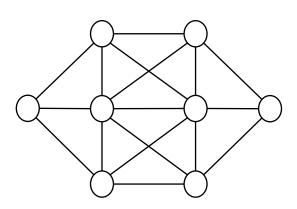


#### The Constraint Satisfaction Problem

Given a set of *variables*  $V = \{X_1, X_2, ..., X_n\}$ , a set of *domains*  $D = \{D_1, D_2, ..., D_n\}$  of allowable values for each variable, and a set of *constraints*  $C = \{C_1, C_2, ..., C_m\}$  restricting the values that groups of variables can take simultaneously,

find an assignment for each variable  $X_i$  of a value  $v_i$  from its domain  $D_i$ , (i.e. an n-tuple  $(v_1, v_2, ..., v_n)$ , where  $v_i \in D_i$ ), so that all constraints are satisfied.



Using only the numbers 1 to 8, put a different number in each circle so that adjacent circles do not have consecutive numbers

### Constraint programming

Modelling: what are the variables, values and constraints?

Searching: guessing values, backtracking on failure

Heuristics: which variable or value to try next

Inference: ruling out options by reasoning

Symmetry: spotting repeat patterns in the problem space

Complexity: understanding the inherent difficulty

Optimisation: are some solutions better than others?

Applications: what real problems can we solve?

Programming: how to implement all of this in programming

languages, so that it is correct and allows us to

find solutions efficiently



#### What is Choco?

Choco is a Free and Open-Source Software [1] dedicated to Constraint Programming [2]. It is a Java library written under BSD license. It aims at describing hard combinatorial problems in the form of Constraint Satisfaction Problems and solving them with Constraint Programming techniques. The user models its problem in a declarative way by stating the set of constraints that need to be satisfied in every solution. Then, Choco solves the problem by alternating constraint filtering algorithms with a search mechanism. Choco is used for:

- · teaching : easy to use
- · research : easy to extend
- real-life applications : easy to integrate

Choco is among the fastest CP solvers on the market. In 2013 and 2014, Choco has been awarded many medals at the MiniZinc challenge that is the world-wide competition of constraint-programming solvers. MiniZinc Challenge 2014 🖈 🖈 🖈
MiniZinc Challenge 2013 🕏

In addition to these performance results, Choco benefits from academic contributors, who provide long term improvements, and the consulting company COSLING, which provides services ranging from training, support to the development of interactive decision support web-services.

- [1]: Choco is hosted on GitHub and distributed under BSD license (Copyright(c) 1999-2015, Ecole des Mines de Nantes).
- [2]: Constraint programming is a technology at the crossroad between Artificial Intelligence and Operational Research, enabling to solve a wide range of complex problems arising in planning, scheduling, logistics, financial analysis, bioinformatics, etc. (read more on wikipedia).

## A very simple problem

Three people have been selected for a job interview: Alice, Bob and Carol. Each interview lasts for 1 hour. Alice is only available at 2pm or 3pm. Bob is only available at 1pm or 2pm. Carol is only available at 1pm or 2pm. Only one person can be interviewed at a time. Find a schedule for the interviews.

Analysis: 3 decisions to be made – a time for each

person -- so three variables?

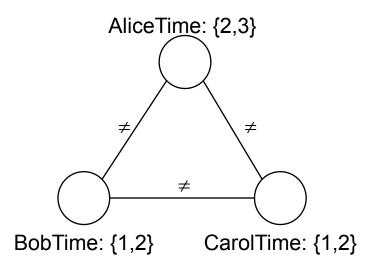
Variables? AliceTime, BobTime, CarolTime

Domains? the hours the people are available

Constraints? for any pair of variables, they must be different

## The very simple CSP

```
V = { AliceTime,
     BobTime,
     CarolTime
D = \{ \{2,3\}, //Alice \}
     {1,2}, //Bob
     {1,2} //Carol
C = \{AliceTime \neq BobTime, \}
    AliceTime ≠ CarolTime,
     BobTime ≠ CarolTime
```



AliceTime  $\neq$ BobTime  $\subseteq \{2,3\} \times \{1,2\}$ 

 $\{(2,1),(3,1),(3,2)\}$ 

## The Choco process

- 1. Create a solver object
- 2. Create the variables and their domains
- 3. Create the constraints and post to the solver
- 4. Specify a search strategy (or take the default)
- 5. Start the solving process
- 6. Print the results

```
import org.chocosolver.solver.Solver;
import org.chocosolver.solver.constraints.IntConstraintFactory;
import org.chocosolver.solver.trace.Chatterbox;
                                                         The Choco program
import org.chocosolver.solver.variables.IntVar;
import org.chocosolver.solver.variables.VariableFactory;
public class SimpleCSP {
   public static void main(String[] args) {
      //create a solver object that will solve the problem for us
      Solver solver = new Solver();
      //create the variables and domains for the problem, and add to the solver
      IntVar AliceTime = VariableFactory.enumerated("Alice time", 2, 3, solver);
      IntVar BobTime = VariableFactory.enumerated("Bob time", 1, 2, solver);
      IntVar CarolTime = VariableFactory.enumerated("Carol time", 1, 2, solver);
      //create the constraints
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", BobTime));
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", CarolTime));
      solver.post(IntConstraintFactory.arithm(BobTime, "!=", CarolTime));
       //use a pretty print object to display the results
       Chatterbox.showSolutions(solver); //just show the final result
       //ask the solver to find a solution
       solver.findSolution();
       //print out the search statistics
       Chatterbox.printStatistics(solver);
```

```
import org.chocosolver.solver.Solver;
import org.chocosolver.solver.constraints.IntConstraintFactory;
import org.chocosolver.solver.trace.Chatterbox;
import org.chocosolver.solver.variables.IntVar;
import org.chocosolver.solver.variables.VariableFactory;
                                                         packages required
public class SimpleCSP {
                                                         for this program
   public static void main(String[] args) {
      //create a solver object that will solve the problem for us
      Solver solver = new Solver();
      //create the variables and domains for the problem, and add to the solver
      IntVar AliceTime = VariableFactory.enumerated("Alice time", 2, 3, solver);
      IntVar BobTime = VariableFactory.enumerated("Bob time", 1, 2, solver);
      IntVar CarolTime = VariableFactory.enumerated("Carol time", 1, 2, solver);
      //create the constraints
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", BobTime));
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", CarolTime));
      solver.post(IntConstraintFactory.arithm(BobTime, "!=", CarolTime));
       //use a pretty print object to display the results
       Chatterbox.showSolutions(solver); //just show the final result
       //ask the solver to find a solution
       solver.findSolution();
       //print out the search statistics
       Chatterbox.printStatistics(solver);
```

```
import org.chocosolver.solver.Solver;
import org.chocosolver.solver.constraints.IntConstraintFactory;
import org.chocosolver.solver.trace.Chatterbox;
import org.chocosolver.solver.variables.IntVar;
import org.chocosolver.solver.variables.VariableFactory;
public class SimpleCSP {
                                                         create the solver
   public static void main(String[] args) {
      //create a solver object that will solve the problem for us
      Solver solver = new Solver();
      //create the variables and domains for the problem, and add to the solver
      IntVar AliceTime = VariableFactory.enumerated("Alice time", 2, 3, solver);
      IntVar BobTime = VariableFactory.enumerated("Bob time", 1, 2, solver);
      IntVar CarolTime = VariableFactory.enumerated("Carol time", 1, 2, solver);
      //create the constraints
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", BobTime));
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", CarolTime));
      solver.post(IntConstraintFactory.arithm(BobTime, "!=", CarolTime));
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       //ask the solver to find a solution
       solver.findSolution();
       //print out the search statistics
       Chatterbox.printStatistics(solver);
```

```
import org.chocosolver.solver.Solver;
import org.chocosolver.solver.constraints.IntConstraintFactory;
import org.chocosolver.solver.trace.Chatterbox;
                                                           VariableFactory creates the
import org.chocosolver.solver.variables.IntVar;
import org.chocosolver.solver.variables.VariableFactory;
                                                          variables for us.
                                                           They have integer values,
public class SimpleCSP {
                                                           so we use "IntVar".
                                                          Add them to the solver.
   public static void main(String[] args) {
      //create a solver object that will solve the problem for us
      Solver solver = new Solver();
      //create the variables and domains for the problem, and add to the solver
      IntVar AliceTime = VariableFactory.enumerated("Alice time", 2, 3, solver);
      IntVar BobTime = VariableFactory.enumerated("Bob time", 1, 2, solver);
       IntVar CarolTime = VariableFactory.enumerated("Carol time", 1, 2, solver);
       //create the constraints
       solver.post(IntConstraintFactory.arithm(AliceTime, "!=", BobTime));
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", CarolTime));
       solver.post(IntConstraintFactory.arithm(BobTime, "!=", CarolTime));
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       solver.findSolution();
       //print out the search statistics
       Chatterbox.printStatistics(solver);
```

```
import org.chocosolver.solver.constraints.IntConst
                                                  Place all numbers between a
import org.chocosolver.solver.trace.Chatterbox;
                                                  lower and upper bound into
import org.chocosolver.solver.variables.IntVar;
import org.chocosolver.solver.variables.VariableF& the domain
public class SimpleCSP {
   public static void main(String[] args) {
      //create a solver object that will solve the problem for us
      Solver solver = new Solver();
      //create the variables and domains for the problem, and add to the solver
      IntVar AliceTime = VariableFactory.enumerated("Alice time", 2, 3, solver);
      IntVar BobTime = VariableFactory.enumerated("Bob time", 1, 2, solver);
      IntVar CarolTime = VariableFactory.enumerated("Carol time", 1, 2, solver);
      //create the constraints
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", BobTime));
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", CarolTime));
      solver.post(IntConstraintFactory.arithm(BobTime, "!=", CarolTime));
       //use a pretty print object to display the results
       Chatterbox.showSolutions(solver); //just show the final result
       //ask the solver to find a solution
       solver.findSolution();
       //print out the search statistics
       Chatterbox.printStatistics(solver);
```

import org.chocosolver.solver.Solver;

```
import org.chocosolver.solver.constraints.IntConst
                                                   IntConstraintFactory creates
import org.chocosolver.solver.trace.Chatterbox;
                                                   the constraints, and we post
import org.chocosolver.solver.variables.IntVar;
import org.chocosolver.solver.variables.VariableFathem to the solver.
public class SimpleCSP {
   public static void main(String[] args) {
      //create a solver object that will solve the problem for us
      Solver solver = new Solver();
      //create the variables and domains for the problem, and add to the solver
      IntVar AliceTime = VariableFactory.enumerated("Alice time", 2, 3, solver);
      IntVar BobTime = VariableFactory.enumerated("Bob time", 1, 2, solver);
      IntVar CarolTime = VariableFactory.enumerated("Carol time", 1, 2, solver);
      //create the constraints
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", BobTime));
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", CarolTime));
      solver.post(IntConstraintFactory.arithm(BobTime, "!=", CarolTime));
       //use a pretty print object to display the results
       Chatterbox.showSolutions(solver); //just show the final result
       //ask the solver to find a solution
       solver.findSolution();
       //print out the search statistics
       Chatterbox.printStatistics(solver);
```

import org.chocosolver.solver.Solver;

```
import org.chocosolver.solver.Solver;
import org.chocosolver.solver.constraints.IntConstraintFactory;
import org.chocosolver.solver.trace.Chatterbox;
import org.chocosolver.solver.variables.IntVar;
import org.chocosolver.solver.variables.VariableF&
                                                   The constraint is of type
                                                   arithmetic (because we are
public class SimpleCSP {
                                                   dealing with numbers)
   public static void main(String[] args) {
      //create a solver object that will solve the problem for xs
      Solver solver = new Solver();
      //create the variables and domains for the problem / and add to the solver
      IntVar AliceTime = VariableFactory.enumerated("Alice time", 2, 3, solver);
      IntVar BobTime = VariableFactory.enumerated("Bob time", 1, 2, solver);
      IntVar CarolTime = VariableFactory.enumerate("Carol time", 1, 2, solver);
      //create the constraints
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", BobTime));
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", CarolTime));
      solver.post(IntConstraintFactory.arithm(BobTime, "!=", CarolTime));
       //use a pretty print object to display the results
       Chatterbox.showSolutions(solver); //just show the final result
       //ask the solver to find a solution
       solver.findSolution();
       //print out the search statistics
       Chatterbox.printStatistics(solver);
```

```
import org.chocosolver.solver.constraints.IntConst
                                                   We will use the default search
import org.chocosolver.solver.trace.Chatterbox;
                                                   method, so don't need to do
import org.chocosolver.solver.variables.IntVar;
import org.chocosolver.solver.variables.VariableFaanything for that.
public class SimpleCSP {
   public static void main(String[] args) {
      //create a solver object that will solve the problem for us
      Solver solver = new Solver();
      //create the variables and domains for the problem, and add to the solver
      IntVar AliceTime = VariableFactory.enumerated("Alice time", 2, 3, solver);
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       IntVar CarolTime = VariableFactory.enumerated("Carol time", 1, 2, solver);
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       solver.post(IntConstraintFactory.arithm(AliceTime, "!=", BobTime));
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", CarolTime));
       solver.post(IntConstraintFactory.arithm(BobTime, "!=", CarolTime));
       //use a pretty print object to display the results
       Chatterbox.showSolutions(solver); //just show the final result
       //ask the solver to find a solution
       solver.findSolution();
       //print out the search statistics
       Chatterbox.printStatistics(solver);
```

import org.chocosolver.solver.Solver;

```
import org.chocosolver.solver.Solver;
import org.chocosolver.solver.constraints.IntConst
                                                   Start preparing the output -
import org.chocosolver.solver.trace.Chatterbox;
                                                   we want the final result
import org.chocosolver.solver.variables.IntVar;
import org.chocosolver.solver.variables.VariableFactory;
public class SimpleCSP {
   public static void main(String[] args) {
      //create a solver object that will solve the problem for us
      Solver solver = new Solver();
      //create the variables and domains for the problem, and add to the solver
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      //create the constraints
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", BobTime));
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", CarolTime));
      solver.post(IntConstraintFactory.arithm(BobTime, "!=", CarolTime));
       //use a pretty print object to display the results
       Chatterbox.showSolutions(solver); //just show the final result
       //ask the solver to find a solution
       solver.findSolution();
       //print out the search statistics
       Chatterbox.printStatistics(solver);
```

```
import org.chocosolver.solver.Solver;
import org.chocosolver.solver.constraints.IntConst

Go find the solution
import org.chocosolver.solver.trace.Chatterbox;
import org.chocosolver.solver.variables.IntVar;
import org.chocosolver.solver.variables.VariableFactory;
public class SimpleCSP {
   public static void main(String[] args) {
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       IntVar CarolTime = VariableFactory.enymerated("Carol time", 1, 2, solver);
       //create the constraints
       solver.post(IntConstraintFactory/arithm(AliceTime, "!=", BobTime));
       solver.post(IntConstraintFactory.arithm(AliceTime, "!=", CarolTime));
       solver.post(IntConstraintFactory.arithm(BobTime, "!=", CarolTime));
       //use a pretty print object to display the results
       Chatterbox.showSolutions(solver); //just show the final result
       //ask the solver to find a solution
       solver.findSolution();
       //print out the search statistics
       Chatterbox.printStatistics(solver);
```

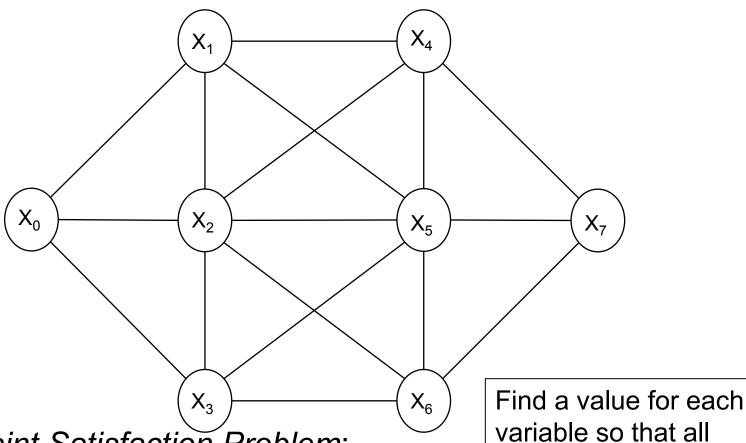
```
import org.chocosolver.solver.Solver;
import org.chocosolver.solver.constraints.IntConst
                                                   Tell us how much work it
import org.chocosolver.solver.trace.Chatterbox;
                                                   required
import org.chocosolver.solver.variables.IntVar;
import org.chocosolver.solver.variables.VariableFactory;
public class SimpleCSP {
   public static void main(String[] args) {
      //create a solver object that will solve the problem for us
      Solver solver = new Solver();
      //create the variables and domains for the problem, and add to the solver
      IntVar AliceTime = VariableFactory.enumerated("Alice time", 2, 3, solver);
      IntVar BobTime = VariableFactory.enumerated("Bob time", 1, 2, solver);
      IntVar CarolTime = VariableFactory.enumerat d("Carol time", 1, 2, solver);
      //create the constraints
      solver.post(IntConstraintFactory.arithm/AliceTime, "!=", BobTime));
      solver.post(IntConstraintFactory.arithm(AliceTime, "!=", CarolTime));
      solver.post(IntConstraintFactory.arithm(BobTime, "!=", CarolTime));
       //use a pretty print object to display the results
       Chatterbox.showSolutions(solver); //just show the final result
       //ask the solver to find a solution
       solver.findSolution();
       //print out the search statistics
       Chatterbox.printStatistics(solver);
```

```
- Solution #1 found. Solver[Solver-0], 1 Solutions, Resolution time 0.022s, 3 Nodes
(139.4 n/s), 1 Backtracks, 1 Fails, 0 Restarts
        Alice time = 3 Bob time = 2 Carol time = 1.
** Choco 3.3.3 (2015-12) : Constraint Programming Solver, Copyleft (c) 2010-2015
- Solver[Solver-0] features:
        Variables: 3
        Constraints : 3
        Default search strategy: yes
        Completed search strategy: no
- Complete search - 1 solution found.
        Solver[Solver-0]
        Solutions: 1
        Building time: 0.165s
        Resolution time : 0.100s
        Nodes: 3 (29.9 n/s)
        Backtracks: 1
        Fails: 1
        Restarts: 0
        Variables: 3
        Constraints: 3
```

```
- Solution #1 found. Solver[Solver-0], 1 Solutions, Resolution time 0.022s, 3 Nodes
(139.4 n/s), 1 Backtracks, 1 Fails, 0 Restarts
        Alice time = 3 Bob time = 2 Carol time = 1.
** Choco 3.3.3 (2015-12) : Constraint Programming Solver, Copyleft (c) 2010-2015
- Solver[Solver-0] features:
        Variables: 3
        Constraints: 3
        Default search strategy : yes
        Completed search strategy: no
                                                 The solution
- Complete search - 1 solution found.
        Solver[Solver-0]
        Solutions: 1
        Building time: 0.165s K
        Resolution time : 0.100s
        Nodes: 3 (29.9 n/s)
        Backtracks: 1
        Fails: 1
        Restarts: 0
```

Variables: 3
Constraints: 3

The search statistics



A Constraint Satisfaction Problem:

Variables:  $\{X_0, X_1, X_2, X_3, X_4, X_5, X_6, X_7\}$ 

Values: {1,2,3,4,5,6,7,8}

Constraints: {alldifferent( $\{X_0, X_1, X_2, X_3, X_4, X_5, X_6, X_7\}$ ), ...,  $|X_0-X_1|>1$ ,  $|X_0-X_2|>1$ , ...}

constraints are satisfied

simultaneously

```
public static void main(String[] args) {
   //create a solver object that will solve the problem for us
    Solver solver = new Solver();
   //create the variables and domains for the problem, and add to the solver
   IntVar[] places = VariableFactory.enumeratedArray("places", 8, 1, 8, solver);
   //now create and post the constraints
   //use the built-in global constraint to say that they are all different
   solver.post(IntConstraintFactory.alldifferent(places));
   //then add the edge constraints
   solver.post(IntConstraintFactory.distance(places[0], places[1],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[0], places[2],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[0], places[3],
                                                                    ">", 1));
   solver.post(IntConstraintFactory.distance(places[1], places[2],
                                                                     ">", 1));
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[1], places[4],
   solver.post(IntConstraintFactory.distance(places[1], places[5],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[2], places[3],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[2], places[4],
                                                                    ">", 1));
   solver.post(IntConstraintFactory.distance(places[2], places[5],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[2], places[6],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[3], places[5],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[3], places[6],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[4], places[5],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[4], places[7],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[5], places[6],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[5], places[7],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[6], places[7],
                                                                     ">", 1));
```

```
public static void main(String[] args) {
    //create a solver object that will solve the problem for us
    Solver solver = new Solver();

    //create the variables and domains for the problem, and add to the solver
    IntVar[] places = VariableFactory.enumeratedArray("places", 8, 1, 8, solver);

    //now create and post the constraints

    //use the built-in global constrain
    solver.post(IntConstraintFactory.al
    IntVars with domain {1,2,3,...,8}
```

```
//then add the edge constraints
solver.post(IntConstraintFactory.distance(places[0], places[1],
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[0], places[2],
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[0], places[3],
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[1], places[2],
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[1], places[4],
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[1], places[5],
                                                                 ">", 1));
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[2], places[3],
solver.post(IntConstraintFactory.distance(places[2], places[4],
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[2], places[5],
                                                                 ">", 1));
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[2], places[6],
solver.post(IntConstraintFactory.distance(places[3], places[5],
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[3], places[6],
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[4], places[5],
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[4], places[7],
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[5], places[6],
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[5], places[7],
                                                                 ">", 1));
solver.post(IntConstraintFactory.distance(places[6], places[7],
                                                                 ">", 1));
```

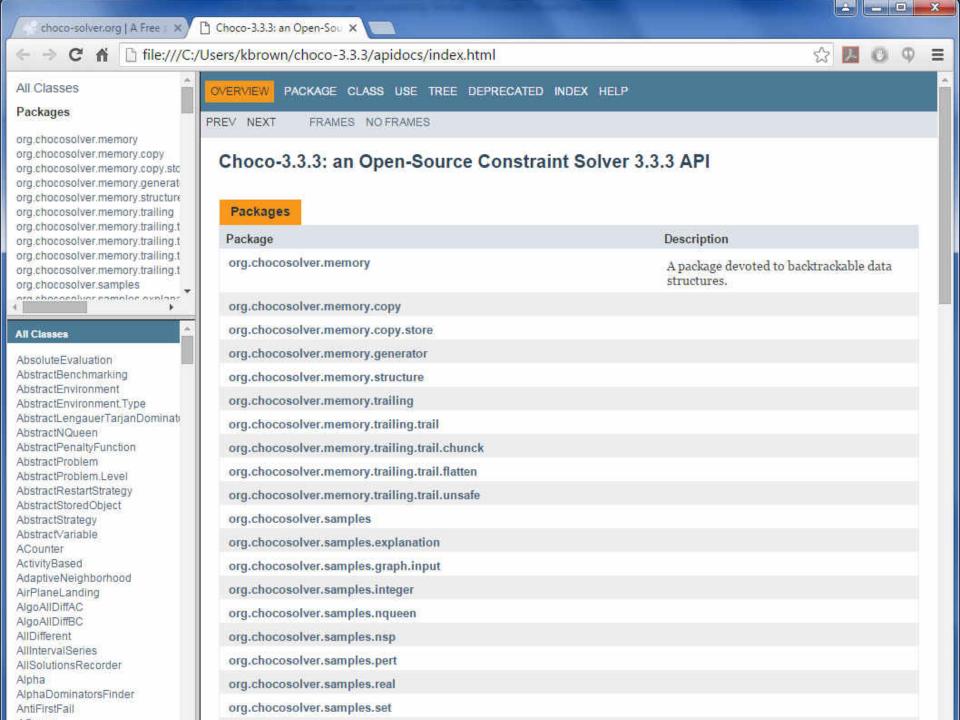
```
public static void main(String[] args) {
   //create a solver object that will solv
                                            alldifferent(vars) is easier to express
    Solver solver = new Solver();
                                           than nested loops of xi≠xj.
   //create the variables and domains for
                                            More importantly, the solver can do
   IntVar[] places = VariableFactory.enume
                                           deeper reasoning.
   //now create and post the constraints
   //use the built-in global constraint to say that they are all different
   solver.post(IntConstraintFactory.alldifferent(places));
   //then add the edge constraints
   solver.post(IntConstraintFactory.distance(places[0], places[1],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[0], places[2],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[0], places[3],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[1], places[2],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[1], places[4],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[1], places[5],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[2], places[3],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[2], places[4],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[2], places[5],
                                                                     ">", 1));
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[2], places[6],
   solver.post(IntConstraintFactory.distance(places[3], places[5],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[3], places[6],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[4], places[5],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[4], places[7],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[5], places[6],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[5], places[7],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[6], places[7],
                                                                     ">", 1));
```

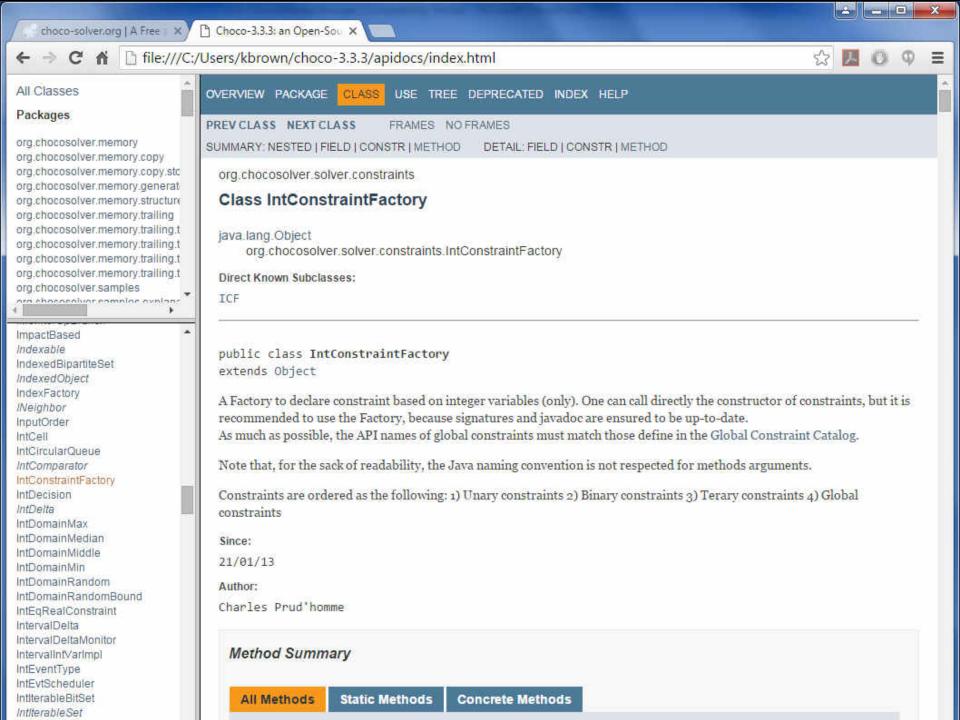
```
public static void main(String[] args) {
   //create a solver object that will solv
                                            distance(X,Y,Rel,Z) is |X-Y| Rel Z
    Solver solver = new Solver();
                                           so this says
   //create the variables and domains for
   IntVar[] places = VariableFactory.enume
                                            | places[0]-places[1] | > 1
   //now create and post the constraints
   //use the built-in global constraint to (i.e. cannot be consecutive)
   solver.post(IntConstraintFactory.alldifferent(places));
   //then add the edge constraints
   solver.post(IntConstraintFactory.distance(places[0], places[1],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[0], places[2],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[0], places[3],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[1], places[2],
                                                                     ">", 1));
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[1], places[4],
   solver.post(IntConstraintFactory.distance(places[1], places[5],
                                                                     ">", 1));
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[2], places[3],
   solver.post(IntConstraintFactory.distance(places[2], places[4],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[2], places[5],
                                                                     ">", 1));
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[2], places[6],
   solver.post(IntConstraintFactory.distance(places[3], places[5],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[3], places[6],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[4], places[5],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[4], places[7],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[5], places[6],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[5], places[7],
                                                                     ">", 1));
   solver.post(IntConstraintFactory.distance(places[6], places[7],
                                                                     ">", 1));
```

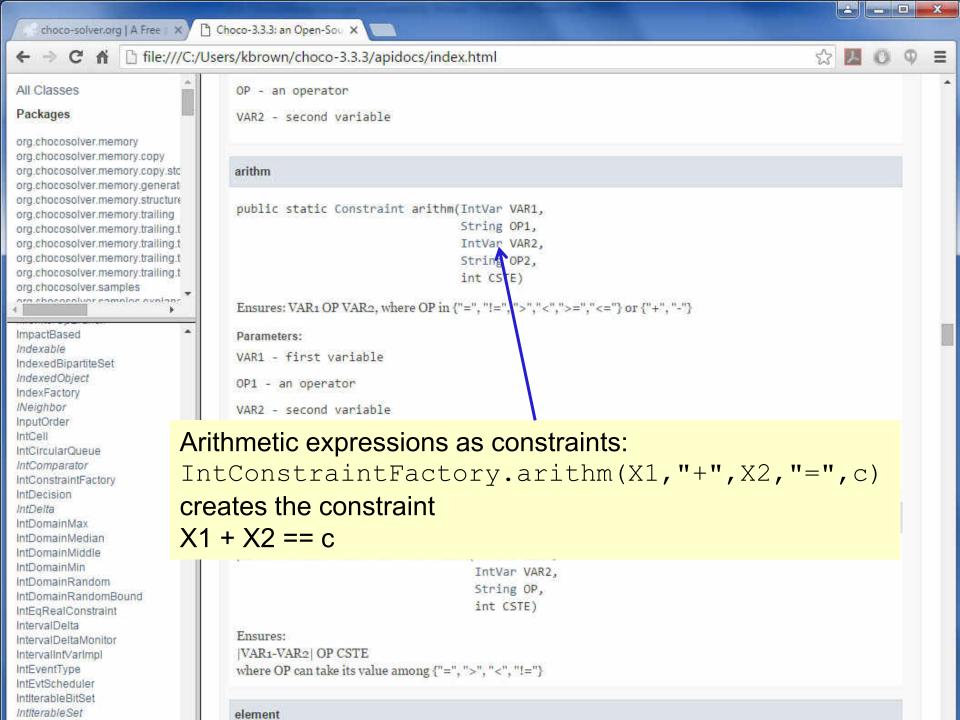
```
//set a search strategy
   solver.set(IntStrategyFactory.domOverWDeg(places, 0));
   //Decide what to display in the output
    Chatterbox.showSolutions(solver);
    //solve the problem (and the Chatterbox will display some output)
    solver.findSolution();
    //display the search statistics
    Chatterbox.printStatistics(solver);
- Solution #1 found. 1 Solutions, Resolution 0.012s, 8 Nodes, 6 Backtracks, 5 Fails
   places[0] = 2 places[1] = 5 places[2] = 8 places[3] = 6 places[4] = 3 places[5]
= 1 \text{ places}[6] = 4 \text{ places}[7] = 7.
- Complete search -
   Solutions: 1
   Building time: 0.101s
   Initialisation: 0.000s
   Initial propagation: 0.004s
   Resolution: 0.017s
   Nodes: 8
   Backtracks: 6
   Fails: 5
   Restarts: 0
   Max depth: 6
   Propagations: 247 + 0
   Memory: Omb
   Variables: 10
```

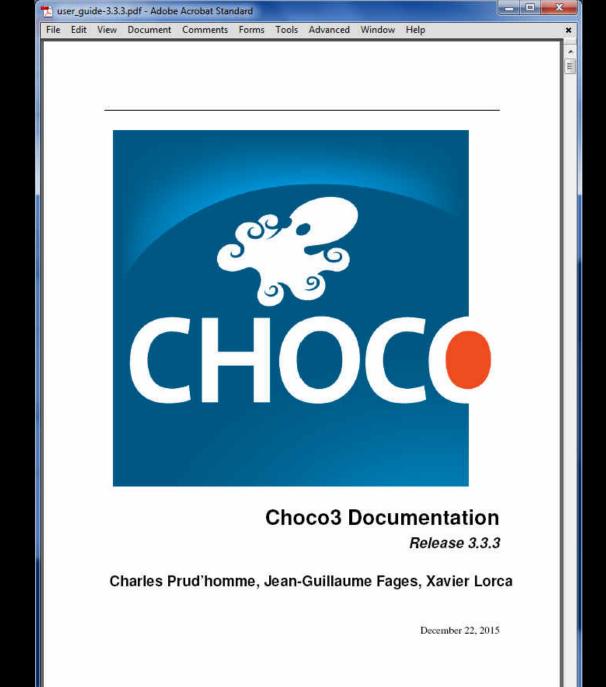
Constraints: 18

```
//set a search strategy
   solver.set(IntStrategyFactory.domOverWDeg(places, 0));
   //Decide what to display in the output
    Chatterbox. showSolutions (solver);
                                         tell the solver which search strategy
    //solve the problem (and the Chatte
                                         to use
    solver.findSolution();
    //display the search statistics
    Chatterbox.printStatistics(solver);
- Solution #1 found. Solver[Solver-0], 1 Solutions, Resolution time 0.013s, 8 Nodes
(637.4 n/s), 6 Backtracks, 5 Fails, 0 Restarts
   places[0] = 2 places[1] = 5 places[2] = 8 places[3] = 6 places[4] = 3 places[5]
= 1 \text{ places}[6] = 4 \text{ places}[7] = 7.
- Complete search - 1 solution found.
   Solver[Solver-0]
   Solutions: 1
   Building time: 0.131s
   Resolution time: 0.044s
   Nodes: 8 (183.5 n/s)
   Backtracks: 6
   Fails: 5
   Restarts: 0
   Variables: 8
   Constraints: 18
```









| I Preliminaries   |
|---|
| I Preliminaries   3   |
| 4   Declaring variables   21   4.1   Principle   21   4.2   Integer variable   21   4.3   Constants   23   4.4   Variable views   23   4.5   Set variable   24   4.6   Real variable   24   4.6   Real variable   25   5.1   Principle   25   5.2   Posting constraints   27   5.3   Reifying constraints   28   28 |
|   |

#### **Exercise:**

(Make sure Java is on your system)
(Make sure Eclipse is on your system)
Download and install Choco as an Eclipse project

Model and solve the following problem:

$$V = \{V1,V2,V3,V4\}$$

$$D = \{1,2,3,4,5\} \text{ for each var }$$

$$C = \{V1 \le V4-1, \\ V1 < V2, \\ V2 + V3 > 6, \\ V2 + V4 = 5, \\ V4 < V3\}$$

Choco

# Setting up Eclipse with Choco on Windows

Choco: http://choco-solver.org/

Download choco 3.3.3, and unzip. Then unzip apidocs.zip Make sure you have Java 1.8 JDK installed Make sure you have Eclipse installed (I use Luna 4.4.2)

In Eclipse, create a new project (e.g. *CS4093*) Select the project (CS4093),

right-click, Build Path / Configure Build Path / Libraries / Add External Jars ...

browse to your choco folder and select it, select choco-solver...dependencies.jar, then OK

In PackageExplorer/CS4093/Referenced Libraries,

right-click the jar file / Properties /Java Source Attachment / External Location, browse to choco folder, select choco-solver...sources.jar, OK

In PackageExplorer/CS4093/Referenced Libraries,

right-click the jar file / Properties / Javadoc Location / Javadoc URL,

browse to Choco folder, apidocs subfolder, OK

In PackageExplorer/CS4093/src, create a new class, and start coding

Next lecture ...

modeling