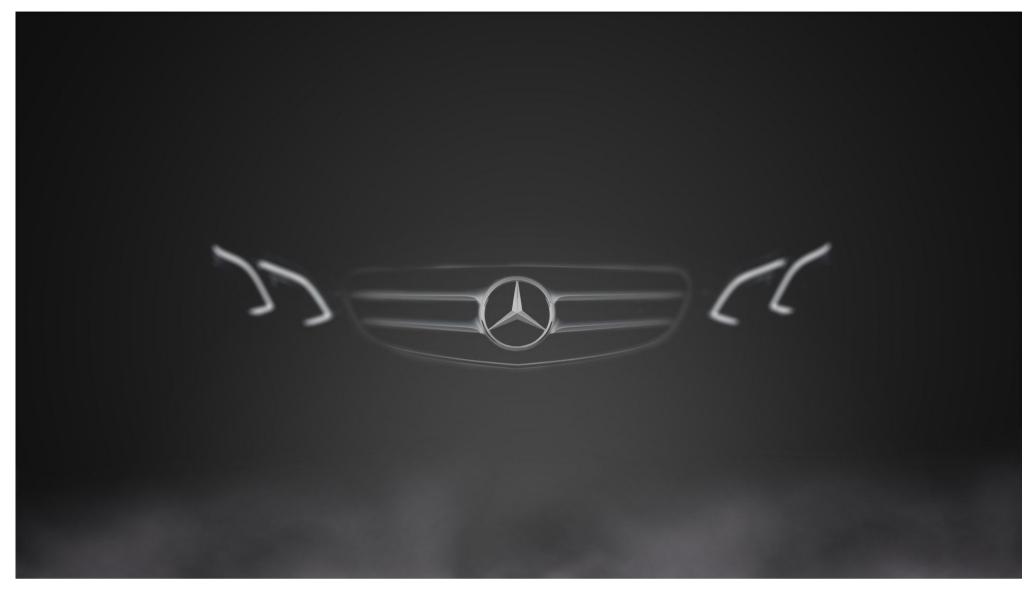
Mercedes-Benz Greener Manufacturing

Can you cut the time a Mercedes-Benz spends on the test bench?



 $\label{lem:lemmageby:https://i.pinimg.com/originals/5b/ac/4e/5bac4e30d414a7eda8d137af0b1b33d4.jpg} $$ $$ \underline{\text{(https://i.pinimg.com/originals/5b/ac/4e/5bac4e30d414a7eda8d137af0b1b33d4.jpg)}}$$$

1. Business Problem

1.1 Description

Since the first automobile, the Benz Patent Motor Car in 1886, Mercedes-Benz has stood for important automotive innovations. These include, for example, the passenger safety cell with crumple zone, the airbag and intelligent assistance systems. Mercedes-Benz applies for nearly 2000 patents per year, making the brand the European leader among premium car makers. Daimler's Mercedes-Benz cars are leaders in the premium car industry. With a huge selection of features and options, customers can choose the customized Mercedes-Benz of their dreams.

Problem Statemtent:

- Any car we see running on the road is not manufactured and put directly on the road for our use. Every car or a bike or any other running vehicle on the road we see on the road goes through several testing procedures which it has to pass so as to hit the road for regular use. These testing is performed so as to ensure safety and reliability of the vehicle when it will be used in real world scenarios. Testing can include many steps so it is obviously a time consuming process. More time is required for testing, since tests should be performed considering all the real life situations, So more testing time leads to more testing cost and also as the testing time increases, Co2 emissions from the vehicle also increases with that. But testing is a very essential step and no automobile manufacturer can skip this because every vehicle configuration they manufacture has to go through all the testings so as to ensure the safety of the occupants and the reliability of that vehicle. So as a popular premium automaker Mercedez cannot compromise about safety of the vehicle and the occupant in fact all the vehicle manufacturer's goal is to have a robust and efficient testing system, and nowadays all of them are moving towards automation.
- Mercedes Benz and all other automakers are trying to automate their testing systems so as to develop efficient testing systems for their vehicles. Automated systems will help to eliminate the errors due to variability in human behaviours which is inherent and also it is safer to auto test than putting a human on the driver seat for testing. So aim is to reduce testing time by analyzing the current available data which is collected from hundreds of tests on thousands of car configurations.
- Basic problem statement is to create a machine learning model that will predict accurate time a car spends on the test bench. The car configuration is nothing
 but selected various customization options available and the features for a particular car. Accurate models will help to reduce the total time spent for testing by
 allowing the vehicles with the same configurations to test successively.
- There are many features in the car configuration, e.g. if there are any cars belong to some class-D but they have one/many additional feature which other class-D cars don't have that/those features, in such cases there will be different testing time for them. Hence for such cases machine learning model can help predicting accurate time spent on test bench for cars with same class but some different features.

Source:

This problem belong to one of the competitions held on kaggle. Which can be found on following link: https://www.kaggle.com/c/mercedes-benz-greener-manufacturing/overview)

1.2. Business Objectives and Constraints

- Predicting accurate time a car spends on the test bench
- No strict latency constraints, few seconds to few minutes prediction time is okay, but not hours.

2. Machine Learning problem

2.1 Data

2.1.1 Data Overview

This dataset contains an anonymized set of variables, each representing a custom feature in a Mercedes car. For example, a variable could be 4WD, added air suspension, or a head-up display.

The ground truth is labeled 'y' and represents the time (in seconds) that the car took to pass testing for each variable.

We have two comma separated files:

- train.csv Contains the training set with 4209 rows (datapoints) and 378 columns (features) with labels
- test.csv Contains the test set with 4209 rows (datapoints) and 377 columns (features) with no labels

Columns:

ID y X0 X1 X2 X3 X4 X5 X6 X8 ... X375 X376 X377 X378 X379 X380 X382 X383 X384 X385

Link to the data set: https://www.kaggle.com/c/mercedes-benz-greener-manufacturing/data (https://www.kaggle.com/c/mercedes-ben

2.2 Mapping the real-world problem to a Machine Learning Problem

2.2.1 Type of Machine Learning Problem

As our aim is to predict the testing time which is a continuous variable, we can surely say this is a **regression** machine learning problem. And as we have a labelled dataset here, it is a supervised machine learning problem. Mercedes Benz will implement the best performing model into their testing procedure which will result in efficient testing without harming their standards and which also will help greener manufacturing by reduction of Co2 emissions.

2.2.2 Performance metric

Now we know this is a machine learning regression problem, we have to use an appropriate metric for the performance evaluation of our prediction model. Here it is already given in the competition to use the R^2 metric for evaluation. R^2 is also known as Coefficient of Determination, R-squared gives the percentage variation in 'y' (test time in this case) explained by 'x-variables' (combination of car custom features in this case). In simple words R^2 gives us the percentage of data points that fall within the regression line. The higher the R^2 value, higher will be the data points that fall within the line. E.g. if R^2 value is 0.66 then it indicates that 66% data points are lying within the regression line of the total data points. Mathematically R^2 is denoted as follows:

$$R^2 = 1 - \frac{SS_{residual}}{SS_{total}}$$

Where,

$$SS_{residual} = \sum_{i=1}^{n} (Y_i - \hat{Y})^2$$

$$SS_{total} = \sum_{i=1}^{n} (Y_i - \overline{Y})^2$$

There 4 cases for the values of R^2:

➤ Case 1:

If,
$$SS_{residual} = 0$$
, $Y_i - \widehat{Y} = 0$

Then $R^2 = 1$ (Best model)

➤ Case 2:

If,
$$SS_{residual} < SS_{total}$$

Then
$$R^2 = 0$$
 to 1

➤ Case 3:

$$\text{If, } \qquad SS_{\textit{residual}} = SS_{\textit{total}}$$

Then
$$R^2 = 0$$

➤ Case 4:

$$\text{If, } \qquad SS_{\textit{residual}} > SS_{\textit{total}}$$

Then R^2 = -Ve value (Worst model)

R^2 metric is very sensitive to outliers. The algorithm that best explains the variation in testing times will be the optimal machine learning model for the task. So this is the best metric to be used for evaluation in this problem, as Mercedes is really interested to know how the different testing times for different configurations can be represented in a machine learning model.

As I have explained the four cases above we can see R^2 metric ranges from $-\infty$ to 1 as $-\infty$ R^2 score being worst and 1 R^2 score being the best model. Also there are very rare cases where R^2 can be negative, so generally we get a R^2 score between 0 and 1. So for R^2 metric upper bound is 1 but in case of RMSE and MAE, score ranges from 0 to ∞ (infinity) there is no upper bound so it will be difficult for us to compare the model with baseline model score. The benifit of using R^2 metric is that it is having an upper bound 1 beyond which the score cannot increase so we can compare our model score with the baseline model score, hence R^2 metric is preffered over RMSE and MAE in this problem.

3. Library Imports

```
In [1]: import pandas as pd
        import numpy as np
        import matplotlib.pyplot as plt
        import seaborn as sns
        from sklearn.preprocessing import LabelEncoder,Normalizer,PolynomialFeatures
        from sklearn.model_selection import train_test_split
        from sklearn.neighbors import KNeighborsRegressor
        from sklearn.svm import SVR
        from sklearn.ensemble import RandomForestRegressor
        from sklearn.tree import DecisionTreeRegressor
        from xgboost.sklearn import XGBRegressor
        from sklearn.model_selection import RandomizedSearchCV,GridSearchCV
        from sklearn.decomposition import TruncatedSVD, PCA
        from sklearn.linear_model import LassoLarsCV, Ridge
        from mlxtend.regressor import StackingCVRegressor
        from sklearn.random_projection import GaussianRandomProjection
        from sklearn.metrics import r2_score
        import joblib
        import warnings
        warnings.filterwarnings("ignore")
```

4. Exploratory Data Analysis and Preprocessing

4.1 Data Loading and EDA

4.1.1 Load the data

	ID	У	X0	X1	X2	Х3	X4	X5	X6	X8	•••	X375	X376	X377	X378	X379	X380	X382	X383	X384	X385
0	0	130.81	k	٧	at	а	d	u	j	О		0	0	1	0	0	0	0	0	0	0
1	6	88.53	k	t	av	е	d	у	- 1	О		1	0	0	0	0	0	0	0	0	0
2	7	76.26	az	w	n	С	d	x	j	x		0	0	0	0	0	0	1	0	0	0
3	9	80.62	az	t	n	f	d	x	- 1	е		0	0	0	0	0	0	0	0	0	0
4	13	78.02	az	٧	n	f	d	h	d	n		0	0	0	0	0	0	0	0	0	0

5 rows × 378 columns

```
In [3]: # now let's have a look at information about dataset
train.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 4209 entries, 0 to 4208
Columns: 378 entries, ID to X385
dtypes: float64(1), int64(369), object(8)
memory usage: 12.1+ MB
```

- Here we can see there are 4209 datapoints indexing from 0 to 4208 and 378 coulmns/features.
- We have three types of data in dataset:
 - float64(1): Dependent feature, testing time in seconds
 - int64(369): Independent Binary features
 - object(8): Independent Categorical features

```
In [4]: # lets use pandas to load csv files we have
    test = pd.read_csv('test.csv')
    print(f"total test datapoints = {len(train)}")
    test.head()
```

total test datapoints = 4209

Out[4]:

	ID	X0	X1	X2	Х3	Х4	Х5	Х6	X8	X10	•••	X375	X376	X377	X378	X379	X380	X382	X383	X384	X385	
0	1	az	٧	n	f	d	t	а	w	0		0	0	0	1	0	0	0	0	0	0	
1	2	t	b	ai	а	d	b	g	у	0		0	0	1	0	0	0	0	0	0	0	
2	3	az	٧	as	f	d	а	j	j	0		0	0	0	1	0	0	0	0	0	0	
3	4	az	- 1	n	f	d	z	- 1	n	0		0	0	0	1	0	0	0	0	0	0	
4	5	W	s	as	С	d	У	i	m	0		1	0	0	0	0	0	0	0	0	0	

5 rows × 377 columns

RangeIndex: 4209 entries, 0 to 4208 Columns: 377 entries, ID to X385 dtypes: int64(369), object(8) memory usage: 12.1+ MB

- Here we can see there are 4209 datapoints indexing from 0 to 4208 and 377 coulmns/features.
- We have three types of data in dataset:
 - int64(369): Independent Binary features
 - object(8): Independent Categorical features
- We can see here we have same number of datapoints in train and test dataset.

4.1.2 Statistical description of ID and Dependent variables

First I will check for any missing values value in the whole data set.

```
In [6]: # check if there are any missing values
    isNan = train.isnull().sum().any()

if isNan == True:
    print("There are NaN values in the dataset")
    else:
        print("There are No NaN values in the dataset")
```

There are No NaN values in the dataset

Let's also check for duplicate rows

```
In [7]: # check if there are any Duplicate rows
isDup = train.duplicated().sum().any()
if isDup == True:
    print("There are Duplicate rows in the dataset")
else:
    print("There are No Duplicate rows in the dataset")
```

There are No Duplicate rows in the dataset

```
In [8]: # now print the description of the 'ID' and 'y' columns in the dataset
    train[['ID','y']].describe()
Out[8]:
```

	ID	у
count	4209.000000	4209.000000
mean	4205.960798	100.669318
std	2437.608688	12.679381
min	0.000000	72.110000
25%	2095.000000	90.820000
50%	4220.000000	99.150000
75%	6314.000000	109.010000
max	8417.000000	265.320000

Now let's check if there are any duplicate values in the 'ID' column.

```
In [9]: dup_ID = train['ID'].duplicated().sum()
print(f"Here we have {dup_ID} duplicate IDs")
```

Here we have 0 duplicate IDs

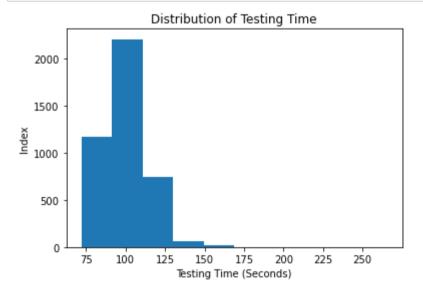
From above description table we can see,

- 'ID' feature: These are not sequentially given in the data set, they are random. Because have total 4209 configurations and here we have the max number in 'ID' column is 8417, also there are no duplicate 'ID' in the dataset.
- 'y': This is testing time to be predicted. Here minimum value is 72 and the maximum value is 265. I will do some further analysis of this dependent feature by checking it's distribution.

4.1.3 Check the distribution of Dependent variable

Histogram of dependent variable

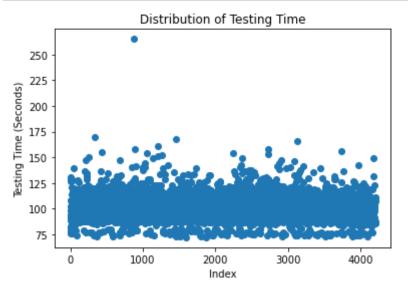
```
In [10]: # lets plot histogram for dependent variable 'y'
plt.hist(train['y'])
plt.title("Distribution of Testing Time")
plt.xlabel("Testing Time (Seconds)")
plt.ylabel("Index")
plt.show()
```



Here I can see the testing time is nearly normal distributed around 100, and most of the configurations are having the testing time between 75 to roughly 150 seconds. Above 150 there are some values as we also checked in previous description table we have one extreme point that we are unable to see here. So let's plot scatter plot of the these times for further analysis.

Scatter plot of dependent variable

```
In [11]: plt.scatter(range(len(train['y'])), train['y'])
    plt.title("Distribution of Testing Time")
    plt.xlabel("Index")
    plt.ylabel("Testing Time (Seconds)")
    plt.show()
```



- From this scatter plot I can see most of the points are belonging to the range 75 to 150 seconds as we previously also seen. Here we are able to see the extreme point which is taking more than 250 seconds for testing. May be this car configuration is one which is bought very rarely, also can be quite expensive one and thus we have only one such datapoint available here. We can consider this as an outlier for sure because it is only one point which is far away from others.
- Now I have found one outlier, we should check for more outliers. For that let's find out percentiles of testing times and then I will decide a threshold for valid datapoints based on that. We know the 75th percentile is 109 from description table, so now I will just check 90th percentile to 100th percentile only.

```
In [12]: # lets find out the 90th to 100th percentiles
    quantiles = [0.9,0.91,0.92,0.93,0.94,0.95,0.96,0.97,0.98,0.99,1]
    for i in quantiles:
        print(f"{i*100}th percentile: ",train["y"].quantile(i))

        90.0th percentile: 115.25
        91.0th percentile: 116.0484
        92.0th percentile: 116.89160000000001
        93.0th percentile: 118.0376
        94.0th percentile: 119.056
        95.0th percentile: 120.8060000000001
        96.0th percentile: 122.4
        97.0th percentile: 125.8931999999998
        98.0th percentile: 125.8931999999998
        99.0th percentile: 127.4304
        100th percentile: 265.32
```

I already declared 100th percentile value i.e. 265.32 as an outlier, now let's check 99th percentile to 99.99th percentile so as to decide the threshold.

```
In [13]: # lets find out the 99th to 99.99th percentiles
    quantiles = np.arange(0.99,0.9999,0.001)
    for i in quantiles:
        print(f"{i*100}th percentile: ",train["y"].quantile(i))

99.0th percentile: 137.4304
    99.1th percentile: 139.09024
    99.2th percentile: 140.1836
    99.3th percentile: 140.8163999999993
    99.4th percentile: 142.648000000001
    99.5th percentile: 142.648000000006
    99.6th percentile: 149.037439999998
    99.7th percentile: 151.427680000003
    99.8th percentile: 154.6869599999994
    99.9th percentile: 160.38328000000087
```

Let's use 155 as threshold time and consider values all above 155 as outliers

```
In [14]: # I will keep only the configurations which have less than 155 seconds test time
         clean_train = train[train['y']<155]</pre>
         print(f"Train data with outlier:{train.shape}")
         print(f"Train data without outlier:{clean_train.shape}")
         clean_train.head()
         Train data with outlier: (4209, 378)
         Train data without outlier: (4201, 378)
Out[14]:
             ID
                    y X0 X1 X2 X3 X4 X5 X6 X8 ... X375 X376 X377 X378 X379 X380 X382 X383 X384 X385
             0 130.81
                                                               0
                                                                               0
                                                                                                0
                                                                                                     0
                                                                                                           0
             6
                 88.53
                                                         1
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                 80.62 az
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                                                                                     0
                                                                                                     0
                 78.02 az
                                     d
                                                                                                           0
```

Now I have removed the outliers from the dataset, Now I will analyze the independent variables. We have two types of independent variables Categorical and Binary variable. The ID variable is unique configuration number, so I think it is just an index for our datapoints but in random form.

4.1.3 Analysis of Independent Features

5 rows × 378 columns

First I will separate the Binary and Categorical feature names by their data types, so that we can use them for analysis separately.

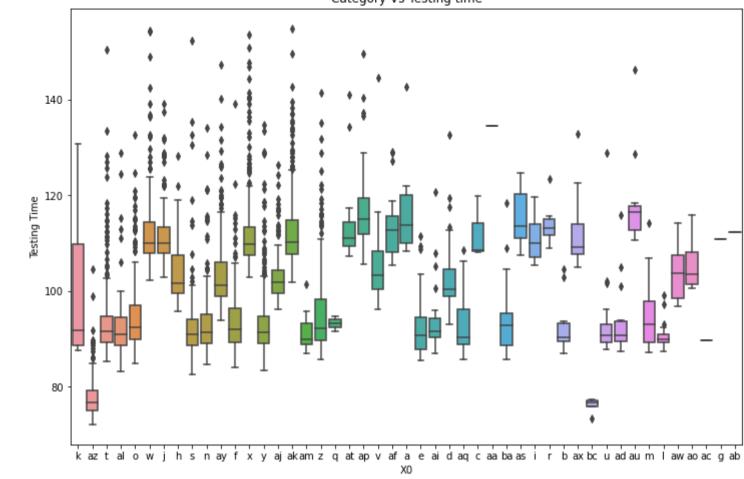
We have total 8 categorical features. We have total 368 Binary features.

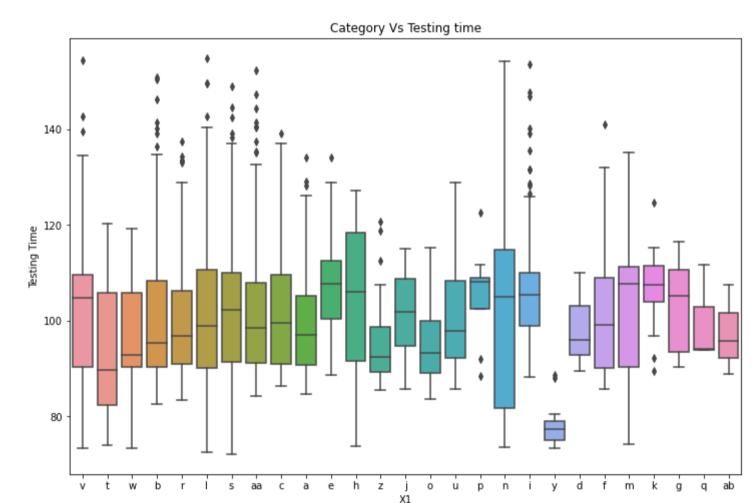
4.1.3.1 Analysis of Categorical Features

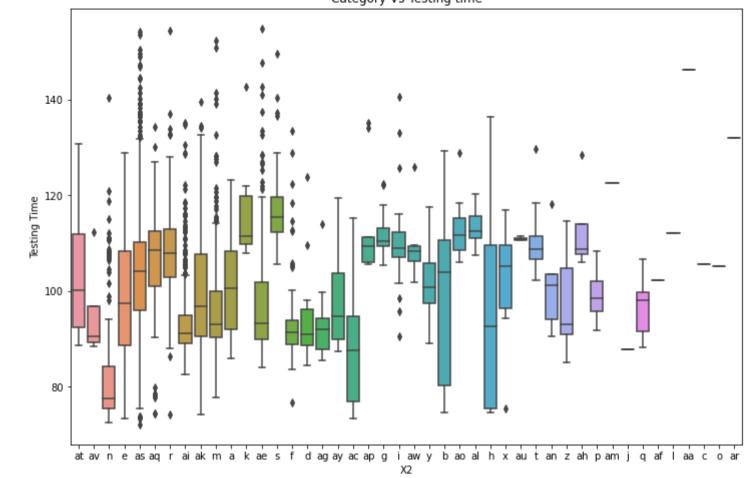
Let's plot Boxplot for each categorical feature,

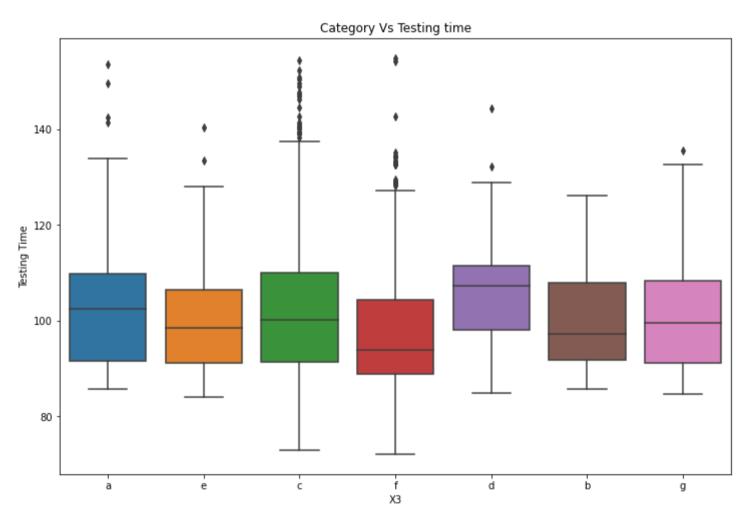
```
In [17]: for cat in cat_features:
    plt.figure(figsize=(12,8))
    sns.boxplot(cat_train_data[cat], clean_train['y'])
    plt.title("Category Vs Testing time")
    plt.xlabel(cat)
    plt.ylabel("Testing Time")
```

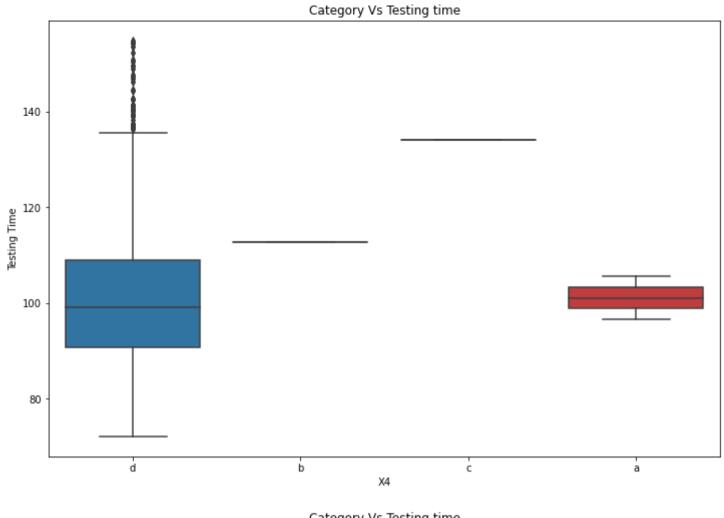


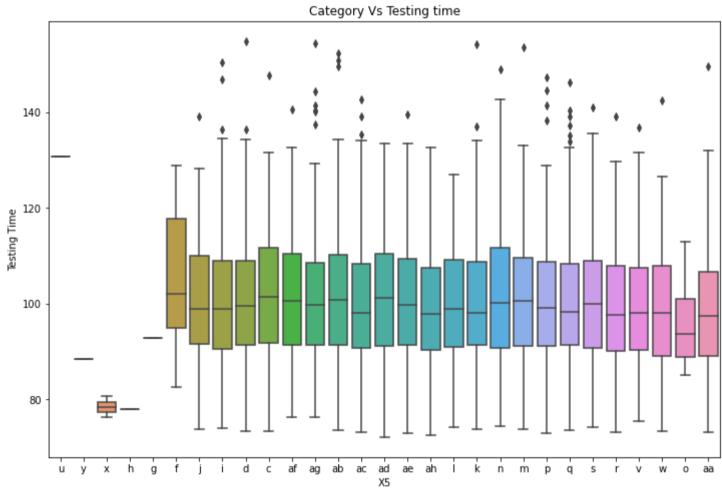


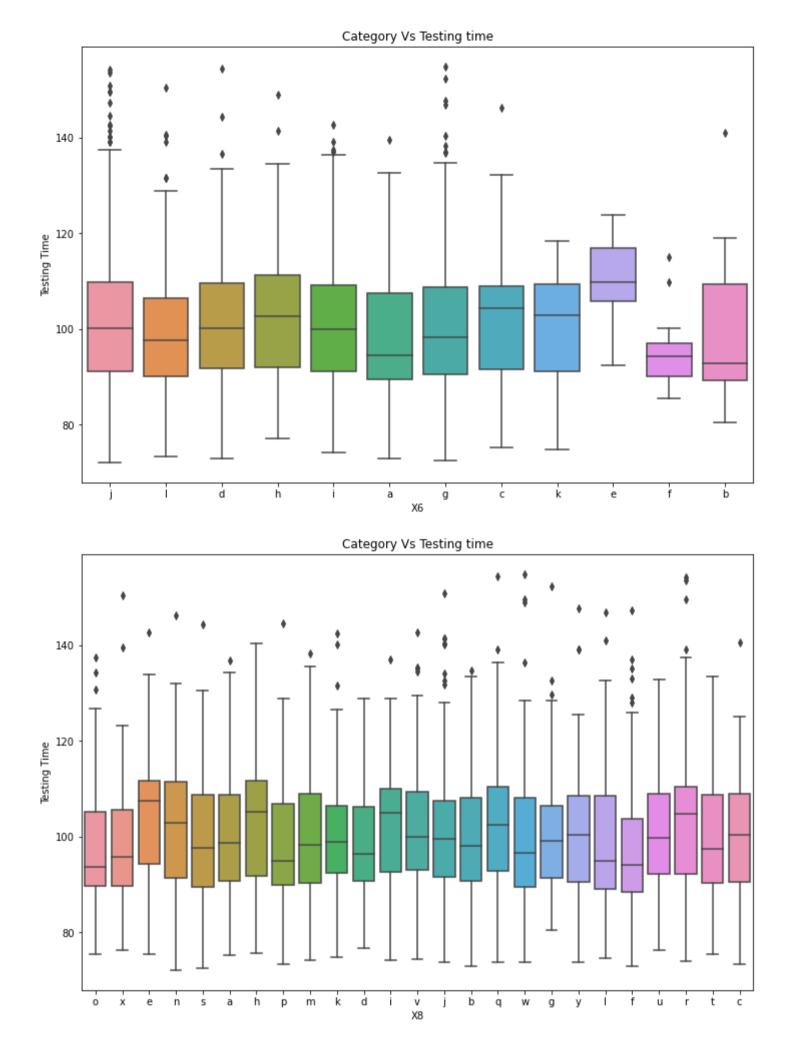












From these above boxplots for categorical features I can say:

- We can see after removal of outliers(extreme 'y' values) dataset is looking much cleaner
- Features X0,X1,X2,X3,X5,X6,X8 contain some important information as their variance is quite high
- Feature X4 seems to have very less variance which means it has very less information

Hence, I can surely remove X4 from the dataset because of it's low variance(less information)

4.1.3.2 Analysis of Binary Features

```
In [18]: | binary_train_data = clean_train[Binary_features]
          print(binary_train_data.shape)
          binary_train_data.head()
          (4201, 368)
Out[18]:
             X10 X11 X12 X13 X14 X15 X16 X17 X18 X19 ... X375 X376 X377 X378 X379 X380 X382 X383 X384 X385
          0
               0
                   0
                        0
                                 0
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                                                                 0
                                                                                                              0
```

Binary features are way more than categorical features in quantity (368), I think it is better to find the variance of all these features and analyze them than visualizing one by one as it will become cumbersome task. So I am finding variances of all the Binary features and will choose the important features based on their variances.

```
In [19]: # now calculate variances of all the Binary features and collect them into list with their feature name
         var = []
         for f in Binary_features:
             v = binary_train_data[f].var()
             var.append((f,v))
         # Convert the list of tuples of feature and respective variance into dictionary
         var_dict = dict(var)
In [20]: # Create a dataframe for feature and it's variance
         var_df = pd.DataFrame(var_dict.keys(), columns=['feature'])
         var_df['variance'] = var_dict.values()
         # let's sort the dataframe by variance
         var_df
Out[20]:
```

	feature	variance
0	X10	0.013156
1	X11	0.000000
2	X12	0.068971
3	X13	0.054510
4	X14	0.244908
363	X380	0.008030
364	X382	0.007561
365	X383	0.001664
366	X384	0.000476
367	X385	0.001427

5 rows × 368 columns

368 rows × 2 columns

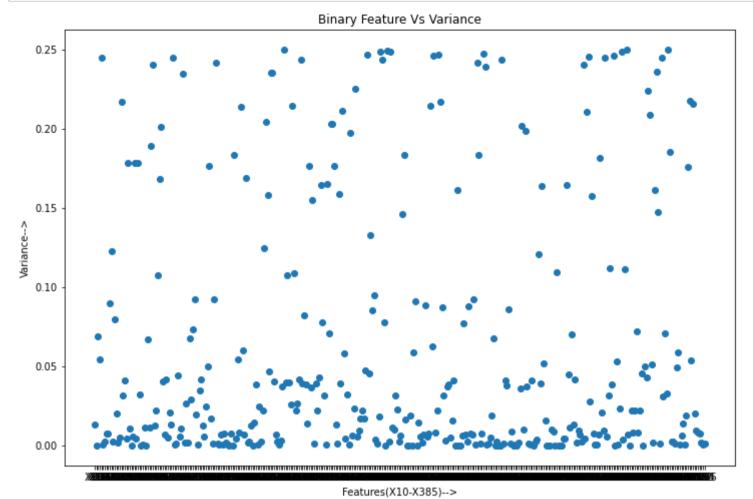
```
In [21]: var_df.describe()
```

Out[21]:

	variance
count	368.000000
mean	0.061796
std	0.080493
min	0.000000
25%	0.003913
50%	0.021880
75%	0.087996
max	0.250040

From above description minimum value of variance is zero and the maximum is 0.250040. Now I am plotting an scatter plot for above dataframe values so as check their distribution.

```
In [22]: plt.figure(figsize=(12,8))
    plt.scatter(var_df['feature'], var_df['variance'])
    plt.title("Binary Feature Vs Variance")
    plt.xlabel("Features(X10-X385)-->")
    plt.ylabel("Variance-->")
    plt.show()
```



- Above scatter plot says there are many values which are having 0 variance.
 Roughly I am also able to see some features with same variance, but it is not clearly visible, I will check it by their exact values.

Now let's check for the features which are having 0 variance and same variance

```
In [23]: # Create dataframe for zero variance features
zero_var_df = var_df[var_df['variance']==0]
zero_var_df.head()
```

Out[23]:

	teature	variance
1	X11	0.0
81	X93	0.0
95	X107	0.0
217	X233	0.0
219	X235	0.0

In [24]: print(f"There following {zero_var_df.shape[0]} features having 0 variance:\n")
print(zero_var_df['feature'].values)

There following 13 features having 0 variance:

```
['X11' 'X93' 'X107' 'X233' 'X235' 'X268' 'X289' 'X290' 'X293' 'X297' 'X330' 'X339' 'X347']
```

```
In [25]: # create a dataframe which have duplicate values which means same variance features
    same_var_df = var_df['variance'].duplicated(keep='first').values]
    # also remove all the 0 variance
    same_var_df = same_var_df[same_var_df['variance']!=0]
    same_var_df.head()
```

Out[25]:

	reature	variance
24	X35	0.178138
26	X37	0.178138
28	X39	0.000238
46	X57	0.013156
64	X76	0.041456

• From above analysis of categorical fetaures and Binary features I have come to the conlcusion that I can drop the features which are having zero variance, same variance and the ones with very less variance. Because their low variance will not contribute much for the prediction of testing time while modeling. Now I will collect all the features to be dropped together.

```
In [27]: # categorical feature with less variance
    cat_drops = ['X4']
    # Binary fearures with zero variance
    zero_drops = list(zero_var_df['feature'].values)
    # Binary features with same variance
    same_drops = list(same_var_df['feature'].values)
    # combine binary drops
    all_binary_drops = zero_drops + same_drops
    # concatenate all the features to be dropped
    drop_feat = cat_drops + all_binary_drops
    print(f"These are the total {len(drop_feat)} features I can drop:\n\n", drop_feat)
```

These are the total 67 features I can drop:

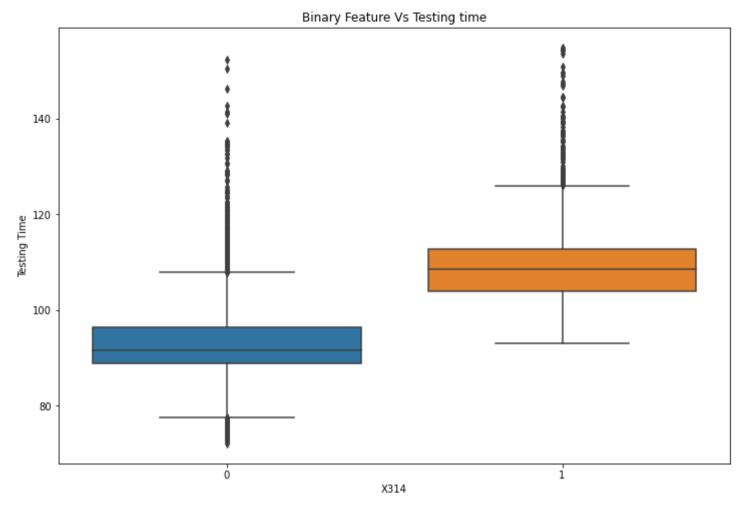
```
['X4', 'X11', 'X93', 'X107', 'X233', 'X235', 'X268', 'X289', 'X290', 'X293', 'X297', 'X330', 'X339', 'X347', 'X35', 'X37', 'X39', 'X57', 'X76', 'X84', 'X94', 'X102', 'X113', 'X119', 'X120', 'X122', 'X130', 'X134', 'X136', 'X146', 'X147', 'X157', 'X172', 'X194', 'X199', 'X205', 'X213', 'X214', 'X216', 'X222', 'X226', 'X227', 'X232', 'X239', 'X242', 'X243', 'X244', 'X245', 'X245', 'X248', 'X253', 'X254', 'X262', 'X263', 'X266', 'X279', 'X296', 'X299', 'X302', 'X320', 'X324', 'X326', 'X360', 'X364', 'X365', 'X382', 'X385']
```

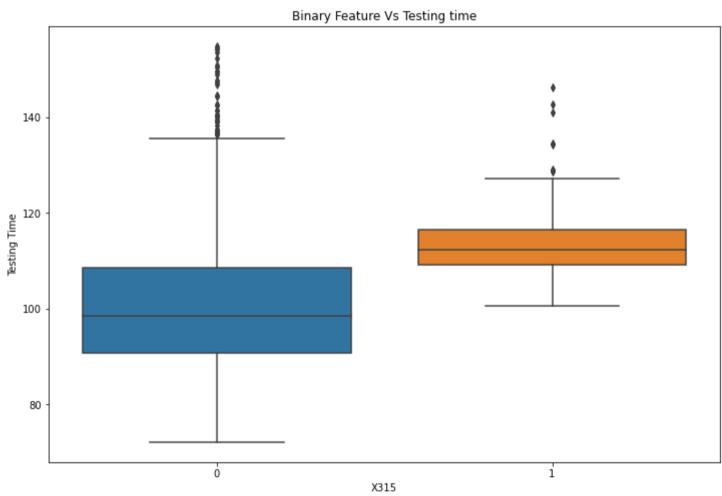
Now let's just find out some important binary by using a random forest model and just perform visual EDA for those features only.

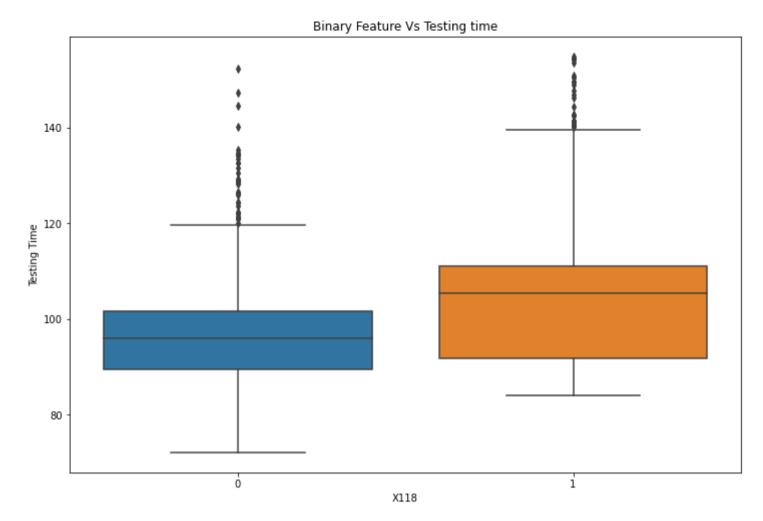
```
In [28]: # First drop the non informative binary variables we found above
         binary_tr_mod = binary_train_data.drop(all_binary_drops, axis=1)
         result_y = clean_train['y']
         def get_imp_features(x_data,y_data, top):
             #create a Regressor model
             rf = RandomForestRegressor(n_estimators = 100, n_jobs = -1)
             # fit the model on data
             rf.fit(x_data, y_data)
             # get the sorted indices of features
             imp_feat_idx = np.argsort(rf.feature_importances_)[::-1]
             # return only top required indices
             return imp_feat_idx[:top]
         top_binary_ids = get_imp_features(binary_tr_mod, result_y, 8)
         top_binary_feat = binary_tr_mod.T.index[top_binary_ids]
         print(f"These are top 8 binary features :\n {list(top_binary_feat)}")
         These are top 8 binary features :
          ['X314', 'X315', 'X118', 'X29', 'X54', 'X189', 'X46', 'X127']
```

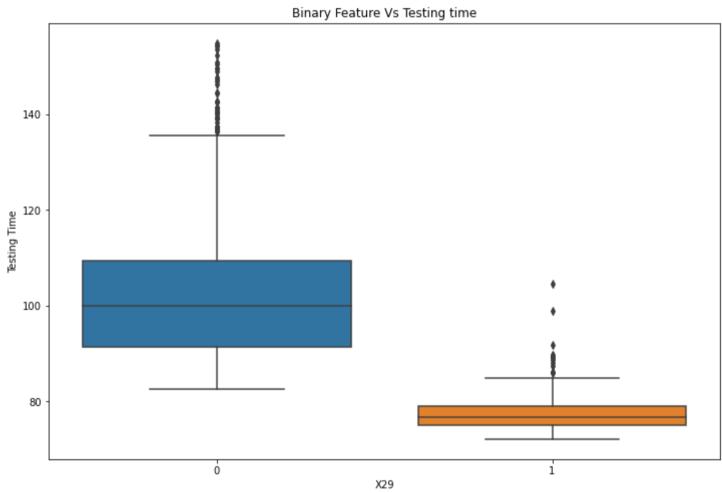
Now I have these 8 important binary features from above let's plot a boxplot for all these features.

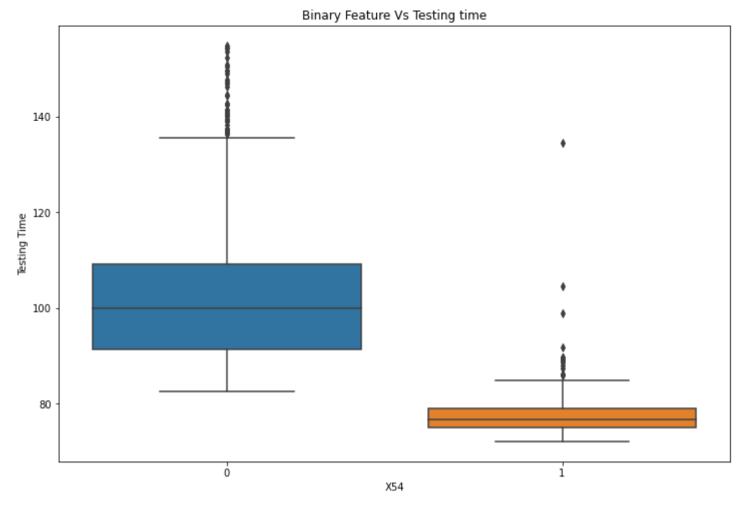
```
In [29]: for feat in top_binary_feat:
    plt.figure(figsize=(12,8))
    sns.boxplot(binary_tr_mod[feat], result_y)
    plt.title("Binary Feature Vs Testing time")
    plt.xlabel(feat)
    plt.ylabel("Testing Time")
```

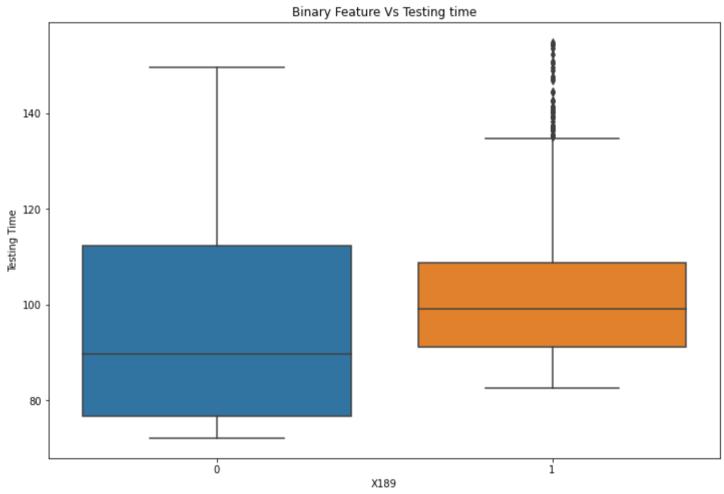


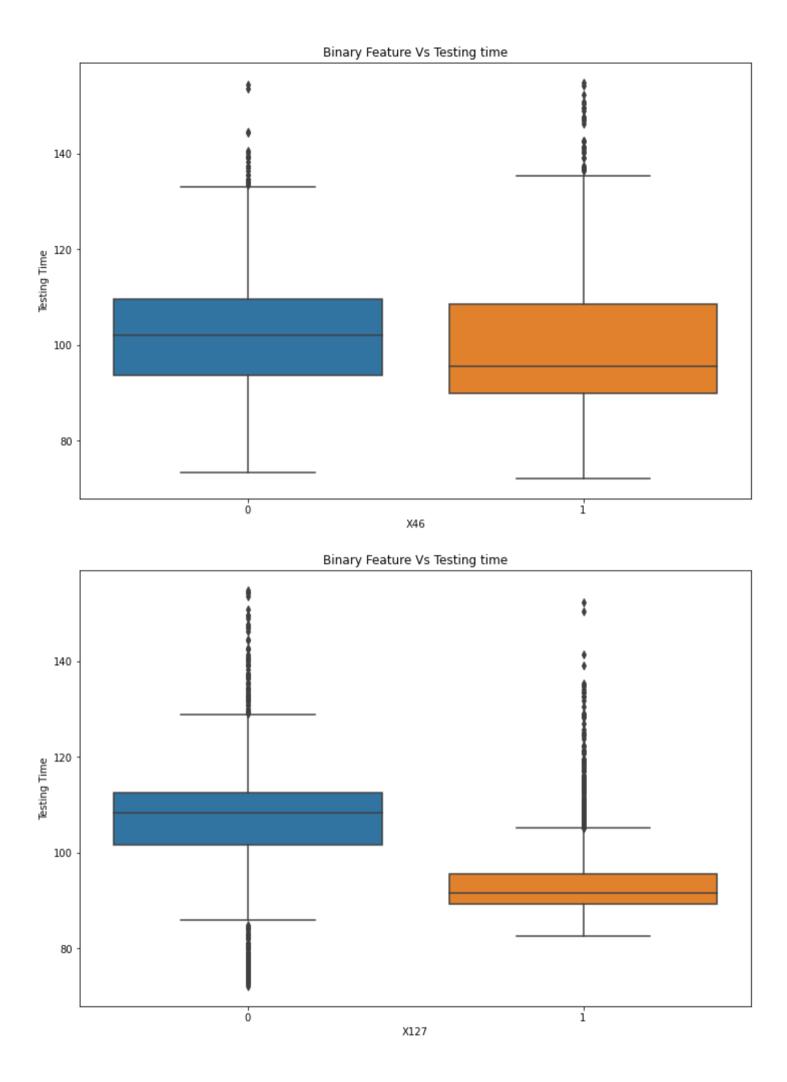












From above plots I can see these important binary variables are prety well distributed. I can say as the feature's presence or absence is affecting the testing time to change.

- For features 'X314', 'X315', 'X118', 'X189' when these are present in the car configuration then most of the configurations take more time for testing.
- For features 'X29', 'X54','X127', the configurations which are not having these features are tending to take more testing time.
- For 'X46', the configurations having almost similar testing when it present and also when it is not presnt in the configuration.

4.1.3 EDA Summary

- There are No NaN values in the dataset
- · There are No duplicate rows in the dataset
- Clipped dependent variable at 155 as threshold time and considered values all above 155 as outliers
- Removed low variance categorical feature:

['X4']

· Removed zero variance binary features:

```
['X11', 'X93', 'X107', 'X233', 'X235', 'X268', 'X289', 'X290', 'X293', 'X297', 'X330', 'X339', 'X347']
```

• Removed same variance binary features:

```
['X35', 'X37', 'X39', 'X57', 'X76', 'X84', 'X94', 'X102', 'X113', 'X119', 'X120', 'X122', 'X130', 'X134', 'X136', 'X146', 'X147', 'X157', 'X172', 'X194', 'X199', 'X205', 'X213', 'X214', 'X216', 'X222', 'X226', 'X227', 'X232', 'X239', 'X242', 'X243', 'X244', 'X245', 'X247', 'X248', 'X253', 'X254', 'X262', 'X263', 'X266', 'X279', 'X296', 'X299', 'X302', 'X320', 'X320', 'X326', 'X360', 'X360', 'X365', 'X382', 'X385']
```

4.2 Data Preprocessing

I am using LabelEncoder for encoding categorical features and Normalizer for normalizing them.

Let's create a function for preprocessing the Categorical features,

```
In [30]: | def preprocess_categorical(data, IDs):
             data : pandas dataframe
             IDs: ID feature
             return: dataframe, labels
             This function takes the dataframe as input,
             encodes and normalizes the
             categorical features.
             # create empty lists for collecting feature names
             cat_features = []
             Binary_features = []
             # Collect the categorical and binary feature names
             for f in data.columns:
                 if data[f].dtype == 'object':
                      cat_features.append(f)
                  elif data[f].dtype == 'int' and f != 'ID':
                      Binary_features.append(f)
             # create categorical feature dataframe
             cat_df = data[cat_features]
             # create binary feature dataframe
             bin_df = data[Binary_features]
             bin_df.insert(0, 'ID', IDs.values)
             # Now encode each categorical feature
             for feature in cat_features:
                  encoder = LabelEncoder()
                  cat_df[feature] = encoder.fit_transform(cat_df[feature].values)
             # normalize the enocded categorical features
             # normalized = Normalizer().fit_transform(cat_df)
             # Create new categorical feature dataframe
              cat_df = pd.DataFrame(cat_df, columns = cat_features)
              cat_df.insert(0, 'ID', IDs.values)
             # Merge binary and categorical dataframes together
             new_data = pd.merge(cat_df, bin_df, on='ID', how='left')
             # return dataframe and labels
             if 'y' in data.columns:
                 labels = data['y']
                  return new data, labels
                  return new_data
```

4.2.1 Preprocess Train set

```
In [31]: final_train = clean_train.drop(drop_feat, axis=1)
    final_train = final_train.drop('ID', axis=1)
    train_ID = clean_train['ID'].copy()
    print(f"Before removing non informative features:{clean_train.shape}")
    print(f"After removing non informative features:{final_train.shape}")
    final_train.head()
```

Before removing non informative features: (4201, 378) After removing non informative features: (4201, 310)

Out[31]:

	у	X0	X1	X2	Х3	X5	X6	X8	X10	X12	 X373	X374	X375	X376	X377	X378	X379	X380	X383	X384
0	130.81	k	٧	at	а	u	j	0	0	0	 0	0	0	0	1	0	0	0	0	0
1	88.53	k	t	av	е	у	I	0	0	0	 0	0	1	0	0	0	0	0	0	0
2	76.26	az	w	n	С	x	j	х	0	0	 0	0	0	0	0	0	0	0	0	0
3	80.62	az	t	n	f	x	I	е	0	0	 0	0	0	0	0	0	0	0	0	0
4	78.02	az	٧	n	f	h	d	n	0	0	 0	0	0	0	0	0	0	0	0	0

5 rows × 310 columns

Encode the training dataset

```
In [32]: # get the encoded and normalized categorical features and labels
X_train, y_train= preprocess_categorical(final_train, train_ID)
X_train.head()
```

Out[32]:

		ID	ΧŪ	Х1	X2	Х3	Х5	Х6	X8	X10	X12	•••	X373	X374	X375	X376	X377	X378	X379	X380	X383	X384	
)	0	32	23	17	0	24	9	14	0	0		0	0	0	0	1	0	0	0	0	0	
	1	6	32	21	19	4	28	11	14	0	0		0	0	1	0	0	0	0	0	0	0	
:	2	7	20	24	34	2	27	9	23	0	0		0	0	0	0	0	0	0	0	0	0	
;	3	9	20	21	34	5	27	11	4	0	0		0	0	0	0	0	0	0	0	0	0	
	1	13	20	23	34	5	12	3	13	0	0		0	0	0	0	0	0	0	0	0	0	

5 rows × 310 columns

```
In [33]: y_train.head()
Out[33]: 0   130.81
```

1 88.53 2 76.26 3 80.62 4 78.02

Name: y, dtype: float64

4.2.2 Preprocess Test set

Remove Non-informative features from test set

```
In [34]: final_test = test.drop(drop_feat, axis=1)
    final_test = final_test.drop('ID', axis=1)
    test_ID = test['ID'].copy()
    print(f"Before removing non informative features:{test.shape}")
    print(f"After removing non informative features:{final_test.shape}")
    final_test.head()
```

Before removing non informative features: (4209, 377) After removing non informative features: (4209, 309)

Out[34]:

	X0	X1	X2	Х3	X5	X6	X8	X10	X12	X13	 X373	X374	X375	X376	X377	X378	X379	X380	X383	X384
0	az	٧	n	f	t	а	w	0	0	0	 0	0	0	0	0	1	0	0	0	0
1	t	b	ai	а	b	g	у	0	0	0	 0	0	0	0	1	0	0	0	0	0
2	az	٧	as	f	а	j	j	0	0	0	 0	0	0	0	0	1	0	0	0	0
3	az	1	n	f	z	1	n	0	0	0	 0	0	0	0	0	1	0	0	0	0
4	W	s	as	С	у	i	m	0	0	0	 0	0	1	0	0	0	0	0	0	0

5 rows × 309 columns

```
In [35]: # get the encoded and normalized categorical features
         X_test = preprocess_categorical(final_test, test_ID)
         X_test.head()
Out[35]:
            ID X0 X1 X2 X3 X5 X6 X8 X10 X12 ... X373 X374 X375 X376 X377 X378 X379 X380 X383 X384
          0 1 21 23 34
                                 0 22
                          5 26
                                             0 ...
                                                           0
                                                                0
                                                                      0
                                                                           0
                                                                                     0
                                                                                                0
                                                                                                     0
            2 42
                                 6 24
                                             0 ...
                  3
                      8
                          0
                              9
                                         0
                                                      0
                                                           0
                                                                0
                                                                      0
                                                                                0
                                                                                     0
                                                                                          0
                                                                                                0
                                                                                                     0
                                                                           1
            3 21 23 17
                          5
                              0
                                 9
                                   9
                                         0
                                             0 ...
                                                      0
                                                           0
                                                                      0
                                                                           0
                                                                                     0
                                                                                                     0
             4 21 13 34
                          5 31 11 13
                                             0 ...
                                                      0
                                                           0
                                                                                1
                                                                                     0
                                                                                                     0
```

5 rows × 310 columns

5 45 20 17 2 30 8 12

5. Feature Engineering

In this section I am going to create new features like PCA, SVD, Feature Interactions.

Now we have X_train and X_test data, let's split train set into train and cross validation set first, then I will add new features

0 ...

0

0

0

0

0

0

0

0

0

0

5.1 Original set

```
In [36]: X_train, y_train = preprocess_categorical(final_train, train_ID)
         X_train = X_train.drop('ID', axis=1)
         X_train, X_cv, y_train, y_cv = train_test_split(X_train, y_train, test_size=0.2, random_state=42)
         X_test = preprocess_categorical(final_test, test_ID)
         X_test = X_test.drop('ID', axis=1)
         print("Train set:")
         print(X_train.shape)
         print(y_train.shape)
         print("CV set:")
         print(X_cv.shape)
         print(y_cv.shape)
         print("Test set:")
         print(X_test.shape)
         Train set:
         (3360, 309)
         (3360,)
         CV set:
         (841, 309)
         (841,)
         Test set:
         (4209, 309)
```

5.2 PCA

PCA of binary features

```
In [47]: # Lets take top 10 pca components
    components = 10
    categories = ['X0','X1', 'X2', 'X3', 'X5','X6', 'X8']

    pca = PCA(n_components=components, random_state=420)

    pca_train = pca.fit_transform(X_train.drop(categories, axis=1))
    pca_cv = pca.transform(X_cv.drop(categories, axis=1))
    pca_test = pca.transform(X_test.drop(categories, axis=1))

    print(pca_train.shape)
    print(pca_train.shape)
    print(pca_test.shape)

(3360, 10)
    (841, 10)
    (4209, 10)
```

Recent work by Gavish and Donoho provides an optimal truncation value, or hard threshold, under certain conditions, providing a principled approach to obtaining low-rank matrix approximations using the SVD.

It determines the optimal hard threshold 'T' for singular value truncation under the assumption that a matrix has a low-rank structure contaminated with Gaussian white noise. This work builds on a significant literature surrounding various techniques for hard thresholding of singular values.

If $X \in \mathbb{R}^n \times m$ is rectangular and m < n, then the aspect ratio

 $\beta = m/n$

When noise is unknown there is no closed-form solution for 'T', and it must be approximated numerically,

For unknown noise, and a rectangular matrix $X \in \mathbb{R}^n \times \mathbb{R}$, the optimal hard threshold is given by:

$$\tau = \omega(\beta)\sigma_{\text{med}}$$
.

omed is the median singular value

Here, $\omega(\beta) = \lambda(\beta)/\mu\beta$, where $\mu\beta$ is the solution to the following problem:

$$\int_{(1-\beta)^2}^{\mu_\beta} \frac{\left[\left((1+\sqrt{\beta})^2 - t \right) \left(t - (1-\sqrt{\beta})^2 \right) \right]^{1/2}}{2\pi t} dt = \frac{1}{2}.$$

The median $\mu\beta$ and hence the coefficient $\omega(\beta)$ are not available analytically;

Some values of coefficient $\omega(\beta)$ are tabulated in Table below for convenience.

β	$\omega(eta)$	β	$\omega(\beta)$
0.05	1.5194	0.55	2.2365
0.10	1.6089	0.60	2.3021
0.15	1.6896	0.65	2.3679
0.20	1.7650	0.70	2.4339
0.25	1.8371	0.75	2.5011
0.30	1.9061	0.80	2.5697
0.35	1.9741	0.85	2.6399
0.40	2.0403	0.90	2.7099
0.45	2.106	0.95	2.7832
0.50	2.1711	1.00	2.8582

Now let's find out the Hard Threshold using above method

```
In [42]: # get the matrix factors
    categories = ['X0','X1', 'X2', 'X3', 'X5','X6', 'X8']
    U, S, VT = np.linalg.svd(X_train.drop(categories, axis=1),full_matrices=1)
    # calculate the aspect ratio θ
    m = X_train.drop(categories, axis=1).shape[1]
    n = X_train.drop(categories, axis=1).shape[0]
    β = m/n
    β
```

Out[42]: 0.08988095238095238

```
In [43]: # 0.08988095238095238 near 0.10

# hence let's take w(6) value for 6 = 0.10 from the above table

w_\beta = 1.6089

# find the median singular value

ymed = np.median(S)

# find Hard threshold

cutoff = w_\beta * ymed

print(f"The Hard Threshold for Truncation = {cutoff}")

# get the number of components

r = np.max(np.where(S > cutoff))

print(f"Number of total components to be selected = {r}")
```

The Hard Threshold for Truncation = 5.349072242419465 Number of total components to be selected = 117

Now by using above value for number of components add SVD feature

SVD of binary features

5. Machine Learning Models

5.1 KNeighborsRegressor

I will use the only original dataset for this model

```
In [57]: import time
         start = time.time()
         leaf_sizes = list(range(1,50))
         neighbors = list(range(1,30))
         norms=[1,2]
         # create parameters dictionary
         parameters = {'leaf_size':leaf_sizes, 'n_neighbors':neighbors, 'p':norms}
         #Create a KNN Regressor model
         knn = KNeighborsRegressor()
         #Tune hyperparameters using RandomizedSearchCV
         regressor = RandomizedSearchCV(knn, param_distributions=parameters, verbose=10, n_jobs=-1)
         #Fit the model
         best_regressor = regressor.fit(X_train, y_train)
         # get the best parameters
         best_K = best_regressor.best_estimator_.get_params()['n_neighbors']
         best_leaf_size = best_regressor.best_estimator_.get_params()['leaf_size']
         norm = best_regressor.best_estimator_.get_params()['p']
         #Print The best parameters
         print('Best K:', best_K)
         print('Best leaf_size=', best_leaf_size)
         print('Best norm:', norm)
         elapsed = time.time() - start
         print(f"Time elapsed: {elapsed}")
         Fitting 5 folds for each of 10 candidates, totalling 50 fits
         [Parallel(n_jobs=-1)]: Using backend LokyBackend with 4 concurrent workers.
         [Parallel(n_jobs=-1)]: Done 5 tasks
                                                    | elapsed:
         [Parallel(n_jobs=-1)]: Done 10 tasks
                                                      elapsed:
                                                                  1.6s
         [Parallel(n_jobs=-1)]: Done 17 tasks
                                                    | elapsed:
                                                                  3.1s
         [Parallel(n_jobs=-1)]: Done 24 tasks
                                                    | elapsed:
                                                                  4.9s
         [Parallel(n_jobs=-1)]: Done 33 tasks
                                                                  7.8s
                                                    | elapsed:
                                                    | elapsed: 10.2s
         [Parallel(n_jobs=-1)]: Done 42 tasks
         Best K: 13
         Best leaf_size= 41
         Best norm: 1
         Time elapsed: 12.097684621810913
         [Parallel(n_jobs=-1)]: Done 50 out of 50 | elapsed: 11.9s finished
In [58]: | # Lets use best parameters found above
         knn = KNeighborsRegressor(n_neighbors=best_K, leaf_size=best_leaf_size, p=norm)
         knn.fit(X_train, y_train)
         pred_train = knn.predict(X_train)
         train_score = r2_score(y_train, pred_train)
         print(f"For K={best_K}, Train R2 = {train_score}")
         pred_cv = knn.predict(X_cv)
         cv_score = r2_score(y_cv, pred_cv)
         print(f"For K={best_K}, CV R2 = {cv_score}")
         For K=13, Train R2 = 0.581966843169116
         For K=13, CV R2 = 0.4738065919984832
In [59]: | X_full_train = np.vstack((X_train, X_cv))
         y_full_train = np.vstack((y_train.values.reshape(-1,1), y_cv.values.reshape(-1,1)))
         knn.fit(X_full_train, y_full_train)
Out[59]: KNeighborsRegressor(leaf_size=41, n_neighbors=13, p=1)
In [60]: | filename = 'KNN_Original_feat_model.sav'
         knn = joblib.dump(knn, filename)
         print(f'Saved {filename}')
         Saved KNN_Original_feat_model.sav
In [61]: | filename = 'KNN_Original_feat_model.sav'
         knn = joblib.load(filename)
         print(f'Loaded {filename}')
         Loaded KNN_Original_feat_model.sav
In [64]: pred train = knn.predict(X full train)
         train_score = r2_score(y_full_train, pred_train)
         print(f"For K={best_K}, Train R2 = {train_score}")
```

For K=13, Train R2 = 0.5817266349749117

```
In [65]: pred_test = knn.predict(X_test)
          submission_knn = pd.read_csv('sample_submission.csv')
          submission_knn['y'] = pred_test
          submission_knn.to_csv(f'sample_submission_knn={best_K}.csv', index=False)
          submission_knn.head()
Out[65]:
             ID
          0 1 77.979231
          1 2 93.309231
          2 3 78.286154
            4 77.040000
           4 5 111.300769
                                                                                    Private Score
                                                                                                       Public Score
              Submission and Description
                                                                                       0.43537
                                                                                                         0.46360
              sample_submission_knn13.csv
              just now by Harsh Jadhav
```

- Train R2 = 0.5817266349749117
- Test Private R2 = 0.43537
- Test Public R2 = 0.46360

Here KNeighborsRegressor() with K=13 is overfitting on the original dataset because we are getting low R^2 value for both cross validation and testing set than training set. But one thing to notice is having a cross validation set is good choice as I can trust the cross validation results before doing testing.

5.2 Decision Tree Regressor

5.2.1 With Original Dataset

```
In [66]: import time
         start = time.time()
         depth = [1, 5, 10, 50, 100, 500, 1000]
         # create parameters dictionary
         parameters = {'max_depth' : depth}
         #Create a Decision Tree Regressor model
         dtr = DecisionTreeRegressor()
         #Tune hyperparameters using RandomizedSearchCV
         regressor = RandomizedSearchCV(dtr, param_distributions=parameters, verbose=10, n_jobs=-1)
         #Fit the model
         best_regressor = regressor.fit(X_train, y_train)
         # get the best parameters
         best_max_depth = best_regressor.best_estimator_.get_params()['max_depth']
         #Print The best parameters
         print('Best max_depth:', best_max_depth)
         elapsed = time.time() - start
         print(f"Time elapsed: {elapsed}")
         Fitting 5 folds for each of 7 candidates, totalling 35 fits
         [Parallel(n_jobs=-1)]: Using backend LokyBackend with 4 concurrent workers.
         [Parallel(n_jobs=-1)]: Done 5 tasks
                                                    | elapsed:
                                                                  0.9s
         [Parallel(n jobs=-1)]: Done 10 tasks
                                                      elapsed:
                                                                  1.0s
         [Parallel(n_jobs=-1)]: Done 17 tasks
                                                      elapsed:
                                                                  1.2s
         [Parallel(n_jobs=-1)]: Done 24 tasks
                                                     | elapsed:
                                                                  1.5s
         Best max_depth: 5
         Time elapsed: 2.031101703643799
         [Parallel(n_jobs=-1)]: Done 32 out of 35 | elapsed:
                                                                  1.8s remaining:
                                                                                      0.2s
         [Parallel(n_jobs=-1)]: Done 35 out of 35 | elapsed:
                                                                  1.9s finished
In [67]: | # Lets use best parameters found above
         dtr1 = DecisionTreeRegressor(max_depth=best_max_depth)
         dtr1.fit(X_train, y_train)
         pred_train = dtr1.predict(X_train)
         train_score = r2_score(y_train, pred_train)
         print(f"For max depth={best max depth}, Train R2 = {train score}")
         pred_cv = dtr1.predict(X_cv)
         cv_score = r2_score(y_cv, pred_cv)
         print(f"For max depth={best max depth}, CV R2 = {cv score}")
         For max_depth=5, Train R2 = 0.6339722490371381
         For max_depth=5, CV R2 = 0.586507102894404
```

```
In [68]: | X_full_train = np.vstack((X_train, X_cv))
         y_full_train = np.vstack((y_train.values.reshape(-1,1), y_cv.values.reshape(-1,1)))
         dtr1 = DecisionTreeRegressor(max_depth=best_max_depth)
         dtr1.fit(X_full_train, y_full_train)
Out[68]: DecisionTreeRegressor(max_depth=5)
In [71]: | filename = 'DTR_Original_feat_model.sav'
         dtr1 = joblib.dump(dtr1, filename)
         print(f'Saved {filename}')
         Saved DTR_Original_feat_model.sav
In [72]: | filename = 'DTR_Original_feat_model.sav'
          dtr1 = joblib.load(filename)
         print(f'Loaded {filename}')
         Loaded DTR_Original_feat_model.sav
In [73]: | pred_train = dtr1.predict(X_full_train)
         train_score = r2_score(y_full_train, pred_train)
         print(f"For max_depth={best_max_depth}, Train R2 = {train_score}")
         For max_depth=5, Train R2 = 0.6312890285381911
In [74]: | pred_test = dtr1.predict(X_test)
          submission_DTR = pd.read_csv('sample_submission.csv')
          submission_DTR['y'] = pred_test
          submission_DTR.to_csv(f'sample_submission_DTR={best_max_depth}.csv', index=False)
         submission_DTR.head()
Out[74]:
             ID
                       У
          0 1 77.659766
          1 2 130.810000
          2 3 77.659766
          3 4 77.659766
           4 5 110.368405
              Submission and Description
                                                                                   Private Score
                                                                                                     Public Score
                                                                                     0.53732
                                                                                                       0.55129
              sample_submission_DTR5.csv
              just now by Harsh Jadhav
```

- Train R2 = 0.6312890285381911
- Test Private R2 = 0.53732
- Test Public R2 = 0.55129

5.2.2 With Original Dataset + PCA + SVD

```
In [75]: train_svd_pca = np.hstack((X_train, pca_train, svd_train))
    cv_svd_pca = np.hstack((X_cv, pca_cv, svd_cv))
    test_svd_pca = np.hstack((X_test, pca_test, svd_test))

    print(train_svd_pca.shape)
    print(cv_svd_pca.shape)
    print(test_svd_pca.shape)

(3360, 436)
(841, 436)
(4209, 436)
```

```
In [76]: import time
         start = time.time()
         depth = [1, 3, 5, 10, 50, 100, 500, 1000]
         # create parameters dictionary
         parameters = {'max_depth' : depth}
         #Create a Decision Tree Regressor model
         dtr = DecisionTreeRegressor()
         #Tune hyperparameters using RandomizedSearchCV
         regressor = RandomizedSearchCV(dtr, param_distributions=parameters, verbose=10, n_jobs=-1)
         #Fit the model
         best_regressor = regressor.fit(train_svd_pca, y_train)
         # get the best parameters
         best_max_depth = best_regressor.best_estimator_.get_params()['max_depth']
         #Print The best parameters
         print('Best max_depth:', best_max_depth)
         elapsed = time.time() - start
         print(f"Time elapsed: {elapsed}")
         Fitting 5 folds for each of 8 candidates, totalling 40 fits
         [Parallel(n_jobs=-1)]: Using backend LokyBackend with 4 concurrent workers.
         [Parallel(n_jobs=-1)]: Done 5 tasks
                                                    | elapsed:
                                                                  1.0s
         [Parallel(n_jobs=-1)]: Done 10 tasks
                                                    | elapsed:
                                                                  1.3s
         [Parallel(n_jobs=-1)]: Done 17 tasks
                                                    elapsed:
                                                                  1.8s
         [Parallel(n_jobs=-1)]: Done 24 tasks
                                                    | elapsed:
                                                                  3.1s
                                                 | elapsed:
         [Parallel(n_jobs=-1)]: Done 33 tasks
                                                                  5.4s
         [Parallel(n_jobs=-1)]: Done 38 out of 40 | elapsed:
                                                                  6.3s remaining:
                                                                                     0.3s
         [Parallel(n_jobs=-1)]: Done 40 out of 40 | elapsed:
                                                                  6.5s finished
         Best max_depth: 3
         Time elapsed: 6.751556634902954
In [77]: # Lets use best parameters found above
         dtr2 = DecisionTreeRegressor(max_depth=best_max_depth)
         dtr2.fit(train_svd_pca, y_train)
         pred_train = dtr2.predict(train_svd_pca)
         train_score = r2_score(y_train, pred_train)
         print(f"For max_depth={best_max_depth}, Train R2 = {train_score}")
         pred_cv = dtr2.predict(cv_svd_pca)
         cv_score = r2_score(y_cv, pred_cv)
         print(f"For max_depth={best_max_depth}, CV R2 = {cv_score}")
         For max_depth=3, Train R2 = 0.6197223844385611
         For max_depth=3, CV R2 = 0.5965378027870976
In [78]: | X_full_train_svd_pca = np.vstack((train_svd_pca, cv_svd_pca))
         y_full_train = np.vstack((y_train.values.reshape(-1,1), y_cv.values.reshape(-1,1)))
         dtr2 = DecisionTreeRegressor(max_depth=best_max_depth)
         dtr2.fit(X_full_train_svd_pca, y_full_train)
Out[78]: DecisionTreeRegressor(max_depth=3)
In [79]: | filename = 'DTR_svd_pca_model.sav'
         dtr2 = joblib.dump(dtr2, filename)
         print(f'Saved {filename}')
         Saved DTR_svd_pca_model.sav
In [80]: | filename = 'DTR_svd_pca_model.sav'
         dtr2 = joblib.load(filename)
         print(f'Loaded {filename}')
         Loaded DTR_svd_pca_model.sav
In [81]: | pred_train = dtr2.predict(X_full_train_svd_pca)
         train_score = r2_score(y_full_train, pred_train)
         print(f"For max_depth={best_max_depth}, Train R2 = {train_score}")
         For max_depth=3, Train R2 = 0.6155964859539103
```

```
In [82]: | pred_test = dtr2.predict(test_svd_pca)
         submission_DTR = pd.read_csv('sample_submission.csv')
         submission_DTR['y'] = pred_test
         submission_DTR.to_csv(f'sample_submission_DTR_svd_pca_={best_max_depth}.csv', index=False)
         submission_DTR.head()
Out[82]:
            ID
          0 1 77.964862
          1 2 94.044258
          2 3 77.964862
            4 77.964862
          4 5 112.319644
              Submission and Description
                                                                                  Private Score
                                                                                                    Public Score
                                                                                    0.53800
              sample_submission_DTR_svd_pca_3.csv
                                                                                                     0.55070
              just now by Harsh Jadhav
```

- Train R2 = 0.6155964859539103
- Test Private R2 = 0.53800
- Test Public R2 = 0.55070

This model is not performing that well but improved from KnearestRegressor(), let's try another model

5.3 Random Forest Regressor

5.3.1 With Original Dataset

```
In [112]: import time
          start = time.time()
          # Number of trees in random forest
          n_estimators = [10, 25, 50, 100, 200, 300, 400, 500]
          # Number of features to consider at every split
          max_features = ['auto', 'sqrt']
          # Maximum number of levels in tree
          max_depth = [3, 5, 10, 15, 20, 25, 30]
          # Minimum number of samples required to split a node
          min_samples_split = [2, 3, 5, 10, 15, 100]
          # Minimum number of samples required at each leaf node
          min_samples_leaf = [1, 2, 5, 10]
          # create parameters dictionary
          parameters = {'n_estimators': n_estimators,
                          'max_features': max_features,
                          'max_depth': max_depth,
                          'min_samples_split': min_samples_split,
                          'min_samples_leaf': min_samples_leaf}
          #Create a Random Forest Regressor model
          rf = RandomForestRegressor()
          #Tune hyperparameters using RandomizedSearchCV
          regressor = RandomizedSearchCV(rf, param_distributions=parameters, verbose=10, n_jobs=-1)
          #Fit the model
          best_regressor = regressor.fit(X_train, y_train)
          # get the best parameters
          best_max_depth = best_regressor.best_estimator_.get_params()['max_depth']
          best_n_estimators = best_regressor.best_estimator_.get_params()['n_estimators']
          best_max_features = best_regressor.best_estimator_.get_params()['max_features']
          best_min_samples_split = best_regressor.best_estimator_.get_params()['min_samples_split']
          best_min_samples_leaf = best_regressor.best_estimator_.get_params()['min_samples_leaf']
          #Print The best parameters
          print('Best max_depth:', best_max_depth)
          print('Best n_estimators:', best_n_estimators)
          print('Best max_features:', best_max_features)
          print('Best min_samples_split:', best_min_samples_split)
          print('Best min_samples_leaf:', best_min_samples_leaf)
          elapsed = time.time() - start
          print(f"Time elapsed: {elapsed}")
          Fitting 5 folds for each of 10 candidates, totalling 50 fits
          [Parallel(n_jobs=-1)]: Using backend LokyBackend with 4 concurrent workers.
          [Parallel(n_jobs=-1)]: Batch computation too fast (0.1685s.) Setting batch_size=2.
          [Parallel(n_jobs=-1)]: Done 5 tasks
                                                     | elapsed:
                                                                   0.3s
          [Parallel(n_jobs=-1)]: Batch computation too slow (18.7115s.) Setting batch_size=1.
          [Parallel(n_jobs=-1)]: Done 12 tasks
                                                     elapsed:
          [Parallel(n_jobs=-1)]: Done 25 tasks
                                                     elapsed:
                                                                  35.1s
          [Parallel(n_jobs=-1)]: Done 32 tasks
                                                     elapsed:
                                                                  53.3s
          [Parallel(n_jobs=-1)]: Done 41 tasks
                                                     elapsed:
                                                                 55.6s
          [Parallel(n_jobs=-1)]: Done 50 out of 50 | elapsed: 1.2min finished
          Best max_depth: 5
          Best n_estimators: 300
          Best max_features: auto
          Best min_samples_split: 100
          Best min_samples_leaf: 2
          Time elapsed: 78.28886032104492
In [113]: | rf1 = RandomForestRegressor(n_estimators=best_n_estimators,
                         max_features=best_max_features,
                         max depth=best max depth,
                         min_samples_split=best_min_samples_split,
                         min_samples_leaf= best_min_samples_leaf)
          rf1.fit(X_train, y_train)
          pred_train = rf1.predict(X_train)
          train_score = r2_score(y_train, pred_train)
          print(f"For max_depth={best_max_depth}, Train R2 = {train_score}")
          pred_cv = rf1.predict(X_cv)
          cv_score = r2_score(y_cv, pred_cv)
          print(f"For max_depth={best_max_depth}, CV R2 = {cv_score}")
          For max_depth=5, Train R2 = 0.6339065646994739
```

For max_depth=5, CV R2 = 0.6022516771441269

```
In [114]: | X_full_train = np.vstack((X_train, X_cv))
          y_full_train = np.vstack((y_train.values.reshape(-1,1), y_cv.values.reshape(-1,1)))
           rf1 = RandomForestRegressor(n_estimators=best_n_estimators,
                          max_features=best_max_features,
                          max_depth=best_max_depth,
                          min_samples_split=best_min_samples_split,
                          min_samples_leaf= best_min_samples_leaf)
          rf1.fit(X_full_train, y_full_train)
Out[114]: RandomForestRegressor(max_depth=5, min_samples_leaf=2, min_samples_split=100,
                                 n_estimators=300)
In [115]: | filename = 'RF_Orig_Feat_model.sav'
           joblib.dump(rf1, filename)
          print(f'Saved {filename}')
          Saved RF_Orig_Feat_model.sav
In [116]: | filename = 'RF_Orig_Feat_model.sav'
           rf1 = joblib.load(filename)
          print(f'Loaded {filename}')
          Loaded RF_Orig_Feat_model.sav
In [117]: | pred_train = rf1.predict(X_full_train)
          train_score = r2_score(y_full_train, pred_train)
          print(f"For max_depth={best_max_depth}, Train R2 = {train_score}")
          For max_depth=5, Train R2 = 0.6290333793346686
In [118]: | pred_test = rf1.predict(X_test)
           submission_DTR = pd.read_csv('sample_submission.csv')
           submission_DTR['y'] = pred_test
           submission_DTR.to_csv(f'sample_submission_RF={best_max_depth}.csv', index=False)
          submission_DTR.head()
Out[118]:
             ID
           0 1 77.785880
              2 93.986622
             3 78.122525
              4 77.586624
           4 5 111.673830
               Submission and Description
                                                                                    Private Score
                                                                                                       Public Score
                                                                                      0.54763
                                                                                                        0.55442
               sample_submission_RF5.csv
               just now by Harsh Jadhav
```

- Train R2 = 0.6290333793346686
- Test Private R2 = 0.54763
- Test Public R2 = 0.55442

5.3.2 With Original Dataset + PCA + SVD

(4209, 436)

```
In [119]: train_svd_pca = np.hstack((X_train, pca_train, svd_train))
    cv_svd_pca = np.hstack((X_cv, pca_cv, svd_cv))
    test_svd_pca = np.hstack((X_test, pca_test, svd_test))

    print(train_svd_pca.shape)
    print(cv_svd_pca.shape)
    print(test_svd_pca.shape)

(3360, 436)
    (841, 436)
```

```
In [133]: import time
          start = time.time()
          # Number of trees in random forest
          n_estimators = [10, 25, 50, 100, 200, 300, 400, 500]
          # Number of features to consider at every split
          max_features = ['auto', 'sqrt']
          # Maximum number of levels in tree
          max_depth = [3, 5, 10, 15, 20, 25, 30]
          # Minimum number of samples required to split a node
          min_samples_split = [2, 3, 5, 10, 15, 100]
          # Minimum number of samples required at each leaf node
          min_samples_leaf = [1, 2, 3, 5, 10]
          # create parameters dictionary
          parameters = {'n_estimators': n_estimators,
                          'max_features': max_features,
                          'max_depth': max_depth,
                          'min_samples_split': min_samples_split,
                          'min_samples_leaf': min_samples_leaf}
          #Create a Random Forest Regressor model
          rf = RandomForestRegressor()
          #Tune hyperparameters using RandomizedSearchCV
          regressor = RandomizedSearchCV(rf, param_distributions=parameters, verbose=10, n_jobs=-1)
          #Fit the model
          best_regressor = regressor.fit(train_svd_pca, y_train)
          # get the best parameters
          best_max_depth = best_regressor.best_estimator_.get_params()['max_depth']
          best_n_estimators = best_regressor.best_estimator_.get_params()['n_estimators']
          best_max_features = best_regressor.best_estimator_.get_params()['max_features']
          best_min_samples_split = best_regressor.best_estimator_.get_params()['min_samples_split']
          best_min_samples_leaf = best_regressor.best_estimator_.get_params()['min_samples_leaf']
          #Print The best parameters
          print('Best max_depth:', best_max_depth)
          print('Best n_estimators:', best_n_estimators)
          print('Best max_features:', best_max_features)
          print('Best min_samples_split:', best_min_samples_split)
          print('Best min_samples_leaf:', best_min_samples_leaf)
          elapsed = time.time() - start
          print(f"Time elapsed: {elapsed}")
          Fitting 5 folds for each of 10 candidates, totalling 50 fits
          [Parallel(n_jobs=-1)]: Using backend LokyBackend with 4 concurrent workers.
          [Parallel(n_jobs=-1)]: Done 5 tasks
                                                     | elapsed:
                                                                   0.9s
          [Parallel(n_jobs=-1)]: Done 10 tasks
                                                       elapsed:
                                                                   3.4s
          [Parallel(n_jobs=-1)]: Done 17 tasks
                                                       elapsed:
                                                                  4.2s
          [Parallel(n_jobs=-1)]: Done 24 tasks
                                                     elapsed: 45.3s
          [Parallel(n_jobs=-1)]: Done 33 tasks
                                                     | elapsed: 1.5min
          [Parallel(n_jobs=-1)]: Done 42 tasks
                                                     elapsed: 2.2min
          [Parallel(n_jobs=-1)]: Done 50 out of 50 | elapsed: 3.9min finished
          Best max_depth: 5
          Best n_estimators: 500
          Best max_features: auto
          Best min_samples_split: 100
          Best min_samples_leaf: 10
          Time elapsed: 290.3807260990143
In [134]: | rf2 = RandomForestRegressor(n_estimators = best_n_estimators,
                         max_features = best_max_features,
                         max_depth = best_max_depth,
                         min samples split = best min samples split,
                         min_samples_leaf = best_min_samples_leaf)
          rf2.fit(train_svd_pca, y_train)
Out[134]: RandomForestRegressor(max_depth=5, min_samples_leaf=10, min_samples_split=100,
                                n_estimators=500)
In [135]: | pred_train = rf2.predict(train_svd_pca)
          train_score = r2_score(y_train, pred_train)
          print(f"For max_depth={best_max_depth}, Train R2 = {train_score}")
          pred_cv = rf2.predict(cv_svd_pca)
          cv_score = r2_score(y_cv, pred_cv)
          print(f"For max_depth={best_max_depth}, CV R2 = {cv_score}")
          For max depth=5, Train R2 = 0.640813585100622
          For max_depth=5, CV R2 = 0.597953780763185
```

```
In [136]: | X_full_train_svd_pca = np.vstack((train_svd_pca, cv_svd_pca))
          y_full_train = np.vstack((y_train.values.reshape(-1,1), y_cv.values.reshape(-1,1)))
          rf2 = RandomForestRegressor(n_estimators = best_n_estimators,
                          max_features = best_max_features,
                          max_depth = best_max_depth,
                          min_samples_split = best_min_samples_split,
                          min_samples_leaf = best_min_samples_leaf)
          rf2.fit(X_full_train_svd_pca, y_full_train)
Out[136]: RandomForestRegressor(max_depth=5, min_samples_leaf=10, min_samples_split=100,
                                 n_estimators=500)
In [137]: | filename = 'RF_PCA_SVD_model.sav'
          joblib.dump(rf2, filename)
          print(f'Saved {filename}')
          Saved RF_PCA_SVD_model.sav
In [138]: | filename = 'RF_PCA_SVD_model.sav'
          rf2 = joblib.load(filename)
          print(f'Loaded {filename}')
          Loaded RF_PCA_SVD_model.sav
In [139]: | pred_train = rf2.predict(X_full_train_svd_pca)
          train_score = r2_score(y_full_train, pred_train)
          print(f"For max_depth={best_max_depth}, Train R2 = {train_score}")
          For max_depth=5, Train R2 = 0.6364927215350347
In [140]:
          pred_test = rf2.predict(test_svd_pca)
           submission_RF = pd.read_csv('sample_submission.csv')
           submission_RF['y'] = pred_test
          submission_RF.to_csv(f'sample_submission_RF_SVD_PCA={best_max_depth}.csv', index=False)
          submission_RF.head()
Out[140]:
             ID
             1 77.648774
           1 2 93.867920
             3 77.561921
             4 77.729999
           4 5 111.977759
               Submission and Description
                                                                                   Private Score
                                                                                                      Public Score
                                                                                     0.54145
                                                                                                       0.55076
               sample_submission_RF_SVD_PCA5.csv
               just now by Harsh Jadhav
```

- Train R2 = 0.6364927215350347
- Test Private R2 = 0.54145
- Test Public R2 = 0.55076

5.4 Add some more features

5.4.1 Interactions

- Two way interactions X314, X315
- Three way interactions X118,X314,X315

https://www.kaggle.com/c/mercedes-benz-greener-manufacturing/discussion/37700 (https://www.kaggle.com/c/mercedes-benz-greener-manufacturing/discussion/37700)

```
In [141]: | def get_interactions(features):
              features : list of features
              return : interaction between features
              train_inter = 0
              cv_inter = 0
              test inter = 0
              for f in range(len(features)):
                  train_inter += X_train[features[f]].values
                   cv_inter += X_cv[features[f]].values
                  test_inter += X_test[features[f]].values
              return train_inter.reshape(-1,1), cv_inter.reshape(-1,1), test_inter.reshape(-1,1)
          train_X314_X315, cv_X314_X315, test_X314_X315 = get_interactions(['X314', 'X315'])
          train_X118_X314_X315, cv_X118_X314_X315, test_X118_X314_X315 = get_interactions(['X118', 'X314',
                                                                                             'X315'])
In [142]: | print(train_X314_X315.shape)
          print(cv_X314_X315.shape)
          print(test_X314_X315.shape)
          print(train_X118_X314_X315.shape)
          print(cv_X118_X314_X315.shape)
          print(test_X118_X314_X315.shape)
          (3360, 1)
          (841, 1)
          (4209, 1)
          (3360, 1)
          (841, 1)
          (4209, 1)
```

5.4.2 Gaussian Random Projections

5.4.3 Random Forest Regressor

With Original, PCA, SVD, GRP, Interactions

(4209, 448)

```
In [177]: import time
          start = time.time()
          # Number of trees in random forest
          n_estimators = [10, 25, 50, 100, 200, 300, 400, 500]
          # Number of features to consider at every split
          max_features = ['auto', 'sqrt']
          # Maximum number of levels in tree
          max_depth = [2, 3, 5, 10, 15, 20, 25]
          # Minimum number of samples required to split a node
          min_samples_split = [2, 3, 5, 10, 15, 25]
          # Minimum number of samples required at each leaf node
          min_samples_leaf = [1, 2, 3, 5, 10]
          # create parameters dictionary
          parameters = {'n_estimators': n_estimators,
                          'max_features': max_features,
                          'max_depth': max_depth,
                          'min_samples_split': min_samples_split,
                          'min_samples_leaf': min_samples_leaf}
          #Create a Random Forest Regressor model
          rf = RandomForestRegressor()
          #Tune hyperparameters using RandomizedSearchCV
          regressor = RandomizedSearchCV(rf, param_distributions=parameters, verbose=10, n_jobs=-1)
          #Fit the model
          best_regressor = regressor.fit(train_grp_pca_svd_inter, y_train)
          # get the best parameters
          best_max_depth = best_regressor.best_estimator_.get_params()['max_depth']
          best_n_estimators = best_regressor.best_estimator_.get_params()['n_estimators']
          best_max_features = best_regressor.best_estimator_.get_params()['max_features']
          best_min_samples_split = best_regressor.best_estimator_.get_params()['min_samples_split']
          best_min_samples_leaf = best_regressor.best_estimator_.get_params()['min_samples_leaf']
          #Print The best parameters
          print('Best max_depth:', best_max_depth)
          print('Best n_estimators:', best_n_estimators)
          print('Best max_features:', best_max_features)
          print('Best min_samples_split:', best_min_samples_split)
          print('Best min_samples_leaf:', best_min_samples_leaf)
          elapsed = time.time() - start
          print(f"Time elapsed: {elapsed}")
          Fitting 5 folds for each of 10 candidates, totalling 50 fits
          [Parallel(n_jobs=-1)]: Using backend LokyBackend with 4 concurrent workers.
          [Parallel(n_jobs=-1)]: Done 5 tasks
                                                     | elapsed:
                                                                  8.6s
          [Parallel(n_jobs=-1)]: Done 10 tasks
                                                     elapsed:
                                                                  14.3s
          [Parallel(n_jobs=-1)]: Done 17 tasks
                                                     elapsed: 17.4s
          [Parallel(n_jobs=-1)]: Done 24 tasks
                                                     elapsed: 33.4s
          [Parallel(n_jobs=-1)]: Done 33 tasks
                                                       elapsed: 2.9min
          [Parallel(n_jobs=-1)]: Done 42 tasks
                                                     elapsed: 5.2min
          [Parallel(n_jobs=-1)]: Done 50 out of 50 | elapsed: 5.5min finished
          Best max_depth: 5
          Best n_estimators: 500
          Best max_features: auto
          Best min_samples_split: 5
          Best min_samples_leaf: 3
          Time elapsed: 390.1909713745117
In [178]: rf3 = RandomForestRegressor(n_estimators = best_n_estimators,
                         max_features = best_max_features,
                         max_depth = best_max_depth,
                         min_samples_split = best_min_samples_split,
                         min_samples_leaf = best_min_samples_leaf)
          rf3.fit(train_grp_pca_svd_inter, y_train)
Out[178]: RandomForestRegressor(max_depth=5, min_samples_leaf=3, min_samples_split=5,
                                n_estimators=500)
In [179]: | pred_train = rf3.predict(train_grp_pca_svd_inter)
          train_score = r2_score(y_train, pred_train)
          print(f"For max_depth={best_max_depth}, Train R2 = {train_score}")
          pred cv = rf3.predict(cv grp pca svd inter)
          cv_score = r2_score(y_cv, pred_cv)
          print(f"For max_depth={best_max_depth}, CV R2 = {cv_score}")
          For max depth=5, Train R2 = 0.6620651156983793
          For max_depth=5, CV R2 = 0.5936390916556575
```

```
In [180]: | X_full_train_grp_pca_svd_inter = np.vstack((train_grp_pca_svd_inter, cv_grp_pca_svd_inter))
          y_full_train = np.vstack((y_train.values.reshape(-1,1), y_cv.values.reshape(-1,1)))
          rf3 = RandomForestRegressor(n_estimators = best_n_estimators,
                          max_features = best_max_features,
                          max_depth = best_max_depth,
                          min_samples_split = best_min_samples_split,
                          min_samples_leaf = best_min_samples_leaf)
          rf3.fit(X_full_train_grp_pca_svd_inter, y_full_train)
Out[180]: RandomForestRegressor(max_depth=5, min_samples_leaf=3, min_samples_split=5,
                                 n_estimators=500)
In [181]: | filename = 'RF_PCA_SVD_inter_GPR_model.sav'
          joblib.dump(rf3, filename)
          print(f'Saved {filename}')
          Saved RF_PCA_SVD_inter_GPR_model.sav
In [182]: | filename = 'RF_PCA_SVD_inter_GPR_model.sav'
          rf3 = joblib.load(filename)
          print(f'Loaded {filename}')
          Loaded RF_PCA_SVD_inter_GPR_model.sav
In [183]: | pred_train = rf3.predict(X_full_train_grp_pca_svd_inter)
          train_score = r2_score(y_full_train, pred_train)
          print(f"For max_depth={best_max_depth}, Train R2 = {train_score}")
          For max_depth=5, Train R2 = 0.6527769059803106
In [184]: | pred_test = rf3.predict(test_grp_pca_svd_inter)
          submission_RF = pd.read_csv('sample_submission.csv')
           submission_RF['y'] = pred_test
          submission_RF.to_csv(f'sample_submission_RF_PCA_SVD_inter_GPR={best_max_depth}.csv', index=False)
          submission_RF.head()
Out[184]:
             ID
                        У
                 78.908862
           1 2 93.734419
              3 78.876308
             4 77.709303
             5 112.009775
               Submission and Description
                                                                                    Private Score
                                                                                                      Public Score
               sample_submission_RF_PCA_SVD_inter_GPR5.csv
                                                                                      0.54220
                                                                                                        0.54920
               just now by Harsh Jadhav
```

- Train R2 = 0.6527769059803106
- Test Private R2 = 0.54220
- Test Public R2 = 0.54920

5.4.4 XGBoost Regressor

With Original, PCA, SVD, GRP, Interactions

(4209, 448)

```
In [207]: | neigh=XGBRegressor(random_state=42, n_jobs=-1)
          parameters = {'learning_rate':[0.001,0.01,0.05,0.1,1],
                         'n_estimators':[100,150,200,500],
                         'max_depth':[2,3,5,10],
                         'colsample_bytree':[0.1,0.5,0.7,1],
                         'subsample':[0.2,0.3,0.5,1],
                         'gamma':[1e-2,1e-3,0,0.1,0.01,0.5,1],
                         'reg_alpha':[1e-5,1e-3,1e-1,1,1e1]}
          reg=RandomizedSearchCV(neigh,parameters,cv=5, scoring='r2', return_train_score=True, n_jobs=-1,
                                  verbose=10)
          reg.fit(train_grp_pca_svd_inter, y_train)
          Fitting 5 folds for each of 10 candidates, totalling 50 fits
          [Parallel(n_jobs=-1)]: Using backend LokyBackend with 4 concurrent workers.
                                                     | elapsed:
          [Parallel(n_jobs=-1)]: Done 5 tasks
                                                                   7.9s
          [Parallel(n_jobs=-1)]: Done 10 tasks
                                                       elapsed:
                                                                   11.2s
          [Parallel(n_jobs=-1)]: Done 17 tasks
                                                                   15.2s
                                                       elapsed:
          [Parallel(n_jobs=-1)]: Done 24 tasks
                                                      | elapsed:
                                                                   20.4s
          [Parallel(n_jobs=-1)]: Done 33 tasks
                                                      | elapsed:
                                                                 51.4s
          [Parallel(n_jobs=-1)]: Done 42 tasks
                                                       elapsed: 1.5min
          [Parallel(n_jobs=-1)]: Done 50 out of 50 | elapsed: 2.8min finished
Out[207]: RandomizedSearchCV(cv=5,
                             estimator=XGBRegressor(base_score=None, booster=None,
                                                     colsample_bylevel=None,
                                                     colsample_bynode=None,
                                                     colsample_bytree=None, gamma=None,
                                                     gpu_id=None, importance_type='gain',
                                                     interaction_constraints=None,
                                                    learning_rate=None,
                                                     max_delta_step=None, max_depth=None,
                                                     min_child_weight=None, missing=nan,
                                                    monotone_constraints=None,
                                                    n_estimators=100, n...
                                                    validate_parameters=None,
                                                    verbosity=None),
                             n_jobs=-1,
                             param_distributions={'colsample_bytree': [0.1, 0.5, 0.7, 1],
                                                   'gamma': [0.01, 0.001, 0, 0.1, 0.01,
                                                             0.5, 1],
                                                   'learning_rate': [0.001, 0.01, 0.05,
                                                                     0.1, 1],
                                                   'max_depth': [2, 3, 5, 10],
                                                   'n_estimators': [100, 150, 200, 500],
                                                   'reg_alpha': [1e-05, 0.001, 0.1, 1,
                                                                 10.0],
                                                   'subsample': [0.2, 0.3, 0.5, 1]},
                             return_train_score=True, scoring='r2', verbose=10)
In [208]: | best_max_depth = reg.best_estimator_.get_params()['max_depth']
          best_n_estimators = reg.best_estimator_.get_params()['n_estimators']
          best_colsample_bytree = reg.best_estimator_.get_params()['colsample_bytree']
          best_subsample = reg.best_estimator_.get_params()['subsample']
          best_gamma = reg.best_estimator_.get_params()['gamma']
          best_reg_alpha = reg.best_estimator_.get_params()['reg_alpha']
          best_learning_rate = reg.best_estimator_.get_params()['learning_rate']
          #Print The best parameters
          print('Best max_depth:', best_max_depth)
          print('Best n_estimators:', best_n_estimators)
          print('Best colsample_bytree:', best_colsample_bytree)
          print('Best subsample:', best_subsample)
          print('Best reg_alpha:', best_reg_alpha)
          print('Best gamma:', best_gamma)
          print('Best learning_rate:', best_learning_rate)
          Best max_depth: 2
          Best n_estimators: 100
          Best colsample_bytree: 1
          Best subsample: 1
          Best reg_alpha: 10.0
          Best gamma: 0
          Best learning_rate: 0.1
```

```
learning_rate = best_learning_rate,
                         max_depth = best_max_depth,
                          subsample = best_subsample,
                         gamma = best_gamma,
                         reg_alpha = best_reg_alpha,
                           colsample_bytree = best_colsample_bytree,
                            random_state=42,n_jobs=-1)
          xgb.fit(train_grp_pca_svd_inter, y_train)
Out[209]: XGBRegressor(base_score=0.5, booster='gbtree', colsample_bylevel=1,
                       colsample_bynode=1, colsample_bytree=1, gamma=3, gpu_id=-1,
                       importance_type='gain', interaction_constraints='',
                       learning_rate=0.1, max_delta_step=0, max_depth=2,
                       min_child_weight=1, missing=nan, monotone_constraints='()',
                       n_estimators=100, n_jobs=-1, num_parallel_tree=1, random_state=42,
                       reg_alpha=10.0, reg_lambda=1, scale_pos_weight=1, subsample=1,
                       tree_method='exact', validate_parameters=1, verbosity=None)
In [210]: pred_train = xgb.predict(train_grp_pca_svd_inter)
          train_score = r2_score(y_train, pred_train)
          print(f"For max_depth={best_max_depth}, Train R2 = {train_score}")
          pred_cv = xgb.predict(cv_grp_pca_svd_inter)
          cv_score = r2_score(y_cv, pred_cv)
          print(f"For max_depth={best_max_depth}, CV R2 = {cv_score}")
          For max_depth=2, Train R2 = 0.6670327858950802
          For max_depth=2, CV R2 = 0.5965159762242921
In [211]: | X_full_train_grp_pca_svd_inter = np.vstack((train_grp_pca_svd_inter, cv_grp_pca_svd_inter))
          y_full_train = np.vstack((y_train.values.reshape(-1,1), y_cv.values.reshape(-1,1)))
          xgb = XGBRegressor(n_estimators = best_n_estimators,
                         learning_rate = best_learning_rate,
                         max_depth = best_max_depth,
                         subsample = best_subsample,
                         gamma = best_gamma,
                         reg_alpha = best_reg_alpha,
                           colsample_bytree = best_colsample_bytree,
                            random_state=42,n_jobs=-1)
          xgb.fit(X_full_train_grp_pca_svd_inter, y_full_train)
Out[211]: XGBRegressor(base_score=0.5, booster='gbtree', colsample_bylevel=1,
                       colsample_bynode=1, colsample_bytree=1, gamma=3, gpu_id=-1,
                       importance_type='gain', interaction_constraints='',
                       learning_rate=0.1, max_delta_step=0, max_depth=2,
                       min_child_weight=1, missing=nan, monotone_constraints='()',
                       n_estimators=100, n_jobs=-1, num_parallel_tree=1, random_state=42,
                       reg_alpha=10.0, reg_lambda=1, scale_pos_weight=1, subsample=1,
                       tree_method='exact', validate_parameters=1, verbosity=None)
In [212]: | filename = 'XGB_PCA_SVD_inter_GPR_model.sav'
          joblib.dump(xgb, filename)
          print(f'Saved {filename}')
          Saved XGB_PCA_SVD_inter_GPR_model.sav
In [213]: filename = 'XGB PCA SVD inter GPR model.sav'
          xgb = joblib.load(filename)
          print(f'Loaded {filename}')
          Loaded XGB_PCA_SVD_inter_GPR_model.sav
In [214]: | pred_train = xgb.predict(X_full_train_grp_pca_svd_inter)
          train_score = r2_score(y_full_train, pred_train)
          print(f"For max_depth={best_max_depth}, Train R2 = {train_score}")
          For max_depth=2, Train R2 = 0.6551805553802594
          pred_test = xgb.predict(test_grp_pca_svd_inter)
In [215]:
          submission_xgb = pd.read_csv('sample_submission.csv')
          submission_xgb['y'] = pred_test
          submission_xgb.to_csv(f'sample_submission_xgb_SVD_PCA_inter_GPR={best_max_depth}.csv', index=False)
          submission_xgb.head()
Out[215]:
             ID
                        У
                 78.033203
             1
              2 94.560959
                78.009758
              4 77.881721
             5 110.964104
```

In [209]: | xgb = XGBRegressor(n_estimators = best_n_estimators,

Submission and Description Private Score Public Score

sample_submission_xgb_SVD_PCA_inter_GPR2.csv
just now by Harsh Jadhav

Private Score Public Score

0.54682
0.54759

- Train R2 = 0.6551805553802594
- Test Private R2 = 0.54682
- Test Public R2 = 0.54759

5.4.5 Stacking Regressor

With Original, PCA, SVD, GRP, Interactions

```
In [216]: | filename = 'RF_Orig_Feat_model.sav'
          rf1 = joblib.load(filename)
          print(f'Loaded {filename}')
          Loaded RF_Orig_Feat_model.sav
In [217]: | filename = 'RF_PCA_SVD_inter_GPR_model.sav'
          rf2 = joblib.load(filename)
          print(f'Loaded {filename}')
          Loaded RF_PCA_SVD_inter_GPR_model.sav
In [218]: | filename = 'RF_PCA_SVD_model.sav'
          rf3 = joblib.load(filename)
          print(f'Loaded {filename}')
          Loaded RF_PCA_SVD_model.sav
In [219]: | filename = 'XGB_PCA_SVD_inter_GPR_model.sav'
          xgb = joblib.load(filename)
          print(f'Loaded {filename}')
          Loaded XGB_PCA_SVD_inter_GPR_model.sav
In [220]: | filename = 'DTR_svd_pca_model.sav'
          dtr2 = joblib.load(filename)
          print(f'Loaded {filename}')
          Loaded DTR_svd_pca_model.sav
In [222]: # Lets take top 10 pca components
          components = 10
          pca = PCA(n_components=components, random_state=420)
          pca_train = pca.fit_transform(X_train)
          pca cv = pca.transform(X cv)
          pca_test = pca.transform(X_test)
          print(pca_train.shape)
          print(pca_cv.shape)
          print(pca_test.shape)
          (3360, 10)
          (841, 10)
          (4209, 10)
In [242]: | train_grp_pca_svd_inter = np.hstack((X_train, pca_train, grp_train, svd_train, train_X314_X315,
                                                train X118 X314 X315))
          cv_grp_pca_svd_inter = np.hstack((X_cv, pca_cv, grp_cv, svd_cv, cv_X314_X315,
                                             cv_X118_X314_X315))
          test_grp_pca_svd_inter = np.hstack((X_test, pca_test, grp_test, svd_test, test_X314_X315,
                                               test_X118_X314_X315))
          print(train_grp_pca_svd_inter.shape)
          print(cv grp pca svd inter.shape)
          print(test_grp_pca_svd_inter.shape)
          (3360, 448)
          (841, 448)
          (4209, 448)
```

```
In [243]: | ridge_reg = Ridge(random_state=42, fit_intercept=False, alpha=0)
          stacked_model = StackingCVRegressor(regressors=(rf1, rf2, rf3, xgb),
                                                   meta_regressor=ridge_reg,
                                                   use_features_in_secondary = False, refit=True, cv=5)
          # cv_score=cross_val_score(stacked, train_grp_pca_svd_inter, y_train,
                                      scoring='r2',cv= 5,verbose= 5,n_jobs=-1)
          # print('Mean Score:',cv_score.mean())
          # print('Standard Deviation:',cv_score.std())
          stacked_model.fit(train_grp_pca_svd_inter, y_train)
Out[243]: StackingCVRegressor(meta_regressor=Ridge(alpha=0, fit_intercept=False,
                                                    random_state=42),
                              regressors=(RandomForestRegressor(max_depth=5,
                                                                 min_samples_leaf=10,
                                                                 min_samples_split=100,
                                                                 n_estimators=500),
                                           XGBRegressor(base_score=0.5, booster='gbtree',
                                                        colsample_bylevel=1,
                                                        colsample_bynode=1,
                                                        colsample_bytree=1, gamma=3,
                                                        gpu_id=-1, importance_type='gain',
                                                        interaction_constraints='',
                                                        learning_rate=0.1,
                                                        max_delta_step=0, max_depth=2,
                                                        min_child_weight=1, missing=nan,
                                                        monotone_constraints='()',
                                                        n_estimators=100, n_jobs=-1,
                                                        num_parallel_tree=1,
                                                        random_state=42, reg_alpha=10.0,
                                                        reg_lambda=1, scale_pos_weight=1,
                                                        subsample=1, tree_method='exact',
                                                        validate_parameters=1,
                                                        verbosity=None)))
In [244]: pred_train = stacked_model.predict(train_grp_pca_svd_inter)
          train_score = r2_score(y_train, pred_train)
          print(f"For Stacked model Train R2 = {train_score}")
          pred_cv = stacked_model.predict(cv_grp_pca_svd_inter)
          cv_score = r2_score(y_cv, pred_cv)
          print(f"For Stacked model CV R2 = {cv_score}")
          For Stacked model Train R2 = 0.6614913902174595
          For Stacked model CV R2 = 0.6008457269092116
In [245]: | train_grp_pca_svd_inter = np.hstack((X_train, pca_train, grp_train, svd_train, train_X314_X315,
                                                train_X118_X314_X315))
          cv_grp_pca_svd_inter = np.hstack((X_cv, pca_cv, grp_cv, svd_cv, cv_X314_X315,
                                             cv_X118_X314_X315))
          Train_plus_Cv = np.vstack((train_grp_pca_svd_inter, cv_grp_pca_svd_inter))
          test_grp_pca_svd_inter = np.hstack((X_test, pca_test, test_X314_X315,
                                               test_X118_X314_X315))
          Y_train_plus_cv = np.vstack((y_train.values.reshape(-1,1), y_cv.values.reshape(-1,1)))
          ridge_reg = Ridge(random_state=42, fit_intercept=False, alpha=0)
          stacked_model = StackingCVRegressor(regressors=(rf1, rf2, rf3, xgb),
                                                   meta_regressor=ridge_reg,
                                                   use_features_in_secondary = False, refit=True, cv=5)
          stacked_model.fit(Train_plus_Cv, Y_train_plus_cv)
          pred_train = stacked_model.predict(Train_plus_Cv)
          train_score = r2_score(Y_train_plus_cv, pred_train)
          print(f"For Stacked model Train R2 = {train_score}")
          For Stacked model Train R2 = 0.6530002337544227
In [241]: pred test = stacked model.predict(test grp pca svd inter)
          submission_stacked = pd.read_csv('sample_submission.csv')
          submission_stacked['y'] = pred_test
          submission_stacked.to_csv(f'svdsample_submission_Stacked_SVD_PCA_inter_GPR={best_max_depth}.csv', index=False)
          submission_stacked.head()
Out[241]:
             ID
                        У
                 81.219992
             1
              2 97.896811
              3 81.929732
              4 77.636613
              5 112.445495
```

Submission and Description	Private Score	Public Score
svdsample_submission_Stacked_SVD_PCA_inter_GPR2.csv	0.55017	0.55310
an hour ago by Harsh Jadhay		

- Train R2 = 0.6530002337544227
- Test Private R2 = 0.55017
- Test Public R2 = 0.55310

With Private R2 Score 0.55017, The stacking reggressor is standing among top 28% on the leaderboard.