Lecture on Electricity Introduction to Electricity: Coulomb's Law

Md. Asaduzzaman Asad
United International University
Reference Books:

1. Fundamentals of Physics
By Halliday-Resnick-Walker (10th edition)

2. Physics for Engineers (Par-II)

By Dr. Giasuddin Ahmed

Concept of charge

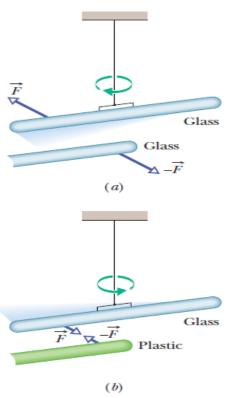


Figure 21-1 (a) The two glass rods were each rubbed with a silk cloth and one was suspended by thread. When they are close to each other, they repel each other. (b) The plastic rod was rubbed with fur. When brought close to the glass rod, the rods attract each other.

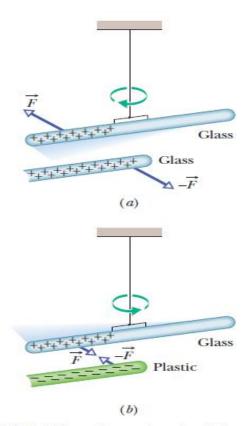


Figure 21-2 (a) Two charged rods of the same sign repel each other. (b) Two charged rods of opposite signs attract each other. Plus signs indicate a positive net charge, and minus signs indicate a negative net charge.

Introduction Continued

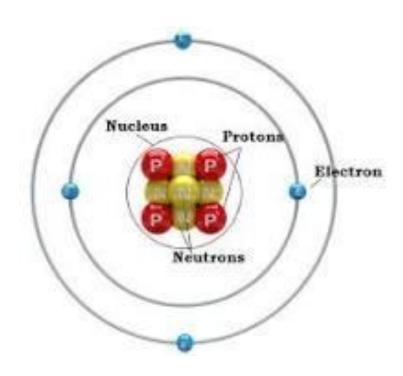
- •What is charge?
- How do we visualize it.
- What is the model.
- We only know charge exists because in experiments electric forces cause objects to move.

• Electrostatics: study of electricity when the charges are not in motion. Good place to start studying E&M because there are lots of demonstrations.



Some preliminaries

- Electron: Considered a point object with radius less than 10⁻¹⁸ meters with electric charge e= -1.6 x 10 ⁻¹⁹ Coulombs (SI units) and mass m_e= 9.11 x 10 ⁻³¹ kg
- Proton: It has a finite size with charge +e, mass m_p= 1.67 x 10⁻²⁷ kg and with radius
 - 0.805 +/-0.011 x 10⁻¹⁵ m scattering experiment
 - 0.890 +/-0.014 x 10⁻¹⁵ m Lamb shift experiment
- Neutron: Similar size as proton, but with total charge = 0 and mass m_n=
 - Positive and negative charges exists inside the neutron



Methods of Charging Objects: Friction, Contact, and Induction

- Normally atoms are in the lowest energy state. This means that the material is electrically neutral. You have the same number of electrons as protons in the material.
- How do we change this?
- How do we add more electrons than protons or remove electrons?

Summary Comments

- •Silk(+) on teflon(-)
- •Silk (-) on acrylic (+)
- Wood doesn't charge
- Charged objects always attract neutral objects

- Show Triboelectric series
- •Not only chemical composition important, structure of surface is important monolayer of molecules involved, quantum effect.

(nanotechnology)

Triboelectric series

http://www.sciencejoywagon.com/physicszone/lesson/07elecst/static/triboele.htm

Positive ((Lose	electrons	easily)

Air

Human Hands

Asbestos

Rabbit Fur

Glass

Mica

Acrylic

Human Hair

Nylon

Wool

Fur

Lead

Silk

Aluminum

Pape r

Cotton

Steel

Wood

Amber

Sealing Wax

Hard Rubber

Nickel, Copper

Brass, Silver

Gold, Platinum

Sulfur

Acetate, Rayon

Polyester

Styrene

Orlon

Saran

Balloon

Polyurethane

Polypropy lene

Vinyl (PVC)

Silicon

Teflon

Negative (Gains electrons easily)

Summary: Electrostatics is based on 4 four empirical facts

- Conservation of charge
- Quantization of charge
- Coulomb's Law
- The principle of superposition

Conservation of charge

- Rubbing does not create charge, it is transferred from one object to another
- Teflon negative silk positive
- Acrylic positive silk negative
- Nuclear reactions $\gamma^0 = e^+ + e^-$
- Radioactive decay $^{238}U_{92} = ^{234}Th_{90} + ^{4}He_2$
- High energy particle reactions $e^- + p^+ = e^- + \pi^+ + n^0$

What is meant by quantization of charge?

- Discovered in 1911 by Robert A. Millikan in the oil drop experiment
- The unit of charge is so tiny that we will never notice it comes in indivisible lumps.

Example-1: Suppose in a typical experiment we charge an object up with a nanoCoulomb of charge (10⁻⁹ C). How many elementary units of charge is this?

Solution: We know,

$$Q=N \times e$$
 so $N = \frac{Q}{e} = \frac{10^{-9}C}{1.6 \times 10^{-19}C} = 6 \times 10^{9}$

= six billion units of charge or 6 billion electrons.

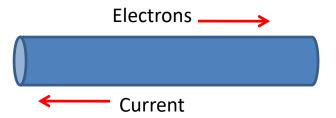
Ans: 6×10^9 unit charge

Electric Charge (Q)

- Characteristic of subatomic particles that determines their electromagnetic interactions
- An electron has a -1.602·10⁻¹⁹ Coulomb charge
- The rate of flow of charged particles is called current

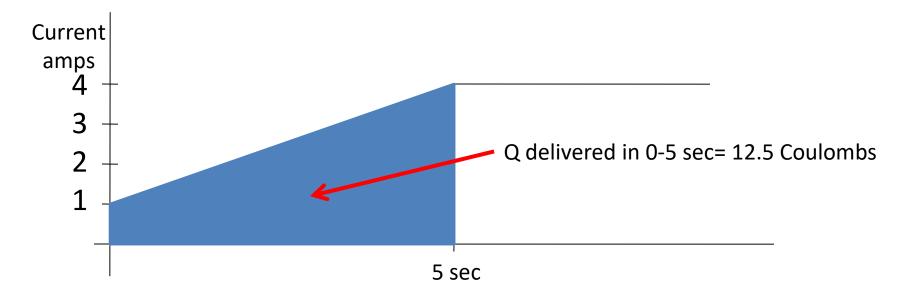
Current (I)

- Current = (Number of electrons that pass in one second) · (charge/electron)
 - \triangleright -1 ampere = (6.242·10¹⁸ e/sec) ·(-1.602 10⁻¹⁹Coulomb/e)
 - Notice that an ampere = Coulomb/second
- The negative sign indicates that the current inside is actually flowing in the opposite direction of the electron flow



Current

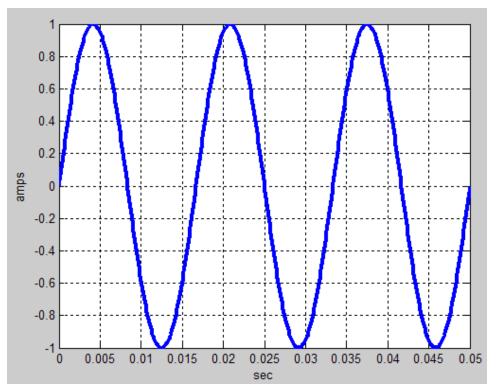
- i = dq/dt the derivitive or slope of the charge when plotted against time in seconds
- Q = ∫ i · dt the integral or area under the current when plotted against time in seconds



AC and DC Current

•DC Current has a constant value

AC Current has a value that changes sinusoidally



- ➤ Notice that AC current changes in value and direction
- ➤ No net charge is transferred

Why Does Current Flow?

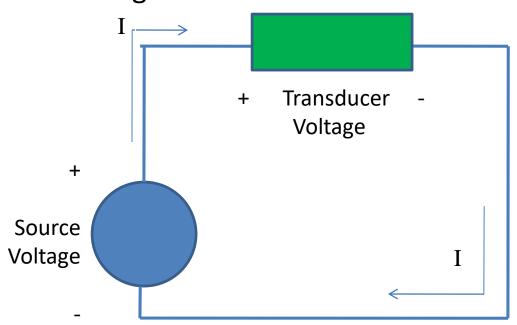
- A voltage source provides the energy (or work) required to produce a current
 - ➤ Volts = joules/Coulomb = dW/dQ
- A source takes charged particles (usually electrons) and raises their potential so they flow out of one terminal into and through a transducer (light bulb or motor) on their way back to the source's other terminal

Voltage

- Voltage is a measure of the potential energy that causes a current to flow through a transducer in a circuit
- Voltage is always measured as a difference with respect to an arbitrary common point called ground
- Voltage is also known as electromotive force or EMF outside engineering

A Circuit

 Current flows from the higher voltage terminal of the source into the higher voltage terminal of the transducer before returning to the source



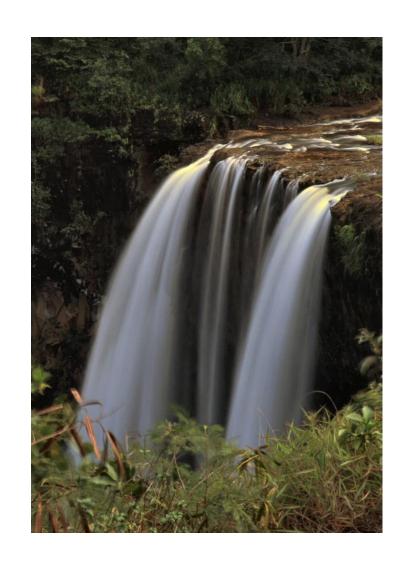
The source expends energy & the transducer converts it into something useful

Power

- The rate at which energy is transferred from an active source or used by a passive device
- P in watts = dW/dt = joules/second
- $P = V \cdot I = dW/dQ \cdot dQ/dt = volts \cdot amps = watts$
- W = \int P \cdot dt so the energy (work in joules) is equal to the area under the power in watts plotted against time in seconds

How you should be thinking about electric circuits:

Voltage: a force that pushes the current through the circuit (in this picture it would be equivalent to gravity)



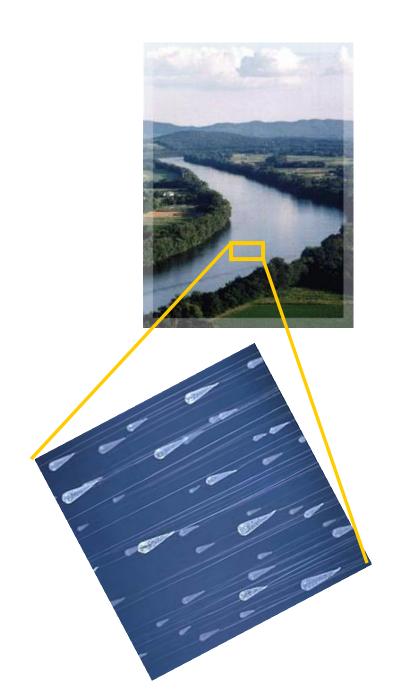
How you should be thinking about electric circuits:

Resistance: friction that impedes flow of current through the circuit (rocks in the river)



How you should be thinking about electric circuits:

Current: the actual "substance" that is flowing through the wires of the circuit (electrons!)







Would This Work?



Would This Work?

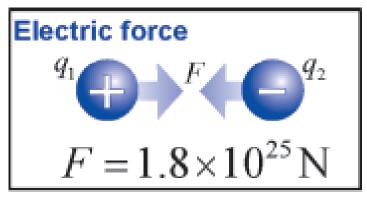


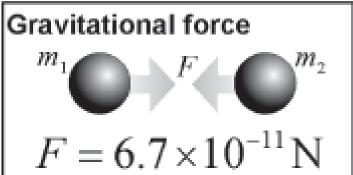
The Central Concept: Closed Circuit



Key Question:

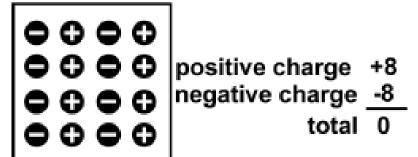
How do electric charges interact?



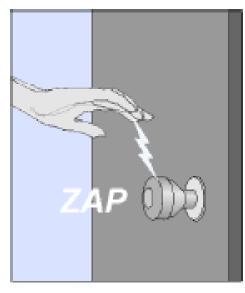


- All ordinary matter contains both positive and negative charge.
- You do not usually notice the charge because most matter contains the exact same number of positive and negative charges.
- An object is electrically neutral when it has equal amounts of both types of charge.

This object is neutral

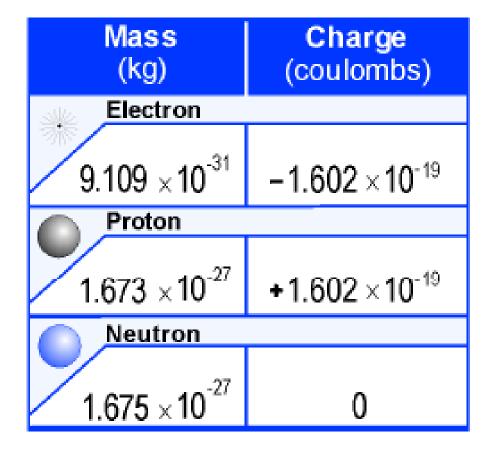


- Objects can lose or gain electric charges.
- The net charge is also sometimes called excess charge because a charged object has an excess of either positive or negative charges.
- A tiny imbalance in either positive or negative charge on an object is the cause of static electricity.

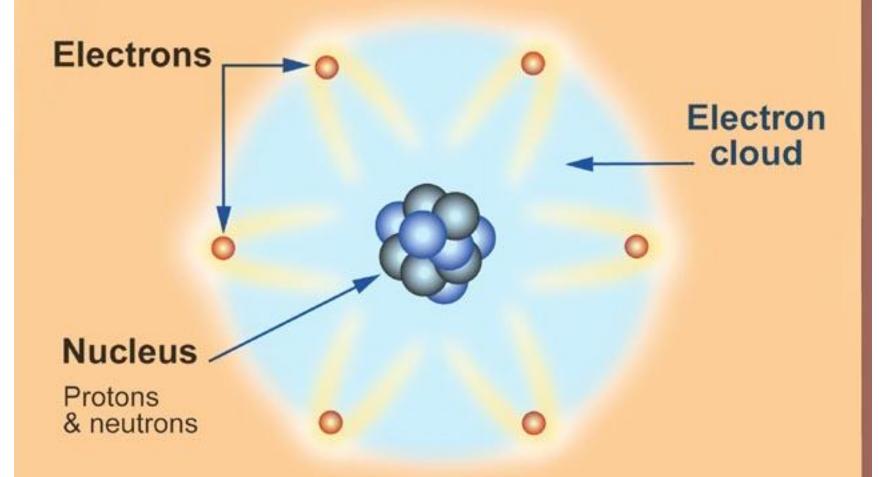


Static electricity

- Electric charge is a property of tiny particles in atoms.
- The unit of electric charge is the coulomb (C).
- A quantity of charge should always be identified with a positive or a negative sign.

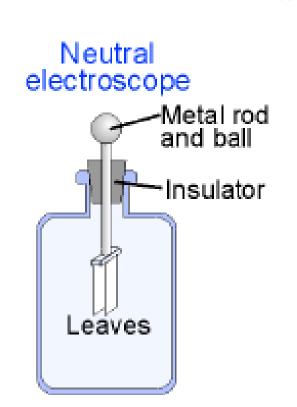


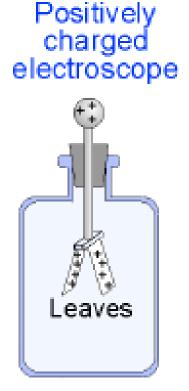
Structure of an Atom

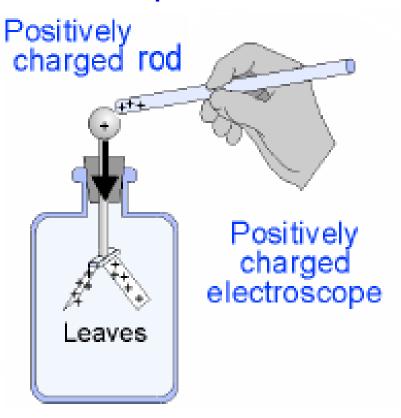


Electric forces

 The forces between the two kinds of charge can be observed with an electroscope.

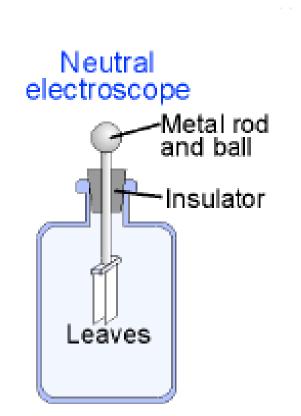


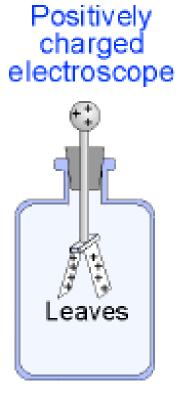


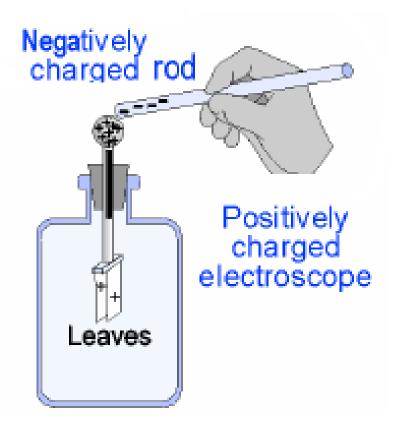


Electric forces

Charge can be transferred by conduction.

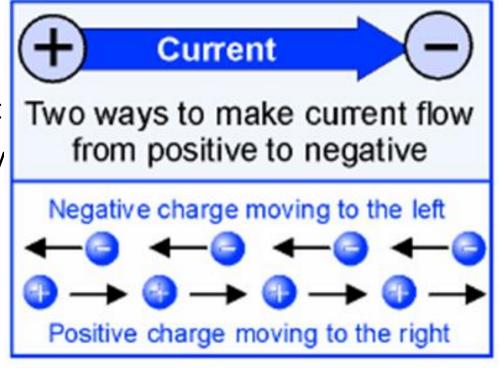






Electric current

- The direction of current was historically defined as the direction that <u>positive charges</u> move.
- Both positive and negative charges can carry current.
- In conductive liquids (salt water) <u>both</u> positive and negative charges carry current
- In solid metal conductors, only the <u>electrons</u> can move, so current is carried by the flow of negative electrons.



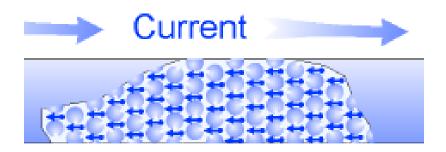
Electric current

 Current is the movement of electric charge through a substance.

Calculate current

Calculate the current from the flow of charge





- Two coulombs of charge pass through a wire in five seconds.
- Calculate the current in the wire.

Conductors and insulators

- All materials contain electrons.
- The electrons are what carry the current in a conductor.
- The electrons in insulators are not free to move—they are tightly bound inside atoms.



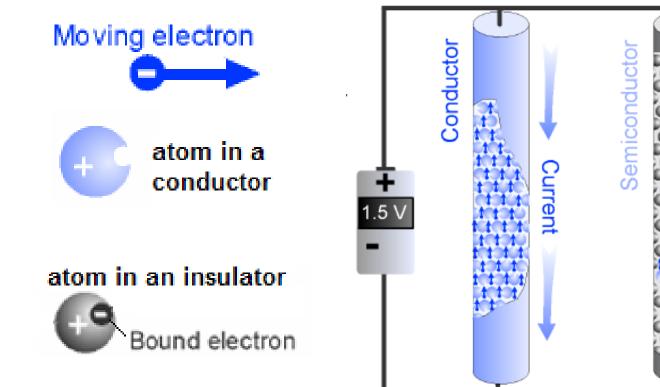


atom in an insulator



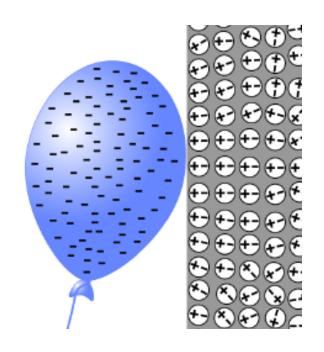
Conductors and insulators

•A semiconductor has a few free electrons and atoms with bound electrons that act as insulators.



Conductors and insulators

- When two neutral objects are rubbed together, charge is transferred from one to the other and the objects become oppositely charged.
- This is called charging by friction.
- Objects charged by this method will attract each other.



Conductors and Insulators

Co	nd		1	ro
CO	IIU	uC	LU	5

Insulators

Electrons flow easily between atoms.

Electron flow is difficult between atoms.

1-3 valence electrons in outer orbit.

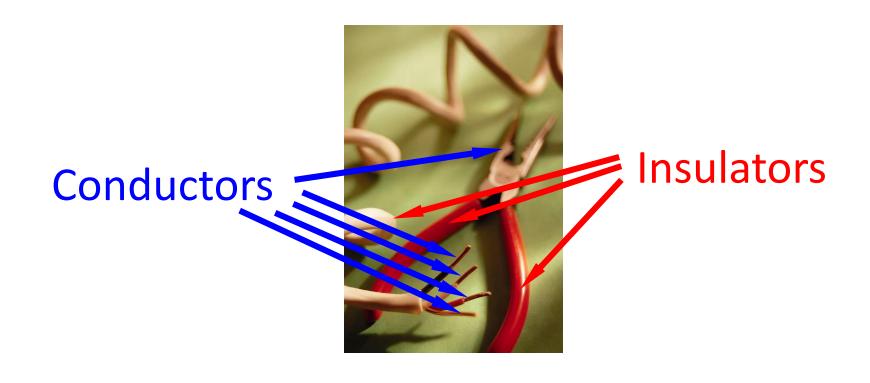
5-8 valence electrons in outer orbit.

Examples: Silver, Copper, Gold, Aluminum, etc.

Examples: Mica, Glass, Quartz, etc.

Conductors and Insulators

Identify conductors and insulators

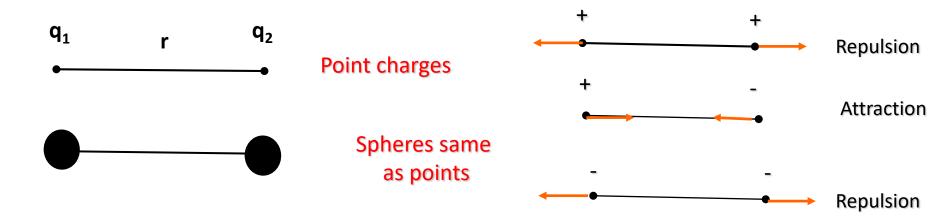


Coulombs Law

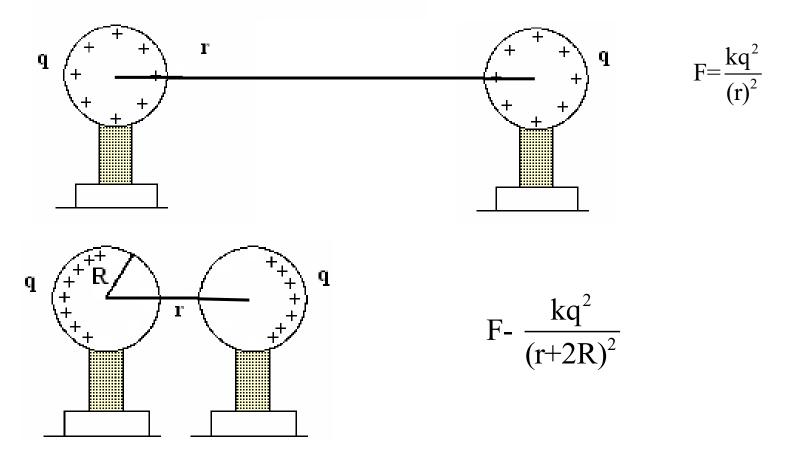
Lab Experiment

In 1785 Charles Augustin Coulomb reported in the Royal Academy Memoires using a torsion balance two charged mulberry pith balls repelled each other with a force that is inversely proportional to the distance.

$$F = \frac{kq_1q_2}{r^2}$$
 where k=8.99*10⁹ Nm²/C² in SI unit k ~ 10¹⁰ Nm²/C²



Uniformly charged metal spheres of Radius R



Demo: Show uniformity of charge around sphere using electrometer.

Demo: Show charging spheres by induction using

electrometer

Coulombs Law Two Positive Charges

Example-2: What is the force between two positive charges each 1 nano Coulomb, 1cm apart in a typical demo? Why is the force so weak here?

Solution:

$$F = \frac{kq_1q_2}{r^2}$$

$$F = \frac{\left(10^{10} \frac{Nm^2}{C^2}\right)\left(10^{-9}c\right)^2}{\left(10^{-2}m\right)^2} = 10^{-4}N$$
Repulsion

(equivalent to a weight of something with a mass of 10⁻⁵ kg = 10⁻² gm or 10 mg - long strand of hair)

Coulombs Law Two Pennies without electrons

Example-3: (i) What is the force between two 3 gm pennies one meter apart if we remove all the electrons from the copper atoms? [Modeling] (ii) What is their acceleration as they separate?

Solution: (i) We know, $F = \frac{kq_1q_2}{r^2} = \frac{\left(10^{10} \frac{Nm^2}{C^2}\right)q^2}{\left(1m\right)^2}$ The force is $F = \frac{\left(10^{10} \frac{Nm^2}{C^2}\right)\left(1.4 \times 10^5 C\right)^2}{1m^2} = 2 \times 10^{20} N$

The atom Cu has 29 protons and a 3 gm penny has

$$= \left(\frac{3gm}{63.5gm}\right) \times 6 \times 10^{23} atoms = 3 \times 10^{22} atoms$$

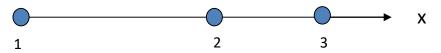
The total charge is $q = 29 \times 3 \times 10^{22} atoms \times 1.6 \times 10^{-19} C = 1.4 \times 10^{5} C$ (ii) What is their acceleration as they separate?

$$a = \frac{F}{m} = \frac{2x10^{20}N}{3x10^{-3}kg} = 7x10^{22} \frac{m}{s^2}$$

Principle of Superposition Three charges In a line

• In the previous example we tacitly assumed that the forces between nuclei simply added and did not interfere with each other. That is the force between two nuclei in each penny is the same as if all the others were not there. This idea is correct and is referred to as the Principle of Superposition.

Example-4: Example of charges in a line.



Three charges lie on the x axis: q_1 =+25 nC at the origin, q_2 = -12 nC at x =2m, q_3 =+18 nC at x=3 m. What is the net force on q_1 ?

Solution: We simply add the two forces keeping track of their directions. Let a positive force be one in the + x direction.

$$F = -kq_1 \left(\frac{q_2}{(2m)^2} + \frac{q_3}{(3m)^2} \right)$$

$$= -\left(10^{10} \, \frac{Nm^2}{C^2}\right) (25 \times 10^{-9} \, C) \left(\frac{-12 \times 10^{-9} \, C}{(2m)^2} + \frac{18 \times 10^{-9} \, C}{(3m)^2}\right)$$

$$=2.5\times10^{-7} N$$

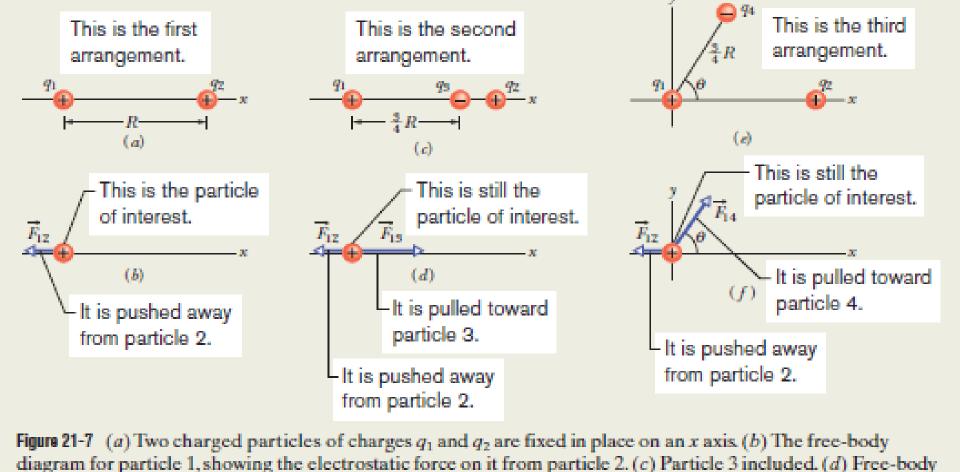


diagram for particle 1.(e) Particle 4 included (f) Free-body diagram for particle 1.

This sample problem actually contains three examples, to build from basic stuff to harder stuff. In each we have the

same charged particle 1. First there is a single force acting on it (easy stuff). Then there are two forces, but they are just in opposite directions (not too bad). Then there are again two forces but they are in very different directions (ah, now we have to get serious about the fact that they are vectors). The key to all three examples is to draw the forces correctly before you reach for a calculator, otherwise you may be calculating nonsense on the calculator. (Figure 21-7 is available in WileyPLUS as an animation with voiceover.)

$$F_{12} = \frac{1}{4\pi\epsilon_0} \frac{|q_1||q_2|}{R^2}$$

$$= (8.99 \times 10^9 \,\mathrm{N \cdot m^2/C^2})$$

$$\times \frac{(1.60 \times 10^{-19} \,\mathrm{C})(3.20 \times 10^{-19} \,\mathrm{C})}{(0.0200 \,\mathrm{m})^2}$$

$$= 1.15 \times 10^{-24} \,\mathrm{N}.$$

Thus, force \vec{F}_{12} has the following magnitude and direction (relative to the positive direction of the x axis):

$$1.15 \times 10^{-24} \,\mathrm{N}$$
 and 180° . (Answer)

We can also write \vec{F}_{12} in unit-vector notation as

$$\vec{F}_{12} = -(1.15 \times 10^{-24} \,\mathrm{N})\hat{i}$$
. (Answer)

Three particles: To find the magnitude of F_{13} , we can rewrite Eq. 21-4 as

$$F_{13} = \frac{1}{4\pi\epsilon_0} \frac{|q_1||q_3|}{(\frac{2}{4}R)^2}$$

$$= (8.99 \times 10^9 \,\mathrm{N} \cdot \mathrm{m}^2/\mathrm{C}^2)$$

$$\times \frac{(1.60 \times 10^{-19} \,\mathrm{C})(3.20 \times 10^{-19} \,\mathrm{C})}{(\frac{3}{4})^2 (0.0200 \,\mathrm{m})^2}$$

$$= 2.05 \times 10^{-24} \,\mathrm{N}.$$

We can also write \vec{F}_{12} in unit-vector notation:

$$\vec{F}_{13} = (2.05 \times 10^{-24} \,\mathrm{N})\hat{i}$$
.

The net force $\vec{F}_{1,net}$ on particle 1 is the vector sum of \vec{F}_{12} and \vec{F}_{13} ; that is, from Eq. 21-7, we can write the net force $\vec{F}_{1,net}$ on particle 1 in unit-vector notation as

$$\begin{split} \vec{F}_{1,\text{net}} &= \vec{F}_{12} + \vec{F}_{13} \\ &= -(1.15 \times 10^{-24} \, \text{N}) \hat{i} \, + (2.05 \times 10^{-24} \, \text{N}) \hat{i} \\ &= (9.00 \times 10^{-25} \, \text{N}) \hat{i}. \end{split} \tag{Answer}$$

Thus, $\vec{F}_{1,net}$ has the following magnitude and direction (relative to the positive direction of the x axis):

$$9.00 \times 10^{-25} \,\text{N}$$
 and 0°. (Answer)

Four particles: We can rewrite Eq. 21-4 as

$$F_{14} = \frac{1}{4\pi\epsilon_0} \frac{|q_1||q_4|}{(\frac{3}{4}R)^2}$$

$$= (8.99 \times 10^9 \,\mathrm{N} \cdot \mathrm{m}^2/\mathrm{C}^2)$$

$$\times \frac{(1.60 \times 10^{-19} \,\mathrm{C})(3.20 \times 10^{-19} \,\mathrm{C})}{(\frac{3}{4})^2(0.0200 \,\mathrm{m})^2}$$

$$= 2.05 \times 10^{-24} \,\mathrm{N}.$$

Then from Eq. 21-7, we can write the net force $\vec{F}_{1,net}$ on particle 1 as

$$\vec{F}_{1,\text{net}} = \vec{F}_{12} + \vec{F}_{14}.$$

Because the forces \vec{F}_{12} and \vec{F}_{14} are not directed along the same axis, we *cannot* sum simply by combining their magnitudes. Instead, we must add them as vectors, using one of the following methods.

Method 1. Summing directly on a vector-capable calculator. For \vec{F}_{12} , we enter the magnitude 1.15×10^{-24} and the angle 180°. For \vec{F}_{14} , we enter the magnitude 2.05×10^{-24} and the angle 60°. Then we add the vectors.

Method 2. Summing in unit-vector notation. First we rewrite F_{14} as

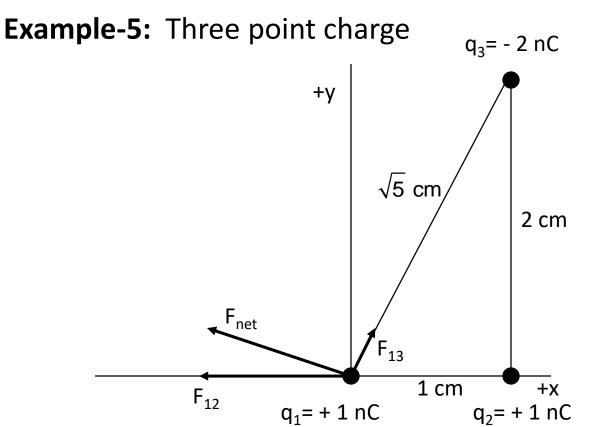
$$\vec{F}_{14} = (F_{14}\cos\theta)\hat{i} + (F_{14}\sin\theta)\hat{j}.$$

Substituting 2.05 \times 10⁻²⁴ N for F_{14} and 60° for θ , this becomes

$$\vec{F}_{14} = (1.025 \times 10^{-24} \,\mathrm{N})\hat{i} + (1.775 \times 10^{-24} \,\mathrm{N})\hat{j}.$$

Then we sum:

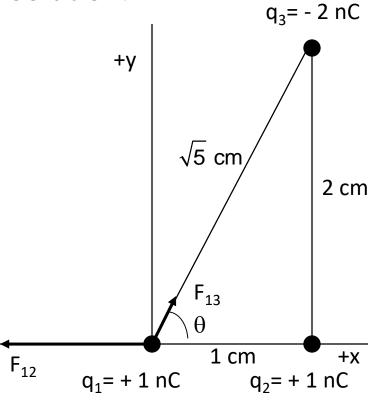
$$\begin{split} \vec{F}_{1,\text{net}} &= \vec{F}_{12} + \vec{F}_{14} \\ &= -(1.15 \times 10^{-24} \, \text{N}) \hat{i} \\ &+ (1.025 \times 10^{-24} \, \text{N}) \hat{i} + (1.775 \times 10^{-24} \, \text{N}) \hat{j} \\ &\approx (-1.25 \times 10^{-25} \, \text{N}) \hat{i} + (1.78 \times 10^{-24} \, \text{N}) \hat{j}. \end{split}$$
(Answer)



Question: What is the net force on q_1 and in what direction?

Hint : Find x and y components of force on q_1 due to q_2 and q_3 and add them up.

Solution:



x and y Components of force due to q₂

$$F_{12x} = -10^{10} \, \frac{Nm^2}{C^2} \, \frac{(10^{-9} \, \text{C})^2}{(10^{-2} \, \text{m})^2} = -1 \times 10^{-4} \, \text{N}$$

$$F_{12y} = 0$$

x and y Components of force due to q₃

Magnitude of Force due to q₃

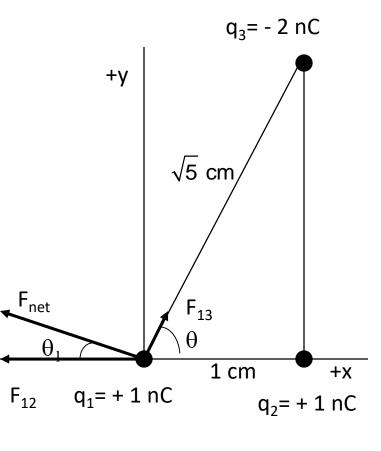
$$\left| F_{13} \right| = 10^{10} \frac{Nm^2}{C^2} \frac{(2 \times 10^{-9} \text{C})(1 \times 10^{-9} \text{C})}{(\sqrt{5} \times 10^{-2} \text{m})^2} = 0.40 \times 10^{-4} \text{N}$$

$$\tan \theta = \frac{y - axis \ value}{x - axis \ value} \implies \theta = \tan^{-1}(\frac{2}{1}) = 63.43 \ deg$$

$$F_{13x} = F\cos\theta = (0.40N)(\cos 63.43) = 0.179 \times 10^{-4}N$$

$$F_{13y} = F \sin \theta = (0.40N)(\sin 63.43) = 0.358 \times 10^{-4} N$$

Example Cont.



Total force along the x-axis

$$F_{x_{net}} = F_{12x} + F_{13x} = (-1 \times 10^{-4} + 0.179 \times 10^{-4})N = -0.821 \times 10^{-4}N$$

Total force along the y-axis

$$F_{y_{net}} = F_{12y} + F_{13y} = (0 + 0.358 \times 10^{-4})N = 0.358 \times 10^{-4}N$$

$$F_{\text{net}} = \sqrt{F_{x_{\text{net}}}^2 + F_{y_{\text{net}}}^2} = \sqrt{((0.821)^2 + (0.358)^2) \times (10^{-4})^2} N$$

$$F_{net} = +0.802 \, 10^{-4} \, N$$

$$\begin{split} \tan\theta_1 &= \frac{F_y}{F_x} \\ \theta_1 &= tan^{-1}\!\!\left(\frac{F_y}{F_x}\right) \qquad \theta_1 = tan^{-1}\!\!\left(\frac{0.358 \times 10^{-4} N}{-0.821 \times 10^{-4} N}\right) \end{split}$$

$$\theta_1 = 23.6^{\circ}$$
 from the - x axis

Example-6: In an atom can we neglect the gravitational force between the electrons and protons? What is the ratio of Coulomb's electric force to Newton's gravity force for 2 electrons separated by a distance r?

Solution:

$$F_{c} = \frac{\text{kee}}{\text{r}^{2}}$$

$$F_{g} = \frac{\text{Gmm}}{\text{r}^{2}}$$

$$\frac{F_{c}}{F_{g}} = \frac{\text{ke}^{2}}{\text{Gm}^{2}}$$

$$\frac{F_{c}}{F_{g}} = \frac{\left(10^{10} Nm^{2} / C^{2}\right) \left(1.6 \times 10^{-19} C\right)^{2}}{\left(6.67 \times 10^{-11} Nm^{2} / kg^{2}\right) \left(9.1 \times 10^{-31} kg\right)^{2}}$$

$$= 4.6 \times 10^{42}$$

Huge number, pure ratio