

## First and Last Occurrences

Difficulty: **Medium**

Accuracy: **37.36%**

Submissions: **271K+**

Points: **4**

sorted  
find 2:-



Given a sorted array **arr** with possibly some duplicates, the task is to find the first and last occurrences of an element **x** in the given array.

**Note:** If the number **x** is not found in the array then return both the indices as -1.  $\{-1, -1\}$

### Examples:

**Input:** arr[] = [1, 3, 5, 5, 5, 5, 67, 123, 125], x = 5

**Output:** [2, 5]

**Explanation:** First occurrence of 5 is at index 2 and last occurrence of 5 is at index 5

**Input:** arr[] = [1, 3, 5, 5, 5, 5, 7, 123, 125], x = 7

**Output:** [6, 6]

**Explanation:** First and last occurrence of 7 is at index 6

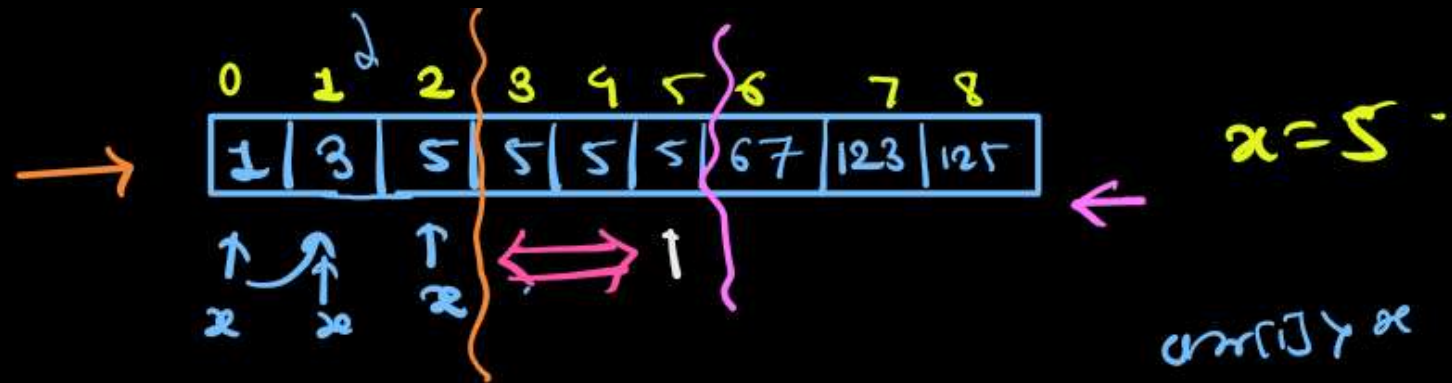
$$\{ a_1^{0,1} a_2 a_3 \dots a_n \} -$$

$$\{ a_1 \underset{\uparrow 0}{a_1} a_1 \underset{\uparrow 2}{a_2}, a_2, a_3, a_4 \dots a_n \} \quad x = a_1$$

$$\text{arr} = \begin{array}{c} 0 \quad 1^2 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7 \quad 8 \\ \boxed{1} \mid \boxed{3} \mid \boxed{5} \mid \boxed{5} \mid \boxed{5} \mid \boxed{5} \mid \boxed{67} \mid \boxed{123} \mid \boxed{125} \end{array} \quad x = 5$$

$$\{ 2, 5 \}$$

Approach 1 -



$\{2, 5\} \rightarrow$

$\{a_1, a_1, \dots, a_{n-1}, a_n\}$

Orange double-headed arrow spans the sequence.

$\{1, 1, \dots, 1, 5\} = 10^5 \quad x=1,$

Blue arrows point to the first and last 1, and the 5.

Yellow arrow points to the first 1.

Red double-headed arrow spans the sequence.

$\{0, n-1\}$

```

class GFG {
    ArrayList<Integer> find(int arr[], int x) {
        int n = arr.length;
        // code here
        ArrayList<Integer> ans = new ArrayList<>();
        int firstOcc = -1;
        int lastOcc = -1;
        // left to right
        for(int i = 0; i < n; i++){
            if(arr[i] == x){
                firstOcc = i;
                break;
            }
        }
        // right to left
        for(int i = n-1; i >= 0; i--){
            if(arr[i] == x){
                lastOcc = i;
                break;
            }
        }
        ans.add(firstOcc);
        ans.add(lastOcc);
        return ans;
    }
}

```

To exit full screen

Time complexity

Best case =  $O(1)$

Average case =  $O(n)$

Worst case =  $O(n)$

$T.C = O(n) + O(n)$   
 $O(n)$   
 $O(n)$

## Approach 2

0	1	2	3	4	5	6	7	8	9
1	3	5	5	5	5	5	7	8	9

$x = 5$

```
while (s <= e) {  
    mid = s + e / 2;
```

```
    if (arr[mid] == x) return true;
```

```
    if (arr[mid] < x) s = mid + 1;
```

```
    else e = mid - 1.
```

firstOcc = ?

lastOcc = ?

0	1	2	3	4	5	6	7	8	9
1	3	5	5	5	5	5	7	8	9
s									e

$$x = 5$$

$$\text{mid} = 0 + 9 / 2 = 4$$

$$\text{firstOcc} = 4$$

```

if (arr[mid] == x) {
    firstOcc = mid;
    e = mid - 1;
}

```

0	1	2	3
1	3	5	5
s			e

$$\text{firstOcc} = 4$$

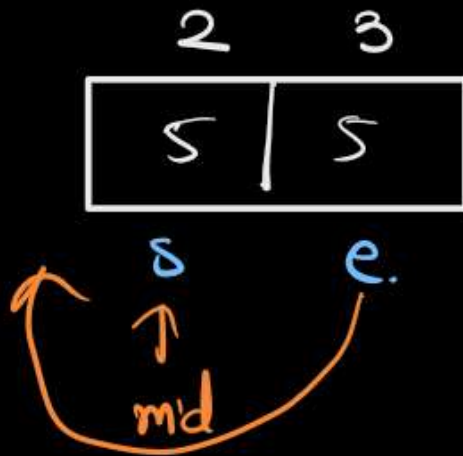
$$x = 5$$

$$\text{mid} = 0 + 3 / 2 = 1.$$

(midEle == x)

<sup>s</sup>                      <sup>s</sup>  
if (midEle < x)  
    s = mid + e

else e = mid - 1



$$\text{mid} = 2 + 3 / 2 = 5 / 2 = 2$$

if (midEle == x) {  
    firstOcc = mid  
    e = mid - 1  
}

firstOcc = 4  
    2



$s = 2, e = 1$

$FOCC = -1$

while( $s \leq e$ ) {

$mid = s + e / 2$ .

    if ( $a[mid] == x$ ) {

$FOCC = mid$

$e = mid - 1$

    }

    else if ( $a[mid] < x$ ) {

$s = mid + 1$ ;

    } else {

$e = mid - 1$ ;

    }



# Last Occurrence

0	1	2	3	4	5	6	7	8	9
1	3	5	5	5	5	5	7	8	9

$s$  (under index 0)  
 $e$  (under index 5)  
 $mid$  (under index 6)

last occ = 4  
~~8~~  
~~6~~

$$mid = 0 + 9 / 2 = 4$$

if (midEle == x)  
   lastOcc = mid  
   s = mid + 1

$$mid = 5 + 9 / 2 = 14 / 2 = 7$$

if (midEle > x) {  
   e = mid + 1  
 }

$$mid = 5 + 6 / 2 = 11 / 2 = 5$$

if (midEle == x)  
   lastOcc = mid  
   s = mid + 1

$$mid = 6 + 6 / 2 = 6$$



LO

while (s < e) {

mid = s + e / 2

if (arr[mid] == x) {

lo = mid

s = mid + 1

}

! { — same as BS

}

```

class GFG {
    int bsFirstOcc(int arr[], int x)
    {
        int start = 0;
        int end = arr.length - 1;
        int firstOcc = -1;
        while(start <= end){
            int mid = (start + end) / 2;
            if(arr[mid] == x){
                firstOcc = mid;
                end = mid - 1;
            }
            else if(arr[mid] < x){
                start = mid + 1;
            }
            else{
                end = mid - 1;
            }
        }
        return firstOcc;
    }
    int bslastOcc(int arr[], int x)
    {
        int start = 0;
        int end = arr.length - 1;
        int lastOcc = -1;
        while(start <= end){
            int mid = (start + end) / 2;
            if(arr[mid] == x){
                lastOcc = mid;
                start = mid + 1;
            }
            else if(arr[mid] < x){
                start = mid + 1;
            }
            else{
                end = mid - 1;
            }
        }
        return lastOcc;
    }
    ArrayList<Integer> find(int arr[], int x) {
        // code here
        int firstOcc = bsFirstOcc(arr, x);
        int lastOcc = bslastOcc(arr, x);
        return new ArrayList<Integer>(Arrays.asList(firstOcc, lastOcc));
    }
}

```