

# 2021 Practical Parallel Computing (実践的並列コンピューティング) No. 4

Part1: OpenMP (2)  
Apr 22, 2021

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# Overview of This Course

- Part 0: Introduction
  - 2 classes
- Part 1: **OpenMP** for shared memory programming
  - 4 classes      ← We are here (2/4)
- Part 2: **GPU** programming
  - OpenACC and CUDA
  - 4 classes
- Part 3: **MPI** for distributed memory programming
  - 3 classes



# Summary of Previous Class

OpenMP is for shared-memory parallel programming

- `#pragma omp parallel` defines a parallel region, where multiple threads work simultaneously
- With `#pragma omp for`, loop-based programs can be parallelized easily
- Shared variables and private variables
- We have reviewed OpenMP version of `mm` sample

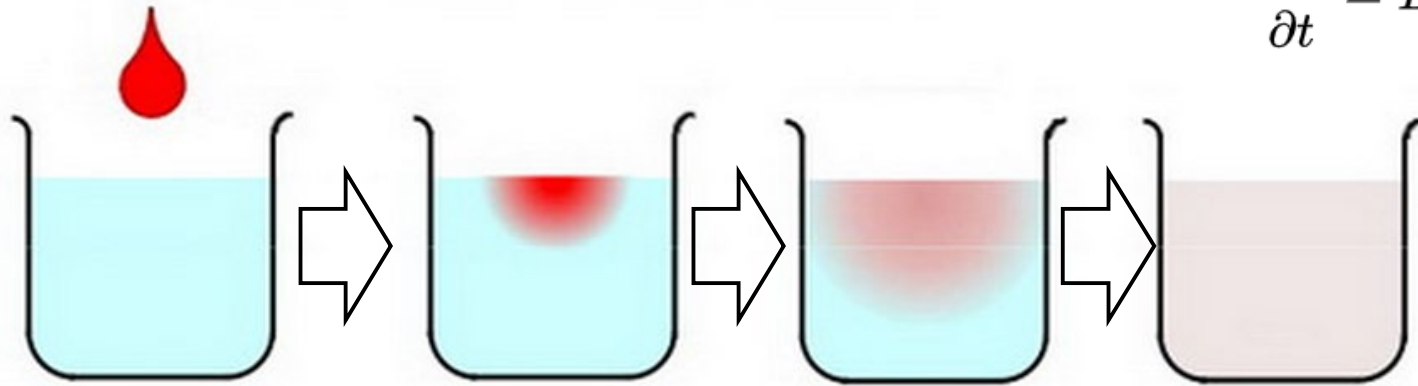
# “diffusion” Sample Program



An example of diffusion phenomena:

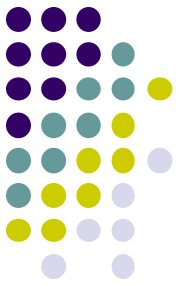
- Pour a drop of ink into a water glass

$$\frac{\partial \phi}{\partial t} = D \nabla^2 \phi(\vec{r}, t)$$



The ink spreads gradually, and finally the density becomes uniform (Figure by Prof. T. Aoki, GSIC)

- Density of ink in each point vary according to time → Simulated by computers
  - cf) Weather forecast compute wind speed, temperature, air pressure...



# “diffusion” Sample on TSUBAME

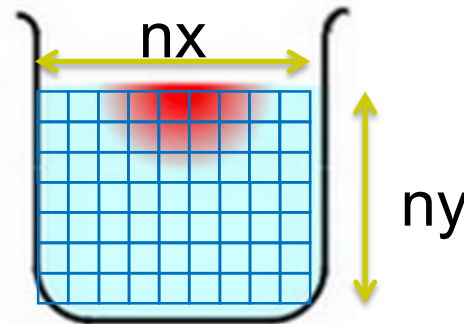
Available at </gs/hs1/tga-ppcomp/21/diffusion/>

- Execution : `./diffusion [nt]`
- nt: Number of time steps
- nx, ny: Space grid size
  - nx=8192, ny=8192 (Fixed. See the code)
  - How can we make them variables? (See mm sample)
- Compute Complexity :  $O(nx \times ny \times nt)$

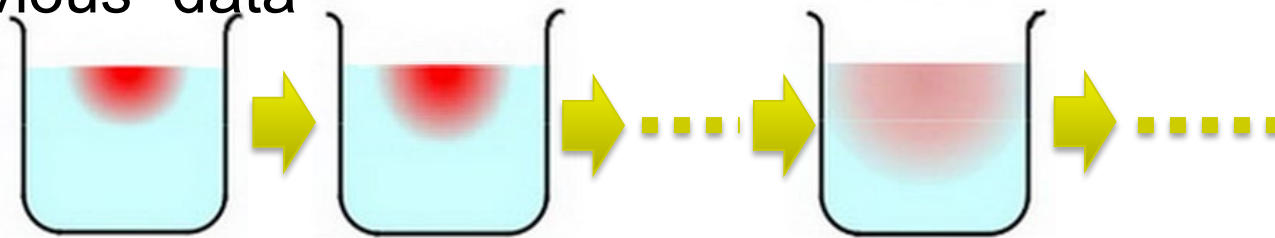
# Expression of Space to be Simulated



- Space to be simulated are divided into grids, and expressed by arrays (2D in this sample)



- Array elements are computed via timestep, by using “previous” data



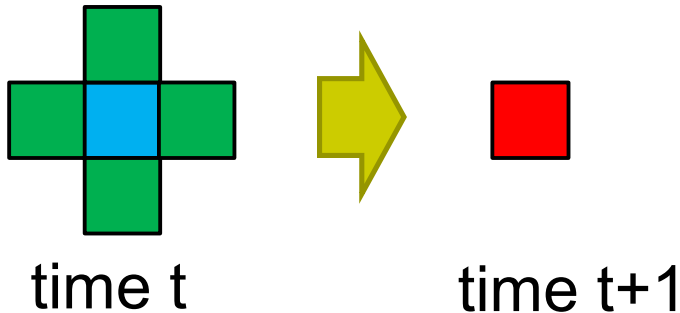
Time step t=0

t=1

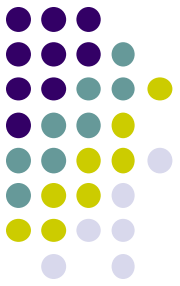
t=20

# Stencil Computations

- A data point  $(x,y)$  at time  $t+1$  is computed using following data
  - point  $(x,y)$  at time  $t$
  - “Neighbor” points of  $(x,y)$  at time  $t$



- In diffusion sample, the computation is simply “average of 5 points”
- Computations of similar type are called “**stencil computations**”
  - Frequently used in fluid simulations



Original meanings of “stencil”

# Initial Conditions & Boundary Conditions



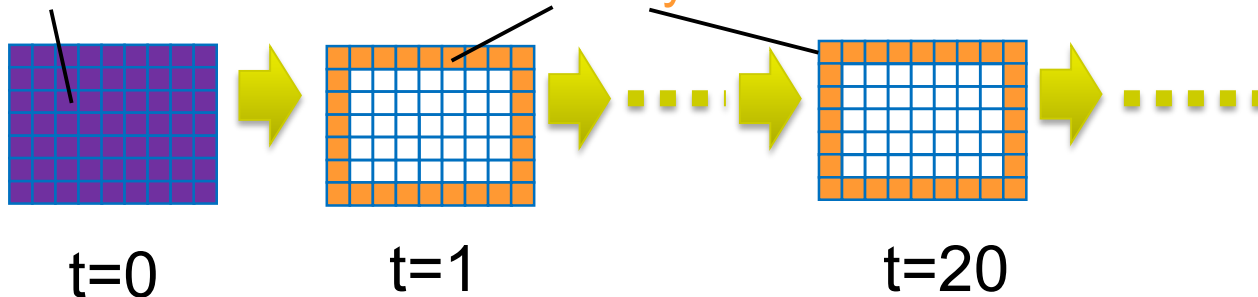
In stencil computations, following data points cannot be computed

Instead, we have to give them (for example, as input data)

- All points at  $t=0$  (Initial conditions)
  - In diffusion sample, given in `init()`
- “Boundary” points for all  $t$  (Boundary conditions)
  - In diffusion sample, they are constant during simulation  
→ See ranges of for-loops in `calc()`; boundaries are skipped
  - This is not good for simulation of a water glass ☹, but it’s simple...

Initial Conditions

Boundary Conditions



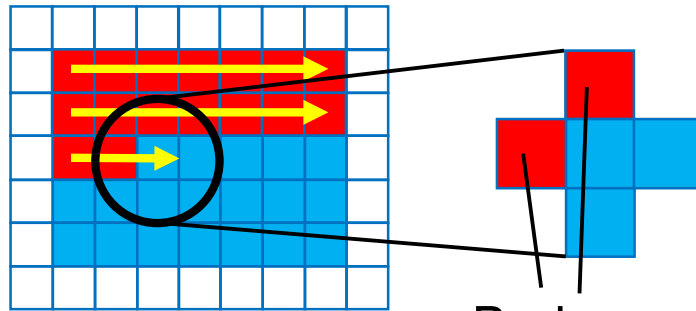




# A Single Array Does not Work

Let us compute  $t \rightarrow t+1$

- With a single 2D array (Bug! ☹️)

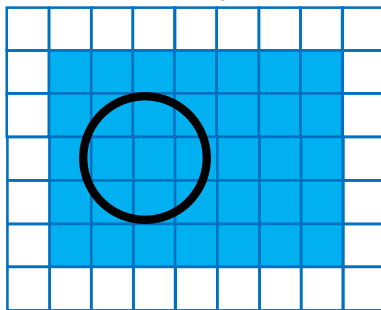


We need neighbor points at time  $t$ , but some have been already updated to  $t+1$  ☹️

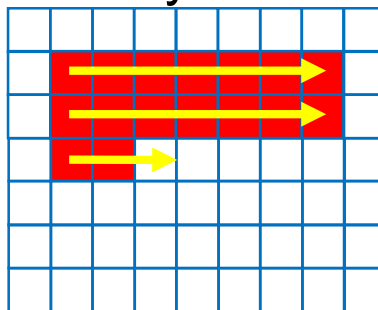
Bad new data

- With separate 2D arrays (Good 😊)

An array for  $t$



An array for  $t+1$

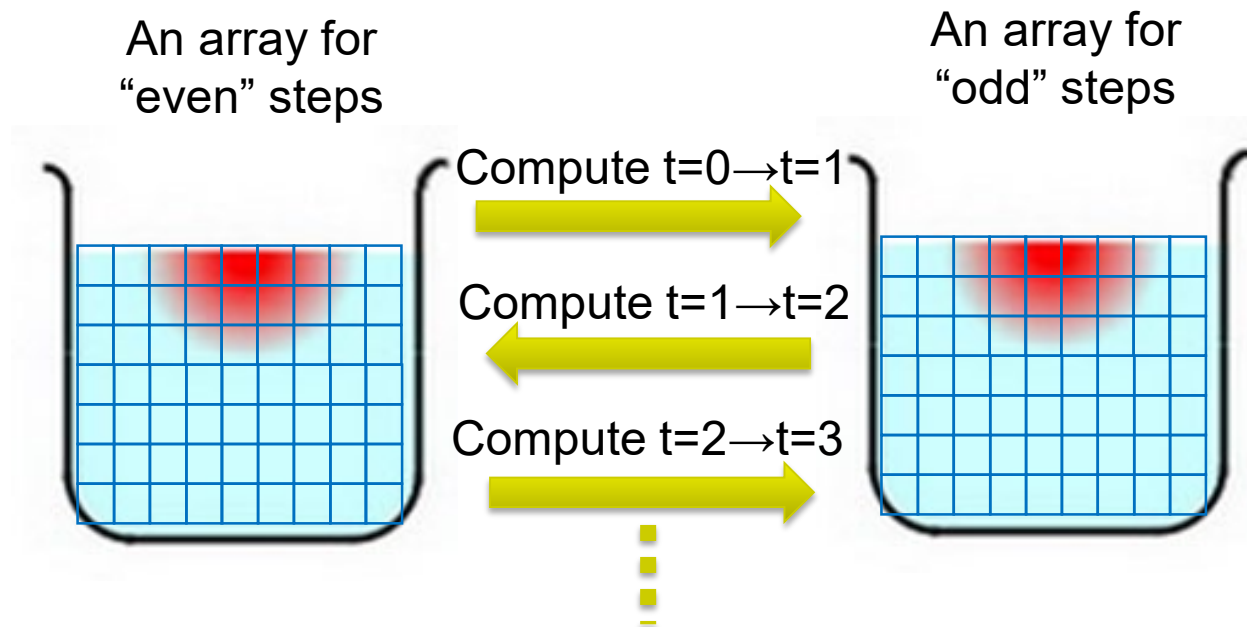


We can access “old” neighbor points correctly 😊

# Double Buffering Technique



- A simple way is to make arrays for all time steps, but it consumes **too much memory!** ( $n_x \times n_y \times n_t$ )
- It is sufficient to have “current” array and “next” array.
- It is better to use only “**Double buffers**”



※ Sample program uses a global variables  
float data[2][NY][NX];

# How We Parallelize “diffusion” sample (Related to Assignment [O1])



calc() takes long time, complexity is  $O(n_x n_y n_t)$

It mainly uses “for” loops

- How about using `#pragma omp parallel for` ?
- Good! but...

There are 3 (t, x, y) loops. Which should be parallelized?

**[Hint1]** Parallelizing either of spatial loop (x, y) would be good. Then spaces are divided into multiple threads

- **[Q]** Parallelizing t loop is a not good idea. Why?

**[Hint2]** Take care of “pitfall in nested loops” (see slides in previous class)

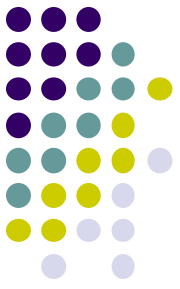
# Towards “Correct” Parallel Programming



There are several types of **bugs** in parallel programming

- Bugs in compile time
- Bugs in run time
  - Bugs that abort execution (cf. segmentation fault)
  - **Silent bugs → Hardest to find!**

All bugs should be avoided!



# When Can We Use “omp for”?

- Loops with some (complex) forms cannot be supported, unfortunately ☹
- The target loop must be in the following form

```
#pragma omp for
  for (i = value; i op value; incr-part)
    body
```

“*op*” : <, >, <=, >=, etc.

“*incr-part*” : i++, i--, i+=c, i-=c, etc.

OK 😊: for (x = n; x >= 0; x-=4) ...

ERROR ☹: for (i = 0; test(i); i++) ...

ERROR ☹: for (p = head; p != NULL; p = p->next)

} Bugs in  
compile time

# What are Differences between These Codes?



```
double D[100];  
:
```

Code A

```
#pragma omp parallel for  
for (i = 0; i < 100; i++) {  
    D[i] = D[i]+1.0;  
}
```

Code B

```
#pragma omp parallel for  
for (i = 0; i < 99; i++) {  
    D[i+1] = D[i]+1.0;  
}
```

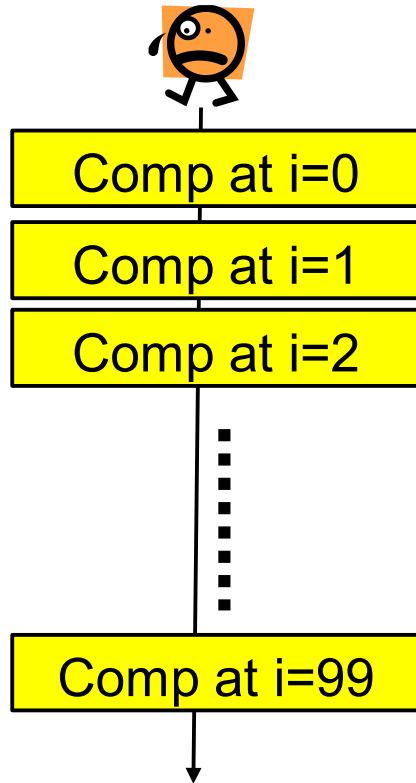
- Both codes are ok in compile time and can be executed
- But **only code A is correct 😊** , **code B has a bug ☹️**
  - Code B's results may be wrong

# Sequential Execution and Parallel Execution of Loop



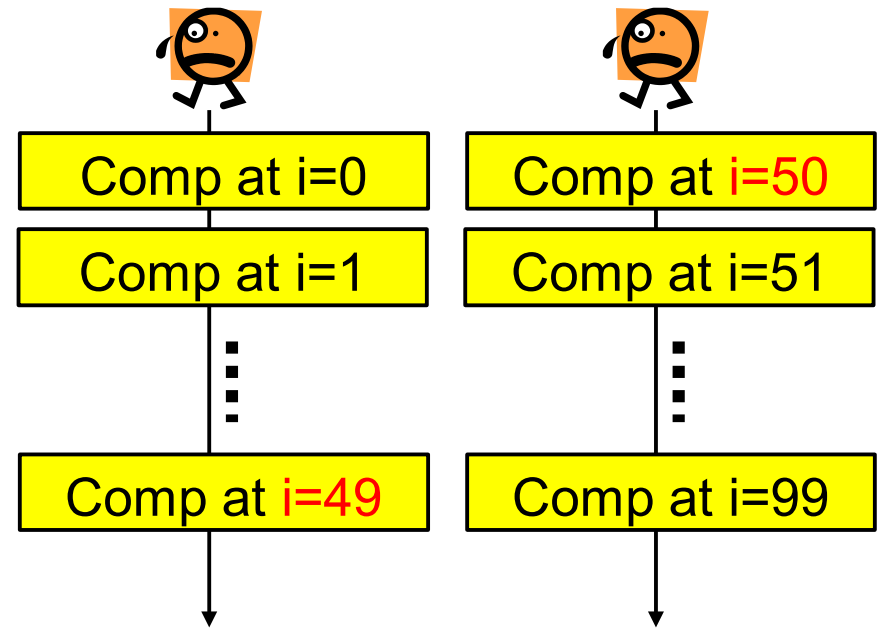
## [Sequential]

for (i = 0; i < 100; i++) ...



## [Parallel]

#pragma omp parallel for  
for (i = 0; i < 100; i++) ...



in case of 2 threads,  
i=50 is computed before i=49



# Difference between Two Codes

Code A

```
#pragma omp parallel for
  for (i = 0; i < 100; i++) {
    D[i] = D[i]+1.0;
  }
```

OK

It is **ok to reorder** 100 computations

Code B

```
#pragma omp parallel for
  for (i = 0; i < 99; i++) {
    D[i+1] = D[i]+1.0;
  }
```

NG

Computations **must be done in an order** (i=0,1,2...)

➔ Parallelization breaks the order



# Dependency between Computations



We define following sets for computation C

- Read set  $R(C)$ : the set of variables **read** by C
- Write set  $W(C)$ : the set of variables **written** by C
  - Ex) C:  $x = y + z \rightarrow R(C) = \{y, z\}, W(C) = \{x\}$

We define **dependency** between C1 and C2

- If  $(W(C1) \cap R(C2) \neq \emptyset)$ , C1 and C2 are **dependent** (**write** vs **read**)
- If  $(R(C1) \cap W(C2) \neq \emptyset)$ , C1 and C2 are **dependent** (**read** vs **write**)
- If  $(W(C1) \cap W(C2) \neq \emptyset)$ , C1 and C2 are **dependent** (**write** vs **write**)
- Otherwise, C1 and C2 are **independent**
  - ✖ **read vs read** cases are independent

If C1 and C2 are **independent**, parallelization of C1 and C2 is safe ☺



# Example of Dependency

Code A

```
#pragma omp parallel for
  for (i = 0; i < 100; i++) {
    D[i] = D[i]+1.0;    ← Ai
  }
```

$R(A_i) = \{D[i]\}, W(A_i) = \{D[i]\}$

All 100 computations are independent

Code B

```
#pragma omp parallel for
  for (i = 0; i < 99; i++) {
    D[i+1] = D[i]+1.0; ← Bi
  }
```

$R(B_i) = \{D[i]\}, W(B_i) = \{D[i+1]\}$

$R(B_{i+1}) \cap W(B_i) = \{D[i+1]\} \neq \emptyset \rightarrow \text{Dependent!}$

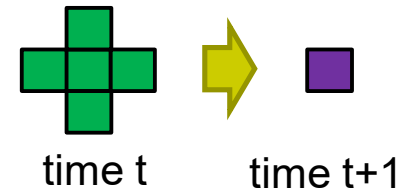
# Dependency and Parallelism in Stencil Computations (1)



Consider 1D stencil computation:

```
for (t = 0; t < NT; t++)
  for (x = 1; x < NX-1; x++)
     $f_{t+1,x} = (f_{t,x-1} + f_{t,x} + f_{t,x+1}) / 3.0$  /*  $C_{t,x}$  */
```

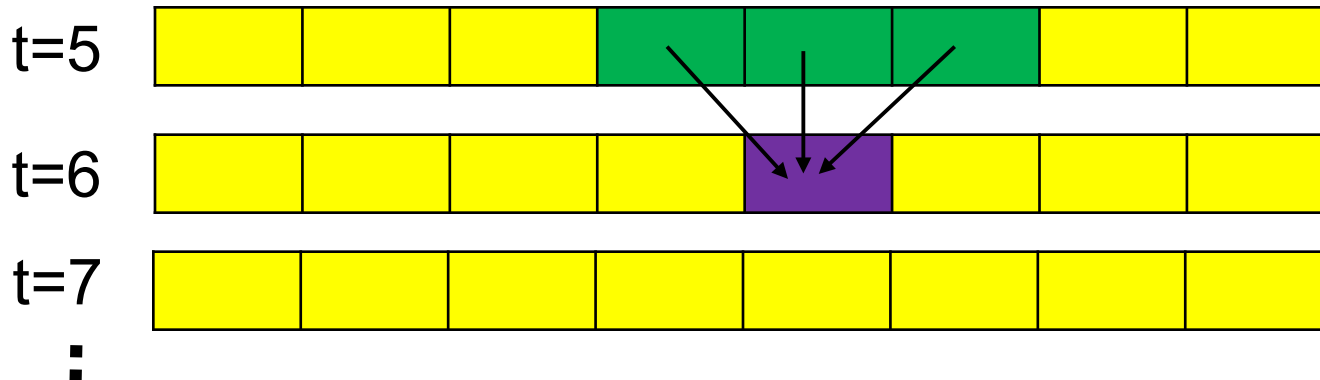
✂ This is simpler than “diffusion” (2D) sample



We let  $C_{t,x}$  be computation of a single point  $f_{t+1,x}$

$R(C_{t,x}) = \{f_{t,x-1}, f_{t,x}, f_{t,x+1}\}$ ,  $W(C_{t,x}) = \{f_{t+1,x}\}$

.....  $x=$  19    20    21    .....



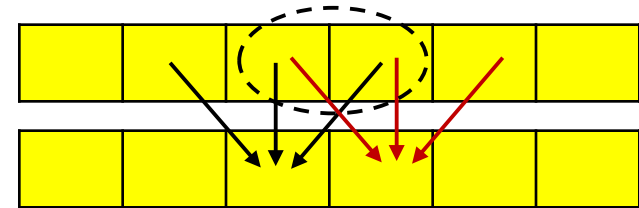
✂ This figure omits double buffering technique

# Dependency and Parallelism in Stencil Computations (2)

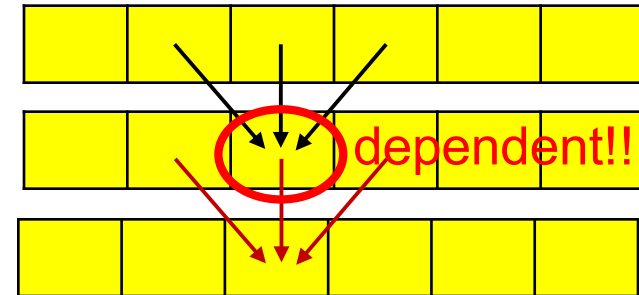


- Can we compute  $C_{5,20}$  and  $C_{5,21}$  in parallel? (*t is same, x is different*)
  - $R(C_{5,20}) = \{f_{5,19}, f_{5,20}, f_{5,21}\}$ ,  $W(C_{5,20}) = \{f_{6,20}\}$
  - $R(C_{5,21}) = \{f_{5,20}, f_{5,21}, f_{5,22}\}$ ,  $W(C_{5,21}) = \{f_{6,21}\}$
 → They are **independent** 😊 (for all pairs of x)

Read vs. Read is Ok



- Can we compute  $C_{5,20}$  and  $C_{6,20}$  in parallel? (*t is different*)
  - $R(C_{5,20}) = \{f_{5,19}, f_{5,20}, f_{5,21}\}$ ,  $W(C_{5,20}) = \{f_{6,20}\}$
  - $R(C_{6,20}) = \{f_{6,19}, f_{6,20}, f_{6,21}\}$ ,  $W(C_{6,20}) = \{f_{7,20}\}$
 → They are **dependent** ☹️



In Assignment [O1]

- it is **OK** to parallelize x-loop or y-loop
- it is **NG** to parallelize t-loop

# Assignments in OpenMP Part (Abstract)



Choose one of [O1]—[O3], and submit a report  
Due date: May 13 (Thu)

- [O1] Parallelize “diffusion” sample program by OpenMP.  
(</gs/hs1/tga-ppcomp/21/diffusion/> on TSUBAME)
- [O2] Parallelize “sort” sample program by OpenMP.  
(</gs/hs1/tga-ppcomp/21/sort/> on TSUBAME)
- [O3] (Freestyle) Parallelize *any* program by OpenMP.

For more detail, please see OpenMP (1) slides on Apr 19



# Next Class:

- OpenMP(3)
  - “task parallelism” for programs with irregular structures
  - sort: Quick sort sample
    - Related to assignment [O2]