

## Assignment -02

1. Show that the following statements are logically equivalent without using truth tables.

$(p \rightarrow r) \vee (q \rightarrow r)$  and  $(p \wedge q) \rightarrow r$

$p \rightarrow q$  and  $\neg q \rightarrow \neg p$

$(p \rightarrow q) \wedge (p \rightarrow r)$  and  $p \rightarrow (q \wedge r)$

$(p \rightarrow r) \wedge (q \rightarrow r)$  and  $(p \vee q) \rightarrow r$

$\neg p \rightarrow (q \rightarrow r)$  and  $q \rightarrow (p \vee r)$

$(p \wedge \neg q) \vee q$  and  $p \vee q$

2. Constructing new logical equivalences show the following

$p \rightarrow p \vee q$  is a tautology

$(p \wedge q) \rightarrow p$  is a tautology

$[(p \wedge \neg(\neg p \vee q)) \vee (p \wedge q)] \rightarrow p$  is a tautology.