

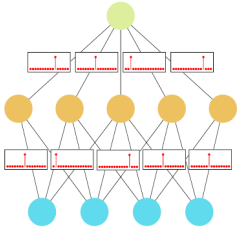
# Uncertainty quantification in Bayesian Neural Networks using cubature rules

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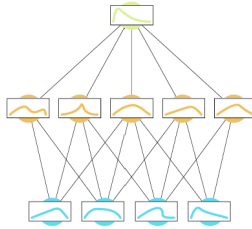
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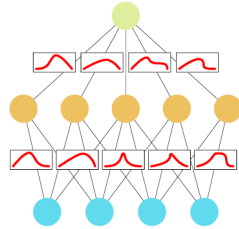
- ① Bayesian neural networks
- ② Uncertainty quantification
- ③ Applications
- ④ supplementary



(a)



(b)



(c)

# Bayesian Neural Networks

What is a Bayesian Neural Network?

A Bayesian Neural Network is a neural networks where the learnable parameters  $\theta_i$  **are probability distributions** instead of scalars.

e.g. the weights could be Normal distributed like so,

$$w_i = \mathcal{N}(\mu_i, \sigma_i^2) \quad (1)$$

- The activation functions could be stochastic too!
- **Ensemble learning** takes place in a BNN by letting the model train with multiple distributions of the learnable parameters  $\theta$

## How does it work?

- Choose a **Stochastic model** i.e. prior distributions for  $p(\theta)$  and  $p(\mathbf{y}|\mathbf{x}, \theta)$
- Obtain the posterior probability

$$p(\theta|D) = \frac{p(D_y|D_x, \theta)p(\theta)}{\int_{\theta} p(D_y|D_x, \theta')p(\theta')d\theta'} \quad (2)$$

where,

$D_y$  = Data labels

$D_x$  = Data inputs

- Computing the integral,  $\int_{\theta} p(D_y|D_x, \theta')p(\theta')d\theta'$  is very difficult.
- To address this, two broad approaches are followed:
  - 1 MCMC (Markov chain monte carlo)
  - 2 Variational inference

# Bayesian Neural Networks

## Motivation

The main goal is to get a better idea about the **uncertainty**. For example, if all the results of the models are vastly different, there's more uncertainty thereby providing a way to *preemptively* assess **generalizability**.

# Uncertainty quantification

Some techniques:

- Particle filtering
- Variational inference
- Cubature rules\*
- and so on...





Part 1: Dealing with the of **Stochastic elements of Neural Gas** ?

- Input sampling
- Control elements: Decay rate, learning rate

Part 2: Extending Probability theory to Neural Gas for other purposes

- Estimating Population distribution