

# Project Euler #74: Digit factorial chains

## Problem Statement

This problem is a programming version of [Problem 74](#) from [projecteuler.net](#)

The number 145 is well known for the property that the sum of the factorial of its digits is equal to 145:

$$1! + 4! + 5! = 1 + 24 + 120 = 145$$

Perhaps less well known is 169, in that it produces the longest chain of numbers that link back to 169; it turns out that there are only three such loops that exist:

$$\begin{aligned} 169 &\rightarrow 363601 \rightarrow 1454 \rightarrow 169 \\ 871 &\rightarrow 45361 \rightarrow 871 \\ 872 &\rightarrow 45362 \rightarrow 872 \end{aligned}$$

It is not difficult to prove that EVERY starting number will eventually get stuck in a loop. For example,

$$\begin{aligned} 69 &\rightarrow 363600 \rightarrow 1454 \rightarrow 169 \rightarrow 363601 (\rightarrow 1454) \\ 78 &\rightarrow 45360 \rightarrow 871 \rightarrow 45361 (\rightarrow 871) \\ 540 &\rightarrow 145 (\rightarrow 145) \end{aligned}$$

Starting with 69 produces a chain of five non-repeating terms, but the longest non-repeating chain with a starting number below one million is sixty terms.

For a given length  $L$  and limit  $N$  print all the integers  $\leq N$  which have chain length  $L$

## Input Format

First line contains  $T$ , followed by  $T$  lines.

Each line contains  $N$  and  $L$  separated by space.

## Constraints

$$1 \leq T \leq 10$$

$$10 \leq N \leq 1000000$$

$$1 \leq L \leq 60$$

## Output Format

Print the integers separated by space for each testcase. Where there are no such number for a given  $L$ , print -1.

## Sample Input

```
10
221 7
147 1
258 4
265 8
210 2
175 7
29 2
24 3
273 4
261 4
```

## Sample Output

```
24 42 104 114 140 141
1 2 145
78 87 196 236
4 27 39 72 93 107 117 170 171
0 10 11 154
24 42 104 114 140 141
0 10 11
-1
78 87 196 236 263
78 87 196 236
```