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| Course Code: CS481 | Course Name: Data Science |
| Instructor Name: Dr Muhammad Atif Tahir and Zeeshan Khan | |
| Student Roll No: | Section No: |

Instructions:

- Return the question paper.
- Read each question completely before answering it. There are **3** questions and **2** pages
- Show all steps clearly.

Time: 60 minutes.

Max Marks: 12.5 points

Question 2 [1.5 Points]: Figure 1 outlines data science progression aiming to reduce the immaturity of capabilities and capacity. Complete the table below regarding space A, B, C, D. (If u wish, you can answer directly in question paper)

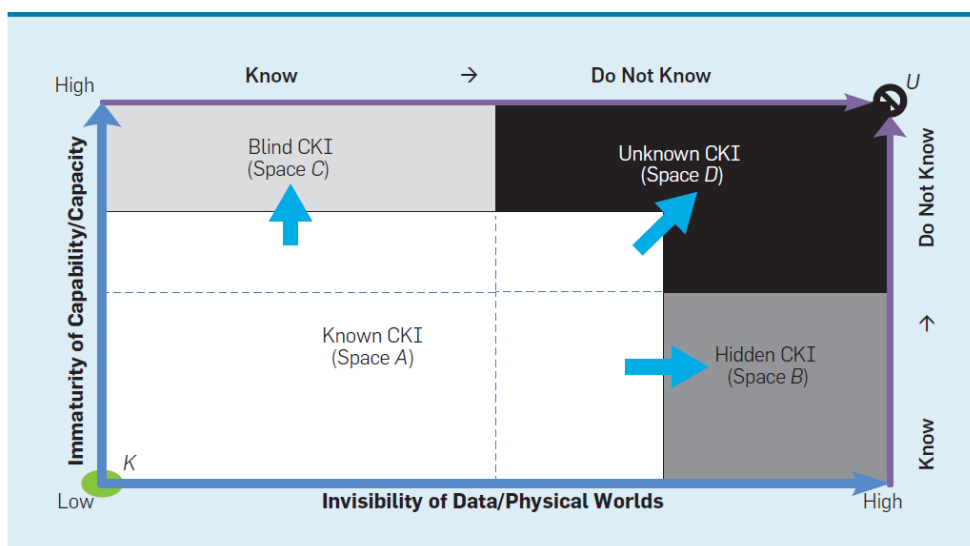


Figure 1: Data Science Space.

| Space | Description | Example |
|-------------------|--------------------|------------------------------------|
| A (Known space) | I know what I know | Profiling and Descriptive Analysis |
| B (Hidden space) | | |
| C (Blind space) | | |
| D (unknown space) | | |

Solution

| Space | Description | Example |
|------------------|---|--|
| A (Known space) | I know what I know about visible world | Profiling and Descriptive Analysis |
| B (Hidden space) | I know what I do not know about unseen world | Examples include existing IID models (such as k-means and the k-nearest neighbors algorithm) that can-not handle non-IID data. |
| C (Blind space) | I do not know what I know about the world | When even established social scientists try to address a data science problem. |

| | | |
|-------------------|----------------------------------|--|
| D (unknown space) | I do not know what I do not know | In the world of fast-evolving big data, CKI invisibility increases, resulting in an ever-larger unknown space. |
|-------------------|----------------------------------|--|

Question 3 [6 Points]

Consider the algorithm below published in paper titled “Weighted k-Nearest-Neighbor Techniques and Ordinal Classification”. This algorithm discusses weighted kNN classifier. You need to classify new data points from Table below using wKNN classifier. Use $k = 4$, city block distance: $d(p,q) = \sum_i |p_i - q_i|$, and compute kernel using inversion kernel $(1/|d|)$. Note that $I(x)$ is the indicator function which evaluates to 1 when the argument x is true and 0 otherwise

| Instance # | Att1 | Att2 | Actual Class |
|------------|------|------|--------------|
| 1 | 2 | 3 | 0 |
| 2 | 1 | 5 | 1 |
| 3 | 4 | 2 | 1 |
| 4 | 2 | 5 | 0 |
| 5 | 6 | 8 | 0 |

| Instance # | Att1 | Att2 | Predicted Class |
|------------|------|------|-----------------|
| 1 | 3 | 1 | ? |
| 2 | 2 | 2 | ? |

Training and Test Data for Question 3.

Weighted k-Nearest-Neighbor classification (wkNN)

1. Let $L = \{(y_i, x_i), i = 1, \dots, n_L\}$ be a learning set of observations x_i with given class membership y_i and let x be a new observation, whose class label y has to be predicted.
2. Find the $k + 1$ nearest neighbors to x according to a distance function $d(x, x_i)$.
3. The $(k + 1)$ th neighbor is used for standardization of the k smallest distances via

$$D_{(i)} = D(x, x_{(i)}) = \frac{d(x, x_{(i)})}{d(x, x_{(k+1)})} \quad .$$

4. Transform the normalized distances $D_{(i)}$ with any kernel function $K(\cdot)$ into weights $w_{(i)} = K(D_{(i)})$.
5. As prediction for the class membership y of observation x choose the class, which shows a weighted majority of the k nearest neighbors

$$\hat{y} = \max_r \left(\sum_{i=1}^k w_{(i)} I(y_{(i)} = r) \right) \quad .$$

Figure 2: wkNN classifier.

For test sample 1

$D1 = |3-2| + |1-3| = 1 + 2 = 3$; $W1 = 3 / 10 = 0.3$, $K(x,x(1)) = 1 / 0.3 = 3.34$
 $D2 = |3-1| + |1-5| = 2 + 4 = 6$, $W2 = 6/10 = 0.6$, $K(x,x(2)) = 1/0.6 = 1.67$
 $D3 = |3-4| + |1-2| = 1 + 1 = 2$, $W3 = 0.2$, $K(x,x(3)) = 1/0.2 = 5$
 $D4 = |3-2| + |1-5| = 1 + 4 = 5$, $W4 = 0.5$, $K(x,x(4)) = 1/0.5 = 2$
 $D5 = |3-6| + |1-8| = 3 + 7 = 10$, $W5 = 1$,

For 0; $3.34 + 2 = 5.34$ and For 1; $1.67+5 = 6.67$ thus belongs to 1

For test sample 2

$D1 = |2-2| + |2-3| = 0 + 1 = 1$; $W1 = 1 / 10 = 0.1$, $K(x,x(1)) = 1 / 0.1 = 10$
 $D2 = |2-1| + |2-5| = 1 + 3 = 4$, $W2 = 4/10 = 0.6$, $K(x,x(2)) = 1/0.4 = 2.5$
 $D3 = |2-4| + |2-2| = 2 + 0 = 2$, $W3 = 0.2$, $K(x,x(3)) = 1/0.2 = 5$
 $D4 = |2-2| + |2-5| = 0 + 3 = 3$, $W4 = 0.3$, $K(x,x(4)) = 1/0.3 = 3.33$
 $D5 = |2-6| + |2-8| = 3 + 7 = 10$, $W5 = 1$,

For 0; $10 + 3.33 = 13.33$ and For 1; $2.5+5 = 7.5$ thus belongs to 0

BEST OF LUCK!