

Quiz 2

Started: Oct 1 at 10:49am

Quiz Instructions

Question 1**2 pts**

Let $A = (a_1, a_2, a_3, \dots, a_9)$ be 9 positive integers. Assume that the longest increasing subsequence of A is $(a_2, a_5, a_7, a_8, a_9)$. Then we have that one of the longest increasing subsequence of its first 7 numbers, i.e., $A' = (a_1, a_2, a_3, a_4, a_5, a_6, a_7)$, is (a_2, a_5, a_7) .

- ☐ True
- ☒ False

Question 2**2 pts**

Let G be a directed graph with n vertices. Let P be the length of the shortest path from vertex s to vertex v with at most n edges. Let Q be the length of the shortest path from vertex s to vertex v with at most $(n+1)$ edges. If we have $P = Q$, then G does not contain negative cycle that can be reached from s .

- ☐ True
- ☒ False

Question 3**2 pts**

Suppose that G does not contain negative cycle. Let (u, v) be an edge of G and $l(u, v)$ be its length. When the Bellman-Ford algorithm terminates (i.e., after $|V| - 1$ iterations), we must have that $\text{dist}(u) + l(u, v) \geq \text{dist}(v)$.

- ☒ True
- ☐ False

Question 4**3 pts**

Let A and B be two strings of length m and n, respectively. Let d be the edit distance between A and B; let d1 be the edit distance between A[1 ... m/2] and B, and let d2 be the edit distance between A[m/2+1 ... m] and B. Then we have

- ☐ $d \geq \min\{d_1, d_2\}$
- ☒ none of the other three is correct.
- ☐ $d \leq \min\{d_1, d_2\}$
- ☐ $d \leq \max\{d_1, d_2\}$

Question 5**3 pts**

For the given instance (vector A and complex number w; shown on screen), FFT(A, w) returns:

- ☐ $(1 - w, 0, w - w^2)$
- ☒ $(0, 1 - w^2, 1 - w)$
- ☐ $(1 - w^2, 0, 1 - w - w^2)$
- ☐ $(0, 1 - w, 1 - w^2)$

Quiz saved at 10:52am

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Question 1. An counter-example is $A = (10, 1, 20, 30, 2, 40, 3, 4, 5)$.

If you think this statement is true, then you did not understand why we define those subproblems in the dynamic programming algorithm (introduced in lecture).

Define $P[k]$ as the subproblem of finding the longest increasing subsequence of $A[1 \dots k]$ such that the last element is $A[k]$ leads to an efficient dynamic problem algorithm (as we did in the lecture).

Define $P[k]$ as the subproblem of finding the longest increasing subsequence of $A[1 \dots k]$ does not lead to such an efficient algorithm, and the above example explains why.

Question 2. If for a single vertex v we have $P = Q$ then it is not sufficient to guarantee that G does not contain negative cycle (that can be reached from s). It suffices if for *every* vertex we have $P = Q$.

Question 3. If G does not contain negative cycle, when Bellman-Ford algorithm terminates, we have $dist(v) = distance(s, v)$ for every $v \in V$. Therefore, we must have $dist(u) + l(u, v) \geq dist(v)$ for every $(u, v) \in E$; otherwise, for v we will have a shorter path: from s to u followed by edge (u, v) .

Alternatively, we have proved that, in the algorithm to identify negative cycles within Bellman-Ford algorithm, after $(|V| - 1)$ iterations, G contain negative cycles if and only if we have $dist(u) + l(u, v) < dist(v)$ for some edge $(u, v) \in E$. Since we are told that G does contain negative cycle, then after $(|V| - 1)$ iterations, we must have $dist(u) + l(u, v) \geq dist(v)$ for every edge $(u, v) \in E$.

Question 4. This problem tests you (quickly) constructing counter-examples:

1. $d \geq \min\{d_1, d_2\}$. False. Let $A = TT, B = TT$.
2. $d \leq \min\{d_1, d_2\}$. False. Let $A = TT, B = T$.
3. $d \leq \max\{d_1, d_2\}$. False. Let $A = TT, B = T$.

Question 5. $FFT(A, w)$ returns $M(w) \cdot A$.