

- Read and attempt to understand Sections 2.8 and 3.1 through 3.3 in the Ross book.
- Continue into Section 3.4 as far as you can (it's 15 pages long).

*Notes: In the 10th edition, this should be Sections 2.9 and 3.1 through 3.3, then 3.4.*

If you roll two 6-sided dice, and you let  $X$  equal the total number of dots shown, what is  $P(X = 4)$ ?

**A**  $\frac{1}{3}$

**B**  $\frac{1}{4}$

**C**  $\frac{1}{6}$

**D**  $\frac{1}{12}$

*Notes: Answer: D. Most of the class obtained this answer. In response to a question, I discussed the reasoning.*

A Bernoulli random variable is a special case of which of the following?

**A** binomial random variable

**B** exponential random variable

**C** geometric random variable

**D** Poisson random variable

*Notes: Answer: A. This is just terminology, and there were several who did not know the answer.*

Which of the following is the probability mass function for a Poisson random variable?

**A**  $p(i) = p(1 - p)^i$

**B**  $p(i) = \binom{n}{i} p^i (1 - p)^{n-i}$

**C**  $p(i) = \frac{\lambda^i}{i!} e^{-\lambda}$

**D**  $p(i) = \frac{1}{n}$

*Notes: Answer: C. We also identified A as geometric, B as binomial, and D as discrete uniform.*

If  $X$  has a continuous distribution, what is true about its cumulative distribution function  $F(x)$ ?

- ☐ A It is strictly increasing.
 ☐ B It is everywhere differentiable.
 ☐ C It integrates to one.
 ☐ D It is continuous.

*Notes: Answer: D. This one was slightly tricky and quite a few people answered A. Also, B was popular, and some said C because they mixed up cumulative distribution function and density function. We saw for a simple example (a uniform cdf) that a continuous cdf need be neither strictly increasing nor everywhere differentiable.*

Which of the following is the probability density function for an exponential random variable?

- ☐ A  $f(i) = \frac{1}{\beta - \alpha}$ 
☐ B  $f(i) = \lambda e^{-\lambda x}$ 
☐ C  $f(i) = \frac{1}{\sigma\sqrt{2\pi}} e^{-(x-\mu)^2/2\sigma^2}$ 
☐ D  $f(i) = \frac{\lambda e^{-\lambda x} (\lambda x)^{\alpha-1}}{\Gamma(\alpha)}$

*Notes: Answer: B. But also notice that D works in the special case  $\alpha = 1$ . We identified D as gamma, A as uniform, and C as normal.*

If  $X$  has a continuous distribution and a density function  $f(x)$ , then  $E(X) = ?$

- ☐ A  $\int_{-\infty}^{\infty} f(x) dx$ 
☐ B  $\int_{-\infty}^{\infty} x f(x) dx$ 
☐ C  $\int_{-\infty}^{\infty} x^2 f(x) dx$ 
☐ D  $\int_{-\infty}^{\infty} (x - \mu) f(x) dx$

*Notes: Answer: B. Most people got this one.*

The variance is...

- ☐ A the expectation of the square.
 ☐ B the square of the expectation.
 ☐ C the expectation of the square
 ☐ D the expectation of the square minus the square of the expectation.

*Notes: Answer: D. Most got this.*

Which is a simpler way to write  $\text{Var}(X) + \text{Var}(Y) + 2\text{Cov}(X, Y)$ ?

- ☐ A  $\text{Var}(X + Y)$       ☐ B  $\text{Corr}(X, Y)$   
☐ C  $E(X + Y)$       ☐ D  $E(X + Y)^2$

Notes: Answer: A. A few weren't sure of this. We didn't spend any time on it, but it's possible to derive this formula without too much difficulty.

If  $X_1, \dots, X_n$  are independent and identically distributed with mean  $\mu$  and variance  $\sigma^2$ ,  $\text{Var } \bar{X}_n = ?$

- ☐ A  $\sigma$       ☐ B  $\sigma/n$   
☐ C  $(\sigma/n)^2$       ☐ D  $\sigma^2/n$

Notes: Answer: D. This is an important one. For instance, it comes up in the proof of the weak law of large numbers using Chebyshev's inequality later.

If a Bernoulli( $p$ ) random variable has MGF  $\phi(t) = 1 - p + pe^t$ , what is the MGF of a binomial( $n, p$ ) random variable?

- ☐ A  $(1 - p + pe^t)^n$       ☐ B  $n(1 - p + pe^t)$   
☐ C  $(1 - np + npe^t)$       ☐ D  $(1 - p + pe^t)/n$

Notes: Answer: A. Most knew it. We discussed moment generating functions for a few minutes.

The inequality  $P(|X - \mu| \geq k) \leq (\sigma/k)^2$  may be used to prove which of the following?

- ☐ A The Strong Law of Large Numbers      ☐ B The Weak Law of Large Numbers  
☐ C The Central Limit Theorem      ☐ D Chebyshev's Inequality

Notes: Answer: B. Few were sure of this. We spent several minutes with the students working together to find a proof of the weak law using Chebyshev's inequality.

If  $X \sim \text{binomial}(100, 1/2)$  and  $\Phi(\cdot)$  is the standard normal cdf, which of the following is the best approximation to  $P(X \leq 50)$ ?

☐ A  $\Phi(0)$

☐ B  $\Phi(0.1)$

☐ C  $\Phi(0.2)$

☐ D  $\Phi(0.3)$

*Notes: Answer: B. I discussed the continuity correction as it applies here; this continuity correction gives a far more accurate approximation than the more naive choice A. (The true value is 0.53979,  $\Phi(0) = 0.5$ , and  $\Phi(0.1) = 0.53983$ .)*