regression algorithm

1.8.1 7.1 Preparing the data

```python
[16]: #from sklearn import metrics
```

```python
[ ]:
```

```python
[17]: x = dataset.iloc[:, :-1].values
y = dataset.iloc[:, 1].values
```

```python
[18]: from sklearn.model_selection import train_test_split
x_train, x_test, y_train, y_test = train_test_split(
    x, y, test_size=0.2, random_state=0)
```

The section of code above ascribes 80% of our data to the training set and 20% of the data to the test set.

1.8.2 7.2 Training the algorithm

Linear regression is easy to implement using Scikit-Learn because all you need to do is import the `LinearRegression` class, instantiate it, and call the fit() method along with our training data. (Robinson, S., 2020, (15)).

```python
[19]: from sklearn.linear_model import LinearRegression
regressor = LinearRegression()
regressor.fit(x_train, y_train)
```

```
[19]: LinearRegression()
```

A linear regression model basically finds the best value for the intercept and slope, which results in a line that best fits the data. To see the value of the intercept and slope calculated by the linear regression algorithm for our dataset, execute the following code.

To retrieve the intercept we run the below code.

```python
[20]: print(regressor.intercept_)
```

```
-13.603433993820211
```

And for the intercept we need to run the below.

```python
[21]: print(regressor.coef_)
```

```
[4.89542079]
```

The above figure tells us that for every one unit of change in wind speed the change in power output is approximately 4.89%.

1.8.3   7.3 Making predictions

The steps we have taken so far dealt with training our algorithm the goal now is to accurately predict wind turbine power output from the wind speed values. In order to this we must use the test data and see how accurately the algorithm predicts the power output %.

The section of code below creates a NumPy array containing all the predicted values for the input values in the `x_test` series.

```
[22]: y_pred = regressor.predict(x_test)
```

Now we are going to compare the actual output values for `x_test` with the predicted values.

```
[23]: df = pd.DataFrame({'Actual': y_test, 'Predicted': y_pred})
      df
```

```
[23]:        Actual    Predicted
      0        7.060    10.408605
      1       51.149    48.632051
      2       71.763    57.326318
      3       99.357    96.161691
      4      113.556   100.327694
      ..         …           …
      95      96.058    77.911562
      96       3.578     1.097515
      97      93.931    95.304992
      98       0.000     1.709442
      99       0.000    37.852334

      [100 rows x 2 columns]
```
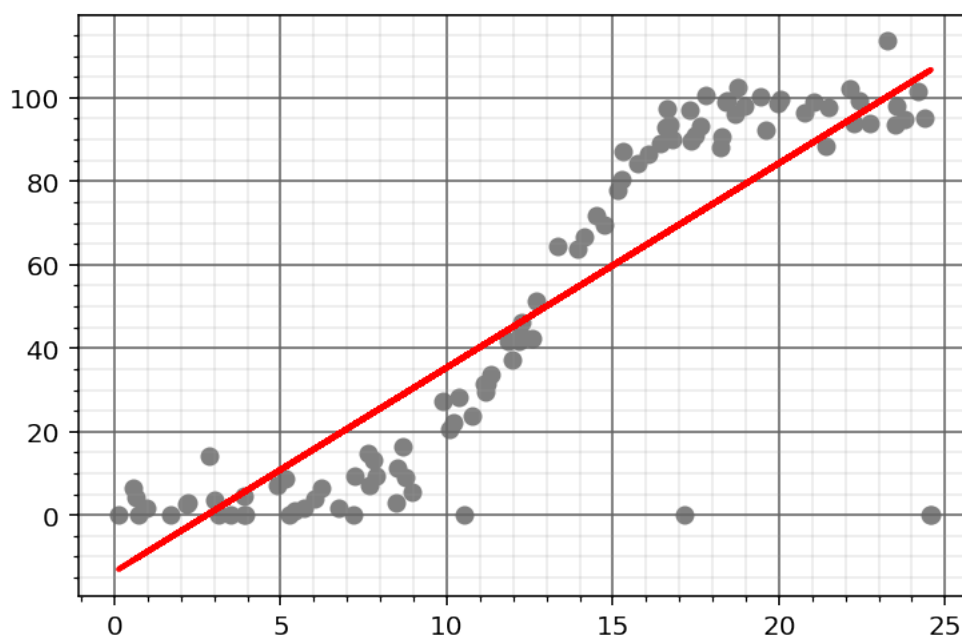
```
[24]: plt.scatter(x_test, y_test, color='grey')
      plt.plot(x_test, y_pred, color='red', linewidth=2)
      plt.grid(b=True, which='major', color='#666666', linestyle='-')
      plt.minorticks_on()
      plt.grid(b=True, which='minor', color='#999999', linestyle='-', alpha=0.2)
      plt.title("Prediction versus Test data", fontsize=15, y=1.012)
      plt.show()
```

Prediction versus Test data

1.8.4 7.4 Evaluating the algorithm

There are three main metrics for testing the performance of a regression machine learning model. They are 1. Mean Absolute Error, 2. Mean Squared Error and 3. Root Mean Squared Error. (McCullum, N., 2020.,(23)). I've outlined below what each one does before implementing them on our data.

Mean Absolute Error (MAE): MAE measures the average magnitude of the errors in a set of predictions, without considering their direction. Its the average over the test sample of the absolute differences between prediction and actual observation where all individual differences have equal weight. (Medium. 2016.,(26))

Mean Squared Error (MSE): In statistics, the mean squared error (MSE)or mean squared deviation (MSD) of an estimator (of a procedure for estimating an unobserved quantity) measures the average of the squares of the errors—that is, the average squared difference between the estimated values and the actual value. MSE is a risk function, corresponding to the expected value of the squared error loss. The fact that MSE is almost always strictly positive (and not zero) is because of randomness or because the estimator does not account for information that could produce a more accurate estimate.(En.wikipedia.org. 2021, (25))

Root Mean Squared Error (RMSE): RMSE is a quadratic scoring rule that also measures the average magnitude of the error. It's the square root of the average of squared differences between prediction and actual observation.(Medium. 2016.,(26))

So lets see how are model did.

```
[25]: from sklearn import metrics
      print('Mean Absolute Error:', metrics.mean_absolute_error(y_test, y_pred))
      print('Mean Squared Error:', metrics.mean_squared_error(y_test, y_pred))
      print('Root Mean Squared Error:', np.sqrt(metrics.mean_squared_error(y_test,
       →y_pred)))
```

```
Mean Absolute Error: 15.371033053882327
Mean Squared Error: 496.3930965626669
Root Mean Squared Error: 22.279880981788637
```

From the above you can see that the root mean squared error is 22.27 which is 46% of of the mean value of of the percentage of power output 48.01. This indicates that the algorithm did not do a very good job.

1.9   8.0 Polynomial regression algorithm

```
[26]: dataset = pd.read_csv('powerproduction.csv', delimiter = ',')
```

```
[27]: from sklearn import metrics
```

```
[28]: x = dataset.iloc[:, :-1].values
      y = dataset.iloc[:, 1].values
```

```
[29]: from sklearn.model_selection import train_test_split
      x_train, x_test, y_train, y_test = train_test_split(
          x, y, test_size=0.2, random_state=0)
```

```
[30]: from sklearn.preprocessing import PolynomialFeatures
```

```
[31]: y_train = y_train[x_train[:, 0].argsort()]
      x_train = x_train[x_train[:, 0].argsort()]
```

```
[32]: poly = PolynomialFeatures(degree=4)
```

```
[33]: x_poly = poly.fit_transform(x_train)
```

```
[34]: poly.fit(x_poly, y_train)
```

```
[34]: PolynomialFeatures(degree=4)
```

```
[35]: from sklearn.linear_model import LinearRegression
      model = LinearRegression()
      model.fit(x_poly, y_train)
```

```
[35]: LinearRegression()
```

```
[36]: y_pred = model.predict(poly.fit_transform(x_test))
```

```
[37]: df2 = pd.DataFrame({'Actual': y_test, 'Predicted': y_pred})
      df2
```

```
[37]:        Actual     Predicted
      0        7.060      1.924069
      1       51.149     47.224790
      2       71.763     65.658059
      3       99.357     95.194583
      4      113.556     83.758251
      ..         …             …
      95      96.058    102.066162
      96       3.578      1.751915
      97      93.931     96.989439
      98       0.000      1.682792
      99       0.000     27.002852

      [100 rows x 2 columns]
```

```
[38]: from sklearn import metrics
      print('Mean Absolute Error:', metrics.mean_absolute_error(y_test, y_pred))
      print('Mean Squared Error:', metrics.mean_squared_error(y_test, y_pred))
      print('Root Mean Squared Error:', np.sqrt(metrics.mean_squared_error(y_test,
       →y_pred)))
```

```
Mean Absolute Error: 7.675597300582747
Mean Squared Error: 225.20783826203305
Root Mean Squared Error: 15.00692634292689
```
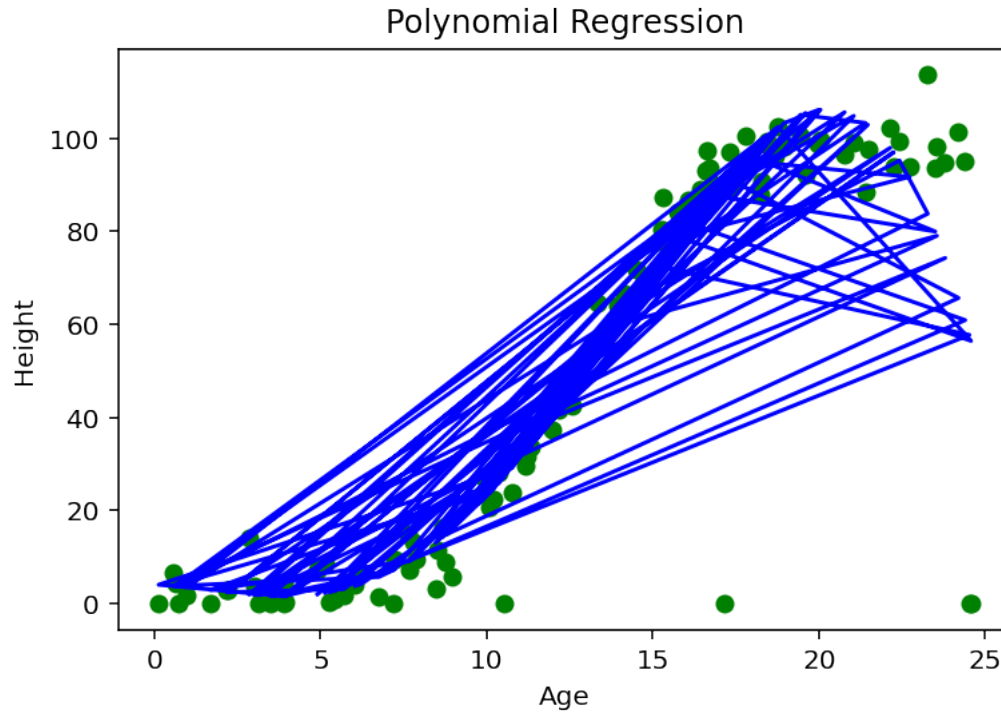
```
[39]: plt.figure(figsize=(10,8));
      plt.scatter(x_test, y_test);
      plt.plot(x_test, y_pred);
```
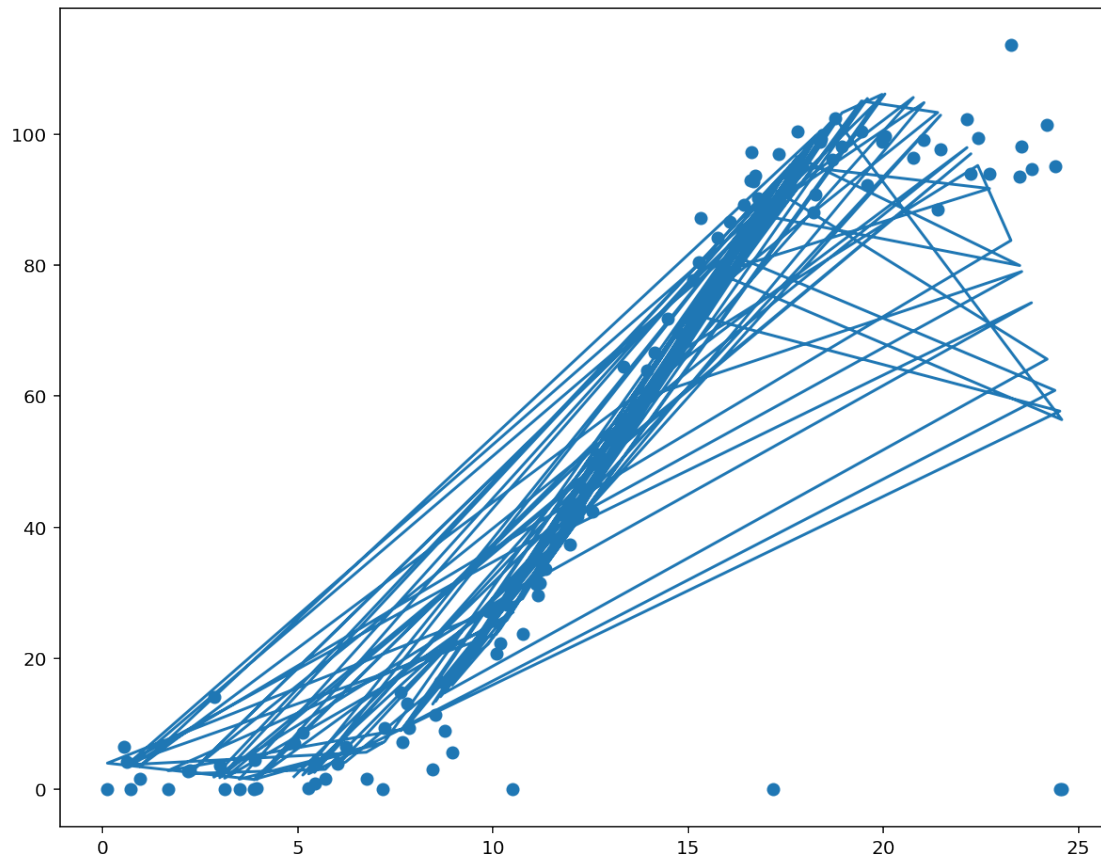
```
[40]: # Visualise the Polynomial Regression Results
      plt.scatter(x_test, y_test, color = 'green')

      plt.plot(x_test, model.predict(poly.fit_transform(x_test)), color = 'blue')
      plt.title('Polynomial Regression')
      plt.xlabel('Age')
      plt.ylabel('Height')

      plt.show()
```

Polynomial Regression

```
[41]: sns.set(style='whitegrid', font_scale=1.1, rc={"figure.figsize": [10, 5]})
      plt.scatter(x_test, y_test, color='grey')
      plt.plot(x_test, y_pred, color='red', linewidth=2)
      plt.grid(b=True, which='major', color='#666666', linestyle='-')
      plt.minorticks_on()
      plt.grid(b=True, which='minor', color='#999999', linestyle='-', alpha=0.2)
      plt.title("Prediction versus Test data", fontsize=15, y=1.012)
      plt.show()
```

Prediction versus Test data
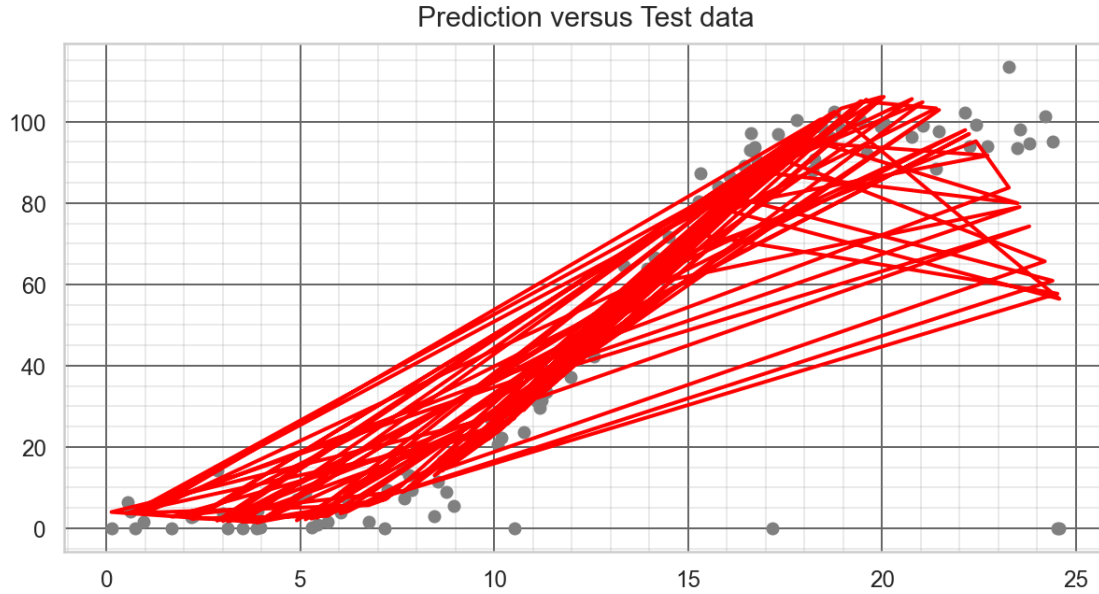
1.10   9.0 References

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