Social network Graph Link Prediction - Facebook Challenge

```
1 #Importing Libraries
In [0]:
           # please do go through this python notebook:
           import warnings
           warnings.filterwarnings("ignore")
            import csv
            import pandas as pd#pandas to create small dataframes
         8 import datetime #Convert to unix time
           import time #Convert to unix time
        10 # if numpy is not installed already : pip3 install numpy
        11 import numpy as np#Do aritmetic operations on arrays
        12 # matplotlib: used to plot graphs
        13 import matplotlib
        14 import matplotlib.pylab as plt
        15 import seaborn as sns#Plots
        16 from matplotlib import rcParams#Size of plots
        17 from sklearn.cluster import MiniBatchKMeans, KMeans#Clustering
        18 import math
        19 import pickle
        20 import os
        21 # to install xgboost: pip3 install xgboost
        22 import xqboost as xqb
        23
        24 import warnings
        25 import networkx as nx
        26 import pdb
        27 import pickle
        28 from pandas import HDFStore, DataFrame
        29 from pandas import read hdf
        30 from scipy.sparse.linalg import svds, eigs
        31 import qc
        32 from tqdm import tqdm
```

1. Reading Data

Name:

Type: DiGraph

Number of nodes: 1780722 Number of edges: 7550015 Average in degree: 4.2399 Average out degree: 4.2399

2. Similarity measures

2.1 Jaccard Distance:

http://www.statisticshowto.com/jaccard-index/ (http://www.statisticshowto.com/jaccard-index/)

$$j = \frac{|X \cap Y|}{|X \cup Y|}$$

```
In [0]:
            #for followees
            def jaccard for followees(a,b):
          3
                     if len(set(train graph.successors(a))) == 0 | len(set(train graph.successors(b))) == 0:
          4
          5
                         return 0
          6
                     sim = (len(set(train graph.successors(a)).intersection(set(train graph.successors(b)))))/\
                                                 (len(set(train graph.successors(a)).union(set(train graph.successors(b)
          7
          8
                except:
          9
                     return 0
         10
                return sim
```

```
In [0]:
         1 #one test case
          2 print(jaccard for followees(273084,1505602))
        0.0
         1 #node 1635354 not in graph
In [0]:
          2 print(jaccard for followees(273084,1505602))
        0.0
In [0]:
            #for followers
            def jaccard for followers(a,b):
          3
                    if len(set(train graph.predecessors(a))) == 0 | len(set(g.predecessors(b))) == 0:
          4
          5
                         return 0
                     sim = (len(set(train graph.predecessors(a)).intersection(set(train graph.predecessors(b)))))/\
          6
                                              (len(set(train graph.predecessors(a)).union(set(train graph.predecessors(b)))
          7
          8
                     return sim
          9
                 except:
         10
                     return 0
         1 print(jaccard for followers(273084,470294))
In [0]:
        0
           #node 1635354 not in graph
In [0]:
          print(jaccard for followees(669354,1635354))
```

2.2 Cosine distance

$$Cosine Distance = \frac{|X \cap Y|}{|X| \cdot |Y|}$$

0

```
In [0]:
           #for followees
            def cosine for followees(a,b):
          3
                 try:
                     if len(set(train graph.successors(a))) == 0 | len(set(train graph.successors(b))) == 0:
          4
          5
                         return 0
          6
                     sim = (len(set(train graph.successors(a)).intersection(set(train graph.successors(b)))))/\
                                                  (math.sqrt(len(set(train graph.successors(a)))*len((set(train graph.successors(a)))
          7
          8
                     return sim
          9
                 except:
         10
                     return 0
         1 print(cosine for followees(273084,1505602))
In [0]:
        0.0
         1 print(cosine for followees(273084,1635354))
In [0]:
        0
            def cosine for followers(a,b):
In [0]:
          2
                 try:
          3
                     if len(set(train graph.predecessors(a))) == 0 | len(set(train graph.predecessors(b))) == 0:
          4
          5
                         return 0
                     sim = (len(set(train_graph.predecessors(a)).intersection(set(train_graph.predecessors(b)))))/\
          6
                                                   (math.sqrt(len(set(train graph.predecessors(a))))*(len(set(train graph)))
          7
          8
                     return sim
          9
                 except:
         10
                     return 0
         1 print(cosine for followers(2,470294))
In [0]:
        0.02886751345948129
         print(cosine for_followers(669354,1635354))
In [0]:
        0
```

3. Ranking Measures

https://networkx.github.io/documentation/networkx-1.10/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html (https://networkx.github.io/documentation/networkx-1.10/reference/generated/networkx.algorithms.link_analysis.pagerank_alg.pagerank.html)

PageRank computes a ranking of the nodes in the graph G based on the structure of the incoming links.



Mathematical PageRanks for a simple network, expressed as percentages. (Google uses a logarithmic scale.) Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value. If web surfers who start on a random page have an 85% likelihood of choosing a random link from the page they are currently visiting, and a 15% likelihood of jumping to a page chosen at random from the entire web, they will reach Page E 8.1% of the time. (The 15% likelihood of jumping to an arbitrary page corresponds to a damping factor of 85%.) Without damping, all web surfers would eventually end up on Pages A, B, or C, and all other pages would have PageRank zero. In the presence of damping, Page A effectively links to all pages in the web, even though it has no outgoing links of its own.

3.1 Page Ranking

https://en.wikipedia.org/wiki/PageRank (https://en.wikipedia.org/wiki/PageRank)

5.615699699389075e-07

4. Other Graph Features

4.1 Shortest path:

Getting Shortest path between twoo nodes, if nodes have direct path i.e directly connected then we are removing that edge and calculating path.

```
#if has direct edge then deleting that edge and calculating shortest path
 In [0]:
             def compute shortest path length(a,b):
           2
           3
                  p = -1
           4
                  try:
           5
                      if train graph.has edge(a,b):
                          train graph.remove edge(a,b)
           6
                          p= nx.shortest path length(train graph,source=a,target=b)
           7
           8
                          train graph.add edge(a,b)
           9
                      else:
          10
                          p= nx.shortest path length(train graph,source=a,target=b)
          11
                      return p
          12
                  except:
          13
                      return -1
 In [0]:
             #testing
            compute shortest path length(77697, 826021)
Out[21]: 10
 In [0]:
           1 #testing
           2 compute shortest path length(669354,1635354)
Out[22]: -1
```

4.2 Checking for same community

```
#getting weekly connected edges from graph
 In [0]:
             wcc=list(nx.weakly connected components(train graph))
             def belongs to same wcc(a,b):
           4
                  index = []
           5
                  if train graph.has edge(b,a):
           6
                      return 1
           7
                  if train graph.has edge(a,b):
           8
                          for i in wcc:
           9
                               if a in i:
          10
                                   index= i
          11
                                   break
                          if (b in index):
          12
          13
                              train graph.remove edge(a,b)
          14
                               if compute shortest path length(a,b)==-1:
                                   train graph.add edge(a,b)
          15
          16
                                   return 0
                              else:
          17
          18
                                   train graph.add edge(a,b)
          19
                                   return 1
          20
                          else:
          21
                               return 0
          22
                  else:
          23
                          for i in wcc:
          24
                               if a in i:
          25
                                   index= i
          26
                                   break
                          if(b in index):
          27
          28
                               return 1
          29
                          else:
          30
                               return 0
 In [0]:
           1 belongs to same wcc(861, 1659750)
Out[24]: 0
             belongs to same wcc(669354,1635354)
 In [0]:
Out[25]: 0
```

4.3 Adamic/Adar Index:

Adamic/Adar measures is defined as inverted sum of degrees of common neighbours for given two vertices.

$$A(x, y) = \sum_{u \in N(x) \cap N(y)} \frac{1}{log(|N(u)|)}$$

```
In [0]:
             #adar index
             def calc adar in(a,b):
           3
                  sum=0
           4
                  try:
           5
                      n=list(set(train graph.successors(a)).intersection(set(train graph.successors(b))))
           6
                      if len(n)!=0:
           7
                          for i in n:
                              sum=sum+(1/np.log10(len(list(train graph.predecessors(i)))))
           8
           9
                          return sum
          10
                      else:
          11
                          return 0
          12
                  except:
          13
                      return 0
          1 calc adar in(1,189226)
 In [0]:
Out[27]: 0
          1 calc adar in(669354,1635354)
 In [0]:
Out[28]: 0
```

4.4 Is persion was following back:

```
In [0]: 1 follows_back(1,189226)
Out[30]: 1
In [0]: 1 follows_back(669354,1635354)
Out[31]: 0
```

4.5 Katz Centrality:

https://en.wikipedia.org/wiki/Katz centrality (https://en.wikipedia.org/wiki/Katz centrality)

https://www.geeksforgeeks.org/katz-centrality-centrality-measure/ (https://www.geeksforgeeks.org/katz-centrality-measure/) Katz centrality computes the centrality for a node based on the centrality of its neighbors. It is a generalization of the eigenvector centrality. The Katz centrality for node i is

$$x_i = \alpha \sum_j A_{ij} x_j + \beta,$$

where A is the adjacency matrix of the graph G with eigenvalues

λ

.

The parameter

β

controls the initial centrality and

$$\alpha < \frac{1}{\lambda_{max}}.$$

```
In [0]: 1 print('min', katz[min(katz, key=katz.get)])
2 print('max', katz[max(katz, key=katz.get)])
3 print('mean', float(sum(katz.values())) / len(katz))

min 0.0007313532484065916
max 0.003394554981699122
mean 0.0007483800935562018

In [0]: 1 mean_katz = float(sum(katz.values())) / len(katz)
2 print(mean_katz)
```

0.0007483800935562018

4.6 Hits Score

The HITS algorithm computes two numbers for a node. Authorities estimates the node value based on the incoming links. Hubs estimates the node value based on outgoing links.

https://en.wikipedia.org/wiki/HITS_algorithm (https://en.wikipedia.org/wiki/HITS_algorithm)

5. Featurization

5. 1 Reading a sample of Data from both train and test

```
In [0]:
            import random
            if os.path.isfile('data/after eda/train after eda.csv'):
                filename = "data/after eda/train after eda.csv"
          3
                # you uncomment this line, if you dont know the lentqh of the file name
          5
                # here we have hardcoded the number of lines as 15100030
                # n train = sum(1 for line in open(filename)) #number of records in file (excludes header)
                n train = 15100028
                s = 100000 #desired sample size
                skip train = sorted(random.sample(range(1, n train+1), n train-s))
         9
                #https://stackoverflow.com/a/22259008/4084039
        10
In [0]:
         1 if os.path.isfile('data/after eda/train after eda.csv'):
                filename = "data/after eda/test after eda.csv"
                # you uncomment this line, if you dont know the lentgh of the file name
          3
                # here we have hardcoded the number of lines as 3775008
                # n test = sum(1 for line in open(filename)) #number of records in file (excludes header)
          6
                n \text{ test} = 3775006
          7
                s = 50000 #desired sample size
                skip test = sorted(random.sample(range(1, n test+1), n test-s))
          8
                #https://stackoverflow.com/a/22259008/4084039
         1 print("Number of rows in the train data file:", n train)
In [0]:
         2 print("Number of rows we are going to elimiate in train data are", len(skip train))
         3 print("Number of rows in the test data file:", n test)
          4 print("Number of rows we are going to elimiate in test data are", len(skip test))
        Number of rows in the train data file: 15100028
        Number of rows we are going to elimiate in train data are 15000028
        Number of rows in the test data file: 3775006
        Number of rows we are going to elimiate in test data are 3725006
```

```
df final train = pd.read csv('data/after eda/train after eda.csv', skiprows=skip train, names=['source node
 In [0]:
           2 df final train['indicator link'] = pd.read csv('data/train y.csv', skiprows=skip train, names=['indicator l
           3 print("Our train matrix size ", df final train.shape)
            df final train.head(2)
         Our train matrix size (100002, 3)
Out[49]:
             source node destination node indicator link
                 273084
                              1505602
          0
          1
                 832016
                              1543415
          df final test = pd.read csv('data/after eda/test after eda.csv', skiprows=skip test, names=['source node',
 In [0]:
           2 df final test['indicator link'] = pd.read csv('data/test y.csv', skiprows=skip test, names=['indicator link']
           3 print("Our test matrix size ", df final test.shape)
            df final test.head(2)
         Our test matrix size (50002, 3)
Out[50]:
             source_node destination_node indicator_link
          0
                 848424
                               784690
                              1255532
          1
                 483294
```

5.2 Adding a set of features

we will create these each of these features for both train and test data points

```
    jaccard_followers
```

- 2. jaccard_followees
- 3. cosine_followers
- 4. cosine_followees
- 5. num_followers_s
- 6. num_followees_s
- 7. num_followers_d
- 8. num_followees_d
- 9. inter_followers

10. inter followees

```
In [0]:
            if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
                #mapping jaccrd followers to train and test data
          2
                df final train['jaccard followers'] = df final train.apply(lambda row:
          3
          4
                                                         jaccard for followers(row['source node'],row['destination node'
          5
                df final test['jaccard followers'] = df final test.apply(lambda row:
                                                         jaccard for followers(row['source node'],row['destination node'
          6
         7
          8
                #mapping jaccrd followees to train and test data
                df final train['jaccard followees'] = df final train.apply(lambda row:
          9
                                                         jaccard for followees(row['source node'],row['destination node'
        10
        11
                df final test['jaccard followees'] = df final test.apply(lambda row:
        12
                                                         jaccard for followees(row['source node'],row['destination node'
        13
        14
        15
                    #mapping jaccrd followers to train and test data
                df final train['cosine followers'] = df final train.apply(lambda row:
        16
                                                         cosine for followers(row['source node'],row['destination node']
        17
                df final test['cosine followers'] = df final test.apply(lambda row:
        18
        19
                                                         cosine for followers(row['source node'],row['destination node']
        20
                #mapping jaccrd followees to train and test data
        21
        22
                df final train['cosine followees'] = df final train.apply(lambda row:
        23
                                                         cosine for followees(row['source node'],row['destination node']
        24
                df final test['cosine followees'] = df final test.apply(lambda row:
        25
                                                         cosine for followees(row['source node'],row['destination node']
```

```
def compute features stage1(df final):
In [0]:
                 #calculating no of followers followees for source and destination
          2
                 #calculating intersection of followers and followees for source and destination
          3
                num followers s=[]
          4
          5
                num followees s=[]
          6
                num followers d=[]
          7
                num followees d=[]
          8
                inter followers=[]
          9
                inter followees=[]
                 for i,row in df final.iterrows():
        10
        11
                     try:
        12
                         s1=set(train graph.predecessors(row['source node']))
                         s2=set(train graph.successors(row['source node']))
        13
        14
                     except:
                         s1 = set()
        15
        16
                         s2 = set()
        17
                     try:
                         d1=set(train_graph.predecessors(row['destination node']))
        18
        19
                         d2=set(train graph.successors(row['destination node']))
        20
                     except:
        21
                         d1 = set()
        22
                         d2 = set()
        23
                     num followers s.append(len(s1))
        24
                     num followees s.append(len(s2))
        25
        26
                     num followers d.append(len(d1))
        27
                     num followees d.append(len(d2))
        28
        29
                     inter followers.append(len(s1.intersection(d1)))
                     inter followees.append(len(s2.intersection(d2)))
        30
        31
         32
                 return num followers s, num followers d, num followees s, num followees d, inter followers, inter followers
```

```
In [0]:
         if not os.path.isfile('data/fea sample/storage sample stage1.h5'):
                df final train['num followers s'], df final train['num followers d'], \
                df final train['num followees s'], df final train['num followees d'], \
          3
                df final train['inter followers'], df final train['inter followees'] = compute features stage1(df final
          5
          6
                df final test['num followers s'], df final test['num followers d'], \
                df final test['num followees s'], df final test['num followees d'], \
          7
                df final test['inter followers'], df final_test['inter_followees'] = compute_features_stage1(df_final_te
          8
          9
                hdf = HDFStore('data/fea sample/storage sample stage1.h5')
         10
                hdf.put('train df', df final train, format='table', data columns=True)
         11
                hdf.put('test df', df final test, format='table', data columns=True)
         12
         13
                hdf.close()
         14
            else:
                df final train = read hdf('data/fea sample/storage sample stage1.h5', 'train df', mode='r')
         15
                df final test = read hdf('data/fea sample/storage sample stage1.h5', 'test df',mode='r')
         16
```

5.3 Adding new set of features

we will create these each of these features for both train and test data points

- 1. adar index
- 2. is following back
- 3. belongs to same weakly connect components
- 4. shortest path between source and destination

```
if not os.path.isfile('data/fea sample/storage sample stage2.h5'):
In [0]:
               #mapping adar index on train
               df final train['adar index'] = df final train.apply(lambda row: calc adar in(row['source node'],row['de
        3
               #mapping adar index on test
               df final test['adar index'] = df final test.apply(lambda row: calc adar in(row['source node'],row['dest
         5
        7
         8
               #mapping followback or not on train
               df final train['follows back'] = df final train.apply(lambda row: follows back(row['source node'],row['
       10
       11
               #mapping followback or not on test
       12
               df final test['follows back'] = df final test.apply(lambda row: follows back(row['source node'],row['de
       13
       14
               #______
               #mapping same component of wcc or not on train
       15
       16
               df final train['same comp'] = df final train.apply(lambda row: belongs to same wcc(row['source node'], re
       17
       18
               ##mapping same component of wcc or not on train
       19
               df final test['same comp'] = df final test.apply(lambda row: belongs to same wcc(row['source node'],row
       20
               #-----
       21
       22
               #mapping shortest path on train
               df final train['shortest path'] = df final train.apply(lambda row: compute shortest path length(row['so
        23
        24
               #mapping shortest path on test
               df final test['shortest path'] = df final test.apply(lambda row: compute shortest path length(row['sour
       25
       26
       27
               hdf = HDFStore('data/fea sample/storage sample stage2.h5')
              hdf.put('train df', df final train, format='table', data columns=True)
       28
       29
              hdf.put('test df', df final test, format='table', data columns=True)
       30
               hdf.close()
       31 else:
       32
               df final train = read hdf('data/fea sample/storage sample stage2.h5', 'train df', mode='r')
               df final test = read hdf('data/fea sample/storage sample stage2.h5', 'test df',mode='r')
        33
```

5.4 Adding new set of features

we will create these each of these features for both train and test data points

- 1. Weight Features
 - · weight of incoming edges

- · weight of outgoing edges
- weight of incoming edges + weight of outgoing edges
- weight of incoming edges * weight of outgoing edges
- 2*weight of incoming edges + weight of outgoing edges
- weight of incoming edges + 2*weight of outgoing edges
- 2. Page Ranking of source
- 3. Page Ranking of dest
- 4. katz of source
- 5. katz of dest
- 6. hubs of source
- 7. hubs of dest
- 8. authorities s of source
- 9. authorities_s of dest

Weight Features

In order to determine the similarity of nodes, an edge weight value was calculated between nodes. Edge weight decreases as the neighbor count goes up. Intuitively, consider one million people following a celebrity on a social network then chances are most of them never met each other or the celebrity. On the other hand, if a user has 30 contacts in his/her social network, the chances are higher that many of them know each other.

credit - Graph-based Features for Supervised Link Prediction William Cukierski, Benjamin Hamner, Bo Yang

$$W = \frac{1}{\sqrt{1 + |X|}}$$

it is directed graph so calculated Weighted in and Weighted out differently

```
1 #weight for source and destination of each link
In [0]:
         2 Weight in = {}
         3 Weight out = {}
            for i in tqdm(train graph.nodes()):
                s1=set(train graph.predecessors(i))
                w in = 1.0/(np.sqrt(1+len(s1)))
          6
                Weight in[i]=w in
         7
          8
         9
                s2=set(train graph.successors(i))
                w \text{ out } = 1.0/(np.sqrt(1+len(s2)))
        10
                Weight out[i]=w out
        11
        12
        13 #for imputing with mean
            mean weight in = np.mean(list(Weight in.values()))
        15 mean weight out = np.mean(list(Weight out.values()))
```

100%| | 1780722/1780722 [00:11<00:00, 1526 | 82.24it/s]

```
if not os.path.isfile('data/fea sample/storage sample stage3.h5'):
In [0]:
                #mapping to pandas train
         2
         3
                df final train['weight in'] = df final train.destination node.apply(lambda x: Weight in.get(x, mean weight)
                df final train['weight out'] = df final train.source node.apply(lambda x: Weight out.get(x, mean weight
          4
          5
          6
                #mapping to pandas test
         7
                df final test['weight in'] = df final test.destination node.apply(lambda x: Weight in.get(x, mean weight
                df final test['weight out'] = df final test.source node.apply(lambda x: Weight out.get(x, mean weight out)
         8
         9
        10
                #some features engineerings on the in and out weights
        11
        12
                df final train['weight f1'] = df final train.weight in + df final train.weight out
                df final train['weight f2'] = df final train.weight in * df final train.weight out
        13
                df final train['weight f3'] = (2*df final train.weight in + 1*df final train.weight out)
        14
        15
                df final train['weight f4'] = (1*df final train.weight in + 2*df final train.weight out)
        16
        17
                #some features engineerings on the in and out weights
                df final test['weight f1'] = df final test.weight in + df final test.weight out
        18
                df final test['weight f2'] = df final test.weight in * df final test.weight out
        19
        20
                df final test['weight f3'] = (2*df final test.weight in + 1*df final test.weight out)
                df final test['weight f4'] = (1*df final test.weight in + 2*df final test.weight out)
        21
```

```
if not os.path.isfile('data/fea sample/storage sample stage3.h5'):
In [0]:
         3
                #page rank for source and destination in Train and Test
                #if anything not there in train graph then adding mean page rank
         5
                df final train['page rank s'] = df final train.source node.apply(lambda x:pr.get(x,mean pr))
                df final train['page rank d'] = df final train.destination node.apply(lambda x:pr.get(x,mean pr))
         6
         7
         8
                df final test['page rank s'] = df final test.source node.apply(lambda x:pr.get(x,mean pr))
         9
                df final test['page rank d'] = df final test.destination node.apply(lambda x:pr.get(x,mean pr))
        10
                #----
        11
        12
                #Katz centrality score for source and destination in Train and test
                #if anything not there in train graph then adding mean katz score
        13
        14
                df final train['katz s'] = df final train.source node.apply(lambda x: katz.get(x,mean katz))
                df final train['katz d'] = df final train.destination node.apply(lambda x: katz.get(x,mean katz))
        15
        16
        17
                df final test['katz s'] = df final test.source node.apply(lambda x: katz.get(x,mean katz))
        18
                df final test['katz d'] = df final test.destination node.apply(lambda x: katz.get(x,mean katz))
        19
        20
        21
                #Hits algorithm score for source and destination in Train and test
        22
                #if anything not there in train graph then adding 0
                df final train['hubs s'] = df final train.source node.apply(lambda x: hits[0].get(x,0))
        23
        24
                df final train['hubs d'] = df final train.destination node.apply(lambda x: hits[0].get(x,0))
        25
        26
                df final test['hubs s'] = df final test.source node.apply(lambda x: hits[0].get(x,0))
        27
                df final test['hubs d'] = df final test.destination node.apply(lambda x: hits[0].get(x,0))
        28
        29
        30
                #Hits algorithm score for source and destination in Train and Test
        31
                #if anything not there in train graph then adding 0
        32
                df final train['authorities s'] = df final train.source node.apply(lambda x: hits[1].get(x,0))
                df final train['authorities d'] = df final train.destination node.apply(lambda x: hits[1].get(x,0))
        33
        34
        35
                df final test['authorities s'] = df final test.source node.apply(lambda x: hits[1].get(x,0))
        36
                df final test['authorities d'] = df final test.destination node.apply(lambda x: hits[1].get(x,0))
        37
        38
               hdf = HDFStore('data/fea sample/storage sample stage3.h5')
        39
               hdf.put('train df', df final train, format='table', data columns=True)
        40
               hdf.put('test df',df final test, format='table', data columns=True)
        41
```

```
hdf.close()
else:

df_final_train = read_hdf('data/fea_sample/storage_sample_stage3.h5', 'train_df',mode='r')
df_final_test = read_hdf('data/fea_sample/storage_sample_stage3.h5', 'test_df',mode='r')
```

5.5 Adding new set of features

we will create these each of these features for both train and test data points

1. SVD features for both source and destination

```
In [0]:
            def svd(x, S):
          2
                try:
          3
                    z = sadj_dict[x]
                    return S[z]
          5
                except:
                    return [0,0,0,0,0,0]
         1 #for svd features to get feature vector creating a dict node val and inedx in svd vector
In [0]:
          2 sadj col = sorted(train graph.nodes())
          3 sadj dict = { val:idx for idx,val in enumerate(sadj col)}
         1 Adj = nx.adjacency matrix(train graph, nodelist=sorted(train graph.nodes())).asfptype()
In [0]:
         1 U, s, V = svds(Adj, k = 6)
In [0]:
         2 print('Adjacency matrix Shape', Adj.shape)
          3 print('U Shape', U.shape)
          4 print('V Shape', V.shape)
          5 print('s Shape',s.shape)
        Adjacency matrix Shape (1780722, 1780722)
        U Shape (1780722, 6)
        V Shape (6, 1780722)
        s Shape (6,)
```

```
In [0]:
        1 if not os.path.isfile('data/fea sample/storage sample stage4.h5'):
              #-----
        2
        3
              df final train[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4', 'svd u s 5', 'svd u s 6']] = \
              df final train.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
        5
        7
              df final train[['svd u d 1', 'svd u d 2', 'svd u d 3', 'svd u d 4', 'svd u d 5', 'svd u d 6']] = \
        8
              df final train.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
              10
              df final train[['svd v s 1','svd v s 2', 'svd v s 3', 'svd v s 4', 'svd v s 5', 'svd v s 6',]] = \
       11
              df final train.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
       12
       13
       14
              df final train[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v d 5','svd v d 6']] = \
       15
              df final train.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
       16
              #-----
       17
       18
              df final test[['svd u s 1', 'svd u s 2', 'svd u s 3', 'svd u s 4', 'svd u s 5', 'svd u s 6']] = \
       19
              df final test.source node.apply(lambda x: svd(x, U)).apply(pd.Series)
       20
       21
              df final test[['svd u d 1', 'svd u d 2', 'svd u d 3', 'svd u d 4', 'svd u d 5', 'svd u d 6']] = \
       22
              df final test.destination node.apply(lambda x: svd(x, U)).apply(pd.Series)
       23
       24
       25
              df final test[['svd v s 1', 'svd v s 2', 'svd v s 3', 'svd v s 4', 'svd v s 5', 'svd v s 6',]] = \
       26
              df final test.source node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
       27
       28
       29
              df final test[['svd v d 1', 'svd v d 2', 'svd v d 3', 'svd v d 4', 'svd v d 5', 'svd v d 6']] = \
              df final test.destination node.apply(lambda x: svd(x, V.T)).apply(pd.Series)
       30
       31
       32
       33
              hdf = HDFStore('data/fea sample/storage sample stage4.h5')
       34
              hdf.put('train df', df final train, format='table', data columns=True)
       35
              hdf.put('test df', df final test, format='table', data columns=True)
       36
              hdf.close()
```