### Special Topics in Deep Learning

COMP 6211D & ELEC 6910T

Instructor: Qifeng Chen

#### Course Website

https://course.cse.ust.hk/comp6211d

#### Who we are

Instructors: Qifeng Chen (cqf@ust.hk)

TA: Hyukryul Yang (hyangbd@connect.ust.hk)
 Nayeon Lee (nayeon.lee@connect.ust.hk)

#### Logistics

- In-class presentation
  - We will send out a list of papers in a couple of days
  - Send us three papers in the list you would like to present in a prioritized order
  - You may add a paper not in the list to your preference list
  - If you do not send us the preference list, we will assign a paper to you
  - Each student will present one paper for up to 12 minutes, followed by 3-minute Q&A
  - 5 students will present in each lecture
- Homework
  - First homework will be out in a week
- Attendance
  - Start after the add&drop period

#### Machine Learning Basis

### Linear Regression

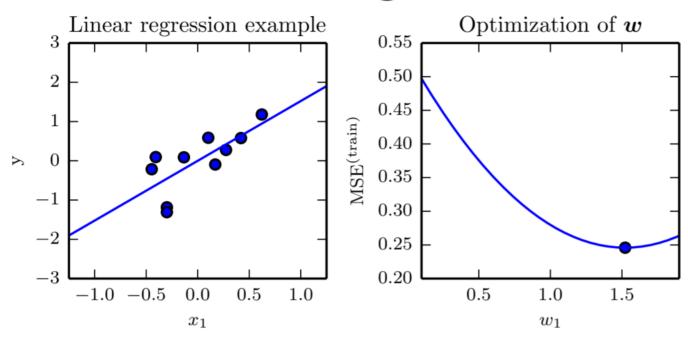
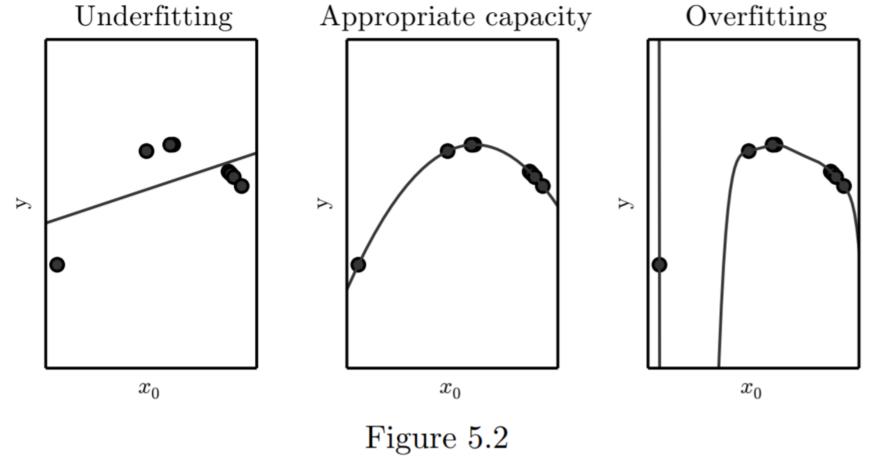


Figure 5.1

# Underfitting and Overfitting in Polynomial Estimation



### Generalization and Capacity

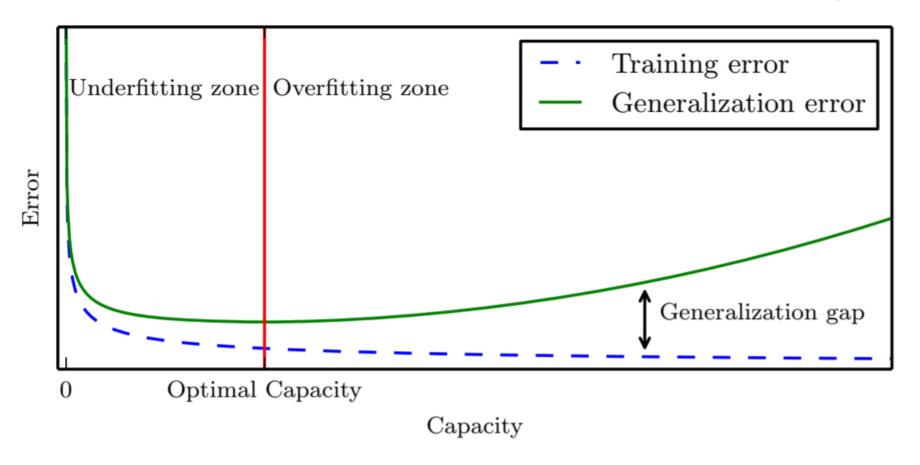
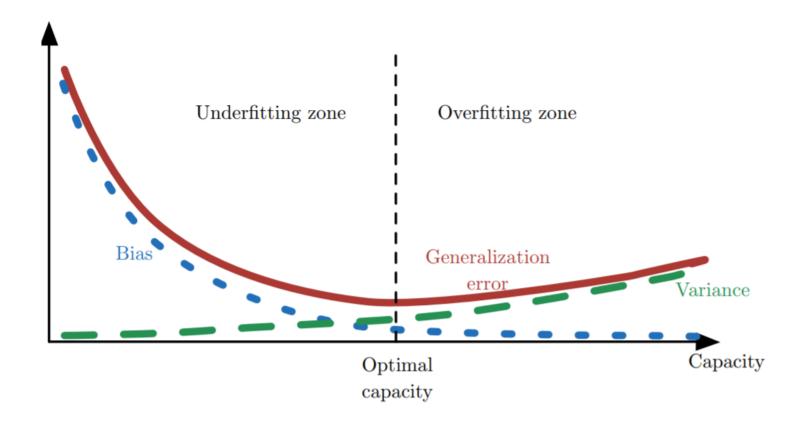


Figure 5.3

### Bias and Variance



#### 'Deep Voice' Software Can Clone Anyone's Voice With Just 3.7 Seconds of Audio

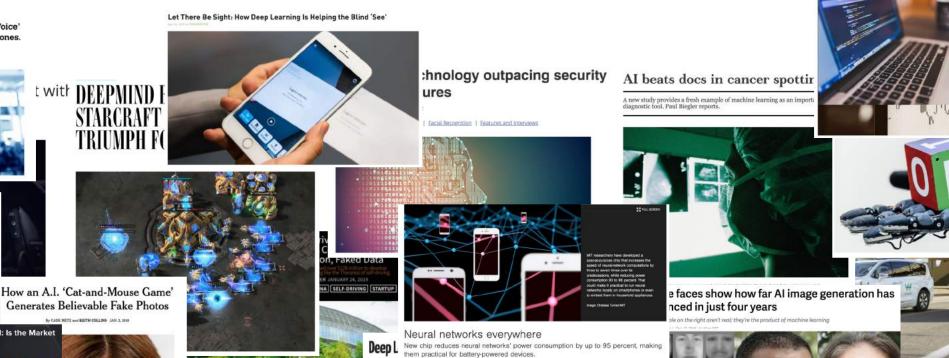
Using snippets of voices, Baidu's 'Deep Voice'

## can generate new speech, accents, and tones. 'Creative' AlphaZero leads way for

chess computers and, maybe, science

Former chess world champion Garry Kasparov likes what he

### The Rise of Deep Learning





To create the final image in this set, the system generated 10 million revisions over 1

After Millions of Trials, These Simulated Humans Learned to Do Perfect Backflips and Cartwheels

Researchers introduce a deep learning method that converts mono audio recordings into 3D sounds using video scenes

**Automation And Algorithms: De-Risking Manufacturing With Artificial Intelligence** 

Al Can Help In Predicting Cryptocurrency

Value



The two key applications of AI in manufacturing are pricing and

By Robert F. Service | Dec. 6, 2018, 12:05 PM

Google's DeepMind aces protein folding

### What is Deep Learning?

## ARTIFICIAL INTELLIGENCE

Any technique that enables computers to mimic human behavior



#### MACHINE LEARNING

Ability to learn without explicitly being programmed



#### **DEEP LEARNING**

Extract patterns from data using neural networks

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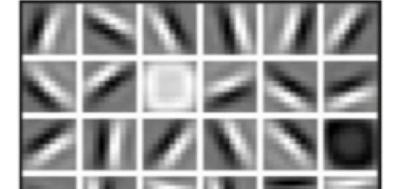
### Why Deep Learning and Why Now?

### Why Deep Learning?

Hand engineered features are time consuming, brittle and not scalable in practice

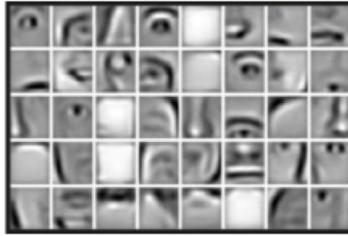
Can we learn the **underlying features** directly from data?

Low Level Features



Lines & Edges

#### Mid Level Features



Eyes & Nose & Ears

#### **High Level Features**



Facial Structure

### Why Now?

Neural Networks date back decades, so why the resurgence?

Stochastic Gradient Descent

Perceptron

• Learnable Weights

Backpropagation

Multi-Layer Perceptron

Deep Convolutional NN

Digit Recognition

#### I. Big Data

- Larger Datasets
- Easier Collection& Storage







#### 2. Hardware

- Graphics Processing Units (GPUs)
- Massively
   Parallelizable



#### 3. Software

- Improved Techniques
- New Models
- Toolboxes





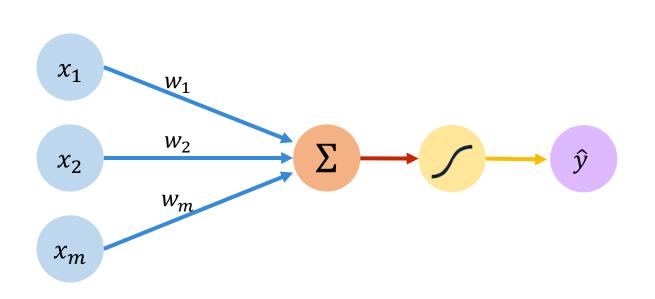
1958

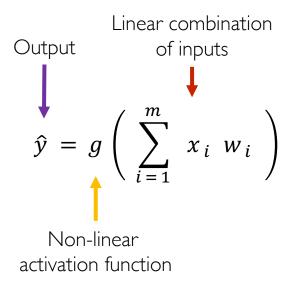
1986

1995

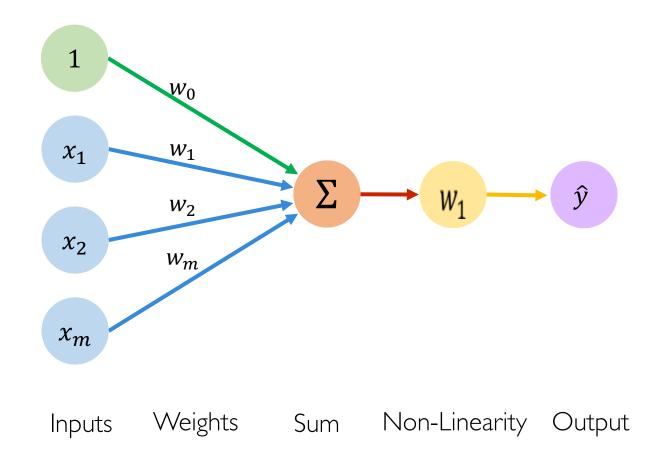


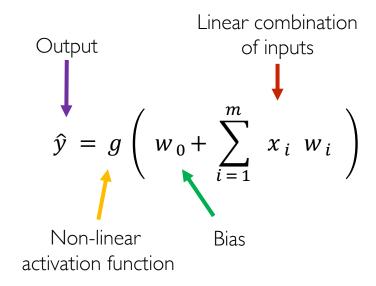
## The Perceptron The structural building block of deep learning



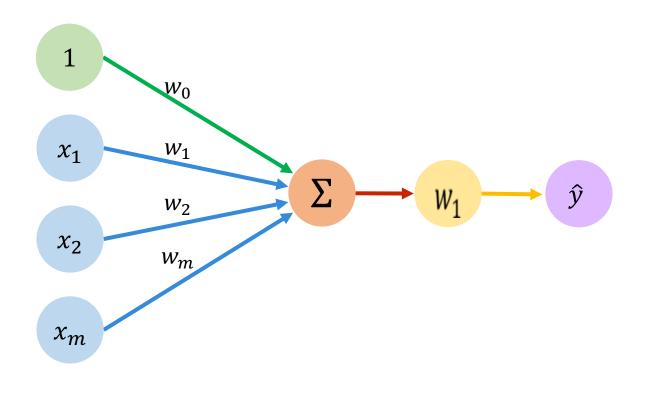


Inputs Weights Sum Non-Linearity Output









$$\hat{y} = g \left( w_0 + \sum_{i=1}^m x_i w_i \right)$$

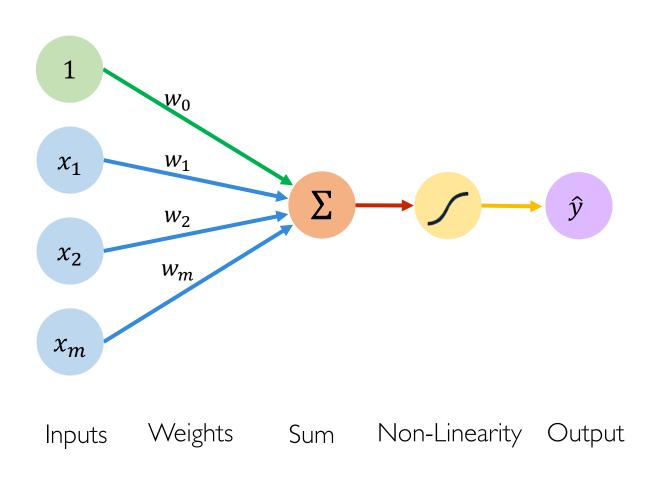
$$\hat{y} = g(w_0 + \boldsymbol{X}^T \boldsymbol{W})$$

where: 
$$\boldsymbol{X} = \begin{bmatrix} x_1 \\ \vdots \\ x_m \end{bmatrix}$$
 and  $\boldsymbol{W} = \begin{bmatrix} w_1 \\ \vdots \\ w_m \end{bmatrix}$ 

Weights

Sum

Non-Linearity Output

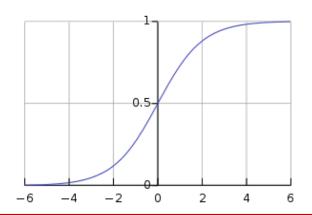


#### **Activation Functions**

$$\hat{y} = g(w_0 + X^T W)$$

• Example: sigmoid function

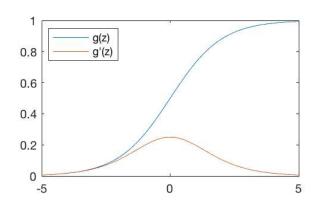
$$g(z) = \sigma(z) = \frac{1}{1 + e^{-z}}$$



 $\boldsymbol{Z}$ 

#### Common Activation Functions

#### Sigmoid Function

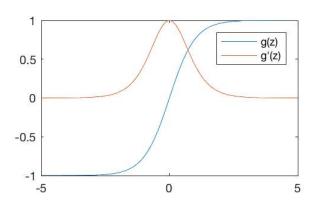


$$g(z) = \frac{1}{1 + e^{-z}}$$

$$g'(z) = g(z)(1 - g(z))$$



#### Hyperbolic Tangent

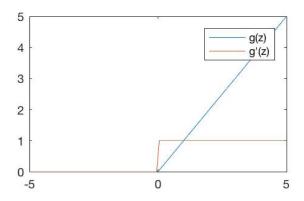


$$g(z) = \frac{e^{z} - e^{-z}}{e^{z} + e^{-z}}$$

$$g'(z) = 1 - g(z)^2$$



#### Rectified Linear Unit (ReLU)



$$g(z) = \max(0, z)$$

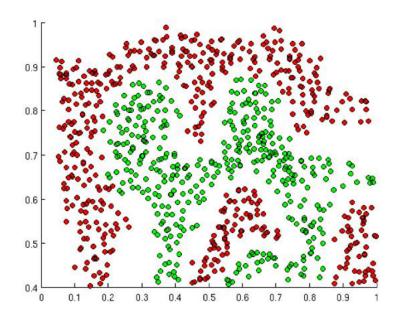
$$g'(z) = \begin{cases} 1, & z > 0 \\ 0, & \text{otherwise} \end{cases}$$



NOTE: All activation functions are non-linear

#### Importance of Activation Functions

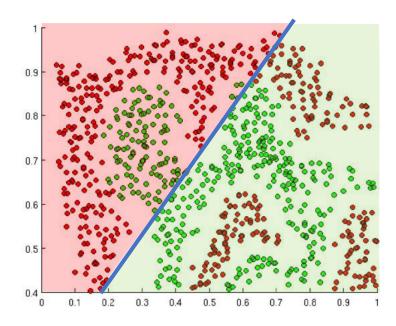
The purpose of activation functions is to **introduce non-linearities** into the network



What if we wanted to build a Neural Network to distinguish green vs red points?

#### Importance of Activation Functions

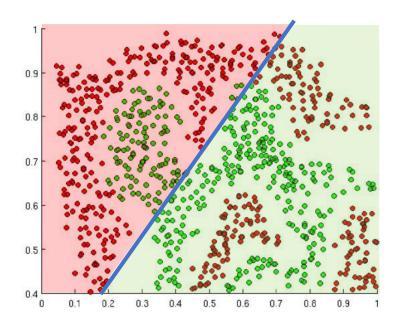
The purpose of activation functions is to **introduce non-linearities** into the network



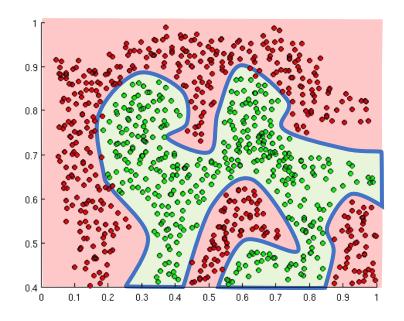
Linear Activation functions produce linear decisions no matter the network size

#### Importance of Activation Functions

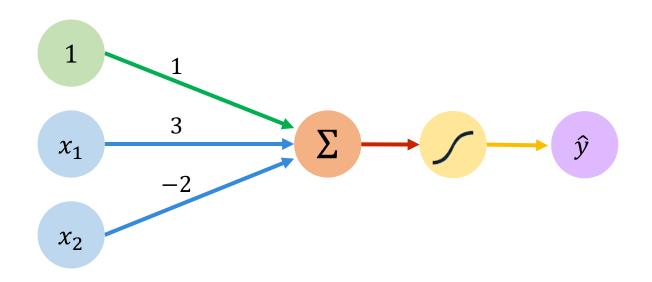
The purpose of activation functions is to **introduce non-linearities** into the network



Linear Activation functions produce linear decisions no matter the network size



Non-linearities allow us to approximate arbitrarily complex functions



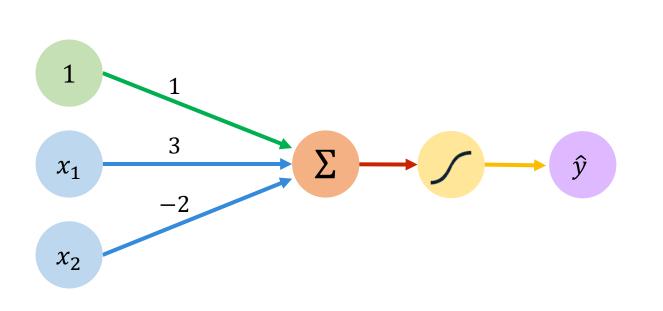
We have: 
$$w_0 = 1$$
 and  $\boldsymbol{W} = \begin{bmatrix} 3 \\ -2 \end{bmatrix}$ 

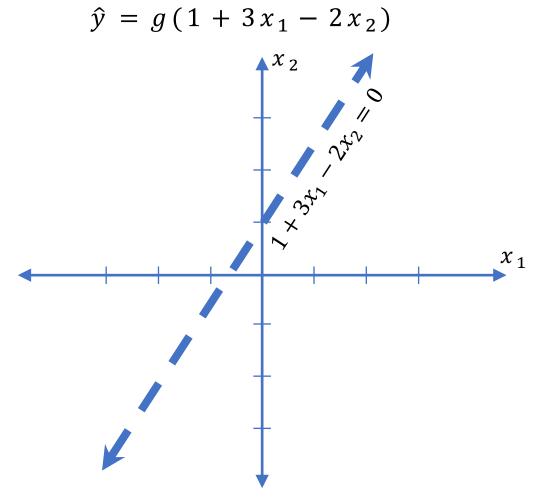
$$\hat{y} = g(w_0 + X^T W)$$

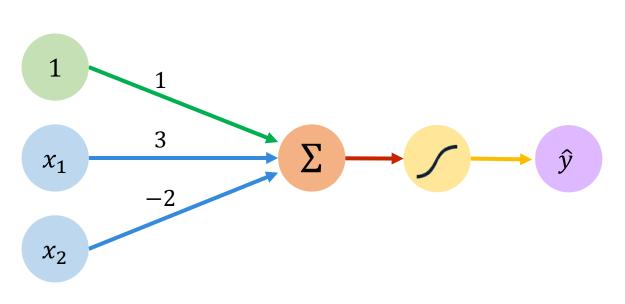
$$= g\left(1 + \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}^T \begin{bmatrix} 3 \\ -2 \end{bmatrix}\right)$$

$$\hat{y} = g(1 + 3x_1 - 2x_2)$$

This is just a line in 2D!

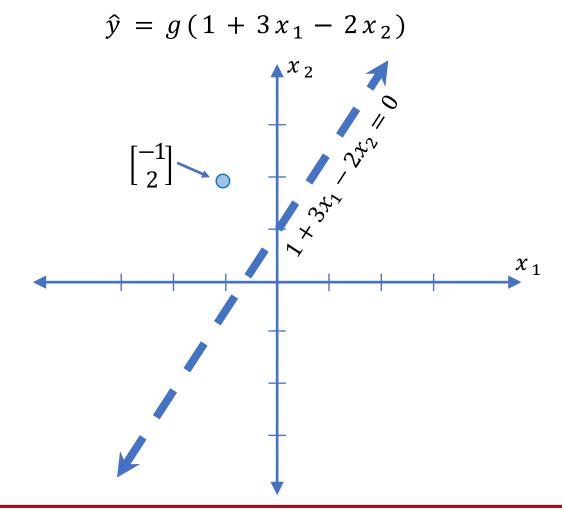


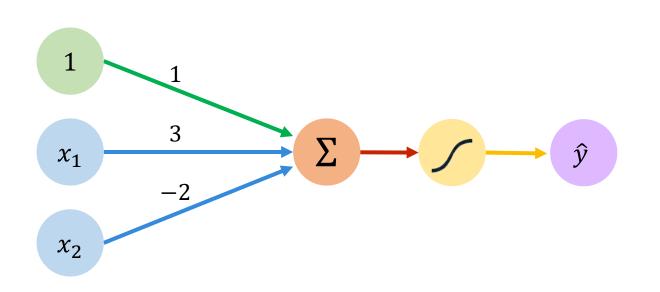


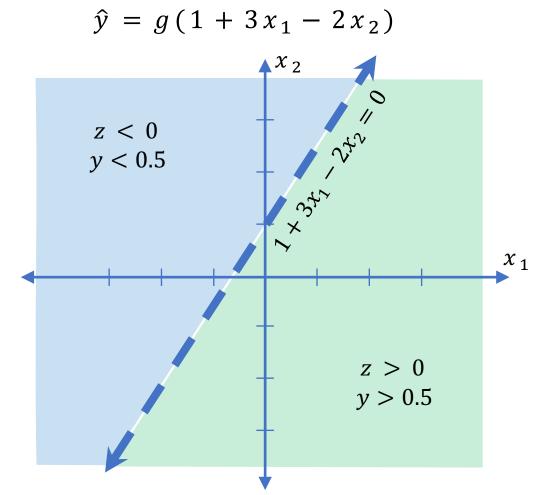


Assume we have input:  $X = \begin{bmatrix} -1 \\ 2 \end{bmatrix}$ 

$$\hat{y} = g (1 + (3*-1) - (2*2))$$
  
=  $g (-6) \approx 0.002$ 

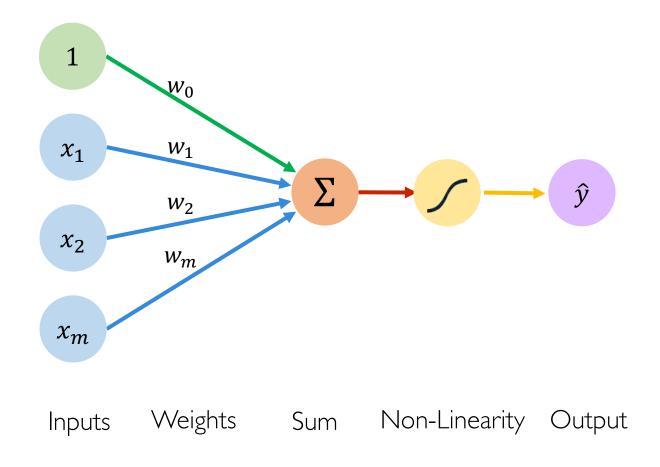




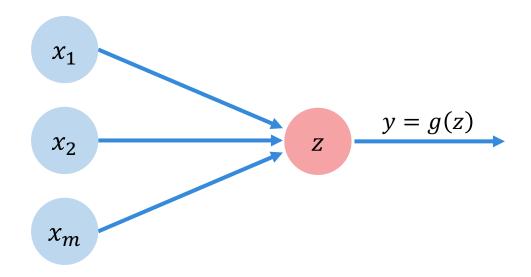


#### Building Neural Networks with Perceptrons

#### The Perceptron: Simplified

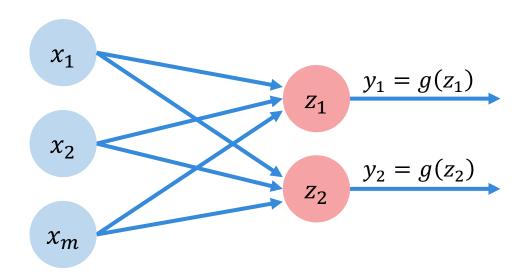


#### The Perceptron: Simplified



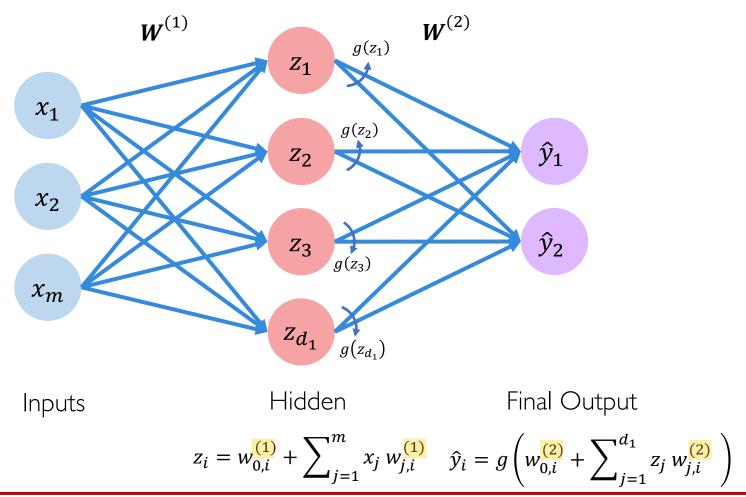
$$z = w_0 + \sum_{j=1}^m x_j w_j$$

#### Multi Output Perceptron



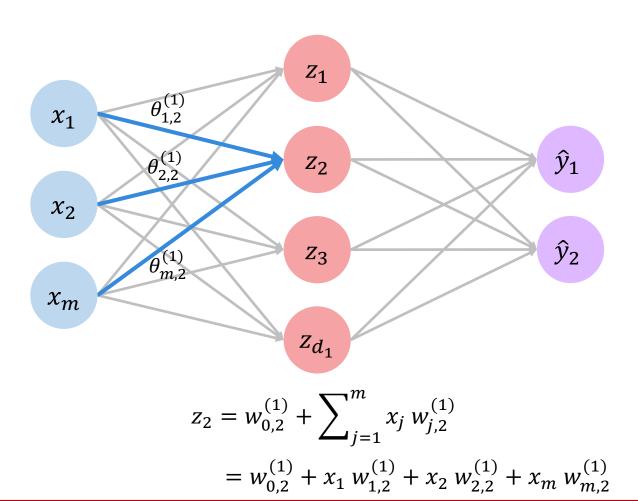
$$z_{\underline{i}} = w_{0,\underline{i}} + \sum_{j=1}^{m} x_j w_{j,\underline{i}}$$

#### Single Layer Neural Network



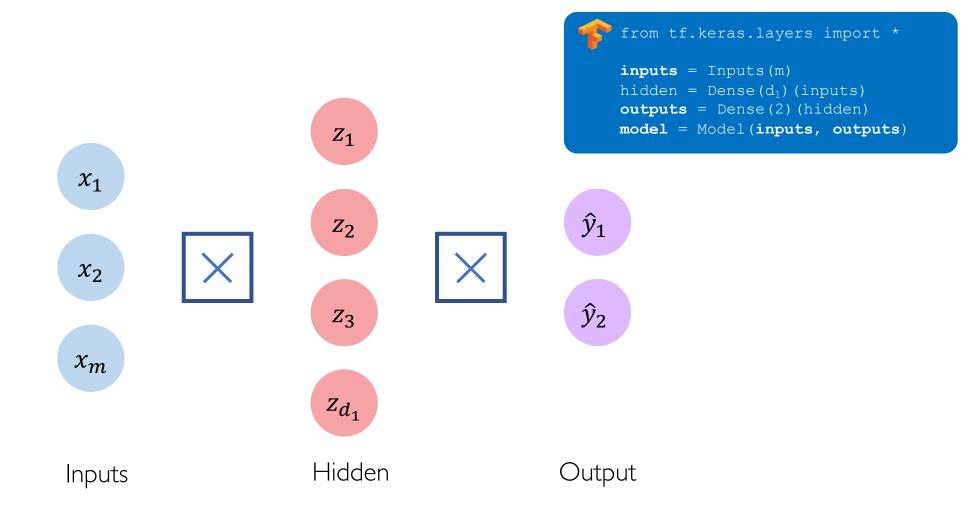


#### Single Layer Neural Network

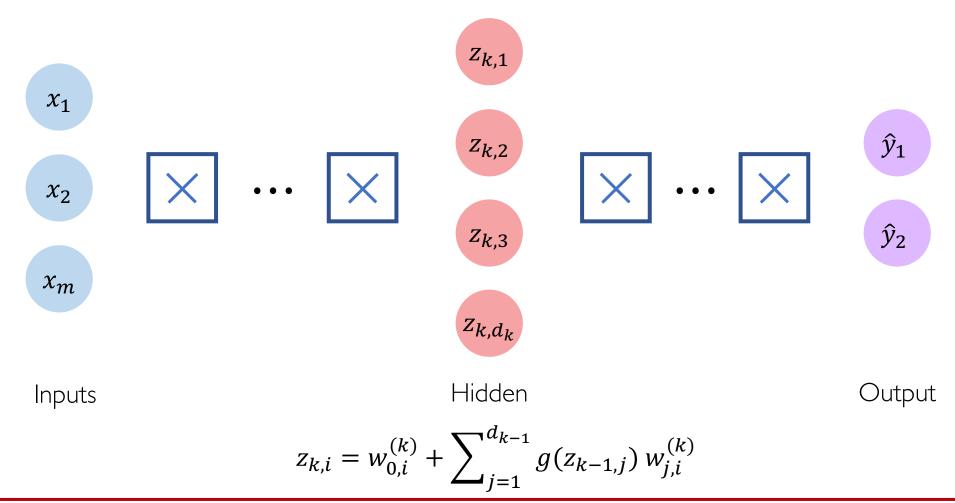




#### Multi Output Perceptron



#### Deep Neural Network



### Applying Neural Networks

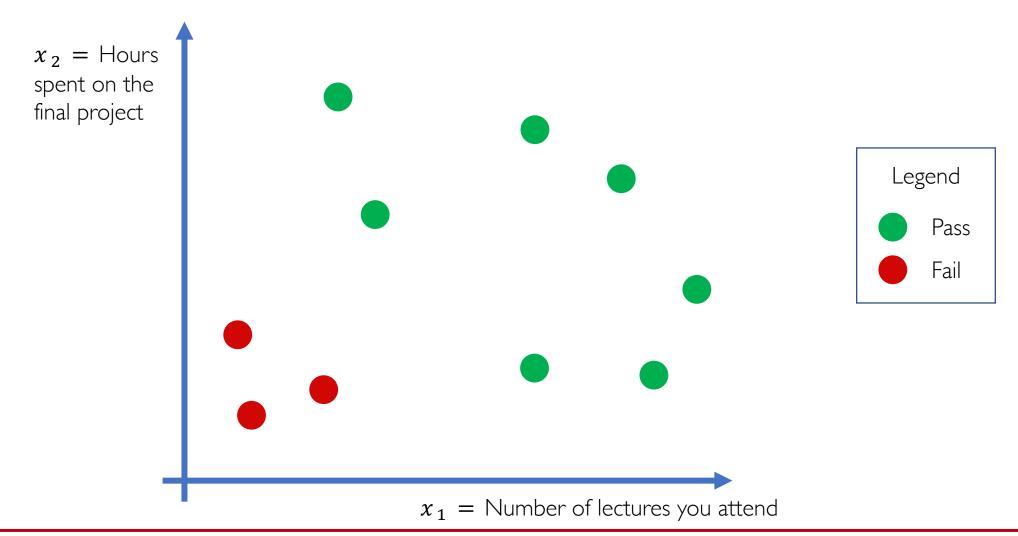
#### **Example Problem**

Will I pass this class?

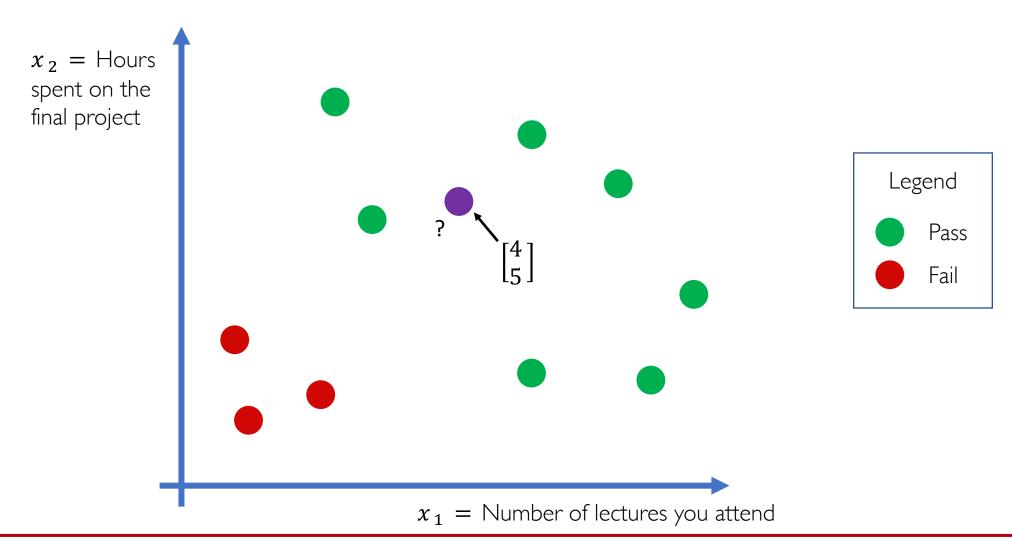
Let's start with a simple two feature model

 $x_1$  = Number of lectures you attend

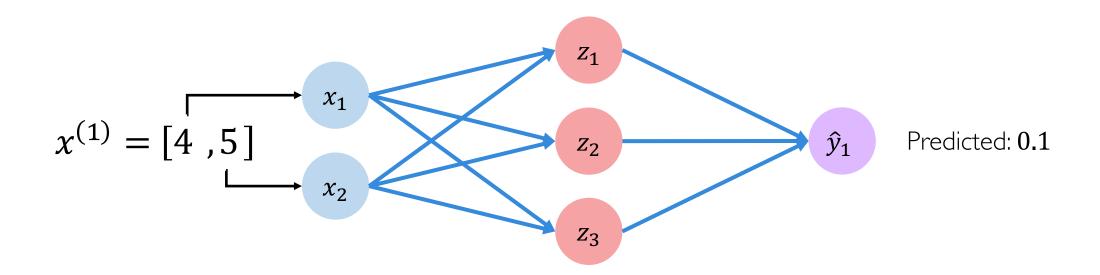
 $x_2$  = Hours spent on the final project

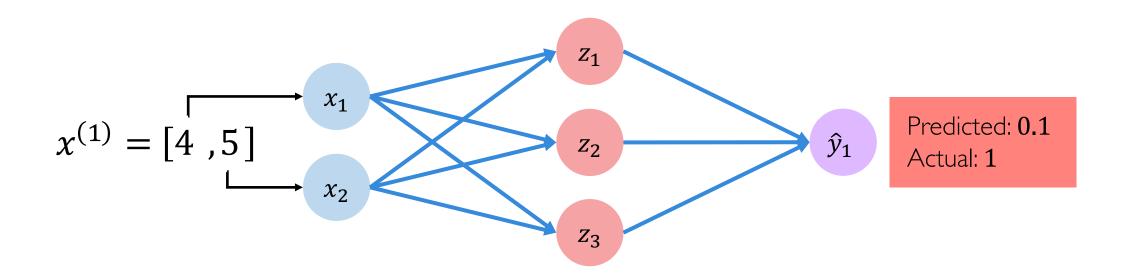






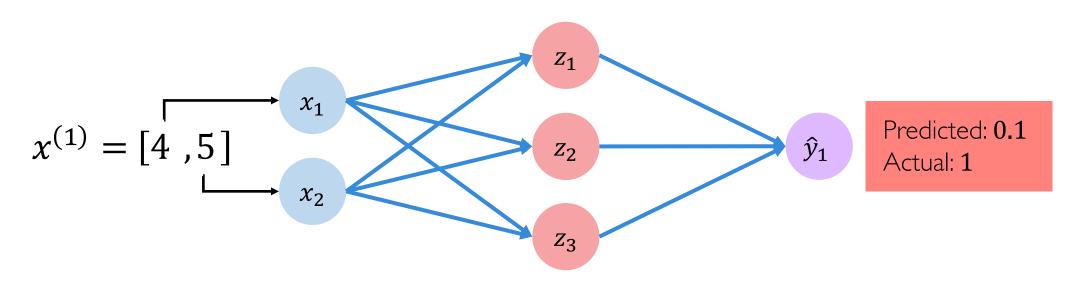






### Quantifying Loss

The **loss** of our network measures the cost incurred from incorrect predictions



$$\mathcal{L}\left(f\left(x^{(i)};W\right),y^{(i)}\right)$$
Predicted Actual



#### **Empirical Loss**

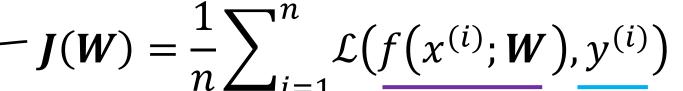
The **empirical loss** measures the total loss over our entire dataset

$$X = \begin{bmatrix} 4 & 5 \\ 2 & 1 \\ 5 & 8 \\ \vdots & \vdots \end{bmatrix} \qquad \begin{array}{c} x_1 \\ x_2 \\ \hline \end{array}$$

$$\begin{array}{c} f(x) & y \\ \hline 0.1 \\ 0.8 \\ 0.6 \\ \vdots \end{array}$$

Also known as:

- Objective function
- Cost function
- Empirical Risk



Predicted

Actual

### Binary Cross Entropy Loss

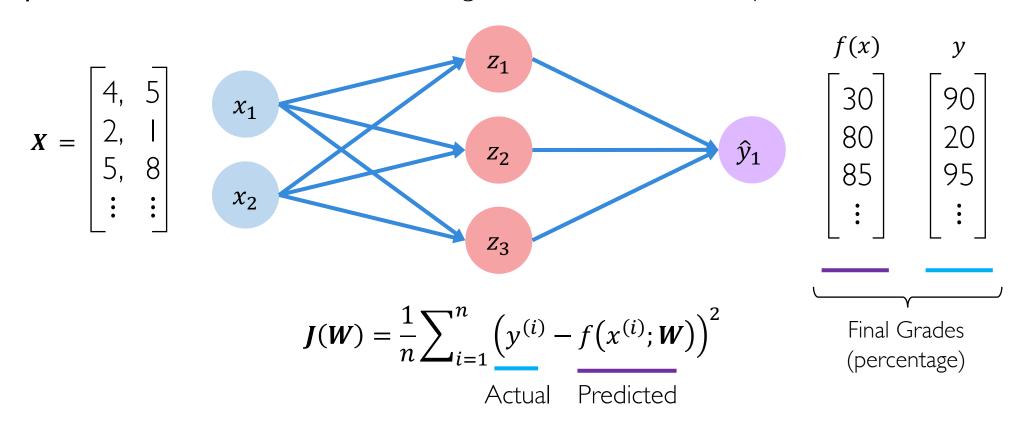
Cross entropy loss can be used with models that output a probability between 0 and 1

$$\mathbf{X} = \begin{bmatrix} 4, & 5 \\ 2, & 1 \\ 5, & 8 \\ \vdots & \vdots \end{bmatrix} \qquad \begin{array}{c} x_1 \\ x_2 \\ x_3 \end{array} \qquad \begin{array}{c} f(x) \\ 0.1 \\ 0.8 \\ 0.6 \\ \vdots \end{array} \qquad \begin{bmatrix} 1 \\ 0 \\ 0.6 \\ \vdots \end{bmatrix}$$

$$J(\mathbf{W}) = \frac{1}{n} \sum_{i=1}^{n} y^{(i)} \log \left( f(x^{(i)}; \mathbf{W}) \right) + (1 - y^{(i)}) \log \left( 1 - f(x^{(i)}; \mathbf{W}) \right)$$
Actual Predicted Actual Predicted

#### Mean Squared Error Loss

Mean squared error loss can be used with regression models that output continuous real numbers



# Training Neural Networks

We want to find the network weights that achieve the lowest loss

$$W^* = \underset{W}{\operatorname{argmin}} \frac{1}{n} \sum_{i=1}^{n} \mathcal{L}(f(x^{(i)}; W), y^{(i)})$$
$$W^* = \underset{W}{\operatorname{argmin}} J(W)$$

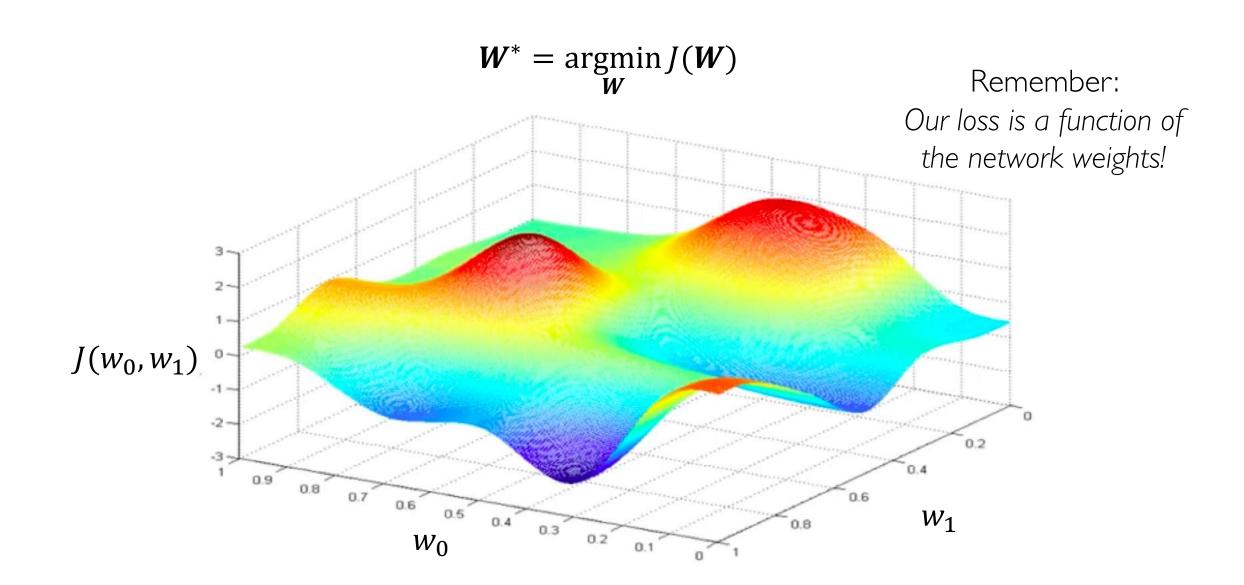
We want to find the network weights that achieve the lowest loss

$$\boldsymbol{W}^* = \underset{\boldsymbol{W}}{\operatorname{argmin}} \frac{1}{n} \sum_{i=1}^{n} \mathcal{L}(f(\boldsymbol{x}^{(i)}; \boldsymbol{W}), \boldsymbol{y}^{(i)})$$

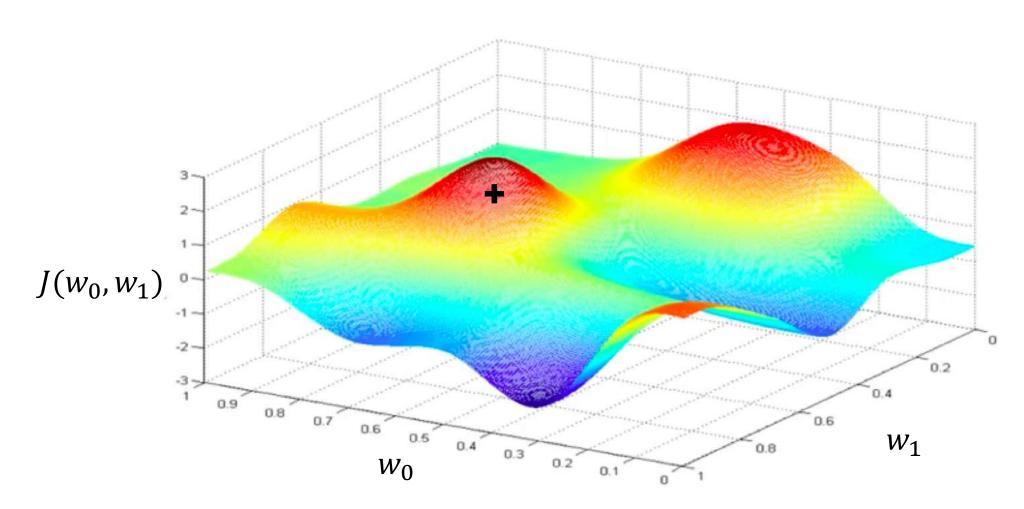
$$\boldsymbol{W}^* = \underset{\boldsymbol{W}}{\operatorname{argmin}} J(\boldsymbol{W})$$

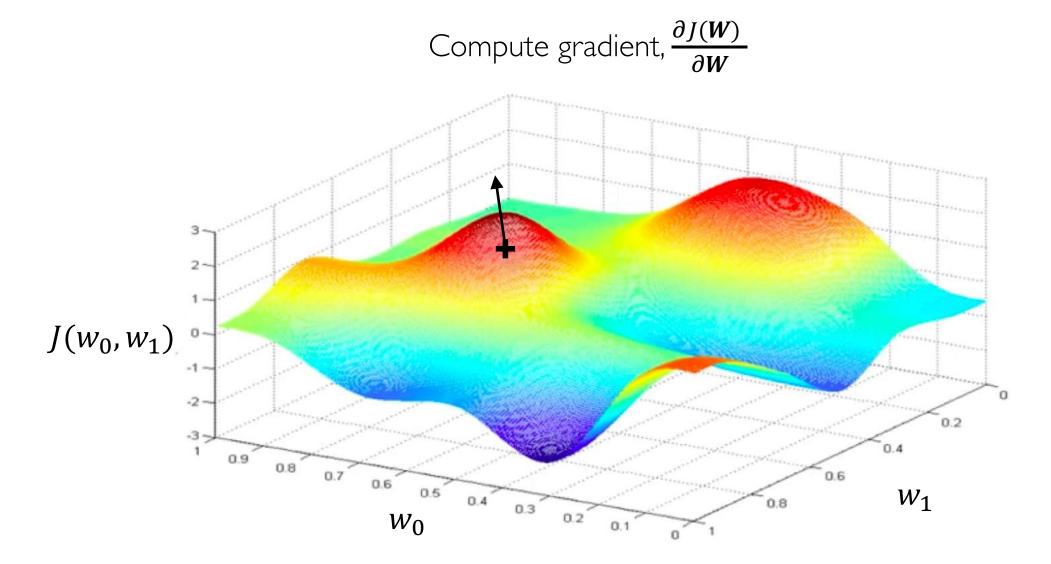
$$\overset{\text{Remember:}}{\boldsymbol{W}}$$

$$\boldsymbol{W} = \{\boldsymbol{W}^{(0)}, \boldsymbol{W}^{(1)}, \dots\}$$

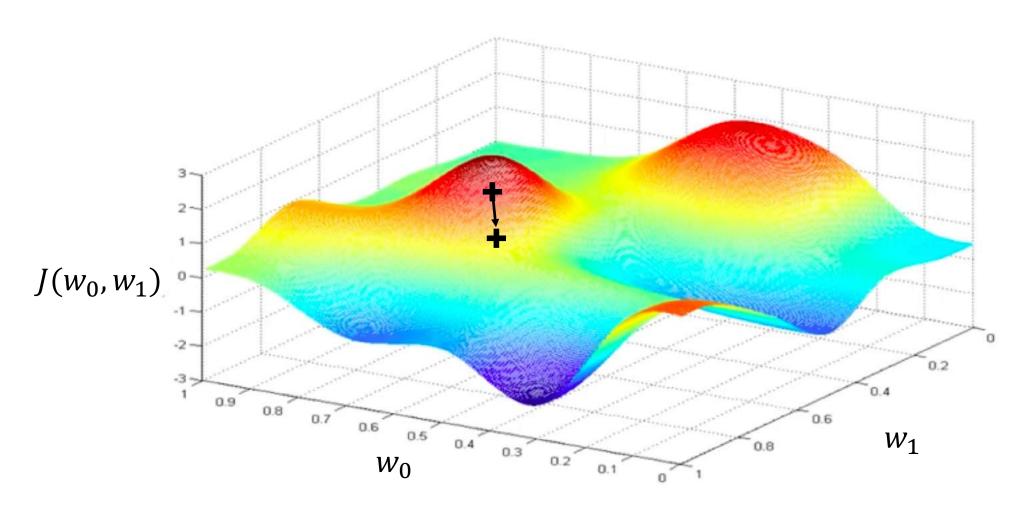


Randomly pick an initial  $(w_0, w_1)$ 



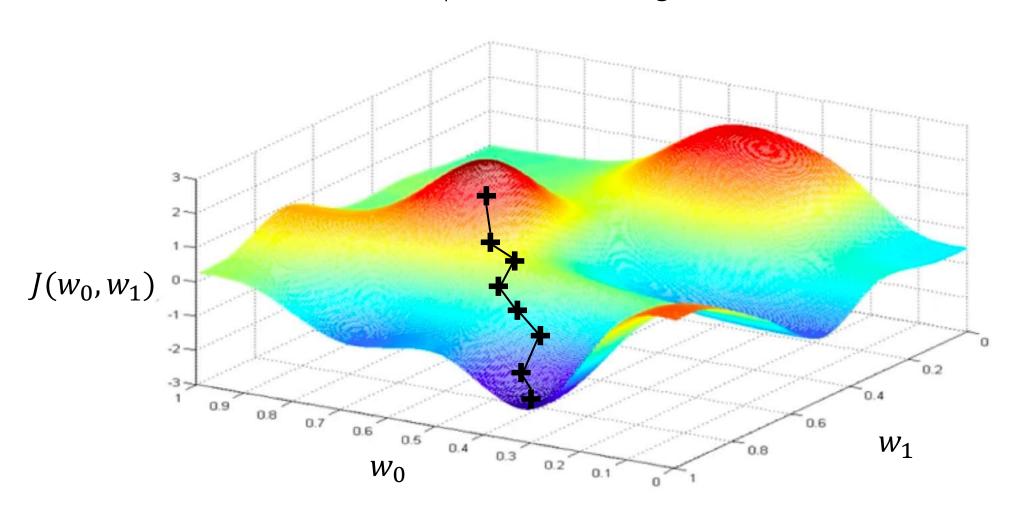


Take small step in opposite direction of gradient



#### Gradient Descent

Repeat until convergence



#### Gradient Descent

#### **Algorithm**

Initialize weights randomly  $\sim \mathcal{N}(0, \sigma^2)$ 



- Loop until convergence:
- Compute gradient,  $\frac{\partial J(W)}{\partial W}$ 3.
- Update weights,  $W \leftarrow W \eta \frac{\partial J(W)}{\partial W}$
- grads = tf.gradients(ys=loss, xs=weights)
- weights\_new = weights.assign(weights lr \* grads)

5. Return weights

#### Gradient Descent

#### **Algorithm**

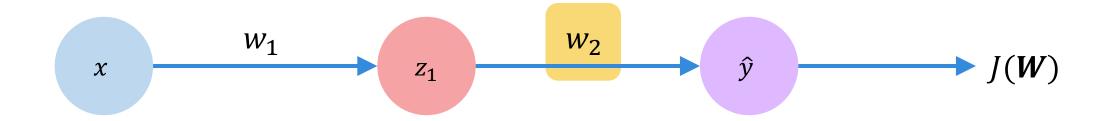
Initialize weights randomly  $\sim \mathcal{N}(0, \sigma^2)$ 



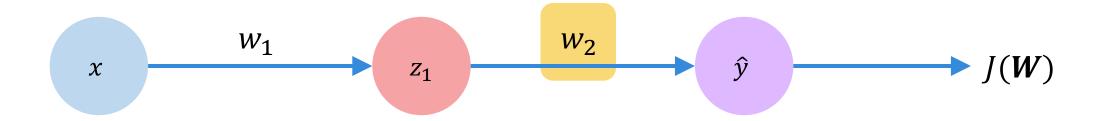
- Loop until convergence:
- 3.
- Compute gradient,  $\frac{\partial J(W)}{\partial W}$ Update weights,  $W \leftarrow W \eta \frac{\partial J(W)}{\partial W}$
- weights\_new = weights.assign(weights lr \* grads)

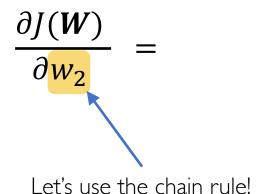
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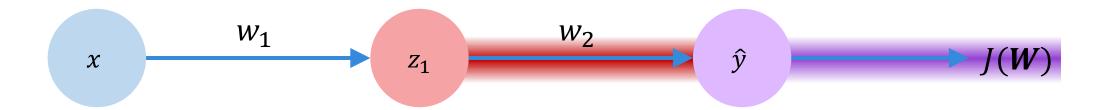


How does a small change in one weight (ex.  $w_2$ ) affect the final loss J(W)?

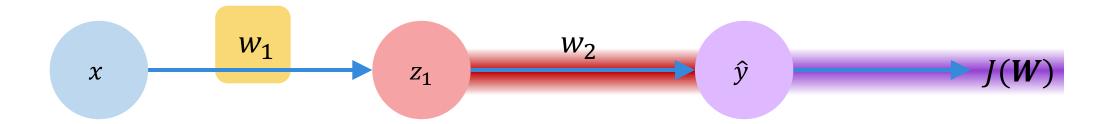


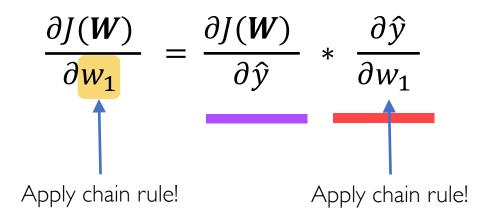




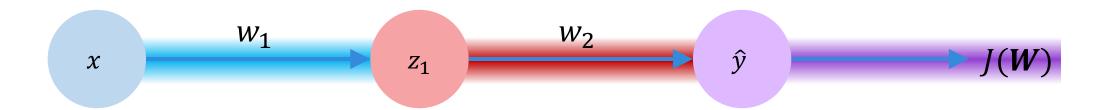


$$\frac{\partial J(\mathbf{W})}{\partial w_2} = \frac{\partial J(\mathbf{W})}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial w_2}$$

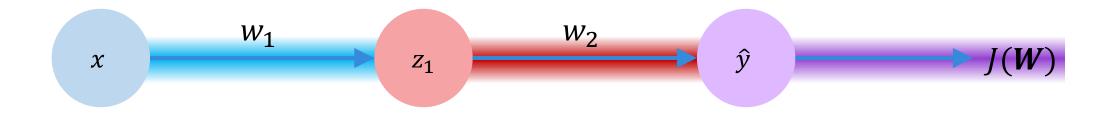








$$\frac{\partial J(\mathbf{W})}{\partial w_1} = \frac{\partial J(\mathbf{W})}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial z_1} * \frac{\partial z_1}{\partial w_1}$$

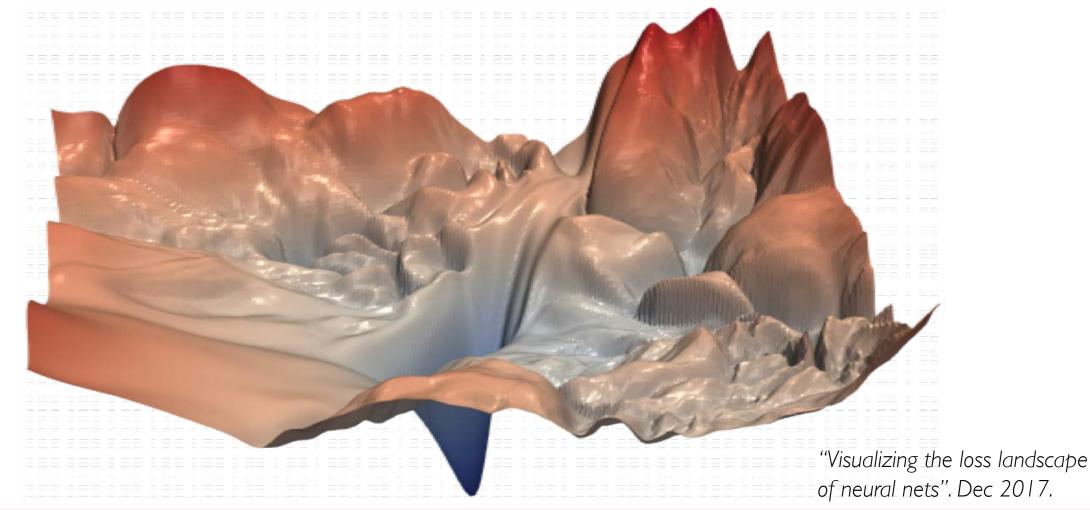


$$\frac{\partial J(\mathbf{W})}{\partial w_1} = \frac{\partial J(\mathbf{W})}{\partial \hat{y}} * \frac{\partial \hat{y}}{\partial z_1} * \frac{\partial z_1}{\partial w_1}$$

Repeat this for every weight in the network using gradients from later layers

# Neural Networks in Practice: Optimization

#### Training Neural Networks is Difficult



#### Loss Functions Can Be Difficult to Optimize

#### Remember:

Optimization through gradient descent

$$\boldsymbol{W} \leftarrow \boldsymbol{W} - \eta \, \frac{\partial J(\boldsymbol{W})}{\partial \boldsymbol{W}}$$

#### Loss Functions Can Be Difficult to Optimize

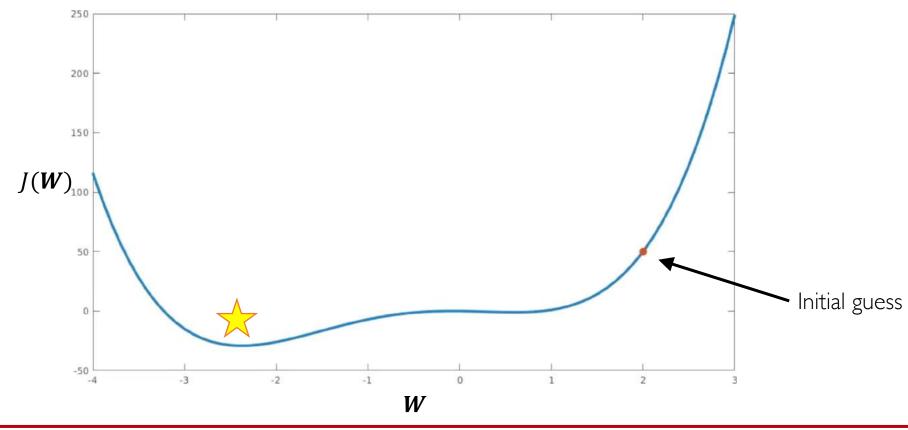
#### Remember:

Optimization through gradient descent

$$W \leftarrow W - \frac{\partial J(W)}{\partial W}$$
How can we set the learning rate?

# Setting the Learning Rate

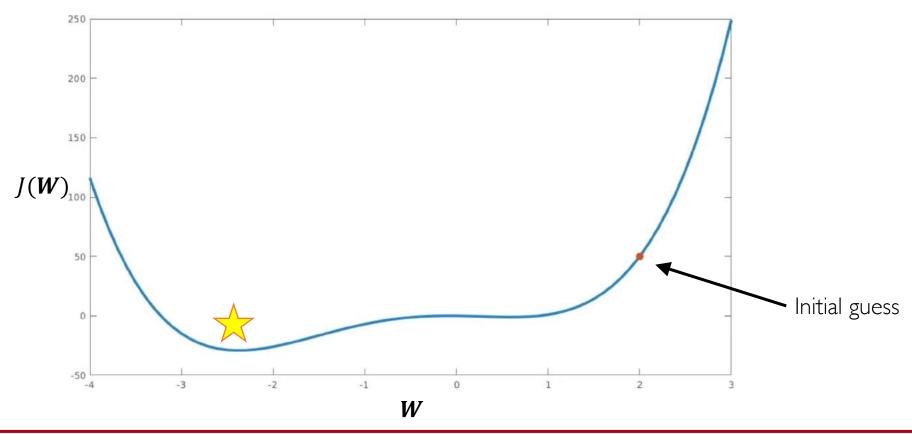
**Small learning rate** converges slowly and gets stuck in false local minima





# Setting the Learning Rate

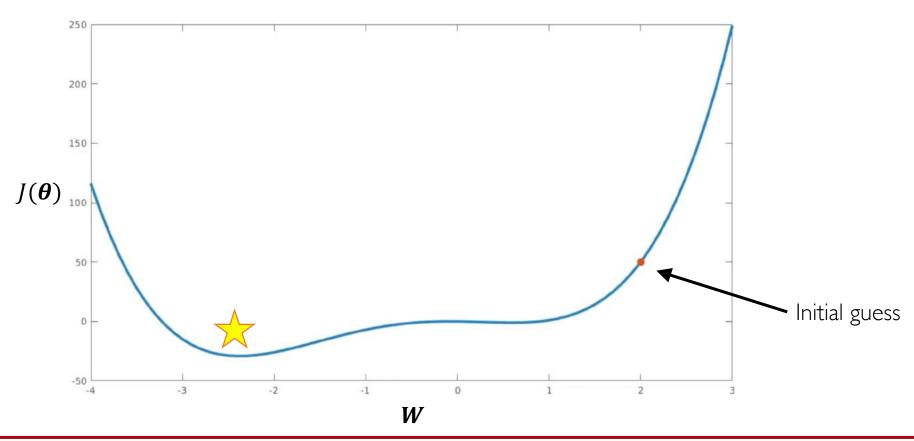
Large learning rates overshoot, become unstable and diverge





# Setting the Learning Rate

Stable learning rates converge smoothly and avoid local minima



#### How to deal with this?

#### Idea I:

Try lots of different learning rates and see what works "just right"

#### How to deal with this?

#### Idea I:

Try lots of different learning rates and see what works "just right"

#### Idea 2:

Do something smarter!

Design an adaptive learning rate that "adapts" to the landscape



#### Adaptive Learning Rates

- Learning rates are no longer fixed
- Can be made larger or smaller depending on:
  - how large gradient is
  - how fast learning is happening
  - size of particular weights
  - etc...

### Adaptive Learning Rate Algorithms

- Momentum
- Adagrad
- Adadelta
- Adam
- RMSProp









tf.train.RMSPropOptimizer

Qian et al. "On the momentum term in gradient descent learning algorithms." 1999.

Duchi et al. "Adaptive Subgradient Methods for Online Learning and Stochastic Optimization." 2011.

Zeiler et al. "ADADELTA: An Adaptive Learning Rate Method." 2012.

Kingma et al. "Adam: A Method for Stochastic Optimization." 2014.

Additional details: <a href="http://ruder.io/optimizing-gradient-descent/">http://ruder.io/optimizing-gradient-descent/</a>

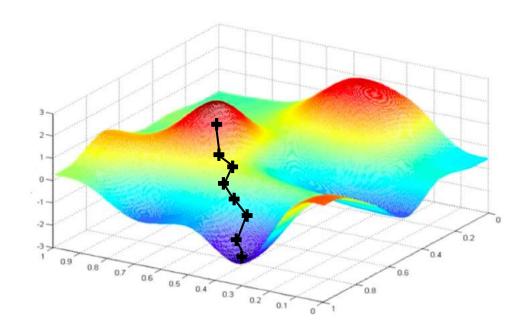


# Neural Networks in Practice: Mini-batches

#### Gradient Descent

#### **Algorithm**

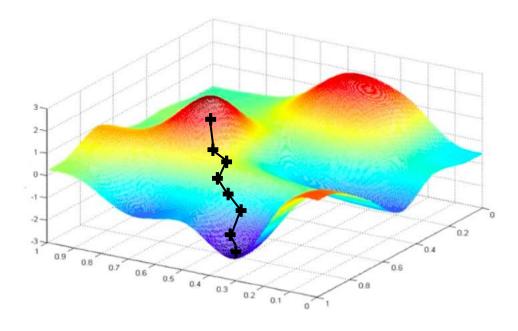
- I. Initialize weights randomly  $\sim \mathcal{N}(0, \sigma^2)$
- 2. Loop until convergence:
- 3. Compute gradient,  $\frac{\partial J(W)}{\partial W}$
- 4. Update weights,  $\mathbf{W} \leftarrow \mathbf{W} \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
- 5. Return weights



## Gradient Descent

#### Algorithm

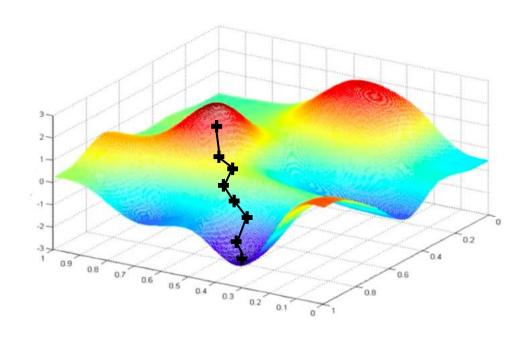
- 1. Initialize weights randomly  $\sim \mathcal{N}(0, \sigma^2)$
- 2. Loop until convergence:
- 3. Compute gradient,  $\frac{\partial J(W)}{\partial W}$
- 4. Update weights,  $\mathbf{W} \leftarrow \mathbf{W} \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
- 5. Return weights



Can be very computational to compute!

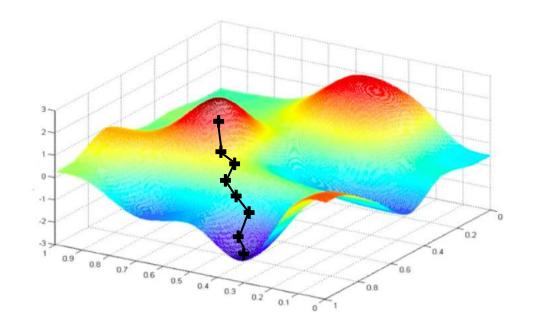
#### Algorithm

- 1. Initialize weights randomly  $\sim \mathcal{N}(0, \sigma^2)$
- 2. Loop until convergence:
- 3. Pick single data point i
- 4. Compute gradient,  $\frac{\partial J_i(W)}{\partial W}$
- 5. Update weights,  $\mathbf{W} \leftarrow \mathbf{W} \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
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#### Algorithm

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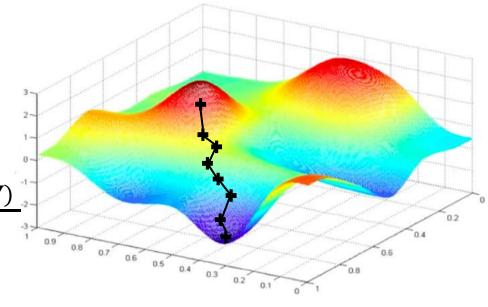
Easy to compute but very noisy (stochastic)!

#### Algorithm

- I. Initialize weights randomly  $\sim \mathcal{N}(0, \sigma^2)$
- 2. Loop until convergence:
- 3. Pick batch of B data points

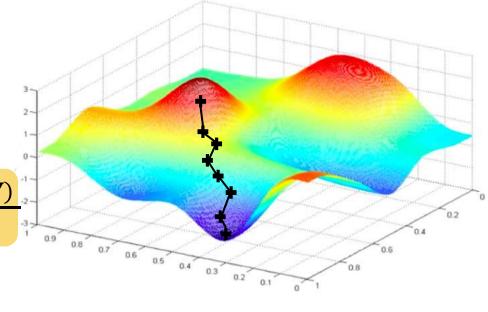
4. Compute gradient, 
$$\frac{\partial J(W)}{\partial W} = \frac{1}{B} \sum_{k=1}^{B} \frac{\partial J_k(W)}{\partial W}$$

- 5. Update weights,  $\mathbf{W} \leftarrow \mathbf{W} \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
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#### **Algorithm**

- I. Initialize weights randomly  $\sim \mathcal{N}(0, \sigma^2)$
- 2. Loop until convergence:
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- 5. Update weights,  $\mathbf{W} \leftarrow \mathbf{W} \eta \frac{\partial J(\mathbf{W})}{\partial \mathbf{W}}$
- 6. Return weights



Fast to compute and a much better estimate of the true gradient!

## Mini-batches while training

#### More accurate estimation of gradient

Smoother convergence Allows for larger learning rates

## Mini-batches while training

#### More accurate estimation of gradient

Smoother convergence
Allows for larger learning rates

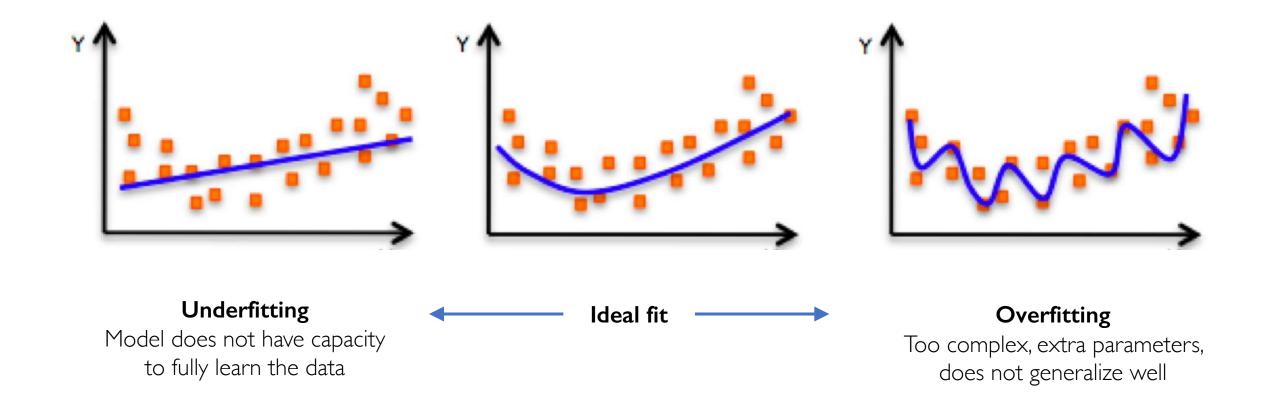
#### Mini-batches lead to fast training!

Can parallelize computation + achieve significant speed increases on GPU's



# Neural Networks in Practice: Overfitting

## The Problem of Overfitting



## Regularization

#### What is it?

Technique that constrains our optimization problem to discourage complex models

## Regularization

#### What is it?

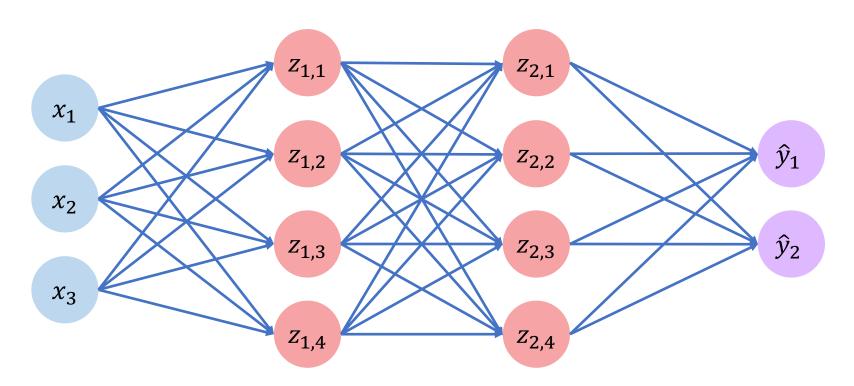
Technique that constrains our optimization problem to discourage complex models

#### Why do we need it?

Improve generalization of our model on unseen data

## Regularization 1: Dropout

During training, randomly set some activations to 0

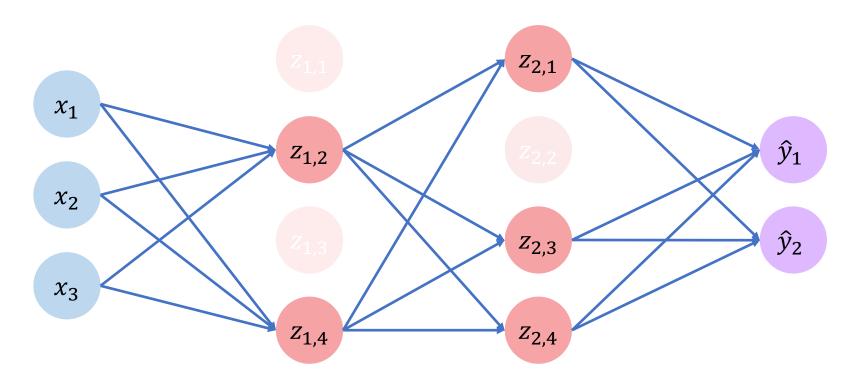




## Regularization 1: Dropout

- During training, randomly set some activations to 0
  - Typically 'drop' 50% of activations in layer
  - Forces network to not rely on any I node



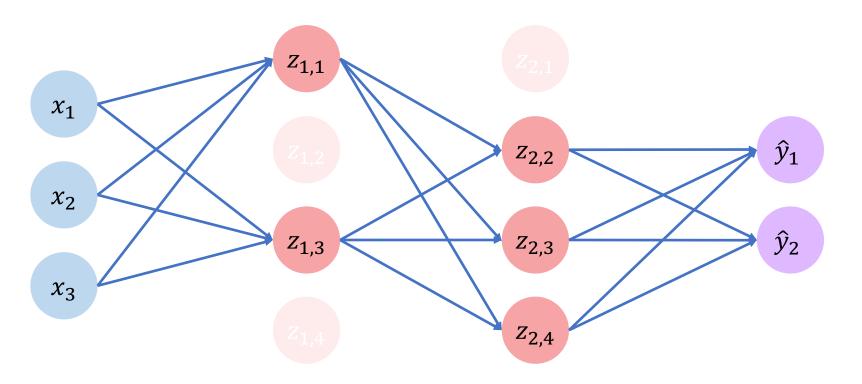




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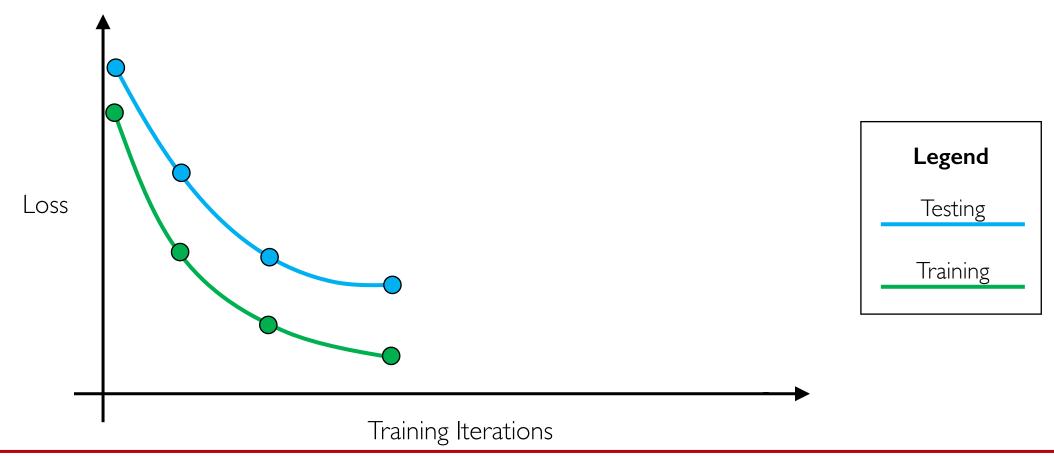


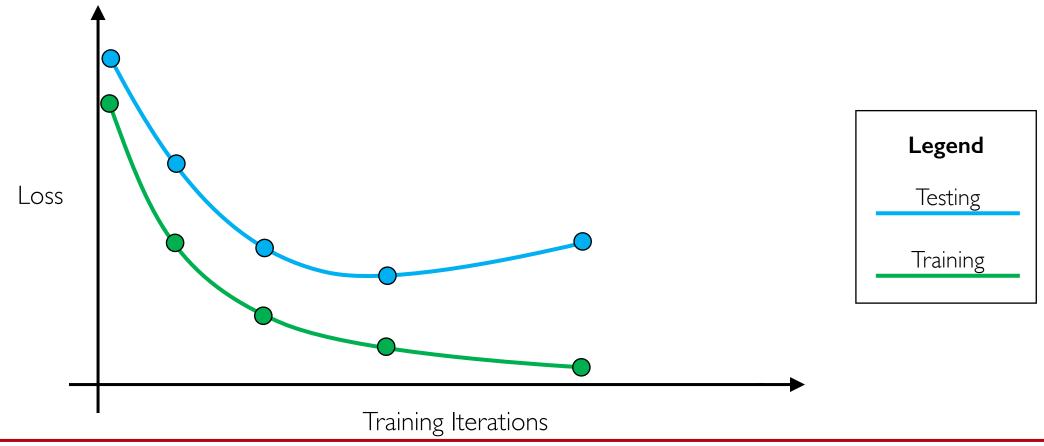




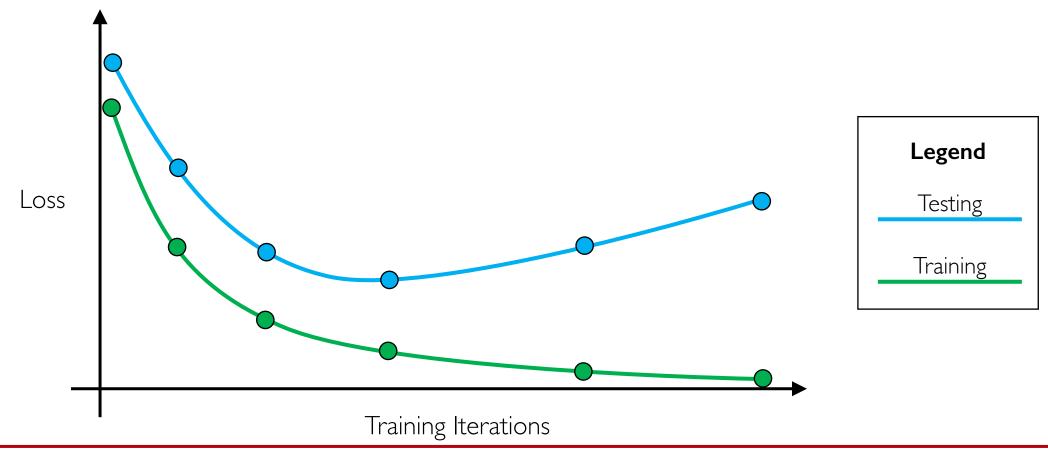


















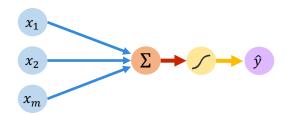




#### Core Foundation Review

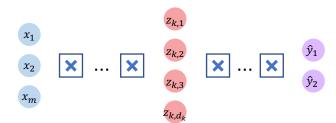
#### The Perceptron

- Structural building blocks
- Nonlinear activation functions



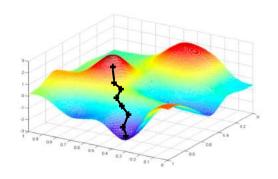
#### Neural Networks

- Stacking Perceptrons to form neural networks
- Optimization through backpropagation



#### Training in Practice

- Adaptive learning
- Batching
- Regularization



# Questions?