## SOLUTION OF ONE DIMENSIONAL HEAT EQUATION

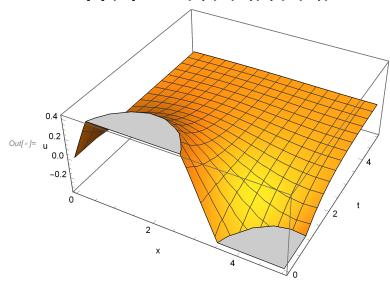
1. 
$$u_t - u_{xx} = 0$$
,  $0 < x < 5$ ,  $t > 0$ 

$$u(x, 0) = Sin[x], 0 \le x \le 5$$

$$u(0, t) = 0, t \ge 0$$

$$u(5, t) = 0, t \ge 0$$

 $m[*]:= eqn1 = {\partial_t u[x, t] - \partial_{x,x} u[x, t] == 0, u[x, 0] == Sin[x], u[0, t] == 0, u[5, t] == 0};$   $sol1 = NDSolve[eqn1, u[x, t], {x, 0, 5}, {t, 0, 10}, PrecisionGoal <math>\rightarrow 3]$  // Quiet; Plot3D[u[x, t] /.  $sol1, {x, 0, 5}, {t, 0, 5}, AxesLabel <math>\rightarrow {"x", "t", "u"}]$ 



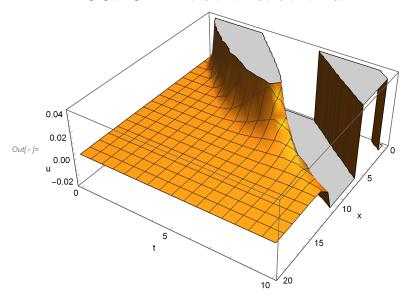
2. 
$$u_t - u_{xx} = 0$$
,  $0 < x < 20$ ,  $t > 0$ 

$$u \ (x, 0) = 0$$
,  $0 \le x \le 20$ 

$$u \ (0, t) = t^2 * Sin[t]$$
,  $t \ge 0$ 

$$u \ (20, t) = 0$$
,  $t \ge 0$ .

 $\begin{aligned} & \textit{In[*]} = \; \mathsf{eqn1} = \left\{ \partial_t \mathsf{u}[\mathsf{x}, \, \mathsf{t}] - \partial_{\mathsf{x}, \mathsf{x}} \mathsf{u}[\mathsf{x}, \, \mathsf{t}] \; = \; \mathsf{0}, \, \mathsf{u}[\mathsf{x}, \, \mathsf{0}] \; = \; \mathsf{0}, \, \mathsf{u}[\mathsf{0}, \, \mathsf{t}] \; = \; \mathsf{t}^2 \; \star \; \mathsf{Sin}[\mathsf{t}], \, \mathsf{u}[\mathsf{20}, \, \mathsf{t}] \; = \; \mathsf{0} \right\}; \\ & \mathsf{sol1} = \; \mathsf{NDSolve}[\mathsf{eqn1}, \, \mathsf{u}[\mathsf{x}, \, \mathsf{t}], \, \{\mathsf{x}, \, \mathsf{0}, \, 20\}, \, \{\mathsf{t}, \, \mathsf{0}, \, 10\}, \, \mathsf{PrecisionGoal} \; \to \; \mathsf{3}] \; / / \; \mathsf{Quiet}; \\ & \mathsf{Plot3D}[\mathsf{u}[\mathsf{x}, \, \mathsf{t}] \; /. \; \; \mathsf{sol1}, \, \{\mathsf{x}, \, \mathsf{0}, \, 20\}, \, \{\mathsf{t}, \, \mathsf{0}, \, 10\}, \, \mathsf{AxesLabel} \; \to \; \{"\mathsf{x}", \, "\mathsf{t}", \, "\mathsf{u}"\}] \end{aligned}$ 

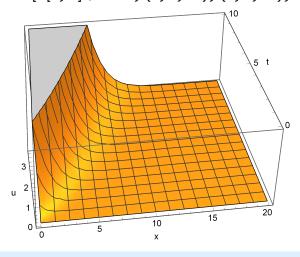


3. 
$$u_t - u_{xx} = 0$$
,  $0 < x < 20$ ,  $t > 0$ 

$$u(x, 0) = 0, 0 \le x \le 20$$

$$u(0, t) = t^2, t \ge 0$$

$$u(20, t) = 0, t \ge 0.$$



4. 
$$u_t - u_{xx} = 0$$
,  $0 < x < 5$ ,  $t > 0$ 

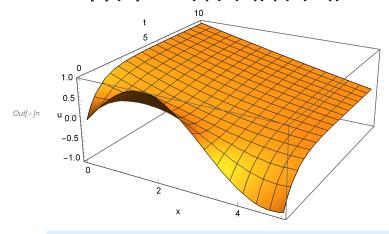
$$u(x, 0) = Sin[x], 0 \le x \le 5$$

$$u(0, t) = 1, t \ge 0$$

Out[ • ]=

 $u(5, t) = 0, t \ge 0.$ 

 $\ln[e]:=$  eqn1 = { $\partial_t u[x, t] - \partial_{x,x} u[x, t] == 0$ , u[x, 0] == Sin[x], u[0, t] == 1, u[5, t] == 0}; sol1 = NDSolve[eqn1, u[x, t],  $\{x, 0, 5\}$ ,  $\{t, 0, 10\}$ , PrecisionGoal  $\rightarrow 3$ ] // Quiet;  $Plot3D[u[x, t] /. sol1, \{x, 0, 5\}, \{t, 0, 10\}, AxesLabel \rightarrow \{"x", "t", "u"\}]$ 



5. 
$$u_t - u_{xx} = 0$$
,  $0 < x < 10$ ,  $t > 0$ 

$$u~(x,~0)~= Tanh~[x],~0 \le x \le 10$$

$$u (0, t) = t, t \ge 0$$

$$u(10, t) = 0, t \ge 0.$$

 $\ln[i] = eqn1 = \{\partial_t u[x, t] - \partial_{x,x} u[x, t] = 0, u[x, 0] = Tanh[x], u[0, t] = t, u[10, t] = 0\};$ sol1 = NDSolve[eqn1, u[x, t],  $\{x, 0, 10\}$ ,  $\{t, 0, 10\}$ , PrecisionGoal  $\rightarrow 3$ ] // Quiet; Plot3D[u[x, t] /. sol1, {x, 0, 10}, {t, 0, 10}, AxesLabel  $\rightarrow$  {"x", "t", "u"}]

