



# BSM307

## İşaretler ve Sistemler

Dr. Seçkin Arı

Fourier Seri Açılımı

# Fourier Seri Açılımı

- Farklı frekanstaki sinüsoidal işaretlerin toplamı
- Tüm Sürekli Zaman Periyodik İşaretler
  - ♦ Fourier Seri Açılımı ile ifade edilir.
  - ♦ Frekans spektrumu elde edilir.

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    - $t_2 - t_1 = T_0$  (Bir periyot boyunca integral)
    - Sabit
    - İlgili frekans bileşeninin ne kadar etkin olduğunu belirler.



# Fourier Seri Açılımı

- $x(t) = \sum_{k=-\infty}^{\infty} a_k e^{jk\omega_0 t}$   
 $= \dots + a_{-2} e^{-j2\omega_0 t} + a_{-1} e^{-j\omega_0 t} + a_0 + a_1 e^{j\omega_0 t} + a_2 e^{j2\omega_0 t} + \dots$
- $a_{\pm 1}$ : Birinci harmonik bileşenler, temel bileşenler



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- $\vdots$

# Fourier Seri Açılımı

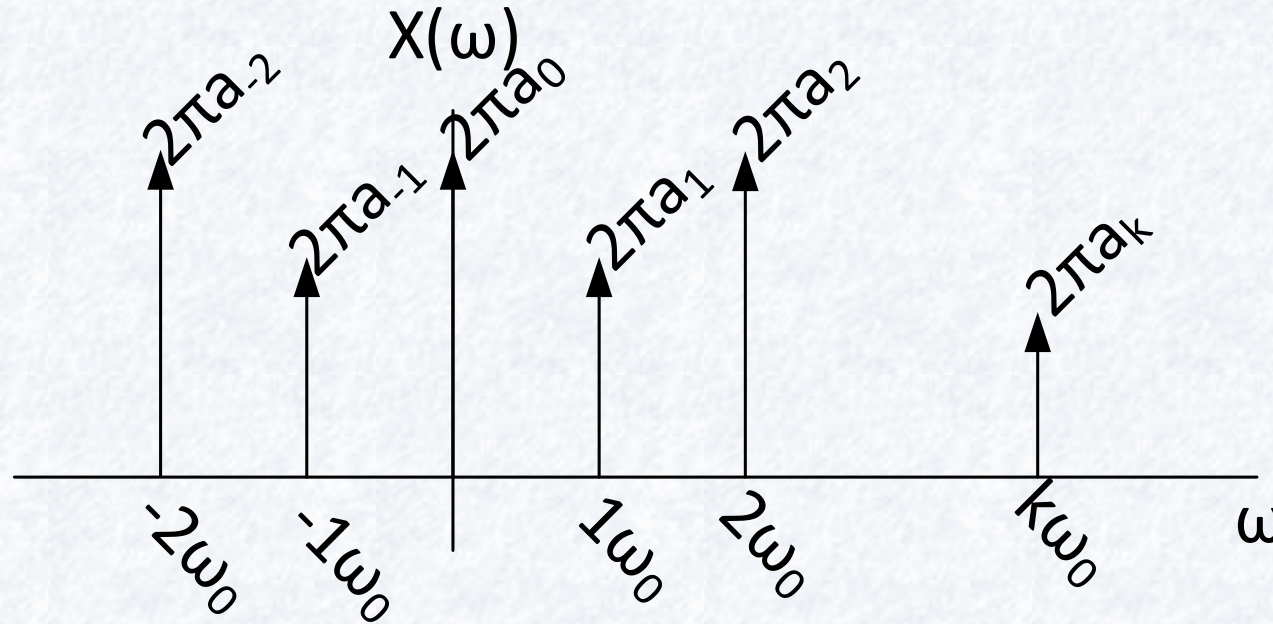
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- $a_{\pm 1}$ : Birinci harmonik bileşenler, temel bileşenler
- $a_{\pm 2}$ : İkinci harmonik bileşenler
- $\vdots$
- $a_0$ : Frekansı olmayan bileşen
  - ♦ DC bileşen

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- $x(t) = \cos(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
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- $x(t) = \cos(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
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- $\forall k \neq \pm 1$  için  $a_k = 0$

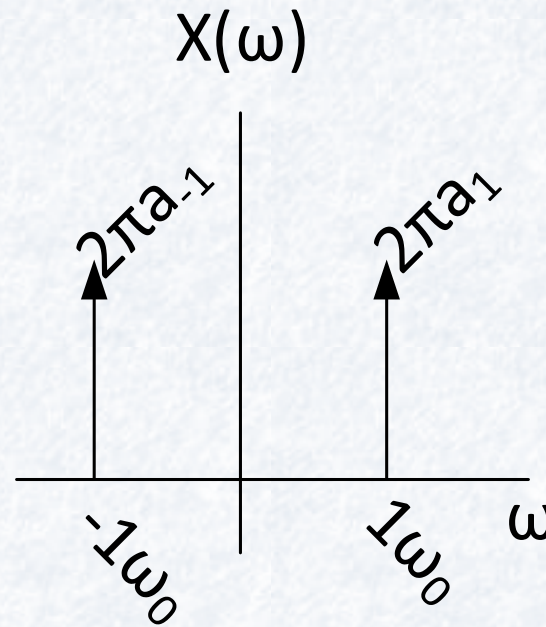


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- Spektrum?

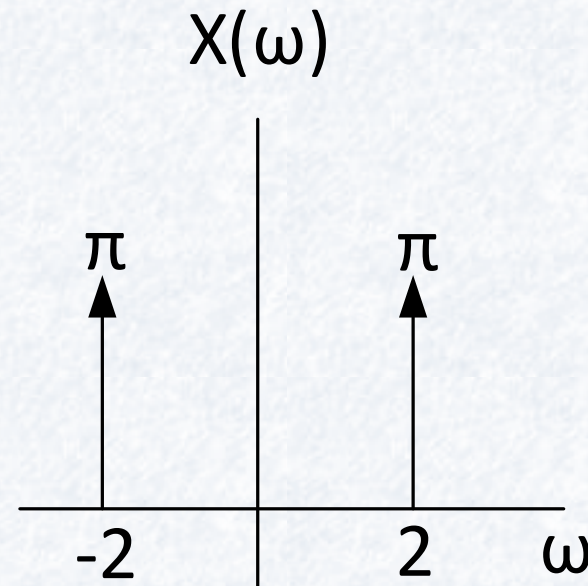
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- $x(t) = \sin(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
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- $x(t) = \sin(2t) = \frac{e^{j2t} - e^{-j2t}}{2j}$

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- $\omega_0 = 2$
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- $a_1 =$

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- $a_1 = \frac{1}{2j}$ ,  $a_{-1} = -\frac{1}{2j}$

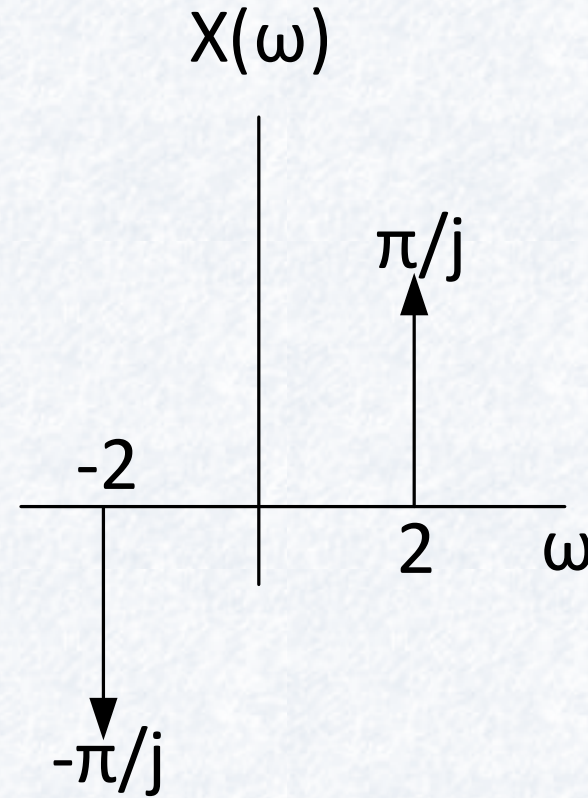
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- $a_1 = \frac{1}{2j}$ ,  $a_{-1} = -\frac{1}{2j}$
- $\forall k \neq \pm 1$  için  $a_k = 0$



## Örnek 3

- $x(t) = \sin\left(2t + \frac{\pi}{4}\right)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
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- $x(t) = \sin\left(2t + \frac{\pi}{4}\right)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $\omega_0 = 2$
- $x(t) = \sin(2t) = \frac{e^{j\left(2t + \frac{\pi}{4}\right)} - e^{-j\left(2t + \frac{\pi}{4}\right)}}{2j} =$

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- $$x(t) = \sin(2t) = \frac{e^{j\left(2t + \frac{\pi}{4}\right)} - e^{-j\left(2t + \frac{\pi}{4}\right)}}{2j} = \frac{e^{j2t} e^{j\frac{\pi}{4}} - e^{-j2t} e^{-j\frac{\pi}{4}}}{2j}$$
$$= \frac{e^{j\frac{\pi}{4}}}{2j} e^{j2t} - \frac{e^{-j\frac{\pi}{4}}}{2j} e^{-j2t}$$
- $a_1 = \frac{e^{j\frac{\pi}{4}}}{2j}$ ,  $a_{-1} =$

## Örnek 3

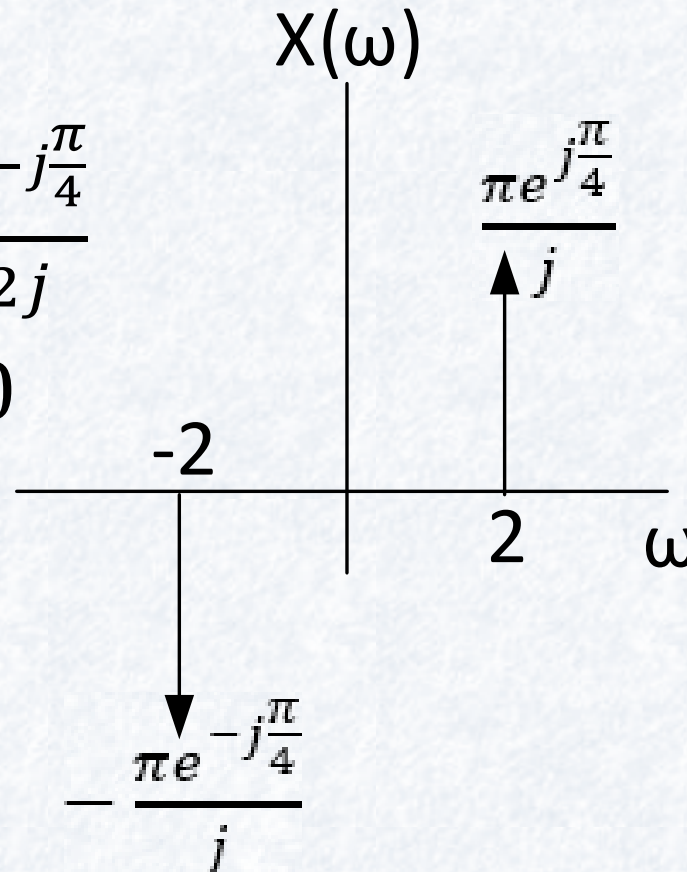
- $x(t) = \sin\left(2t + \frac{\pi}{4}\right)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $\omega_0 = 2$
- $$x(t) = \sin(2t) = \frac{e^{j\left(2t + \frac{\pi}{4}\right)} - e^{-j\left(2t + \frac{\pi}{4}\right)}}{2j} = \frac{e^{j2t} e^{j\frac{\pi}{4}} - e^{-j2t} e^{-j\frac{\pi}{4}}}{2j}$$
$$= \frac{e^{j\frac{\pi}{4}}}{2j} e^{j2t} - \frac{e^{-j\frac{\pi}{4}}}{2j} e^{-j2t}$$
- $a_1 = \frac{e^{j\frac{\pi}{4}}}{2j}$ ,  $a_{-1} = -\frac{e^{-j\frac{\pi}{4}}}{2j}$
- $\forall k \neq \pm 1$  için  $a_k = 0$

## Örnek 3

- $x(t) = \sin\left(2t + \frac{\pi}{4}\right)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $\omega_0 = 2$
- $a_1 = \frac{e^{j\frac{\pi}{4}}}{2j}$ ,  $a_{-1} = -\frac{e^{-j\frac{\pi}{4}}}{2j}$
- $\forall k \neq \pm 1$  için  $a_k = 0$
- Spektrum?

# Örnek 3

- $x(t) = \sin\left(2t + \frac{\pi}{4}\right)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $\omega_0 = 2$
- $a_1 = \frac{e^{j\frac{\pi}{4}}}{2j}$ ,  $a_{-1} = -\frac{e^{-j\frac{\pi}{4}}}{2j}$
- $\forall k \neq \pm 1$  için  $a_k = 0$



## Örnek 4

- $x(t) = \cos(4t) + \sin(6t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$



## Örnek 4

- $x(t) = \cos(4t) + \sin(6t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $k\omega_0 = 4t$
- $l\omega_0 = 6t$

## Örnek 4

- $x(t) = \cos(4t) + \sin(6t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $k\omega_0 = 4t$
- $l\omega_0 = 6t$ 
  - ♦ EBOB,  $\omega_0 = 2$
- $x(t) =$

## Örnek 4

- $x(t) = \cos(4t) + \sin(6t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$

- $k\omega_0 = 4t$

- $l\omega_0 = 6t$

- ♦ EBOB,  $\omega_0 = 2$

- $$x(t) = \frac{e^{j4t} + e^{-j4t}}{2} + \frac{e^{j6t} - e^{-j6t}}{2j} = \frac{1}{2}e^{j4t} + \frac{1}{2}e^{-j4t} + \frac{1}{2j}e^{j6t} - \frac{1}{2j}e^{-j6t}$$

- $a_2 =$

## Örnek 4

- $x(t) = \cos(4t) + \sin(6t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$

- $k\omega_0 = 4t$

- $l\omega_0 = 6t$

- ♦ EBOB,  $\omega_0 = 2$

- $$x(t) = \frac{e^{j4t} + e^{-j4t}}{2} + \frac{e^{j6t} - e^{-j6t}}{2j} = \frac{1}{2}e^{j4t} + \frac{1}{2}e^{-j4t} + \frac{1}{2j}e^{j6t} - \frac{1}{2j}e^{-j6t}$$

- $a_2 = \frac{1}{2}, a_{-2} =$

# Örnek 4

- $x(t) = \cos(4t) + \sin(6t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $k\omega_0 = 4t$
- $l\omega_0 = 6t$ 
  - ♦ EBOB,  $\omega_0 = 2$
- $$x(t) = \frac{e^{j4t} + e^{-j4t}}{2} + \frac{e^{j6t} - e^{-j6t}}{2j} = \frac{1}{2}e^{j4t} + \frac{1}{2}e^{-j4t} + \frac{1}{2j}e^{j6t} - \frac{1}{2j}e^{-j6t}$$
- $a_2 = \frac{1}{2}, a_{-2} = \frac{1}{2}$
- $a_3 =$

# Örnek 4

- $x(t) = \cos(4t) + \sin(6t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $k\omega_0 = 4t$
- $l\omega_0 = 6t$ 
  - ♦ EBOB,  $\omega_0 = 2$
- $$x(t) = \frac{e^{j4t} + e^{-j4t}}{2} + \frac{e^{j6t} - e^{-j6t}}{2j} = \frac{1}{2}e^{j4t} + \frac{1}{2}e^{-j4t} + \frac{1}{2j}e^{j6t} - \frac{1}{2j}e^{-j6t}$$
- $a_2 = \frac{1}{2}, a_{-2} = \frac{1}{2}$
- $a_3 = \frac{1}{2j}, a_{-3} =$



# Örnek 4

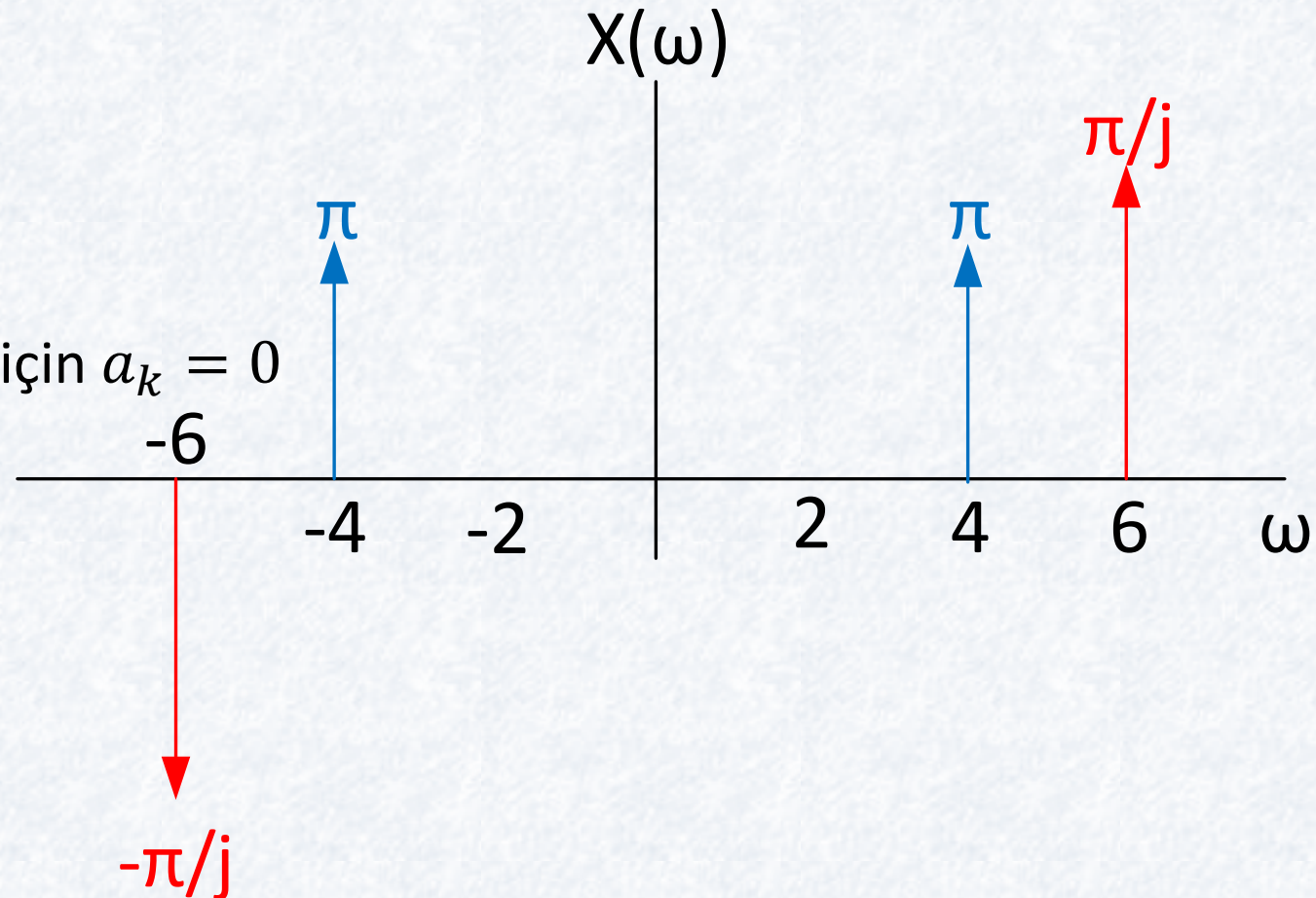
- $x(t) = \cos(4t) + \sin(6t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $k\omega_0 = 4t$
- $l\omega_0 = 6t$ 
  - ♦ EBOB,  $\omega_0 = 2$
- $$x(t) = \frac{e^{j4t} + e^{-j4t}}{2} + \frac{e^{j6t} - e^{-j6t}}{2j} = \frac{1}{2}e^{j4t} + \frac{1}{2}e^{-j4t} + \frac{1}{2j}e^{j6t} - \frac{1}{2j}e^{-j6t}$$
- $a_2 = \frac{1}{2}, a_{-2} = \frac{1}{2}$
- $a_3 = \frac{1}{2j}, a_{-3} = -\frac{1}{2j}$
- $\forall k \neq \pm 2$  ve  $\forall k \neq \pm 3$  için  $a_k = 0$

## Örnek 4

- $x(t) = \cos(4t) + \sin(6t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $\omega_0 = 2$
- $a_2 = \frac{1}{2}$ ,  $a_{-2} = \frac{1}{2}$
- $a_3 = \frac{1}{2j}$ ,  $a_{-3} = -\frac{1}{2j}$
- $\forall k \neq \pm 2$  ve  $\forall k \neq \pm 3$  için  $a_k = 0$
- Spektrum?

# Örnek 4

- $x(t) = \cos(4t) + \sin(6t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $\omega_0 = 2$
- $a_2 = \frac{1}{2}$ ,  $a_{-2} = \frac{1}{2}$
- $a_3 = \frac{1}{2j}$ ,  $a_{-3} = -\frac{1}{2j}$
- $\forall k \neq \pm 2$  ve  $\forall k \neq \pm 3$  için  $a_k = 0$
- $\cos(4t) + \sin(6t)$



## Örnek 5

- $x(t) = \sin^2(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $x(t) =$

## Örnek 5

- $x(t) = \sin^2(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$

- $x(t) = \left( \frac{e^{j2t} - e^{-j2t}}{2j} \right)^2 =$

## Örnek 5

- $x(t) = \sin^2(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $x(t) = \left( \frac{e^{j2t} - e^{-j2t}}{2j} \right)^2 = \frac{e^{j4t} - 2 + e^{-j4t}}{-4} =$



## Örnek 5

- $x(t) = \sin^2(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $$x(t) = \left( \frac{e^{j2t} - e^{-j2t}}{2j} \right)^2 = \frac{e^{j4t} - 2 + e^{-j4t}}{-4} = -\frac{1}{4}e^{j4t} + \frac{1}{2} - \frac{1}{4}e^{-j4t}$$
- $\omega_0 =$

## Örnek 5

- $x(t) = \sin^2(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $$x(t) = \left( \frac{e^{j2t} - e^{-j2t}}{2j} \right)^2 = \frac{e^{j4t} - 2 + e^{-j4t}}{-4} = -\frac{1}{4}e^{j4t} + \frac{1}{2} - \frac{1}{4}e^{-j4t}$$
- $\omega_0 = 4$
- $a_1 =$

## Örnek 5

- $x(t) = \sin^2(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $$x(t) = \left( \frac{e^{j2t} - e^{-j2t}}{2j} \right)^2 = \frac{e^{j4t} - 2 + e^{-j4t}}{-4} = -\frac{1}{4}e^{j4t} + \frac{1}{2} - \frac{1}{4}e^{-j4t}$$
- $\omega_0 = 4$
- $a_1 = -\frac{1}{4}$ ,  $a_{-1} =$

## Örnek 5

- $x(t) = \sin^2(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $$x(t) = \left( \frac{e^{j2t} - e^{-j2t}}{2j} \right)^2 = \frac{e^{j4t} - 2 + e^{-j4t}}{-4} = -\frac{1}{4}e^{j4t} + \frac{1}{2} - \frac{1}{4}e^{-j4t}$$
- $\omega_0 = 4$
- $a_1 = -\frac{1}{4}$ ,  $a_{-1} = -\frac{1}{4}$
- $a_0 =$

## Örnek 5

- $x(t) = \sin^2(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $$x(t) = \left( \frac{e^{j2t} - e^{-j2t}}{2j} \right)^2 = \frac{e^{j4t} - 2 + e^{-j4t}}{-4} = -\frac{1}{4}e^{j4t} + \frac{1}{2} - \frac{1}{4}e^{-j4t}$$
- $\omega_0 = 4$
- $a_1 = -\frac{1}{4}$ ,  $a_{-1} = -\frac{1}{4}$
- $a_0 = \frac{1}{2}$
- $\forall k \neq \pm 1$  ve  $\forall k \neq 0$  için  $a_k = 0$

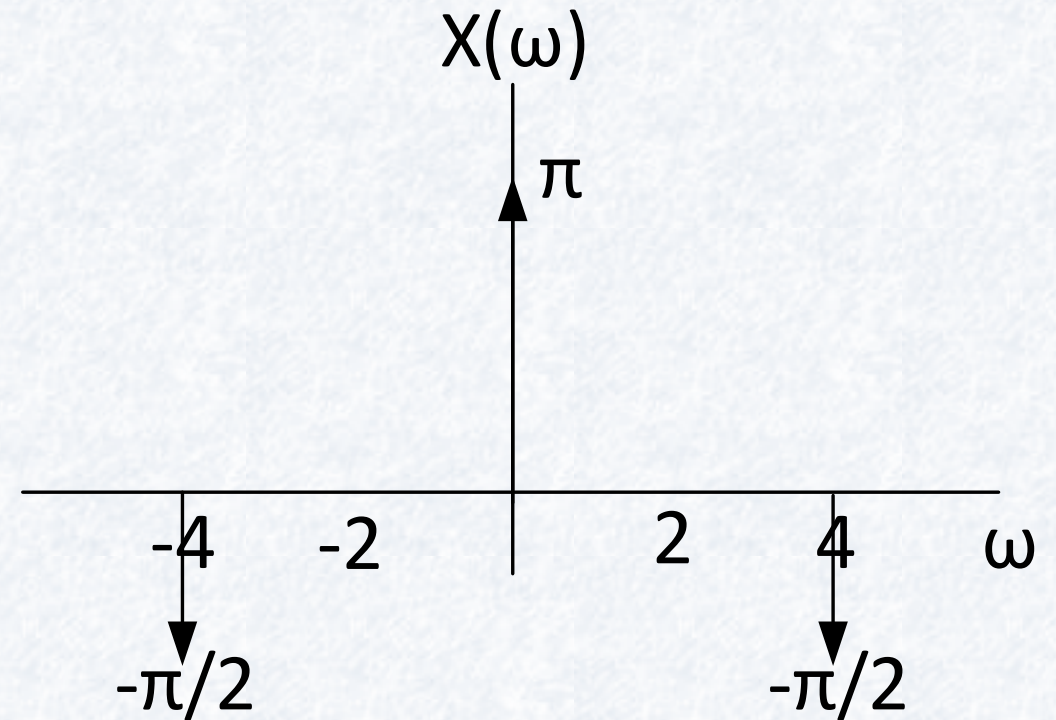
## Örnek 5

- $x(t) = \sin^2(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $\omega_0 = 4$
- $a_1 = -\frac{1}{4}$ ,  $a_{-1} = -\frac{1}{4}$
- $a_0 = \frac{1}{2}$
- $\forall k \neq \pm 1$  ve  $\forall k \neq 0$  için  $a_k = 0$
- Spektrum?



# Örnek 5

- $x(t) = \sin^2(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$
- $\omega_0 = 4$
- $a_1 = -\frac{1}{4}$ ,  $a_{-1} = -\frac{1}{4}$
- $a_0 = \frac{1}{2}$
- $\forall k \neq \pm 1$  ve  $\forall k \neq 0$  için  $a_k = 0$
- $x(t) =$



## Örnek 5

- $x(t) = \sin^2(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$

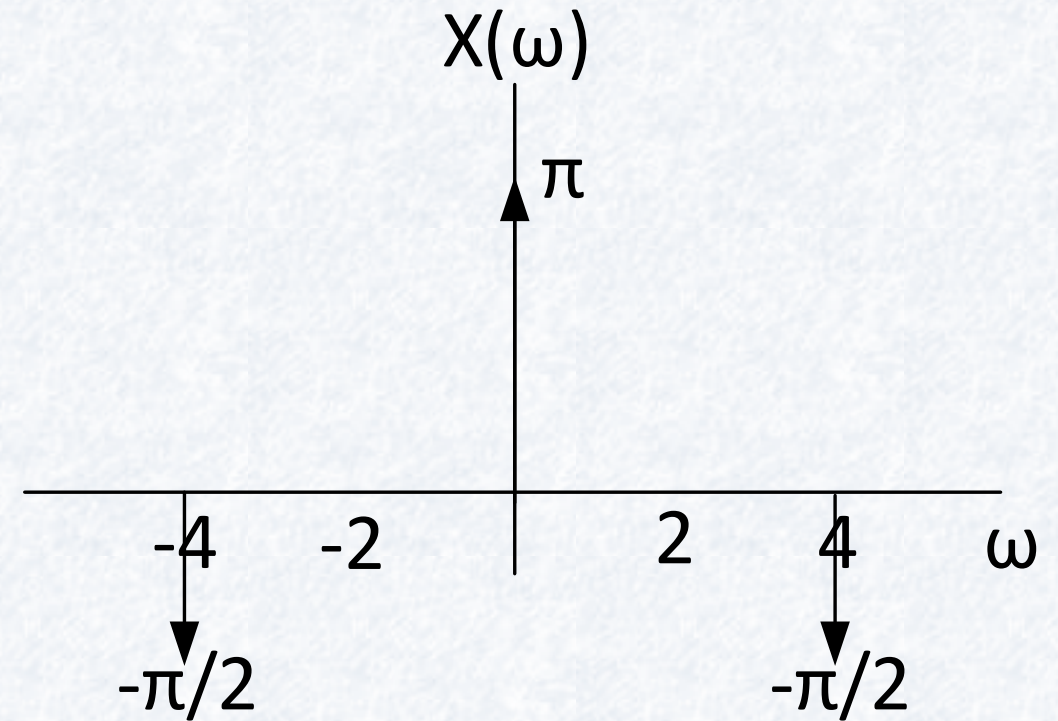
- $\omega_0 = 4$

- $a_1 = -\frac{1}{4}$ ,  $a_{-1} = -\frac{1}{4}$

- $a_0 = \frac{1}{2}$

- $\forall k \neq \pm 1$  ve  $\forall k \neq 0$  için  $a_k = 0$

- $x(t) = \frac{1}{2} +$



## Örnek 5

- $x(t) = \sin^2(2t)$  ise  $\omega_0 = ?$ ,  $a_k = ?$

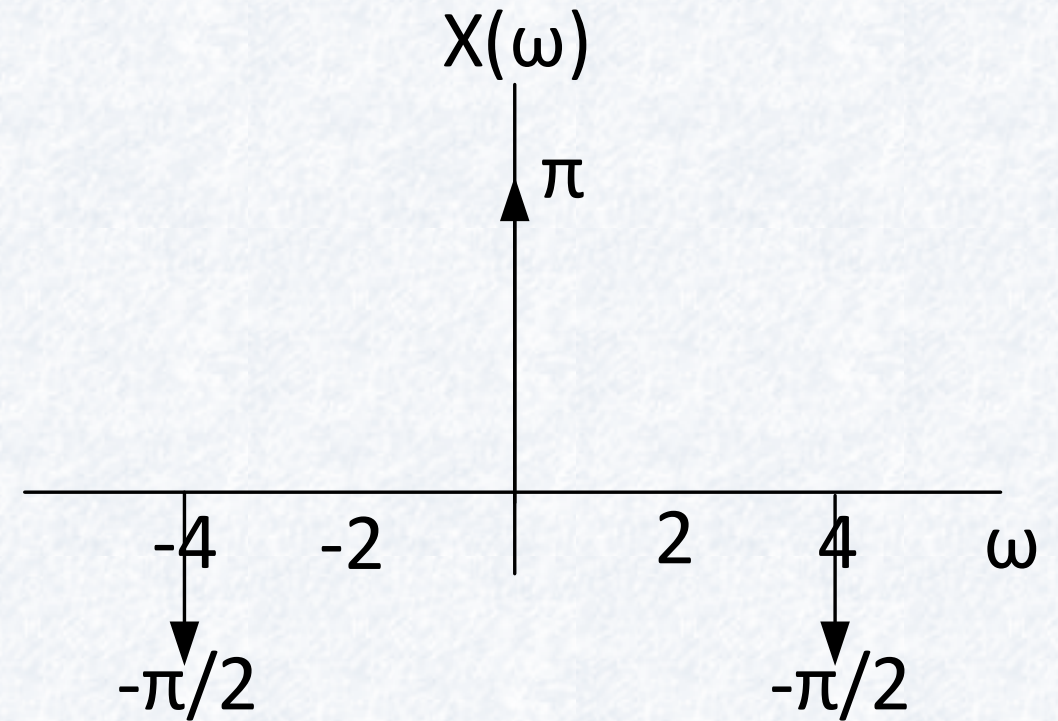
- $\omega_0 = 4$

- $a_1 = -\frac{1}{4}$ ,  $a_{-1} = -\frac{1}{4}$

- $a_0 = \frac{1}{2}$

- $\forall k \neq \pm 1$  ve  $\forall k \neq 0$  için  $a_k = 0$

- $x(t) = \frac{1}{2} - \frac{1}{2} \cos(4t)$



## Örnek 6

- $\omega_0 = 2\pi$
- $a_0 = 1, a_{\pm 1} = \frac{1}{4}, a_{\pm 2} = \frac{1}{3}, a_{\pm 4} = \frac{1}{2}$  ise  $x(t) = ?$

## Örnek 6

- $\omega_0 = 2\pi$
- $a_0 = 1, a_{\pm 1} = \frac{1}{4}, a_{\pm 2} = \frac{1}{3}, a_{\pm 4} = \frac{1}{2}$  ise  $x(t) = ?$
- $x(t) = \sum_{k=-4}^4 a_k e^{jk\omega_0 t}$

## Örnek 6

- $\omega_0 = 2\pi$
- $a_0 = 1, a_{\pm 1} = \frac{1}{4}, a_{\pm 2} = \frac{1}{3}, a_{\pm 4} = \frac{1}{2}$  ise  $x(t) = ?$
- $x(t) = \sum_{k=-4}^4 a_k e^{jk\omega_0 t}$   
 $= a_{-4}e^{-j8\pi t} + a_{-3}e^{-j6\pi t} + a_{-2}e^{-j4\pi t} + a_{-1}e^{-j2\pi t} + a_0$   
 $+ a_4e^{j8\pi t} + a_3e^{j6\pi t} + a_2e^{j4\pi t} + a_1e^{j2\pi t}$



## Örnek 6

- $\omega_0 = 2\pi$
- $a_0 = 1, a_{\pm 1} = \frac{1}{4}, a_{\pm 2} = \frac{1}{3}, a_{\pm 4} = \frac{1}{2}$  ise  $x(t) = ?$
- $x(t) = \sum_{k=-4}^4 a_k e^{jk\omega_0 t}$   
 $= a_{-4}e^{-j8\pi t} + a_{-3}e^{-j6\pi t} + a_{-2}e^{-j4\pi t} + a_{-1}e^{-j2\pi t} + a_0$   
 $+ a_4e^{j8\pi t} + a_3e^{j6\pi t} + a_2e^{j4\pi t} + a_1e^{j2\pi t}$   
 $= \frac{1}{2}e^{-j8\pi t} + 0e^{-j6\pi t} + \frac{1}{3}e^{-j4\pi t} + \frac{1}{4}e^{-j2\pi t} + 1$   
 $+ \frac{1}{2}e^{j8\pi t} + 0e^{j6\pi t} + \frac{1}{3}e^{j4\pi t} + \frac{1}{4}e^{j2\pi t}$

## Örnek 6

- $\omega_0 = 2\pi$
- $a_0 = 1, a_{\pm 1} = \frac{1}{4}, a_{\pm 2} = \frac{1}{3}, a_{\pm 4} = \frac{1}{2}$  ise  $x(t) = ?$
- $x(t) = \frac{1}{2}e^{-j8\pi t} + 0e^{-j6\pi t} + \frac{1}{3}e^{-j4\pi t} + \frac{1}{4}e^{-j2\pi t} + 1 + \frac{1}{2}e^{j8\pi t} + 0e^{j6\pi t} + \frac{1}{3}e^{j4\pi t} + \frac{1}{4}e^{j2\pi t}$
- $x(t) = 1 +$

## Örnek 6

- $\omega_0 = 2\pi$
- $a_0 = 1, a_{\pm 1} = \frac{1}{4}, a_{\pm 2} = \frac{1}{3}, a_{\pm 4} = \frac{1}{2}$  ise  $x(t) = ?$
- $$x(t) = \frac{1}{2}e^{-j8\pi t} + 0e^{-j6\pi t} + \frac{1}{3}e^{-j4\pi t} + \frac{1}{4}e^{-j2\pi t} + 1 + \frac{1}{2}e^{j8\pi t} + 0e^{j6\pi t} + \frac{1}{3}e^{j4\pi t} + \frac{1}{4}e^{j2\pi t}$$
- $$x(t) = 1 + \frac{1}{2}\cos(2\pi t)$$

## Örnek 6

- $\omega_0 = 2\pi$
- $a_0 = 1, a_{\pm 1} = \frac{1}{2}, a_{\pm 2} = \frac{1}{3}, a_{\pm 4} = \frac{1}{2}$  ise  $x(t) = ?$
- $x(t) = \frac{1}{2}e^{-j8\pi t} + 0e^{-j6\pi t} + \frac{1}{3}e^{-j4\pi t} + \frac{1}{4}e^{-j2\pi t} + 1 + \frac{1}{2}e^{j8\pi t} + 0e^{j6\pi t} + \frac{1}{3}e^{j4\pi t} + \frac{1}{4}e^{j2\pi t}$
- $x(t) = 1 + \frac{1}{2}\cos(2\pi t) + \frac{2}{3}\cos(4\pi t)$

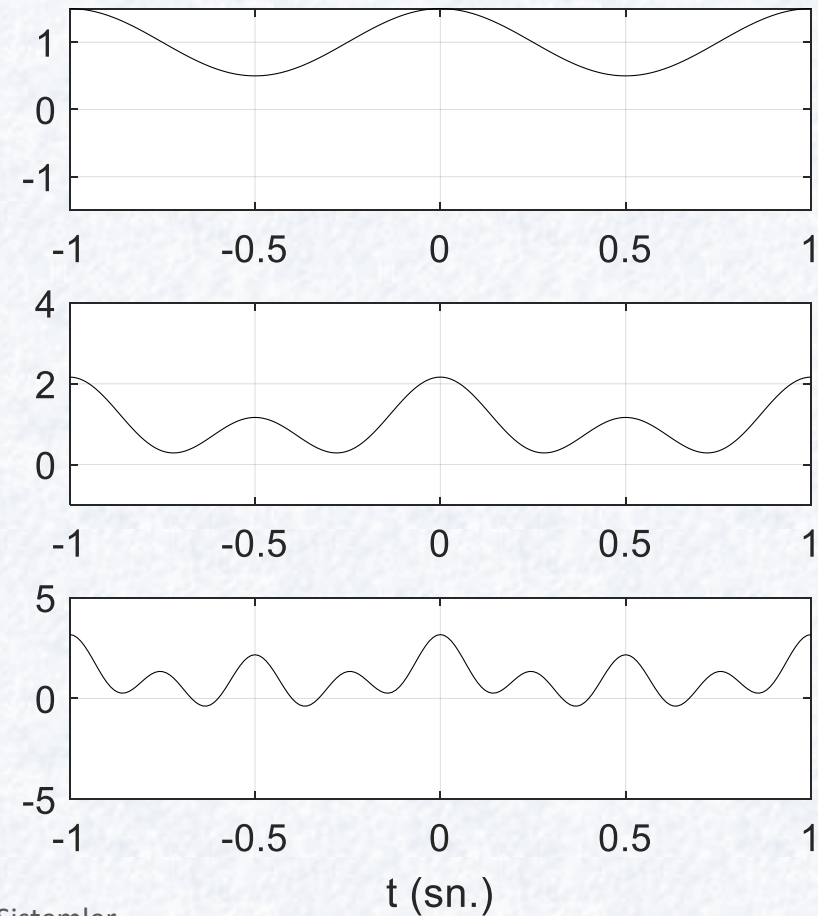
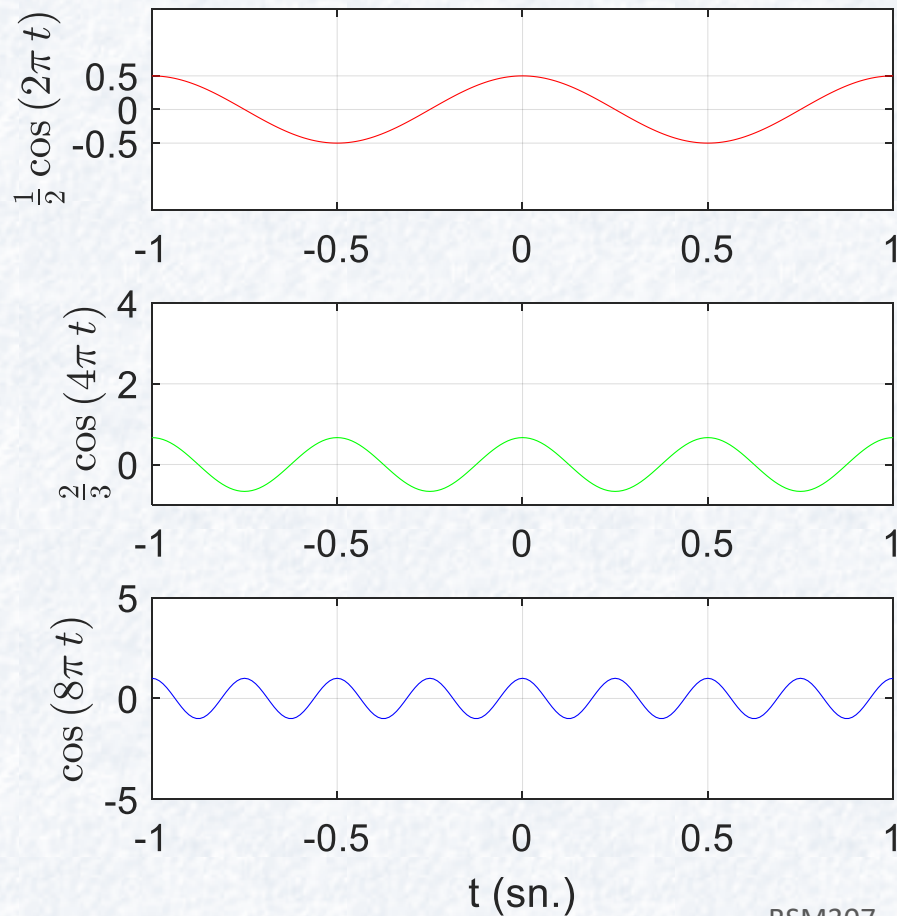
## Örnek 6

- $\omega_0 = 2\pi$
- $a_0 = 1, a_{\pm 1} = \frac{1}{2}, a_{\pm 2} = \frac{1}{3}, a_{\pm 4} = \frac{1}{2}$  ise  $x(t) = ?$
- $x(t) = \frac{1}{2}e^{-j8\pi t} + 0e^{-j6\pi t} + \frac{1}{3}e^{-j4\pi t} + \frac{1}{4}e^{-j2\pi t} + 1 + \frac{1}{2}e^{j8\pi t} + 0e^{j6\pi t} + \frac{1}{3}e^{j4\pi t} + \frac{1}{4}e^{j2\pi t}$
- $x(t) = 1 + \frac{1}{2}\cos(2\pi t) + \frac{2}{3}\cos(4\pi t) + \cos(8\pi t)$



# Örnek 6

- $x(t) = 1 + \frac{1}{2} \cos(2\pi t) + \frac{2}{3} \cos(4\pi t) + \cos(8\pi t)$





## Örnek 7

- $x(t) = 1 + \sin(\omega_0 t) + 2 \cos(2\omega_0 t) + \cos\left(\omega_0 t + \frac{\pi}{4}\right)$  Fourier Seri Açılımı?

## Örnek 7

- $x(t) = 1 + \sin(\omega_0 t) + 2 \cos(2\omega_0 t) - \cos\left(\omega_0 t + \frac{\pi}{4}\right)$
- $x(t) =$

## Örnek 7

- $x(t) = 1 + \sin(\omega_0 t) + 2 \cos(2\omega_0 t) - \cos\left(\omega_0 t + \frac{\pi}{4}\right)$
- $x(t) = 1 + \frac{e^{j\omega_0 t} - e^{-j\omega_0 t}}{2j} + e^{j2\omega_0 t} + e^{-j2\omega_0 t} - \frac{e^{j\omega_0 t} e^{j\frac{\pi}{4}} + e^{-j\omega_0 t} e^{-j\frac{\pi}{4}}}{2} =$

## Örnek 7

- $x(t) = 1 + \sin(\omega_0 t) + 2 \cos(2\omega_0 t) - \cos\left(\omega_0 t + \frac{\pi}{4}\right)$
- $$x(t) = 1 + \frac{e^{j\omega_0 t} - e^{-j\omega_0 t}}{2j} + e^{j2\omega_0 t} + e^{-j2\omega_0 t} - \frac{e^{j\omega_0 t} e^{j\frac{\pi}{4}} + e^{-j\omega_0 t} e^{-j\frac{\pi}{4}}}{2}$$
$$= 1 + \left(\frac{1}{2j} - \frac{e^{j\frac{\pi}{4}}}{2}\right) e^{j\omega_0 t} - \left(\frac{1}{2j} + \frac{e^{-j\frac{\pi}{4}}}{2}\right) e^{-j\omega_0 t} + e^{j2\omega_0 t} + e^{-j2\omega_0 t}$$
- $a_0 =$

## Örnek 7

- $x(t) = 1 + \sin(\omega_0 t) + 2 \cos(2\omega_0 t) - \cos\left(\omega_0 t + \frac{\pi}{4}\right)$
- $$x(t) = 1 + \frac{e^{j\omega_0 t} - e^{-j\omega_0 t}}{2j} + e^{j2\omega_0 t} + e^{-j2\omega_0 t} - \frac{e^{j\omega_0 t} e^{j\frac{\pi}{4}} + e^{-j\omega_0 t} e^{-j\frac{\pi}{4}}}{2}$$
$$= 1 + \left(\frac{1}{2j} - \frac{e^{j\frac{\pi}{4}}}{2}\right) e^{j\omega_0 t} - \left(\frac{1}{2j} + \frac{e^{-j\frac{\pi}{4}}}{2}\right) e^{-j\omega_0 t} + e^{j2\omega_0 t} + e^{-j2\omega_0 t}$$
- $a_0 = 1$
- $a_1 =$

# Örnek 7

- $x(t) = 1 + \sin(\omega_0 t) + 2 \cos(2\omega_0 t) - \cos\left(\omega_0 t + \frac{\pi}{4}\right)$
- $$x(t) = 1 + \frac{e^{j\omega_0 t} - e^{-j\omega_0 t}}{2j} + e^{j2\omega_0 t} + e^{-j2\omega_0 t} - \frac{e^{j\omega_0 t} e^{j\frac{\pi}{4}} + e^{-j\omega_0 t} e^{-j\frac{\pi}{4}}}{2}$$
$$= 1 + \left(\frac{1}{2j} - \frac{e^{j\frac{\pi}{4}}}{2}\right) e^{j\omega_0 t} - \left(\frac{1}{2j} + \frac{e^{-j\frac{\pi}{4}}}{2}\right) e^{-j\omega_0 t} + e^{j2\omega_0 t} + e^{-j2\omega_0 t}$$
- $a_0 = 1$
- $a_1 = \frac{1}{2j} - \frac{e^{j\frac{\pi}{4}}}{2} = 0,9239 e^{-j112,5^\circ}$
- $a_{-1} =$



# Örnek 7

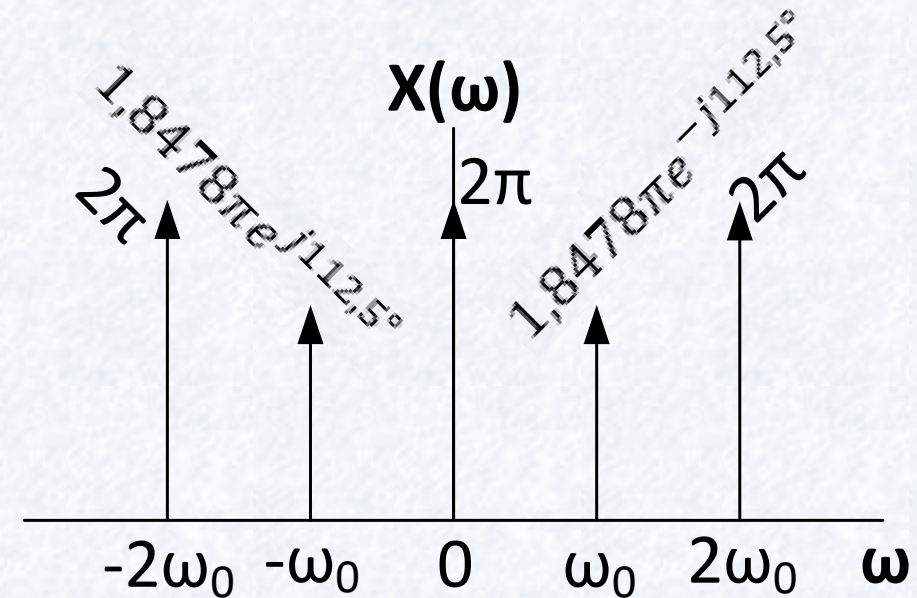
- $x(t) = 1 + \sin(\omega_0 t) + 2 \cos(2\omega_0 t) - \cos\left(\omega_0 t + \frac{\pi}{4}\right)$
- $x(t) = 1 + \frac{e^{j\omega_0 t} - e^{-j\omega_0 t}}{2j} + e^{j2\omega_0 t} + e^{-j2\omega_0 t} - \frac{e^{j\omega_0 t} e^{j\frac{\pi}{4}} + e^{-j\omega_0 t} e^{-j\frac{\pi}{4}}}{2} = 1 + \left(\frac{1}{2j} - \frac{e^{j\frac{\pi}{4}}}{2}\right) e^{j\omega_0 t} - \left(\frac{1}{2j} + \frac{e^{-j\frac{\pi}{4}}}{2}\right) e^{-j\omega_0 t} + e^{j2\omega_0 t} + e^{-j2\omega_0 t}$
- $a_0 = 1$
- $a_1 = \frac{1}{2j} - \frac{e^{j\frac{\pi}{4}}}{2} = 0,9239e^{-j112,5^\circ}$
- $a_{-1} = -\frac{1}{2j} - \frac{e^{-j\frac{\pi}{4}}}{2} = 0,9239e^{j112,5^\circ}$
- $a_2 = a_{-2} =$

# Örnek 7

- $x(t) = 1 + \sin(\omega_0 t) + 2 \cos(2\omega_0 t) - \cos\left(\omega_0 t + \frac{\pi}{4}\right)$
- $$x(t) = 1 + \frac{e^{j\omega_0 t} - e^{-j\omega_0 t}}{2j} + e^{j2\omega_0 t} + e^{-j2\omega_0 t} - \frac{e^{j\omega_0 t} e^{j\frac{\pi}{4}} + e^{-j\omega_0 t} e^{-j\frac{\pi}{4}}}{2} = 1 + \left(\frac{1}{2j} - \frac{e^{j\frac{\pi}{4}}}{2}\right) e^{j\omega_0 t} - \left(\frac{1}{2j} + \frac{e^{-j\frac{\pi}{4}}}{2}\right) e^{-j\omega_0 t} + e^{j2\omega_0 t} + e^{-j2\omega_0 t}$$
- $a_0 = 1$
- $a_1 = \frac{1}{2j} - \frac{e^{j\frac{\pi}{4}}}{2} = 0,9239e^{-j112,5^\circ}$
- $a_{-1} = -\frac{1}{2j} - \frac{e^{-j\frac{\pi}{4}}}{2} = 0,9239e^{j112,5^\circ}$
- $a_2 = a_{-2} = 1$

# Örnek 7

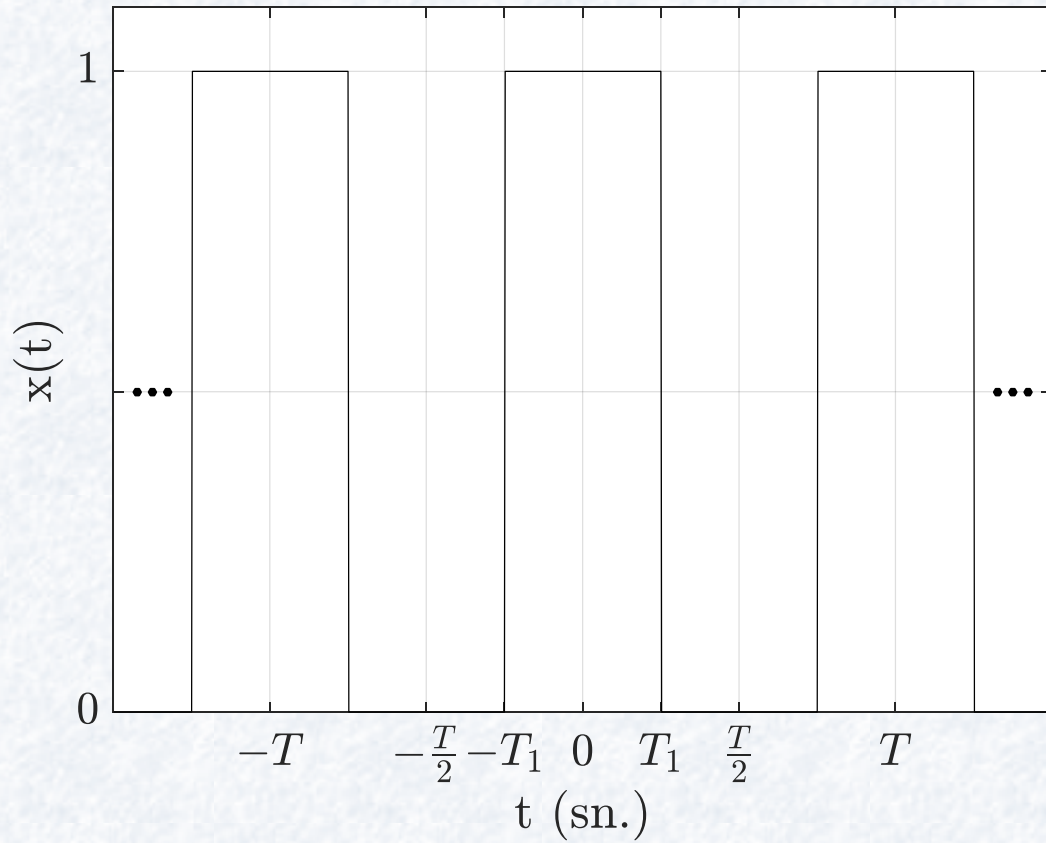
- $x(t) = 1 + \sin(\omega_0 t) + 2 \cos(2\omega_0 t) - \cos\left(\omega_0 t + \frac{\pi}{4}\right)$
- $a_0 = 1$
- $a_1 = \frac{1}{2j} - \frac{e^{j\frac{\pi}{4}}}{2} = 0,9239e^{-j112,5^\circ}$
- $a_{-1} = -\frac{1}{2j} - \frac{e^{-j\frac{\pi}{4}}}{2} = 0,9239e^{j112,5^\circ}$
- $a_2 = a_{-2} = 1$



# Örnek 8

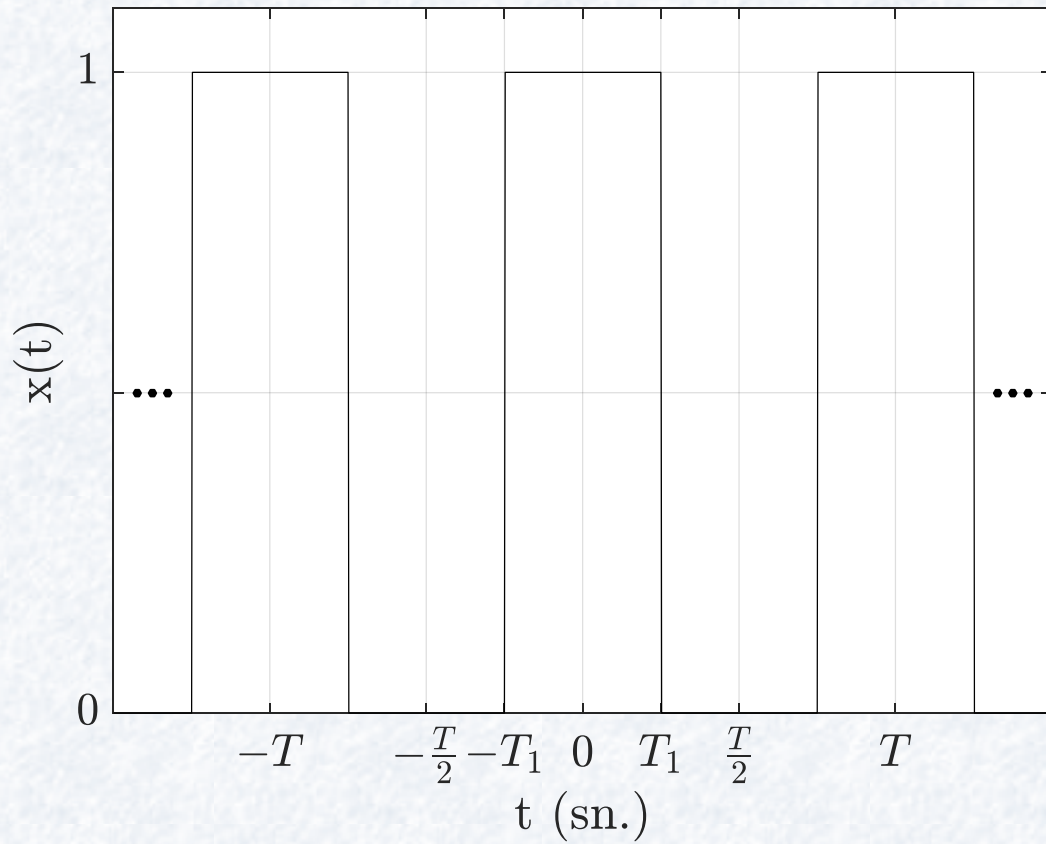
- Fourier seri açılımı?

- $\omega_0 =$



# Örnek 8

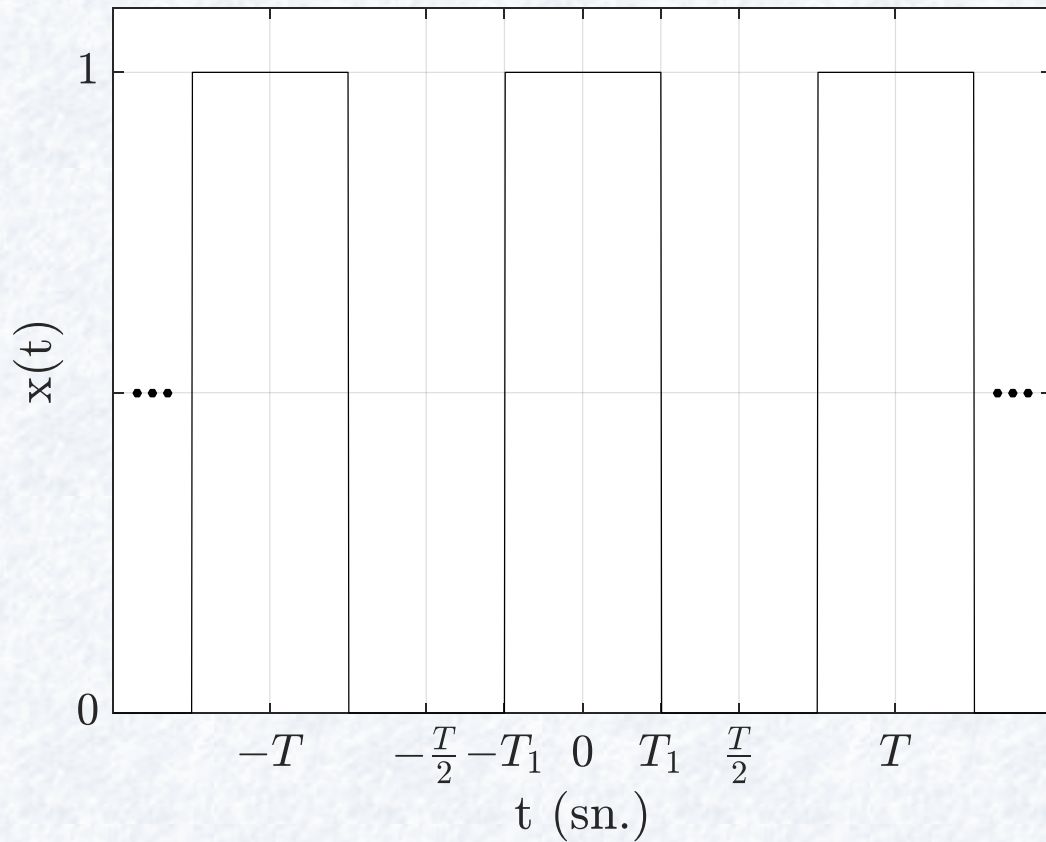
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$

# Örnek 8

- Fourier seri açılımı?

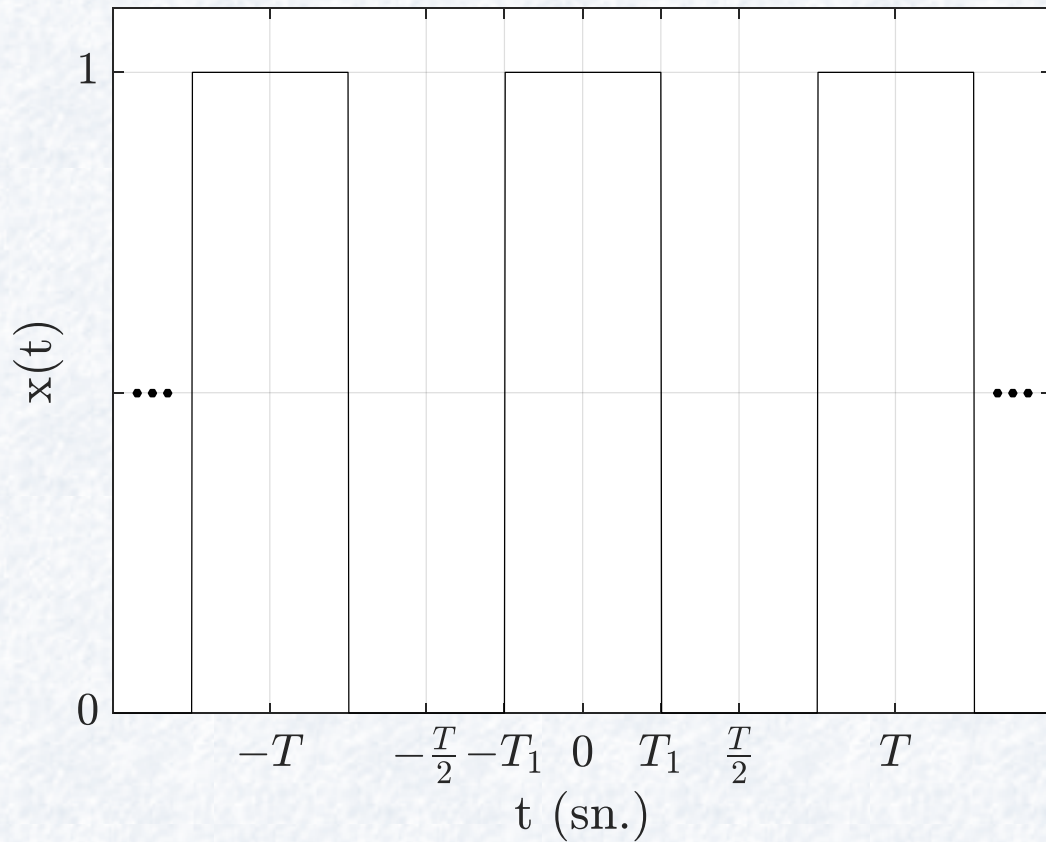


- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T_0} \int_{t_1}^{t_2} x(t) e^{-jk\omega_0 t} dt$



# Örnek 8

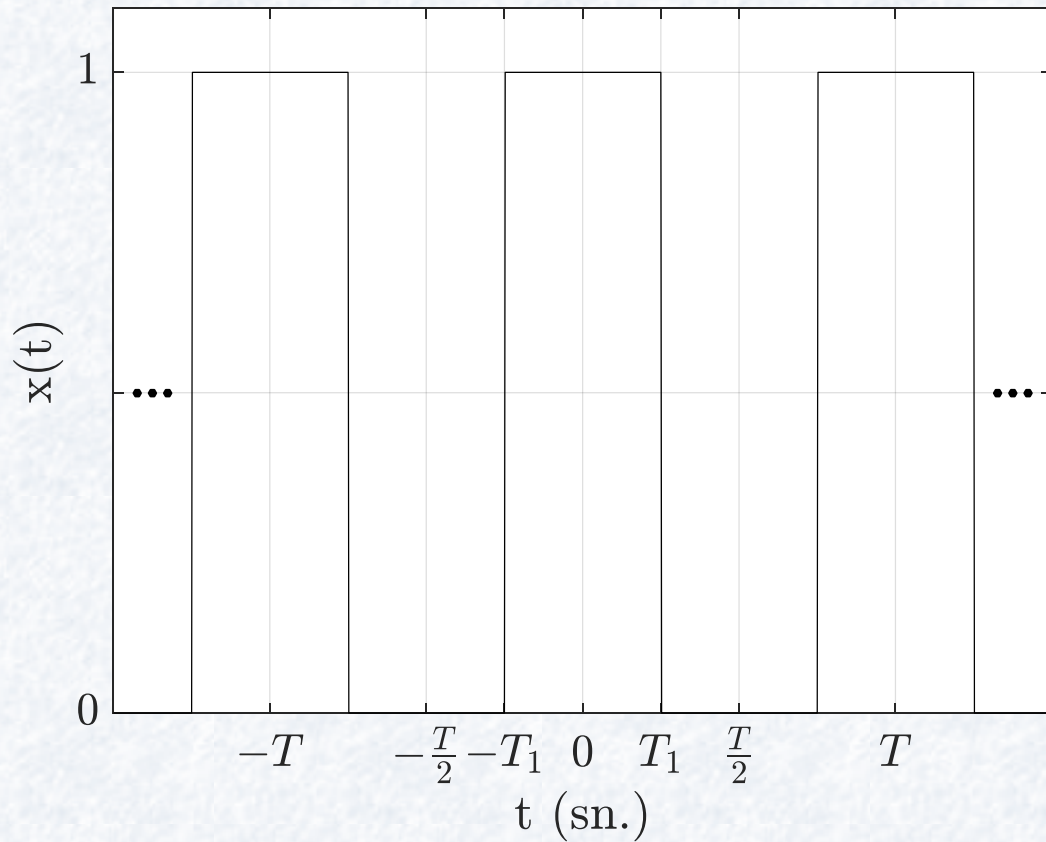
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \int_{t_1}^{t_2} x(t) e^{-jk\omega_0 t} dt$

# Örnek 8

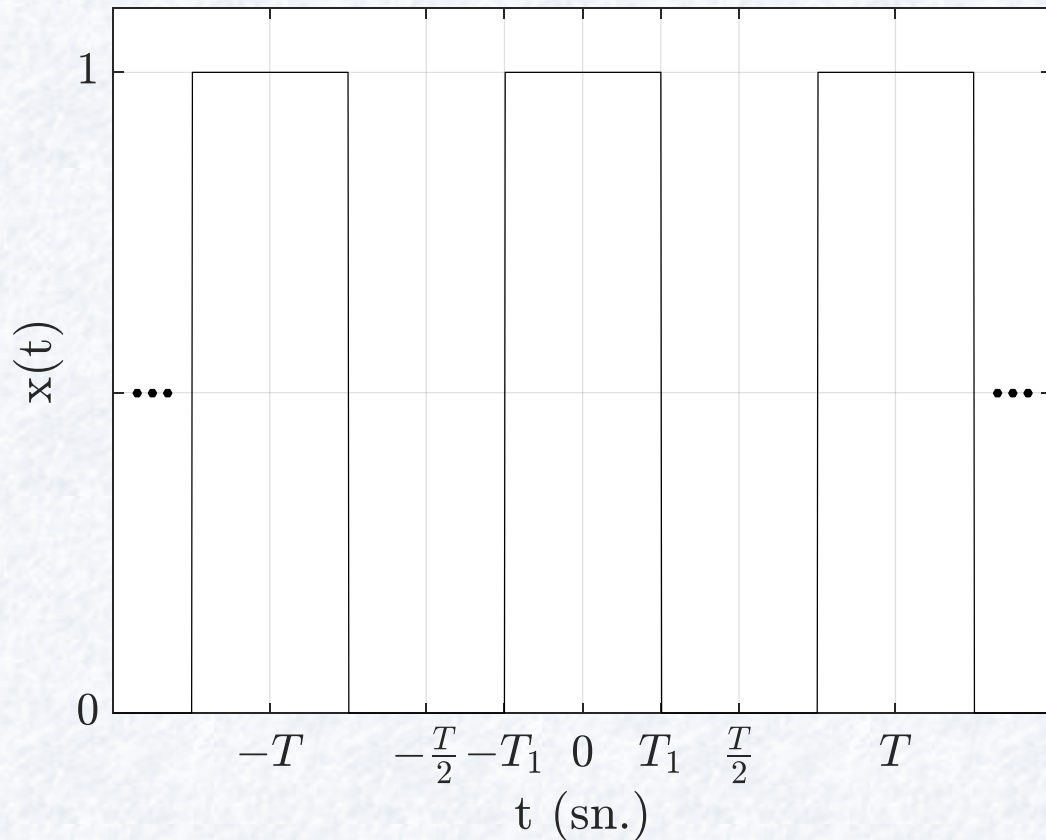
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \int_{-T/2}^{T/2} x(t) e^{-jk\omega_0 t} dt$

# Örnek 8

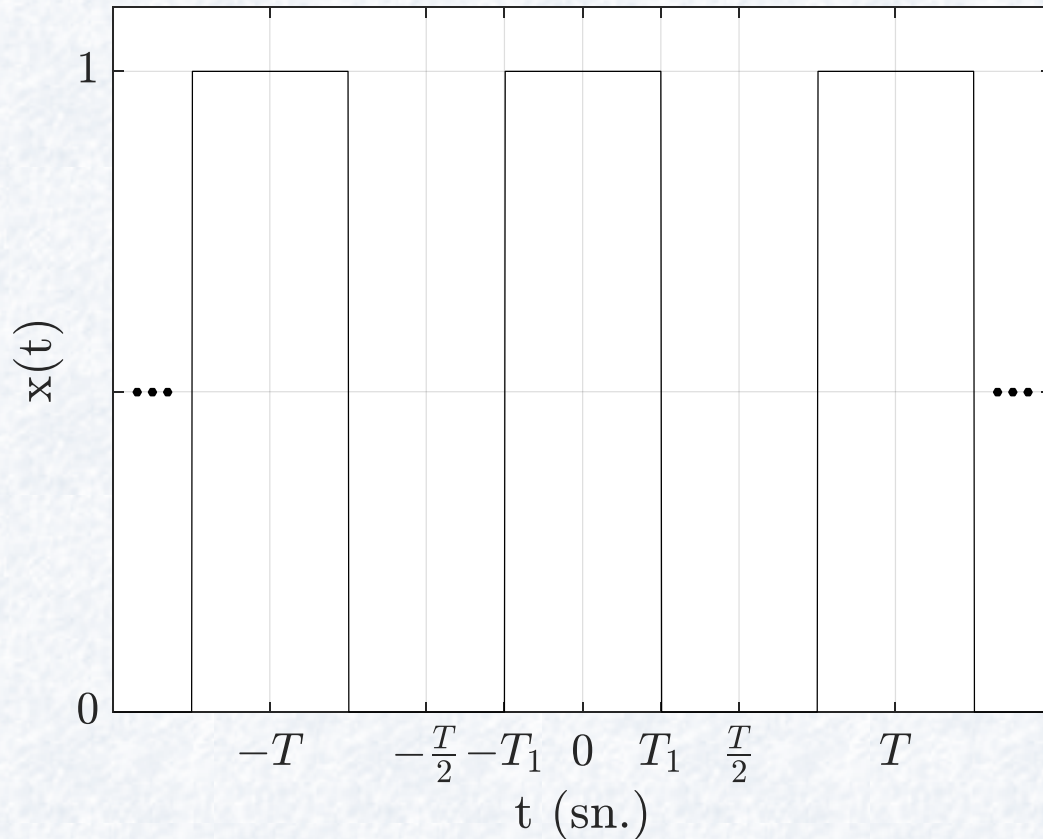
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \int_{-T/2}^{T/2} x(t) e^{-jk\omega_0 t} dt$
- $a_k = \frac{1}{T} \int_{-T/2}^{-T_1} 0 dt + \int_{-T_1}^{T_1} 1 dt + \int_{T_1}^{T/2} 0 dt$

# Örnek 8

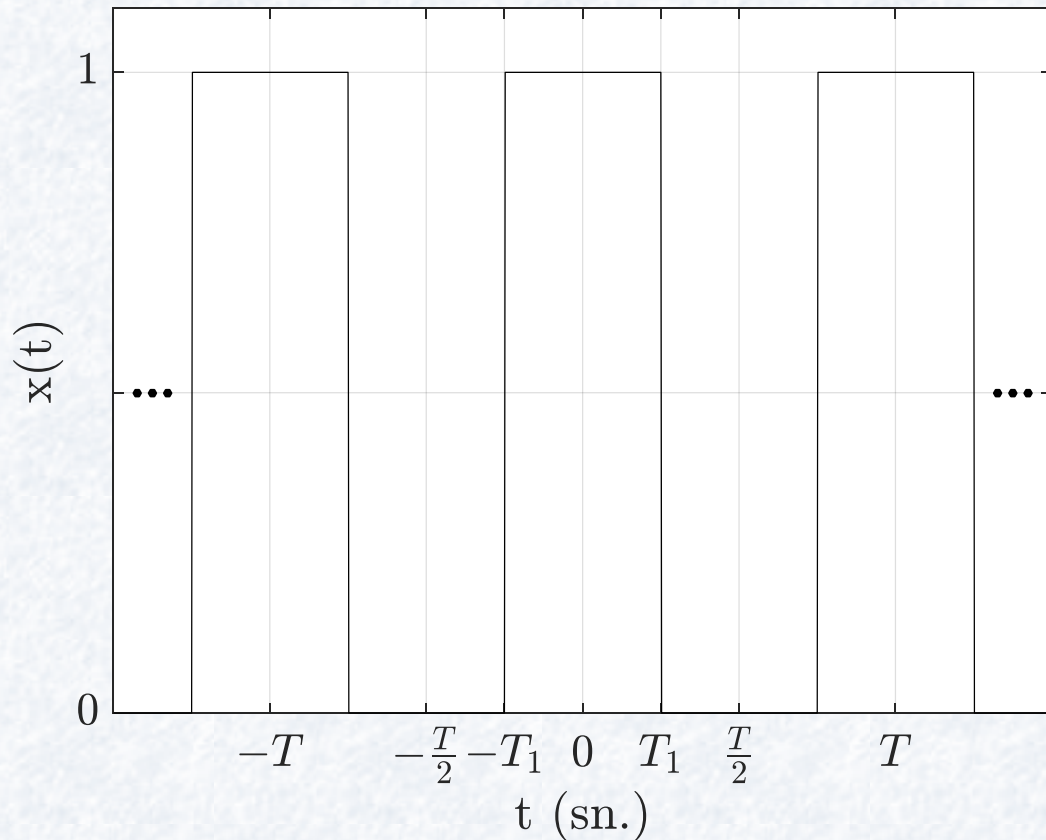
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \int_{-T/2}^{T/2} x(t) e^{-jk\omega_0 t} dt$
- $a_k = \frac{1}{T} \int_{-T_1}^{T_1} 1 e^{-jk\omega_0 t} dt$

# Örnek 8

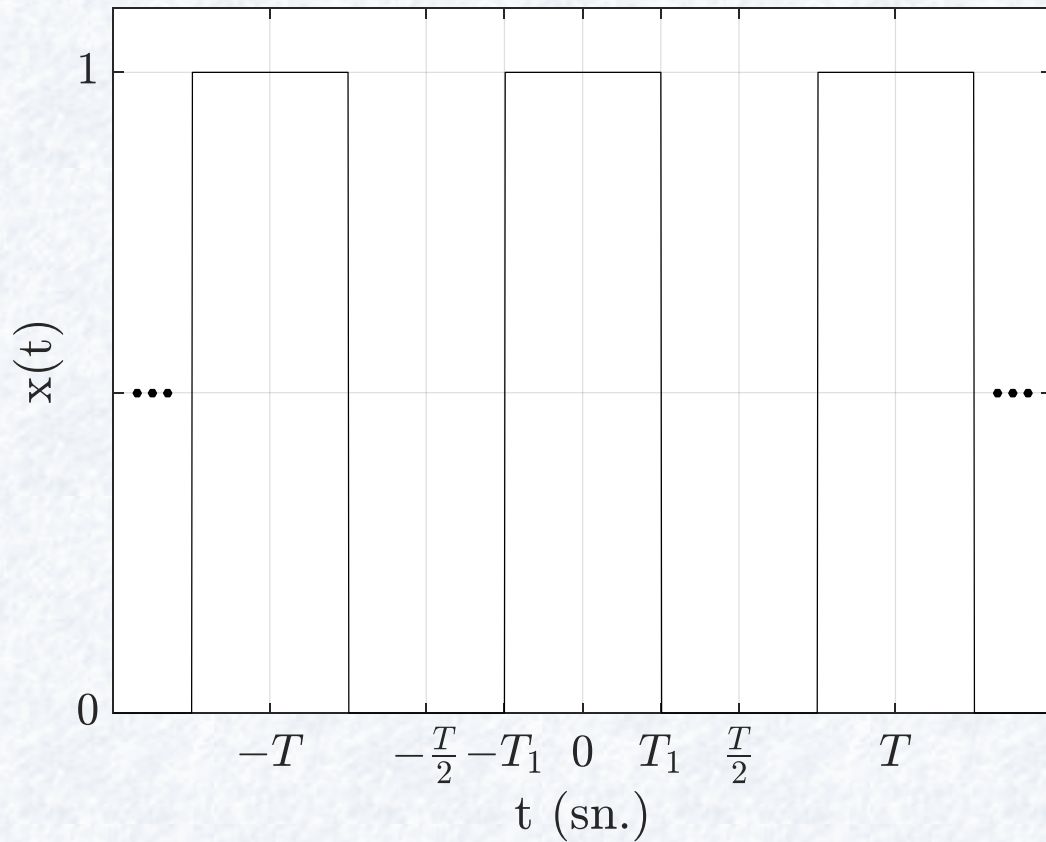
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \int_{-T/2}^{T/2} x(t) e^{-jk\omega_0 t} dt$
- $a_k = \frac{1}{T} \int_{-T_1}^{T_1} 1 e^{-jk\frac{2\pi}{T} t} dt$

# Örnek 8

- Fourier seri açılımı?

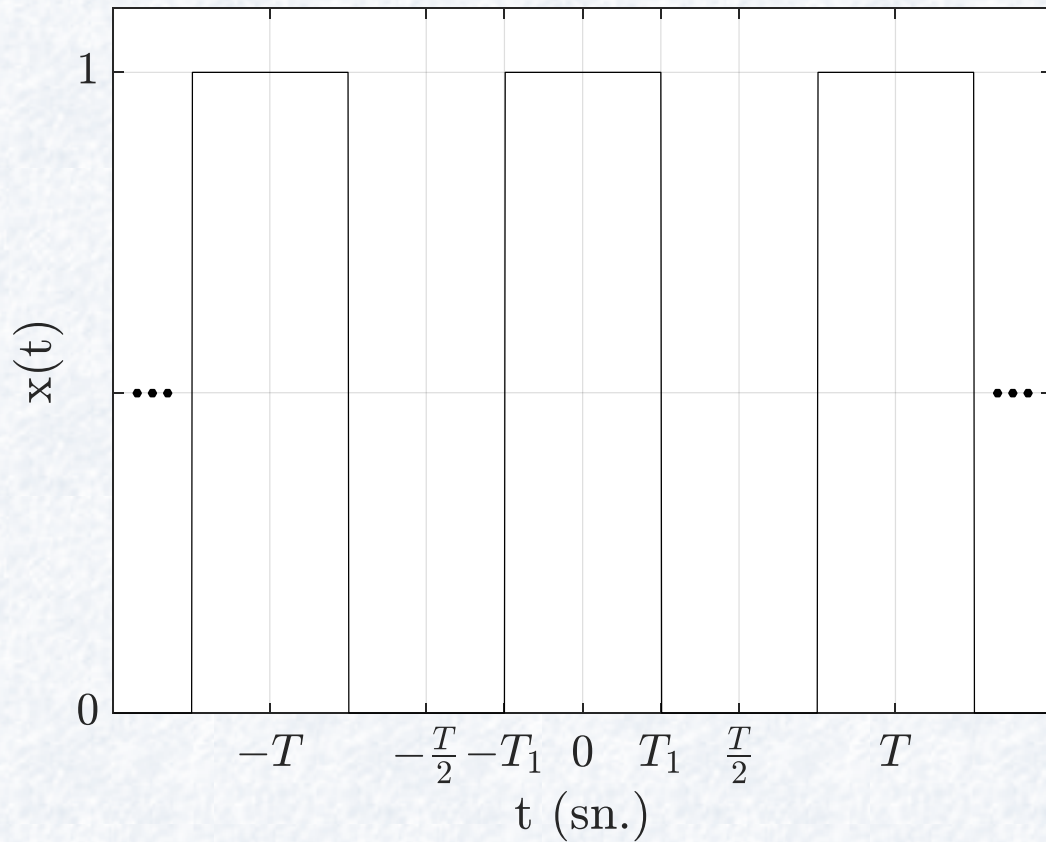


- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \int_{-T_1}^{T_1} 1 e^{-jk\frac{2\pi}{T}t} dt$
- $a_k =$



# Örnek 8

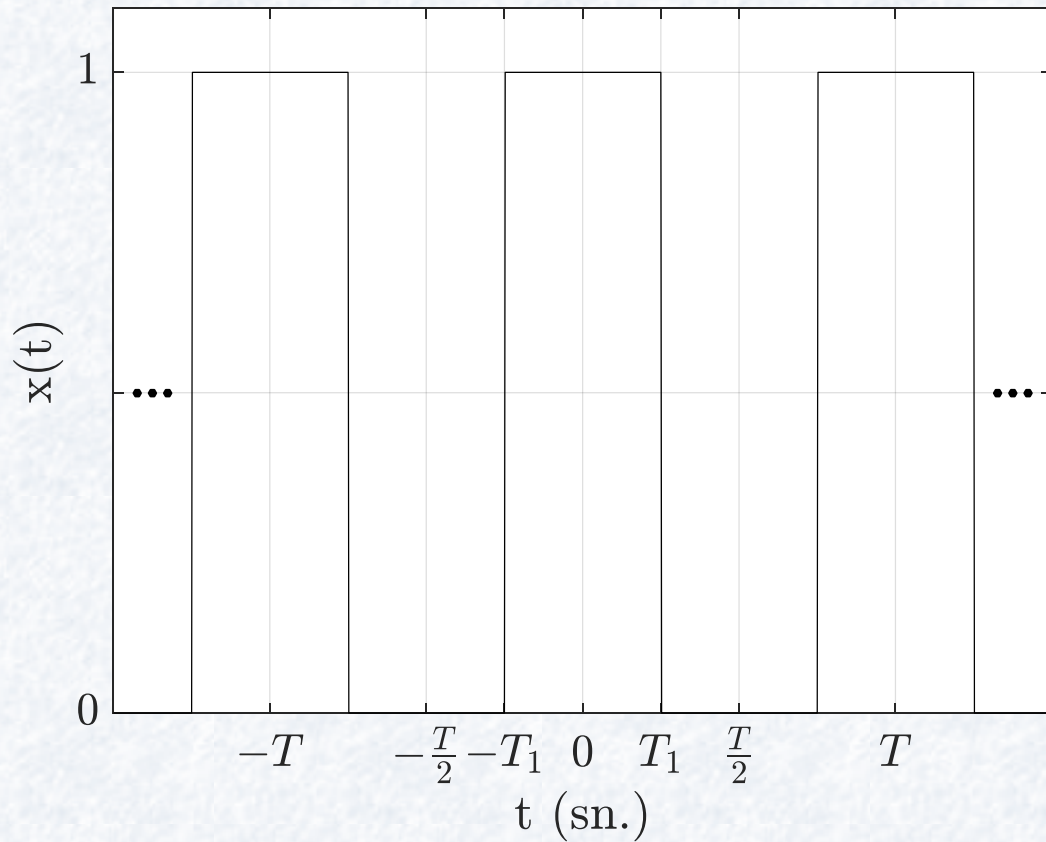
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \int_{-T_1}^{T_1} 1 e^{-jk\frac{2\pi}{T}t} dt$
- $a_k = \frac{1}{T} \frac{-1}{jk\frac{2\pi}{T}} e^{-jk\frac{2\pi}{T}t} \Big|_{-T_1}^{T_1}$

# Örnek 8

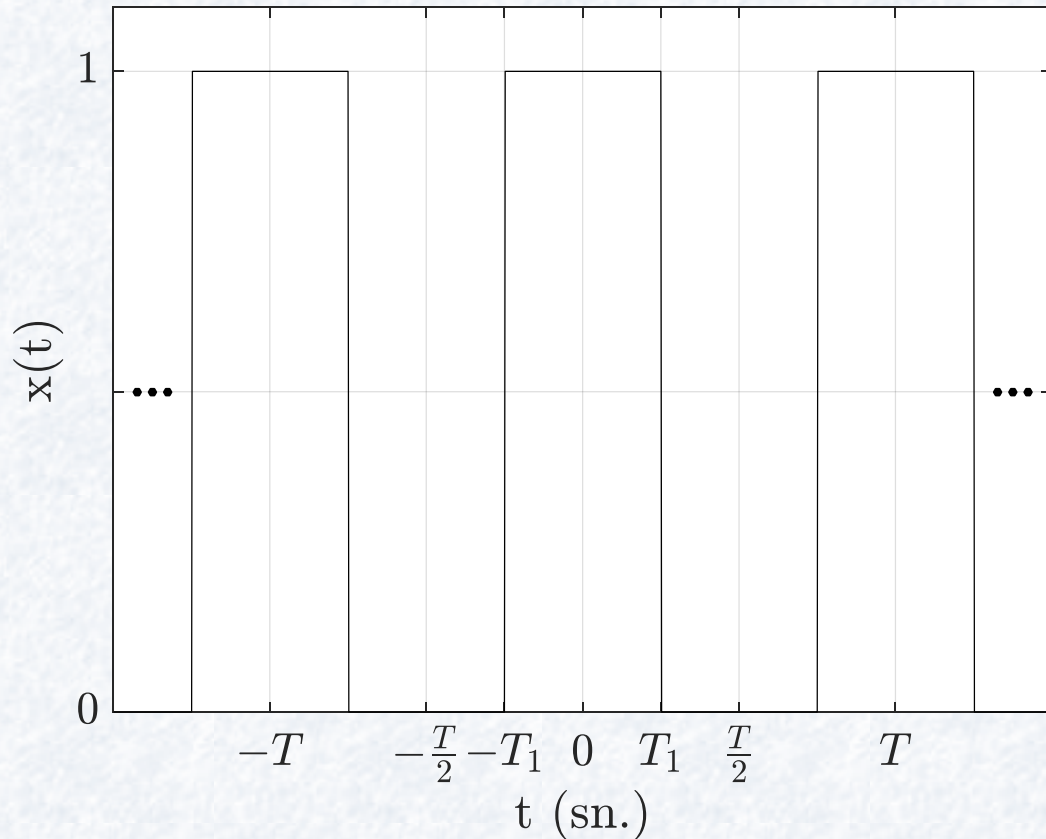
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \int_{-T_1}^{T_1} 1 e^{-jk\frac{2\pi}{T}t} dt$
- $a_k = \frac{1}{T} \frac{-1}{jk\frac{2\pi}{T}} e^{-jk\frac{2\pi}{T}t} \Big|_{-T_1}^{T_1}$
- $a_k =$

# Örnek 8

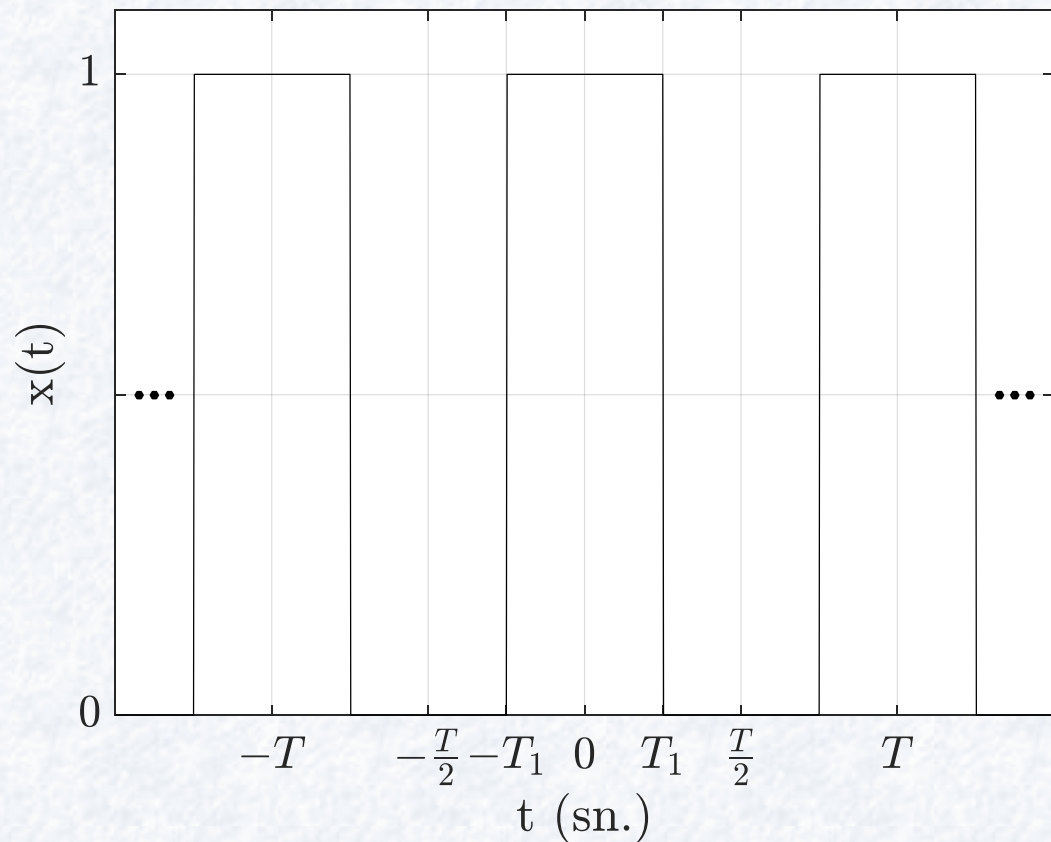
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \int_{-T_1}^{T_1} 1 e^{-jk\frac{2\pi}{T}t} dt$
- $a_k = \frac{1}{T} \frac{-1}{jk\frac{2\pi}{T}} e^{-jk\frac{2\pi}{T}t} \Big|_{-T_1}^{T_1}$
- $a_k = \frac{-1}{j2\pi k} \left( e^{-jk\frac{2\pi T_1}{T}} - e^{jk\frac{2\pi T_1}{T}} \right)$

# Örnek 8

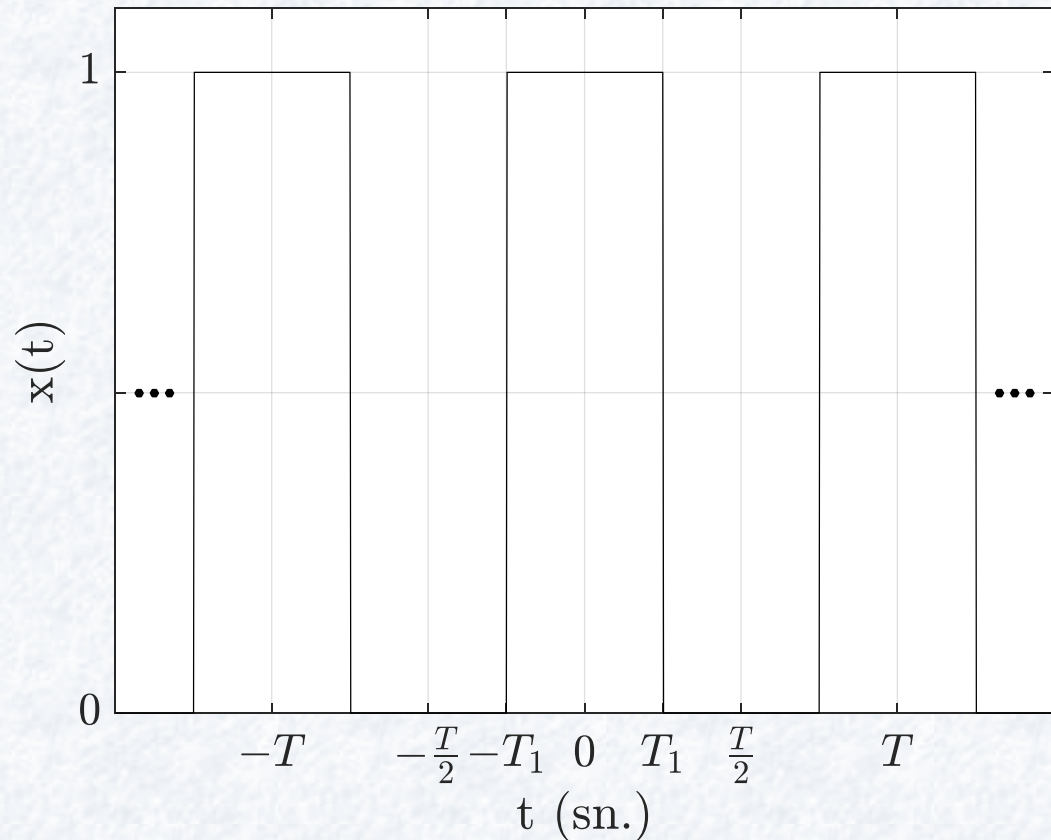
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{j2\pi k} \left( -e^{-jk\frac{2\pi T_1}{T}} + e^{jk\frac{2\pi T_1}{T}} \right)$
- $a_k = \frac{1}{\pi k} \left( \frac{e^{jk\frac{2\pi T_1}{T}} - e^{-jk\frac{2\pi T_1}{T}}}{2j} \right)$
- $a_k =$

# Örnek 8

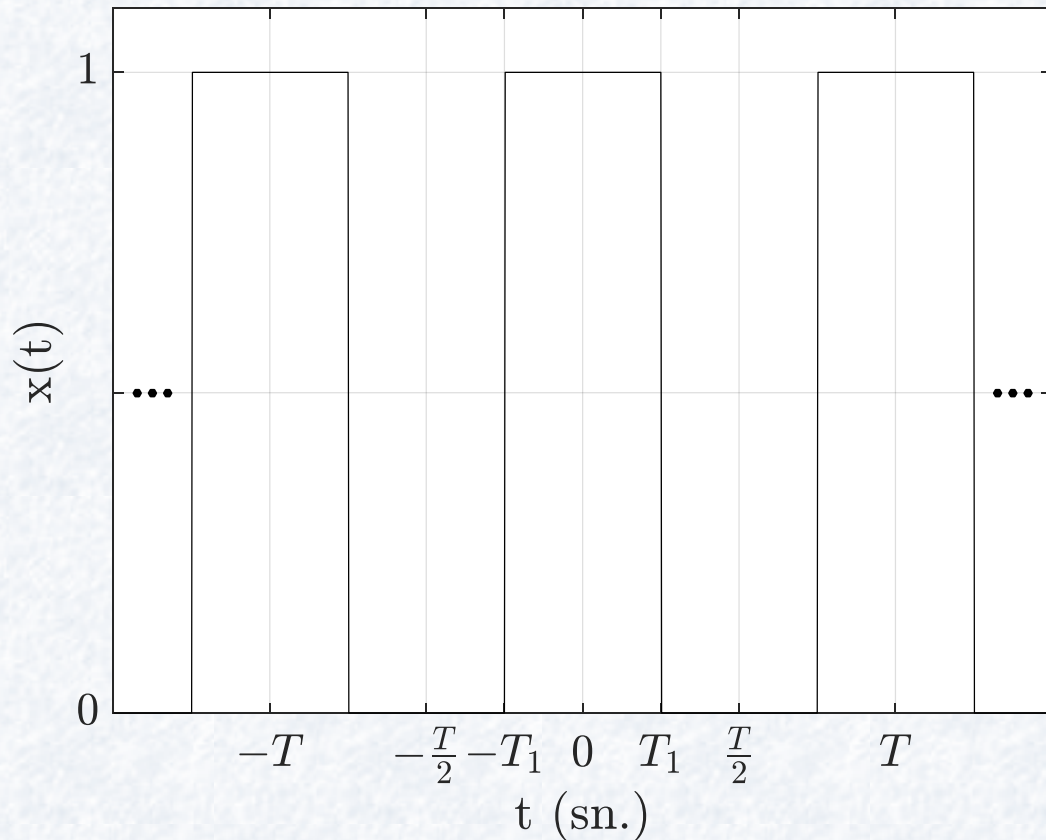
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{j2\pi k} \left( -e^{-jk\frac{2\pi T_1}{T}} + e^{jk\frac{2\pi T_1}{T}} \right)$
- $a_k = \frac{1}{\pi k} \left( \frac{e^{jk\frac{2\pi T_1}{T}} - e^{-jk\frac{2\pi T_1}{T}}}{2j} \right)$
- $a_k = \frac{\sin\left(k\frac{2\pi T_1}{T}\right)}{\pi k}$

# Örnek 8

- Fourier seri açılımı?

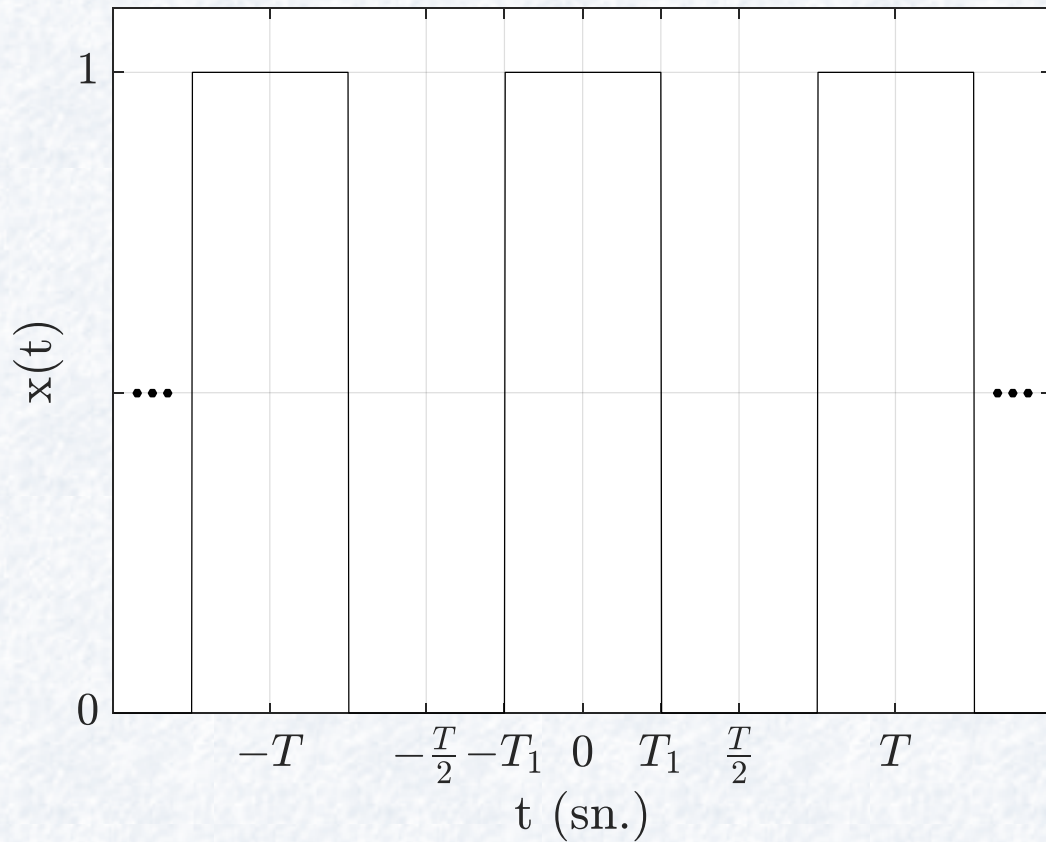


- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{\sin\left(k\frac{2\pi T_1}{T}\right)}{\pi k}$ 
  - ♦  $\text{sinc}(\theta) = \frac{\sin(\pi\theta)}{\pi\theta}$
- $a_0 =$



# Örnek 8

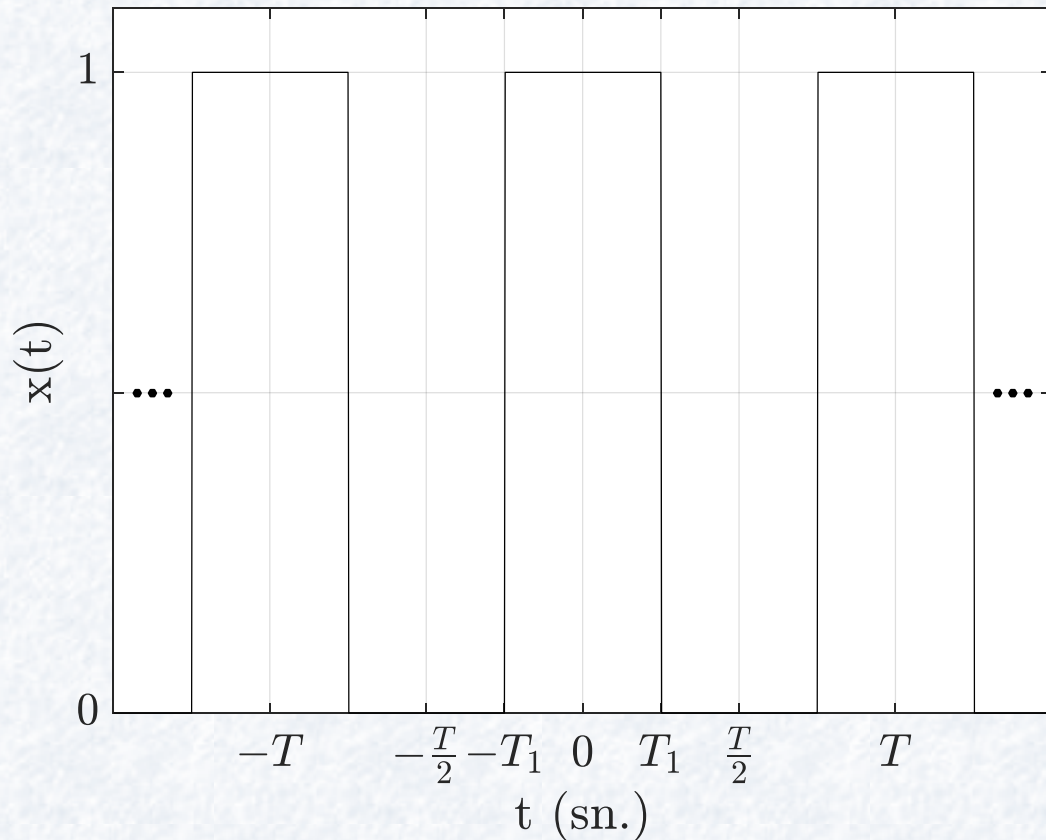
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{\sin\left(k\frac{2\pi T_1}{T}\right)}{\pi k}$
- $a_0 = \frac{\frac{2\pi T_1}{T} \cos\left(k\frac{2\pi T_1}{T}\right)}{\pi} \Big|_{k=0} = \frac{2T_1}{T}$

# Örnek 8

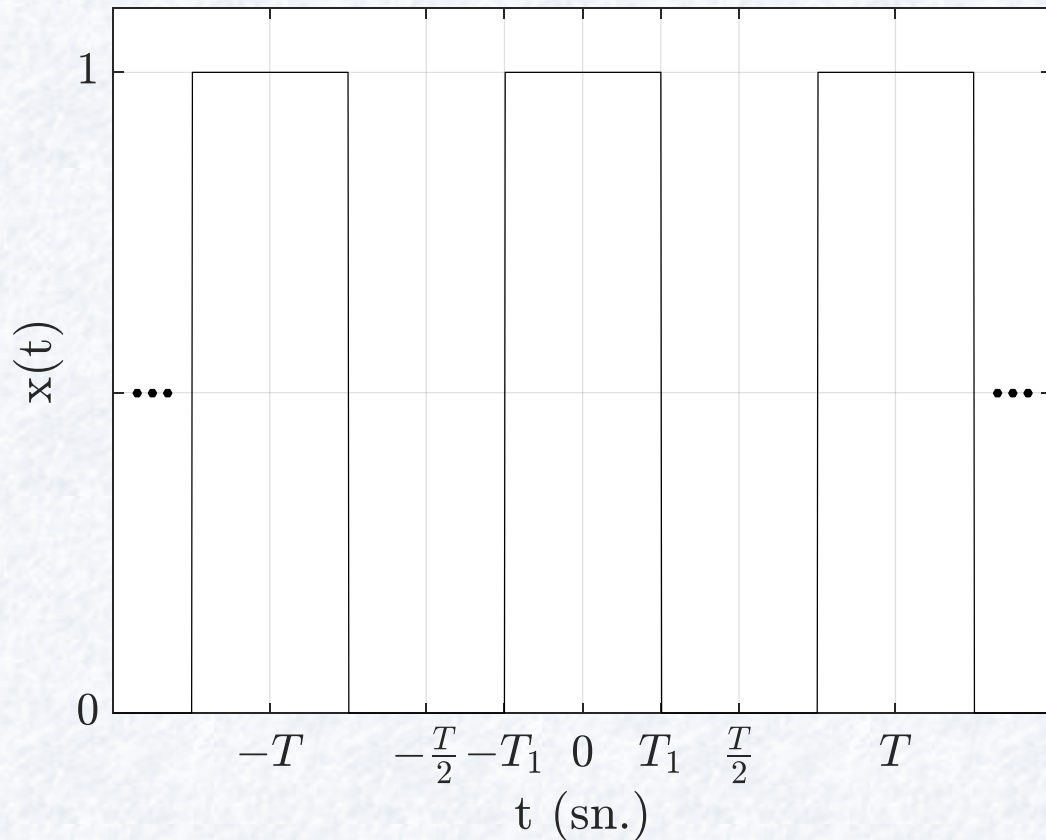
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{\sin\left(k\frac{2\pi T_1}{T}\right)}{\pi k}$
- $a_0 = \frac{\frac{2\pi T_1}{T} \cos\left(k\frac{2\pi T_1}{T}\right)}{\pi} \Big|_{k=0} = \frac{2T_1}{T}$
- $a_0 = \frac{1}{T} \int_{-T_1}^{T_1} 1 e^{-j0\frac{2\pi}{T}t} dt$

# Örnek 8

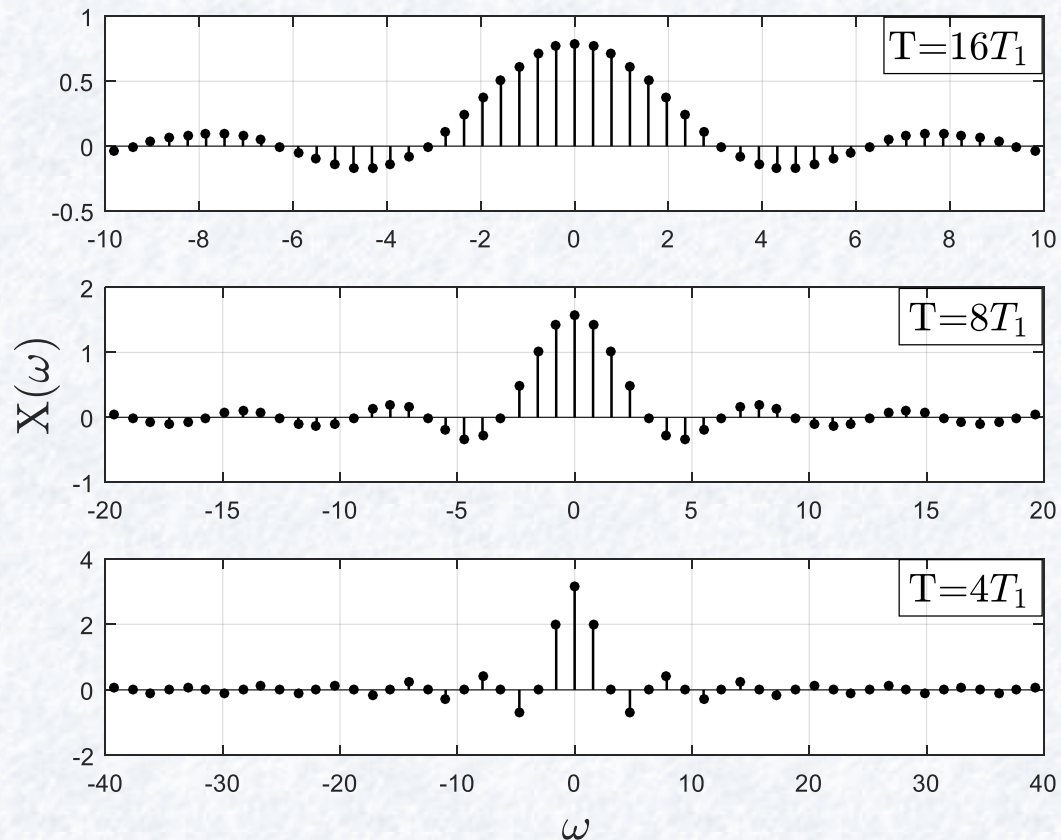
- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{\sin\left(k\frac{2\pi T_1}{T}\right)}{\pi k}$
- $a_0 = \frac{\frac{2\pi T_1}{T} \cos\left(k\frac{2\pi T_1}{T}\right)}{\pi} \Big|_{k=0} = \frac{2T_1}{T}$
- $a_0 = \frac{1}{T} \int_{-T_1}^{T_1} dt = \frac{1}{T} t \Big|_{-T_1}^{T_1} = \frac{2T_1}{T}$

# Örnek 8

- Fourier seri açılımı?



- $\omega_0 = \frac{2\pi}{T}$

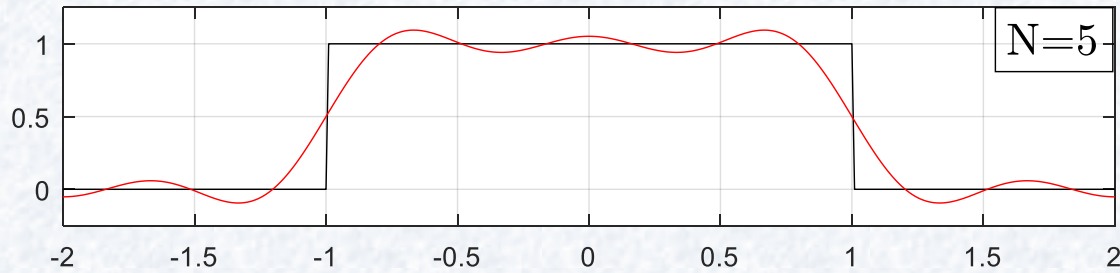
- $a_k = \frac{\sin\left(k\frac{2\pi T_1}{T}\right)}{\pi k}$

- $a_0 = \frac{\frac{2\pi T_1}{T} \cos\left(k\frac{2\pi T_1}{T}\right)}{\pi} \Big|_{k=0} = \frac{2T_1}{T}$

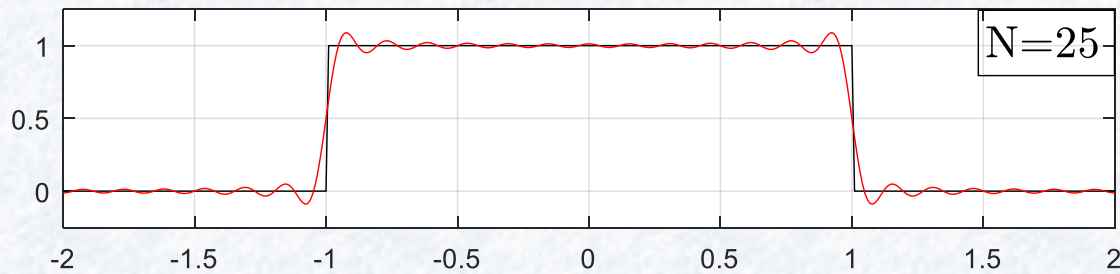
- $a_0 = \frac{1}{T} \int_{-T_1}^{T_1} dt = \frac{1}{T} t \Big|_{-T_1}^{T_1} = \frac{2T_1}{T}$

# Örnek 8

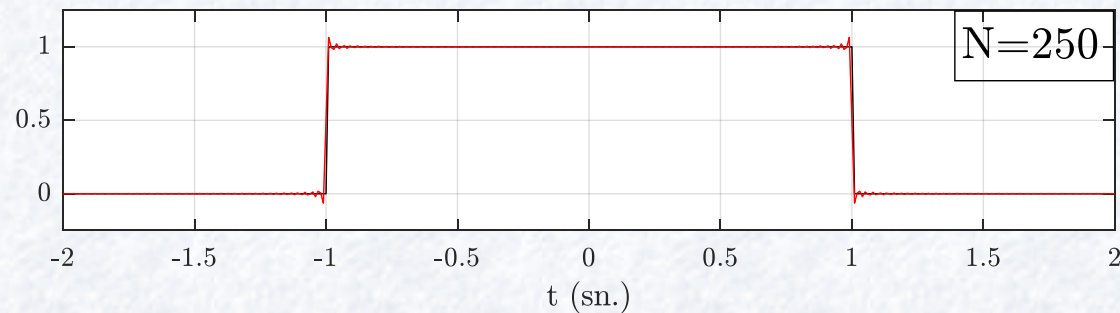
- Fourier seri açılımı?



- $x(t) = \sum_{k=-5}^5 a_k e^{jk\frac{2\pi}{T}t}$



- $x(t) = \sum_{k=-25}^{25} a_k e^{jk\frac{2\pi}{T}t}$



- $x(t) = \sum_{k=-250}^{250} a_k e^{jk\frac{2\pi}{T}t}$

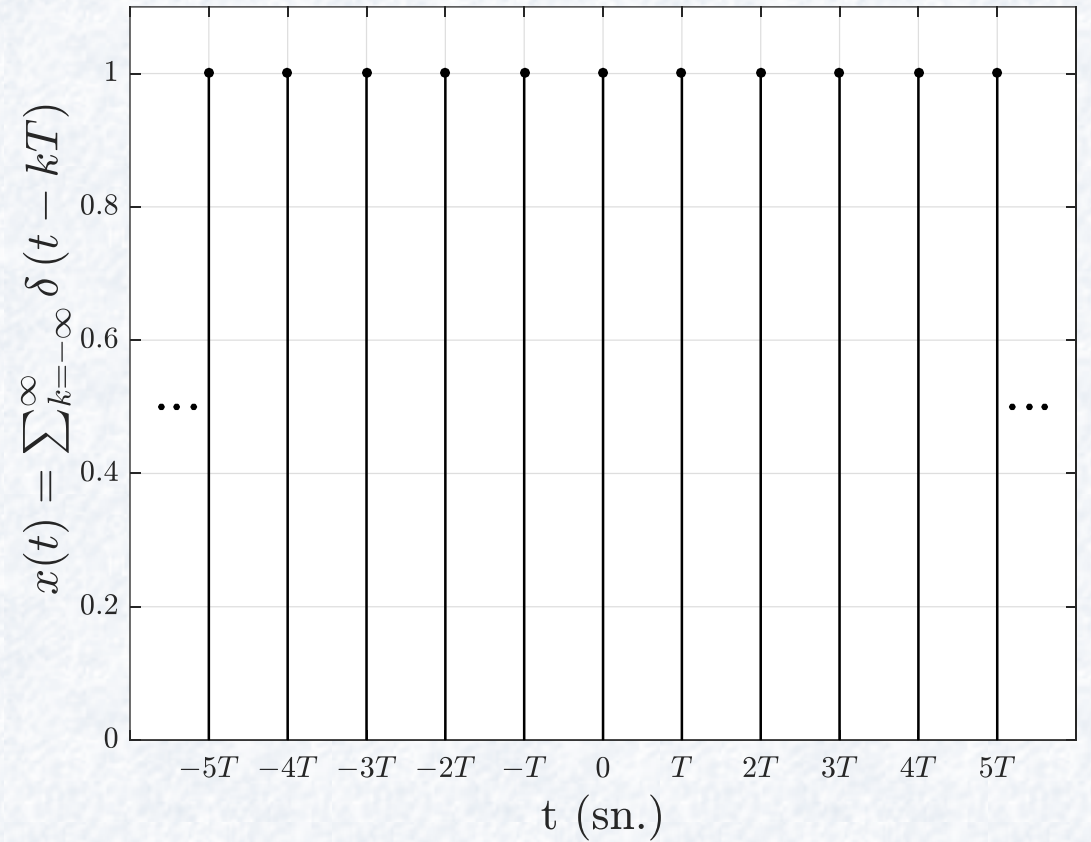
## Örnek 9

- $x(t) = \sum_{k=-\infty}^{\infty} \delta(t - kT)$  ise Fourier seri açılımı?



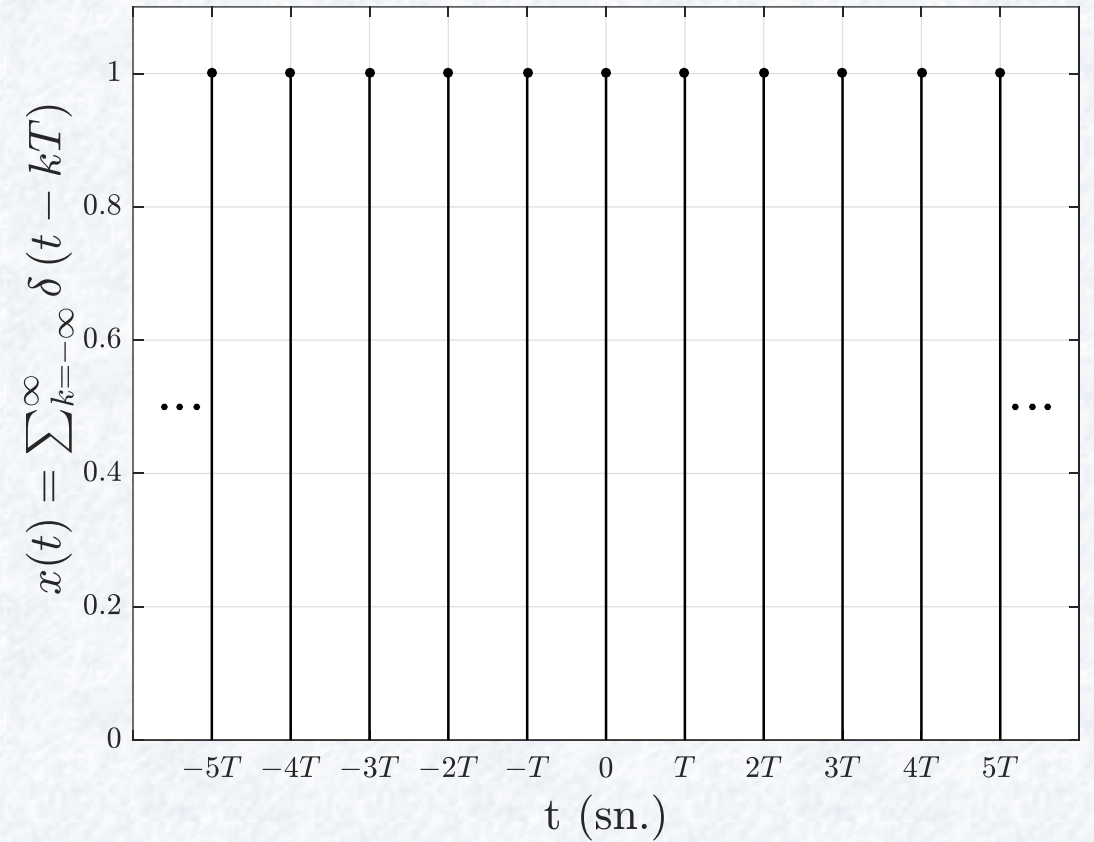
# Örnek 9

- $x(t) = \sum_{k=-\infty}^{\infty} \delta(t - kT)$  ise Fourier seri açılımı?
- $\omega_0 =$



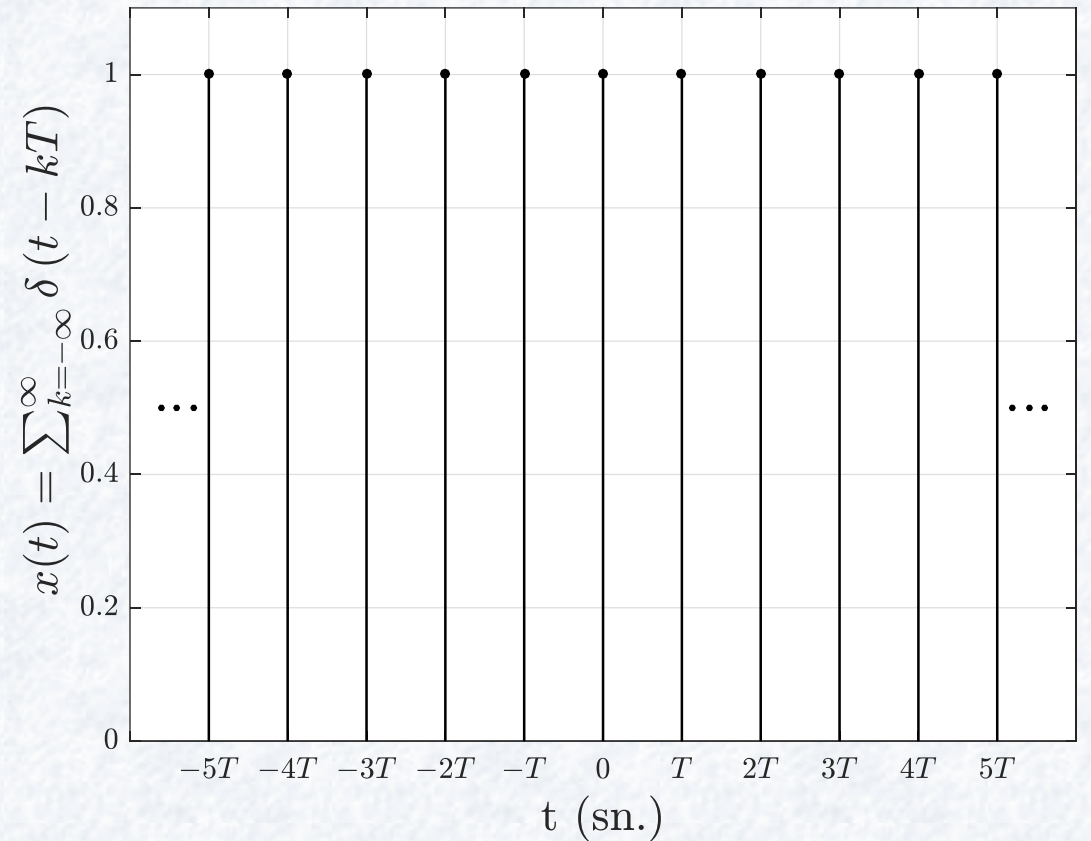
# Örnek 9

- $x(t) = \sum_{k=-\infty}^{\infty} \delta(t - kT)$  ise Fourier seri açılımı?
- $\omega_0 = \frac{2\pi}{T}$
- $a_k =$



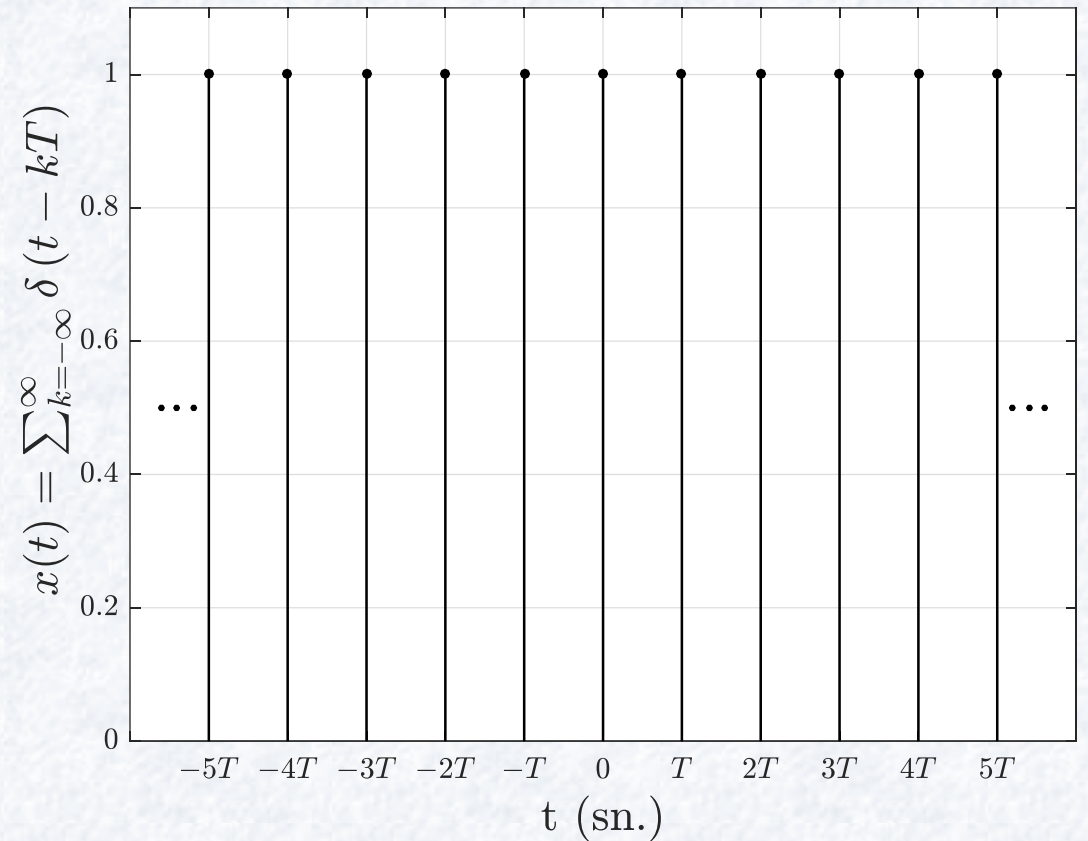
# Örnek 9

- $x(t) = \sum_{k=-\infty}^{\infty} \delta(t - kT)$  ise Fourier seri açılımı?
- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \int_{-T/2}^{T/2} x(t) e^{-jk\omega_0 t} dt$



# Örnek 9

- $x(t) = \sum_{k=-\infty}^{\infty} \delta(t - kT)$  ise Fourier seri açılımı?
- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \underbrace{\int_{-T/2}^{T/2} \delta(t) e^{-jk\omega_0 t} dt}_{?}$
- $a_k = \frac{1}{T} \boxed{\phantom{000}}$



# Örnek 9

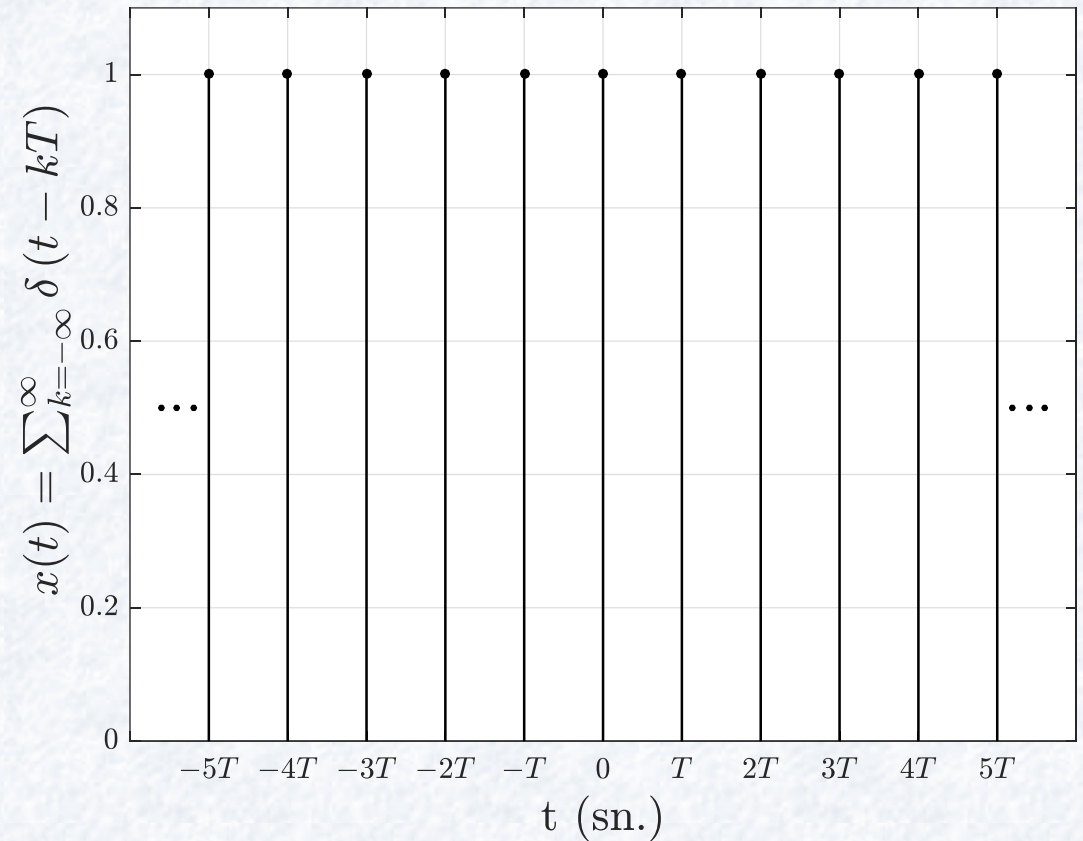
- $x(t) = \sum_{k=-\infty}^{\infty} \delta(t - kT)$  ise Fourier seri açılımı?

- $\omega_0 = \frac{2\pi}{T}$

- $a_k = \frac{1}{T} \underbrace{\int_{-T/2}^{T/2} \delta(t) e^{-jk\omega_0 t} dt}_{e^{-jk\omega_0 0}}$

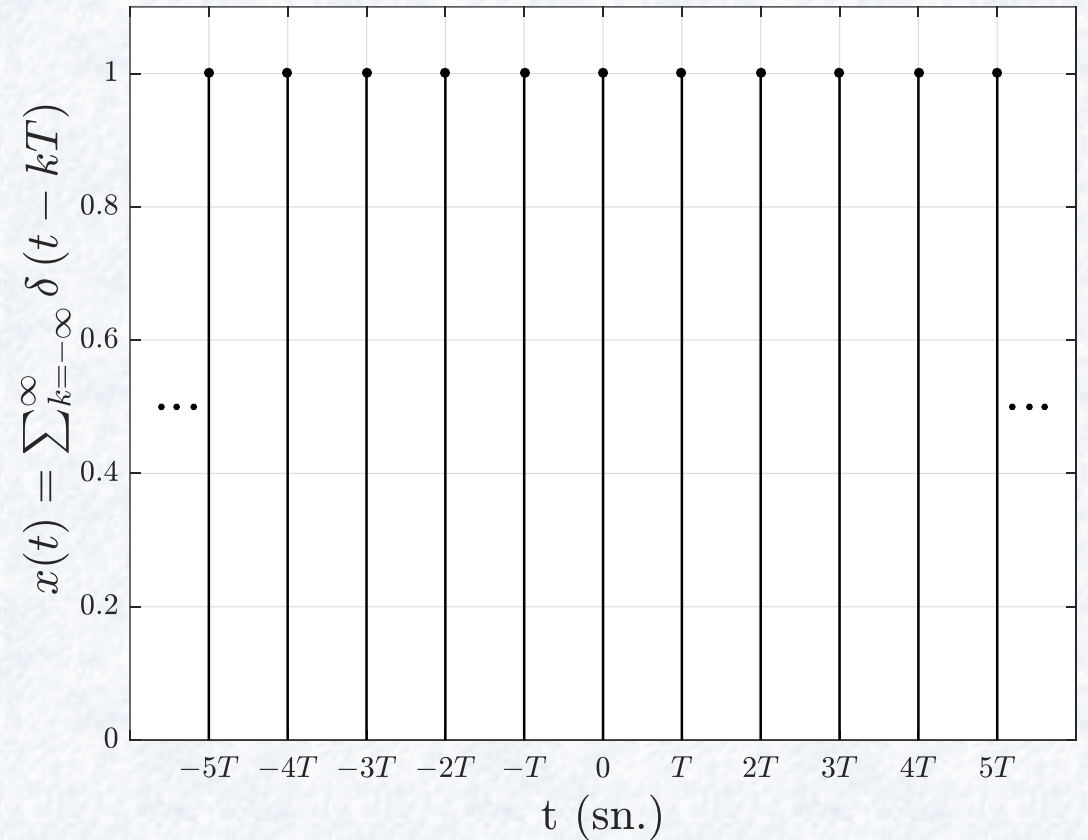
- $a_k = \frac{1}{T} 1 = \frac{1}{T}$

- $a_0 =$



# Örnek 9

- $x(t) = \sum_{k=-\infty}^{\infty} \delta(t - kT)$  ise Fourier seri açılımı?
- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \underbrace{\int_{-T/2}^{T/2} \delta(t) e^{-jk\omega_0 t} dt}_{e^{-jk\omega_0 0}}$
- $a_k = \frac{1}{T} 1 = \frac{1}{T}$
- $a_0 = \frac{1}{T}$
- $x(t) = \sum_{k=-\infty}^{\infty} \frac{1}{T} e^{jk\frac{2\pi}{T}t}$





# Örnek 9

- $x(t) = \sum_{k=-\infty}^{\infty} \delta(t - kT)$  ise Fourier seri açılımı?
- $\omega_0 = \frac{2\pi}{T}$
- $a_k = \frac{1}{T} \underbrace{\int_{-T/2}^{T/2} \delta(t) e^{-jk\omega_0 t} dt}_{e^{-jk\omega_0 0}}$
- $a_k = \frac{1}{T} 1 = \frac{1}{T}$
- $a_0 = \frac{1}{T}$
- $x(t) = \sum_{k=-\infty}^{\infty} \frac{1}{T} e^{jk\frac{2\pi}{T}t}$

