

Project Euler #122: Efficient exponentiation

Problem Statement

This problem is a programming version of [Problem 122](#) from [projecteuler.net](#)

The most naive way of computing n^{15} requires fourteen multiplications:

$$n \times n \times \cdots \times n = n^{15}$$

But using a "binary" method you can compute it in six multiplications:

$$n \times n = n^2$$

$$n^2 \times n^2 = n^4$$

$$n^4 \times n^4 = n^8$$

$$n^8 \times n^4 = n^{12}$$

$$n^{12} \times n^2 = n^{14}$$

$$n^{14} \times n = n^{15}$$

However it is yet possible to compute it in only five multiplications:

$$n \times n = n^2$$

$$n^2 \times n = n^3$$

$$n^3 \times n^3 = n^6$$

$$n^6 \times n^6 = n^{12}$$

$$n^{12} \times n^3 = n^{15}$$

We shall define $m(k)$ to be the minimum number of multiplications to compute n^k . For example $m(15) = 5$.

For a given k , compute $m(k)$, and also output the sequence of multiplications needed to compute n^k . See the sample output for more details.

Input Format

The first line of input contains T , the number of test cases.

Each test case consists of a single line containing a single integer, k .

Constraints

$$1 \leq T \leq 500$$

$$2 \leq k$$

Input file #1: $k \leq 111$.

Input file #2: $k \leq 275$.

Output Format

For each test case, first output $m(k)$ in a single line. Then output $m(k)$ lines, each of the form $n^a * n^b = n^c$, where a , b and c are natural numbers. You may also output n instead of n^1 . Use the $*$

(asterisk/star) symbol, not the letter **x** or something else.

The sequence of multiplications must be valid. Any valid sequence will be accepted.

Sample Input

```
2
2
15
```

Sample Output

```
1
n^1 * n^1 = n^2
5
n * n = n^2
n^2 * n = n^3
n^3 * n^3 = n^6
n^6 * n^6 = n^12
n^12 * n^3 = n^15
```

Explanation

The second case, $k = 15$, is the example given in the problem statement.

The sample output illustrates that you can use **n** instead of **n^1**.