

1)

# A) Wafer area

Wafer-X's wafer area:

$$\text{Radius} = 16/2 = 8 \text{ cm}$$

$$\text{Wafer area} = \pi r^2 = 3.14 \times 8^2 = 200.96 \text{ cm}^2$$

Die area:

$$\text{dies per wafer} = 64$$

$$\text{die area} = \frac{200.96}{64} = 3.14 \text{ cm}^2$$

Wafer-Y's wafer area:

$$\text{Radius} = 20/2 = 10 \text{ cm}$$

$$\text{Wafer Area} = \pi r^2 = 3.14 \times 10^2 = 314 \text{ cm}^2$$

Die Area:

$$\text{dies per Wafer} = 100$$

$$\text{die Area} = \frac{314}{100} = 3.14 \text{ cm}^2$$

$$\begin{aligned} \text{B) Yield} &= \frac{1}{\left(1 + \left(\text{Defects per Area} \times \frac{\text{Die Area}}{2}\right)\right)^2} \\ &= \frac{1}{\left(1 + \left(0.02 \times \frac{3.14}{2}\right)\right)^2} \end{aligned}$$

$$\text{yield} = 0.94$$

$$\begin{aligned} \text{Cost per die} &= \frac{\text{Cost per wafer}}{\text{Dies per wafer} \times \text{Yield}} \\ &= \frac{15}{64 \times 0.94} \\ &= 0.249 \end{aligned}$$

$$\begin{aligned} \text{B) yield} &= \frac{1}{\left(1 + \left(0.03 \times \frac{3.14}{2}\right)\right)^2} \end{aligned}$$

$$\text{yield} = 0.91$$

$$\begin{aligned} \text{Cost per die} &= \frac{24}{100 \times 0.91} \\ &= 0.26 \end{aligned}$$

C) Wafer cost decreases by 20%

We are calculating again for previous year.

$$\text{Wafer X's wafer cost} = 15 \times \frac{5}{4} = 18.75 \quad \text{Wafer Y's wafer cost} = 24 \times \frac{5}{4} = 30$$

Dies per wafer is increased by 10%

$$64 \times \frac{100}{110} = 58.18 = \text{Wafer X's dies per wafer}$$

$$\text{Wafer Y's dies per wafer} = 100 \times \frac{10}{11} = 90.9$$

Defects per area unit increases by 15%

$$0.02 \times \frac{100}{115} = 0.017 = \text{Wafer X's defects}$$

$$\text{Wafer Y's defects} = 0.03 \times \frac{100}{115} = 0.026$$

A)

Wafer X:

$$\text{Wafer Area} = 3.14 \times 8^2 = 200.96 \text{ cm}^2$$

$$\text{Die Area: } \frac{\text{Wafer Area}}{\text{Dies per wafer}} = \frac{200.96}{58.18} = 3.45 \text{ cm}^2$$

$$\text{B) Yield: } \frac{1}{(1 + (0.017 \times \frac{3.45}{2}))^2} = 0.943$$

$$\text{Cost per die: } \frac{18.75}{58.18 \times 0.943} = 0.341$$

in previous year

$$\text{Cost per die this year: } 0.249$$

$$\frac{0.249}{0.341} = 0.73$$

This year cost per die is %27 cheaper than previous year

Wafer Y:

$$\text{Wafer area} = 3.14 \times 10^2 = 314 \text{ cm}^2$$

$$\text{Die Area: } \frac{314}{90.9} = 3.45 \text{ cm}^2$$

$$\text{Yield: } \frac{1}{(1 + (0.026 \times \frac{3.45}{2}))^2} = 0.916$$

$$\text{Cost per die: } \frac{30}{90.9 \times 0.916} = 0.36$$

in previous year

$$\text{Cost per die this year: } 0.26$$

$$\frac{0.26}{0.36} = 0.72$$

This year cost per die is %27.7 cheaper than previous year

2) P1's clock rate = 3 GHz  
 P2's clock rate = 1.5 GHz

1 billion instructions =  $10^9$  instructions, %30 R Type, %50 I Type, %20 J Type

	P <sub>1</sub>	P <sub>2</sub>
%30 R Type	2	3
%50 I Type	4	3
%20 J Type	3	3

A) Find clock cycles

$$P_1 \Rightarrow \left( \frac{30}{100} \times 2 + \frac{50}{100} \times 4 + \frac{20}{100} \times 3 \right) \times 10^9 = \left( \frac{60 + 200 + 60}{100} \right) \times 10^9 = \boxed{3.2 \times 10^9 \text{ clock cycle}}$$

$$P_2 \Rightarrow \left( \frac{30}{100} \times 3 + \frac{50}{100} \times 3 + \frac{20}{100} \times 3 \right) \times 10^9 = \left( \frac{90 + 150 + 60}{100} \right) \times 10^9 = \boxed{3 \times 10^9 \text{ clock cycle}}$$

B) Average clock cycle per instructions:

$$P_1 \Rightarrow \frac{3.2 \times 10^9}{10^9} = 3.2 \text{ clock cycle per instruction}$$

$$P_2 \Rightarrow \frac{3 \times 10^9}{10^9} = 3 \text{ clock cycle per instructions}$$

C) Execution time:

$$P_1 \Rightarrow \text{Execution time} = \frac{\text{clock cycle}}{\text{clock rate}} = \frac{3.2 \times 10^9}{3 \times 10^9} = 1.06 \text{ seconds}$$

$$P_2 = \frac{3 \times 10^9}{1.5 \times 10^9} = 2 \text{ seconds}$$

D)  $\frac{2}{1.06} = 1.88 \Rightarrow P_1 \text{ is } 1.88 \text{ times faster than } P_2$