

DECOMPOSING AND CLUSTERING WORLD ECONOMIC FREEDOM CLOUD

ABSTRACT

Economic freedom is the fundamental right of every human to control his or her own labor and property. In an economically free society, individuals are free to work, produce, consume and invest in any way they please. For much of the human history, most individuals have lacked economic freedom and opportunity, condemning them to poverty and deprivation. Therefore, understanding the way these problems emerge is of high importance. To do so, we will use the Economic Freedom index provided by heritage.com covering 12 freedoms—from property rights to financial freedom— in 184 countries.

The index of Economic Freedom documents the positive relationship between economic freedom and a variety of positive social and economic goals. The ideals of economic freedom are strongly associated with healthier societies, cleaner environments, greater per capita wealth, human development, democracy and poverty elimination.

This analysis tries to the partition of 184 countries given by the heritage.org based on their economic freedoms and tries to figure out possible explanations why certain countries are good at it and why some others are not. We make use of the unsupervised statistical technique of Principal Component Analysis in order to decompose the high-dimensional indicator space and evaluate the economic-freedom position of each country after which a Cluster Analysis is performed to demonstrate how countries are grouped in the cloud of economic freedom.

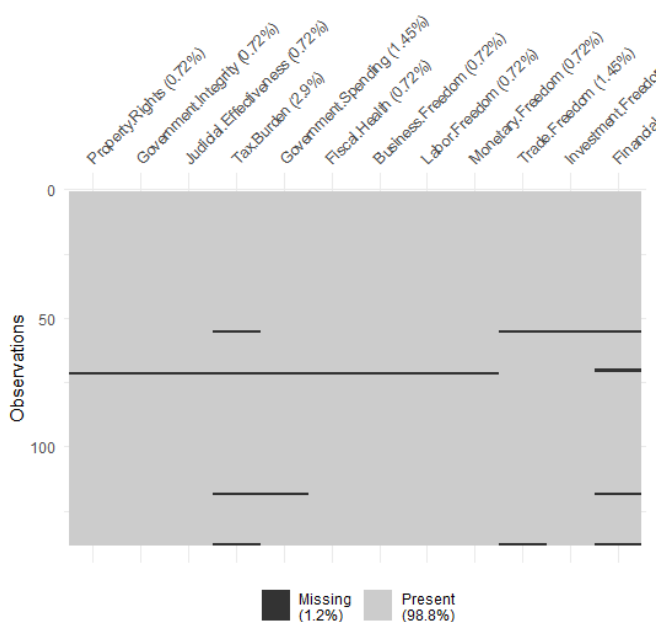
ECONOMIC FREEDOM INDEX STATISTICS

Heritage provides official and reliable data source for measuring Economic Freedom. They measure the economic freedom based on 12 quantitative and qualitative factors, grouped into four broad categories of economic freedom:

1. Rule of Law(property rights, government integrity, judicial effectiveness)
2. Government size(government spending, tax burden, fiscal health)
3. Regulatory Efficiency(business freedom, labor freedom, monetary freedom)
4. Open Markets (trade freedom, investment freedom, financial freedom)

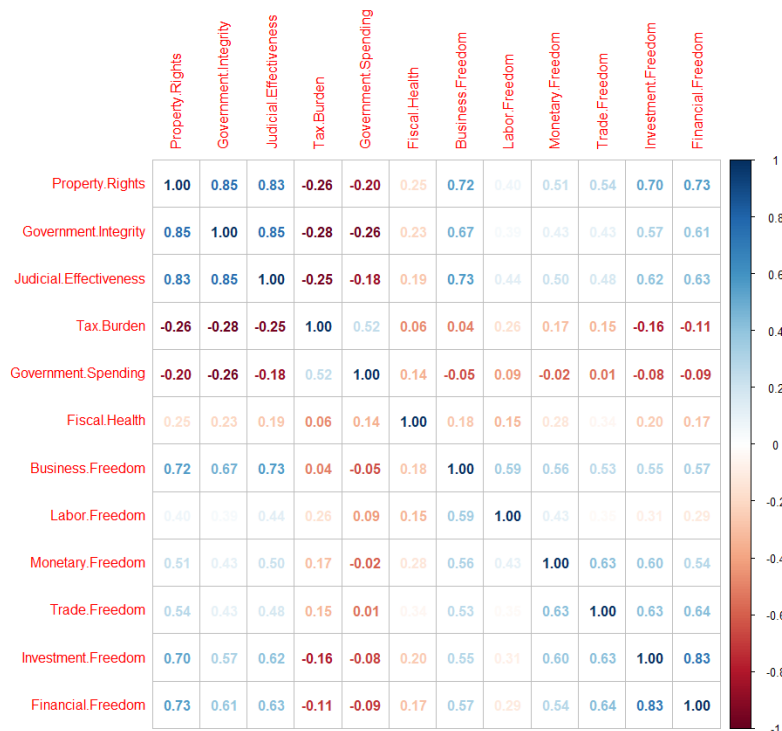
Each of the twelve economic freedoms within these categories is graded on a scale of 0 to 100. A country's overall score is derived by averaging these twelve economic freedoms, with equal weight being given to each.

NAs handling



This plot shows the locations of the missing values in a given row and column. 1.2% of the whole dataset is missing which amounts to only five countries which are Liechtenstein, Yemen, Iraq, Libya and Syria. They are missing because probably it is substantially difficult in these countries to collect the data due to internal conflict that has been going on for years or because they are too small to provide such data(i.e. Liechtenstein). We therefore decided to drop them because it is a negligible part of the whole dataset.

Multicollinearity

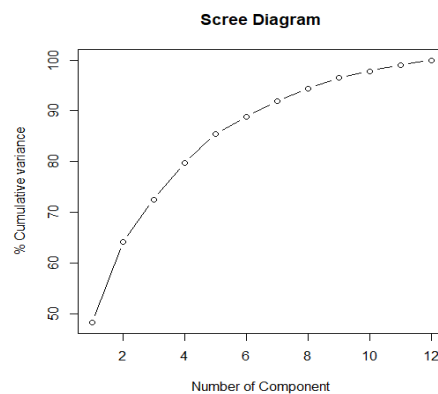
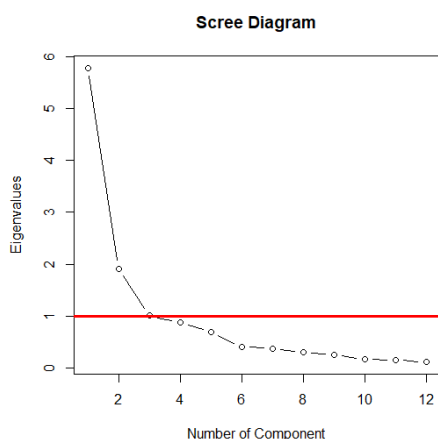


We have a few variables showing multicollinearity caused by the very structure of the dataset. For example, it is highly intuitive the positive relationship between government integrity, property rights and judicial effectiveness since government integrity is a sort of guarantee for such institutions. They are highly related with economic variables as well since such institutions are essential for having economic freedom related to business, investment and finance. We therefore expect to see such variables' loading vectors closely

projected to each other. In particular, government integrity, property rights and judicial effectiveness should set out themselves relatively apart from others in the biplot.

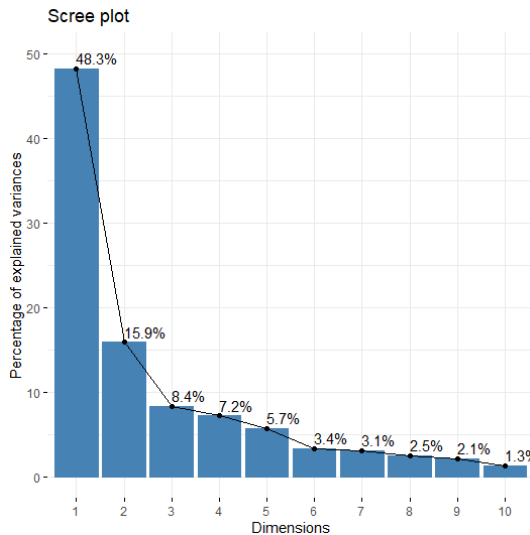
PRINCIPAL COMPONENT ANALYSIS

Here we want to figure out amount of information carried by each country namely its score, collecting all the correlated information contained in whole dataset and shrink it. This is done through the PCA analysis that responds to such aim by reducing the dataset dimension to a few components that are keeping most of the information contained in it. In particular, two is a desirable number of dimensions for graphical applications.



Any principal component with $\lambda > 1$ is able to explain more variance than just one variable. We have three eigenvalues satisfying this condition however the third one is right at the border.

With only two eigenvalues, we are able to explain around 64% of the variability contained in the whole dataset that is good enough for our exploratory purpose.



The first eigenvalue explains over 48% of the variance while the second around 16%.

| Dimensions | eigenvalue | variance.percent | cumulative.variance.percent |
|------------|-------------------|-------------------|-----------------------------|
| Dim.1 | 5.79069043194095 | 48.2557535995079 | 48.2557535995079 |
| Dim.2 | 1.90993354319429 | 15.9161128599524 | 64.1718664594603 |
| Dim.3 | 1.00202912529292 | 8.35024271077434 | 72.5221091702347 |
| Dim.4 | 0.866775199506875 | 7.22312666255729 | 79.745235832792 |
| Dim.5 | 0.685181820492614 | 5.70984850410512 | 85.4550843368971 |
| Dim.6 | 0.404623269607264 | 3.37186058006053 | 88.8269449169576 |
| Dim.7 | 0.370328251812346 | 3.08606876510289 | 91.9130136820605 |
| Dim.8 | 0.297950604407282 | 2.48292170339402 | 94.3959353854545 |
| Dim.9 | 0.254180566923283 | 2.11817139102736 | 96.5141067764819 |
| Dim.10 | 0.159636472374626 | 1.33030393645522 | 97.8444107129371 |
| Dim.11 | 0.148883175148435 | 1.24069312623696 | 99.0851038391741 |
| Dim.12 | 0.109787539299111 | 0.914896160825928 | 100 |

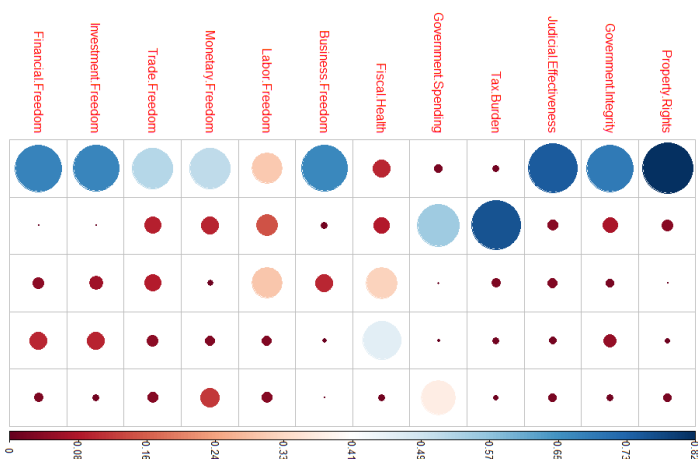
As shown in the table, eigenvalues drop to under 1 after the third component which would add only 8% of variance if included in the analysis.

The sum of all the eigenvalues give a total variance of 12. The proportion of variation explained by each eigenvalue is given in the second column. For example, 5.79 divided by 12 equals to .4825 or about 48.25% of the variation is explained by this first eigenvalue. The cumulative percentage explained is obtained by adding the successive proportions of variation explained to obtain the running total.

RESULTS

We first present the result of correlation circle between the principal components and the features. The correlation between a variable and a principal component (PC) is used as the coordinates of the variable on the PC. The representation of variables differs from the plot of the observations: The observations are represented by their projections but the variables are represented by their correlations.

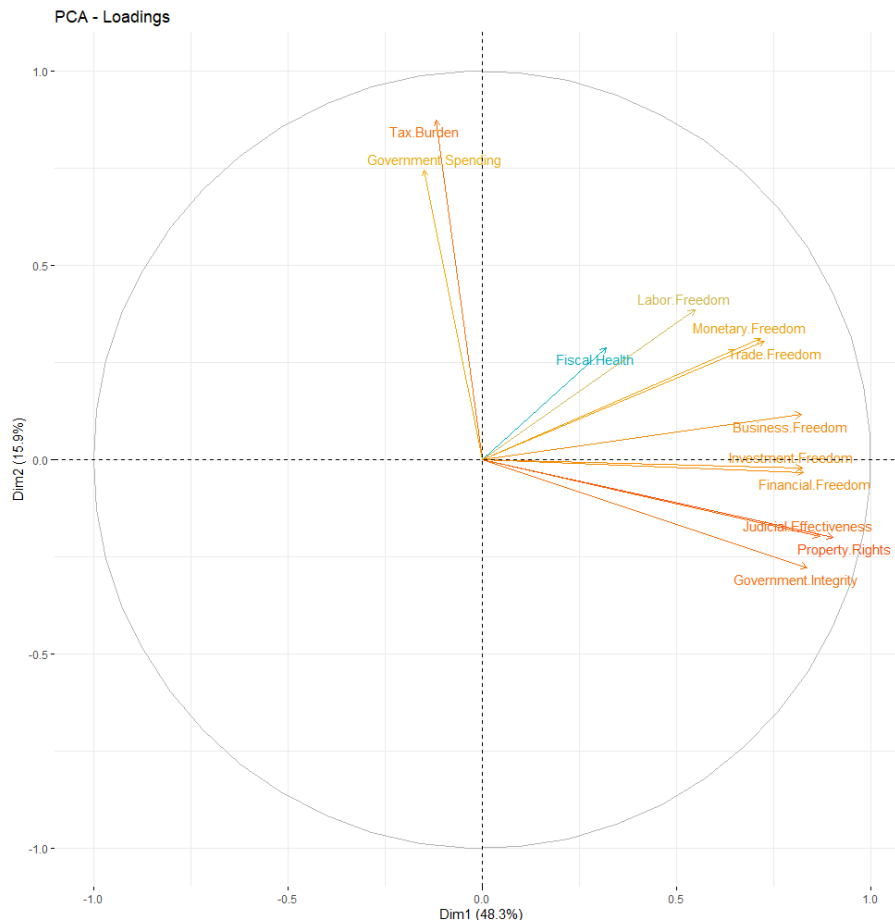
| Indicators | Dim.1 | Dim.2 | Dim.3 | Dim.4 | Dim.5 | communality |
|------------------------|--------------------|----------------------|---------------------|--------------------|---------------------|-------------------|
| Property.Rights | 0.903673894655057 | -0.199297654700422 | -0.0329394664186658 | 0.096284916231259 | 0.152340677986112 | 0.889909538761003 |
| Government.Integrity | 0.837017031409686 | -0.277938625241318 | -0.143384123220817 | 0.225879109500373 | 0.119637429999668 | 0.863740883828326 |
| Judicial.Effectiveness | 0.868275777080463 | -0.197643892687018 | -0.179129223442665 | 0.139802393884063 | 0.14594475637612 | 0.865897793321731 |
| Tax.Burden | -0.117325209980524 | 0.874189471484714 | -0.162671435627019 | -0.121345979332084 | -0.0918252268176782 | 0.827591151900834 |
| Government.Spending | -0.149057771159788 | 0.744714306336731 | 0.044284498432632 | 0.0555510931820532 | 0.607753722868522 | 0.951229245621421 |
| Fiscal.Health | 0.31989104722888 | 0.287628984077428 | 0.564586597897522 | 0.680213772807437 | -0.120511262093742 | 0.981032482112455 |
| Business.Freedom | 0.822653528791828 | 0.116043470168614 | -0.315687673295671 | 0.0874370785588845 | 0.00354046790166395 | 0.797541400093131 |
| Labor.Freedom | 0.547475102316944 | 0.384972279432201 | -0.544431529911246 | 0.176505875259614 | -0.189079621474776 | 0.81124376160788 |
| Monetary.Freedom | 0.717581335306479 | 0.310988104648286 | 0.10711089485726 | -0.175749799573599 | -0.34614018805885 | 0.773810339649662 |
| Trade.Freedom | 0.726463014039094 | 0.304106829186474 | 0.296024394985415 | -0.202707988684592 | -0.18790343968905 | 0.784258148074626 |
| Investment.Freedom | 0.823413930011764 | -0.02171110153624277 | 0.251031430951204 | -0.308154755240311 | 0.121141262923406 | 0.851133206410788 |
| Financial.Freedom | 0.827091338494753 | -0.032066521955178 | 0.207201179255254 | -0.317331600988781 | 0.168766558688518 | 0.85722216904578 |



Here we see how our features are correlated with the given dimensions. The first and most important dimension is highly correlated with all the variables except Fiscal Health, Tax Burden and Government Spending. This dimension seems like an indexed shrunk to only one number showing how a country is developed with respect to its economic policies and democratic institutions. Therefore, we can say being projected on the negative side of the X axis representing the first dimension will show us the poor and economically underdeveloped countries. We expect the

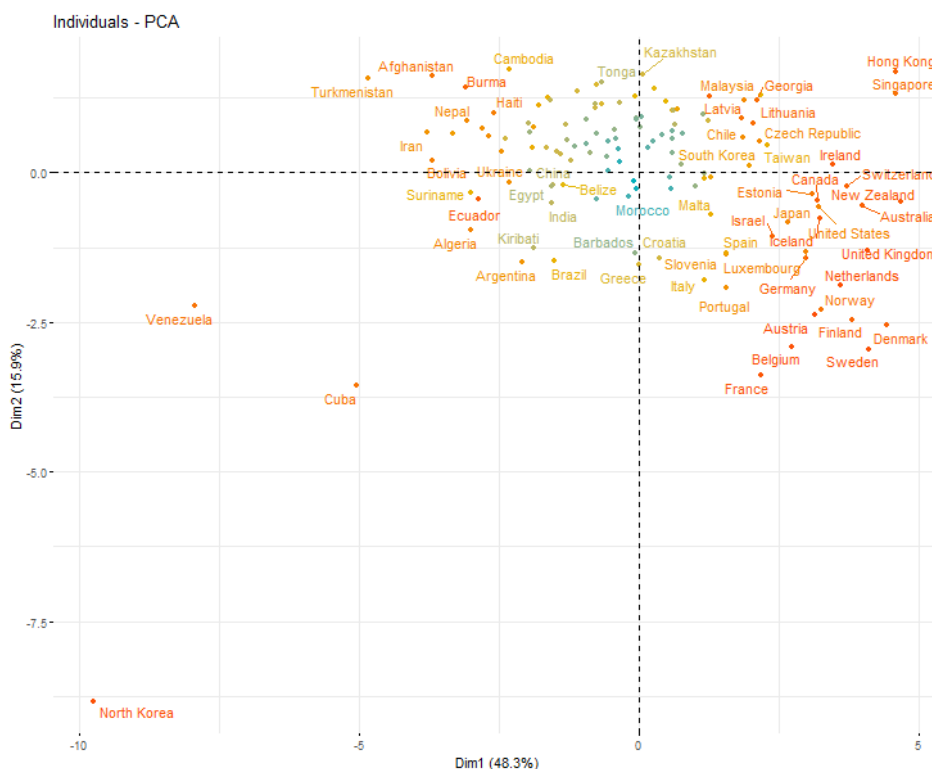
EU countries to cluster around this happy cone. On the other hand, the second PC is highly correlated with Fiscal Health, Tax Burden and Government Spending. So we recover the information that is not contained in

the first PC about these three features of our dataset. This dimension seems to measure the overall democratic and economic problems in a given country. We expect underdeveloped countries to be correlated with this dimension.



As we expected from our multicollinearity, government integrity, judicial effectiveness and property rights show and lie over almost exact the same direction having the highest correlation with the first PC. On the other hand, Tax Burden and Government Spending becoming best friends on the second quadrant well set apart from other features being the infamous features of this index.

Here is the biplot of our PCA result. As expected, many developed EU and non EU countries fall in the happy fourth quadrant having high correlations with the first PC. On the other hand, worst performing countries with respect to



Economic Freedom is on the second quadrant having high Government Spending and Tax Burden. This is really intuitive to understand. Since, in these countries it is substantially difficult to invest and enjoy financial and economic opportunities equally, all the economy seems to be run by government with government spending coming through high taxes. As an example, we can count Afghanistan and Turkmenistan.

