

Chapter 14: Basics of Functional Dependencies and Normalization of Relational Databases

Database Systems CS203



Outline

- Informal Design Guidelines for Relational Schema
- Functional Dependencies
- Normalization

Informal Design Guidelines for Relational Databases

- What is relational database design?
 - The grouping of attributes to form "good" relation schemas
- Two levels of relation schemas
 - The logical "user view" level
 - The storage "base relation" level
- Design is concerned mainly with base relations
- What are the criteria for "good" base relations?

Information Design Guidelines for Relational Databases

- We first discuss informal guidelines for good relational design
- Then we discuss formal concepts of functional dependencies and normal forms
 - - 1NF (First Normal Form)
 - - 2NF (Second Normal Form)
 - - 3NF (Third Normal Form)
 - - BCNF (Boyce-Codd Normal Form)
- Additional types of dependencies, further normal forms, relational design algorithms by synthesis are discussed in Chapter 15

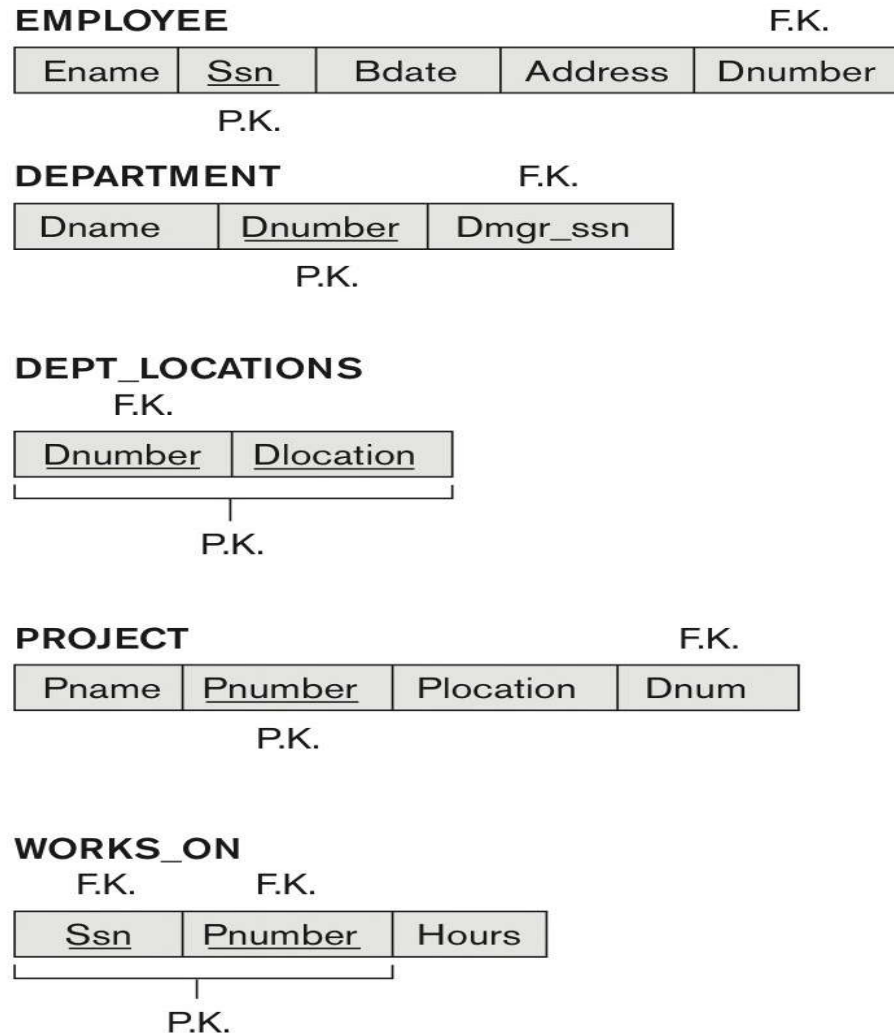
Four Informal Guidelines

- Semantics of attributes should be clear.
- Reducing the redundant information in tuples
- Reducing the NULL values in tuples
- Avoiding fake tuples

Semantics of the Relational Attributes must be clear

- GUIDELINE 1: Informally, each tuple in a relation should represent one entity or relationship instance. (Applies to individual relations and their attributes).
 - Attributes of different entities (EMPLOYEEs, DEPARTMENTs, PROJECTs) should not be mixed in the same relation
 - Only foreign keys should be used to refer to other entities
 - Entity and relationship attributes should be kept apart as much as possible.
- Bottom Line: *Design a schema that can be explained easily relation by relation. The semantics of attributes should be easy to interpret.*

Figure 14.1 A simplified COMPANY relational database schema



Redundant Information in Tuples

- Information is stored redundantly
 - Wastes storage
 - Causes problems with update anomalies
 - Insertion anomalies
 - Deletion anomalies
 - Modification anomalies

Example of An UPDATE Anomaly

- Consider the relation:
 - EMP_PROJ(Emp#, Proj#, Ename, Pname, No_hours)
- Update Anomaly:
 - Changing the name of project number P1 from “Billing” to “Customer-Accounting” may cause this update to be made for all 100 employees working on project P1.

Example of An INSERT Anomaly

- Consider the relation:
 - EMP_PROJ(Emp#, Proj#, Ename, Pname, No_hours)
- Insert Anomaly:
 - Cannot insert a project unless an employee is assigned to it.
- Conversely
 - Cannot insert an employee unless he/she is assigned to a project.

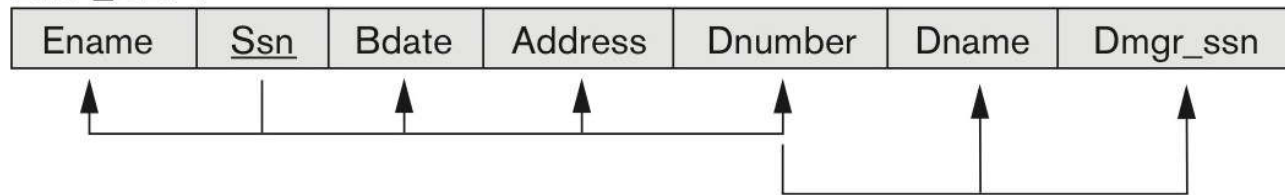
Example of a DELETE Anomaly

- Consider the relation:
 - EMP_PROJ(Emp#, Proj#, Ename, Pname, No_hours)
- Delete Anomaly:
 - When a project is deleted, it will result in deleting all the employees who work on that project.
 - Alternately, if an employee is the sole employee on a project, deleting that employee would result in deleting the corresponding project.

Figure 14.3 Two relation schemas suffering from update anomalies

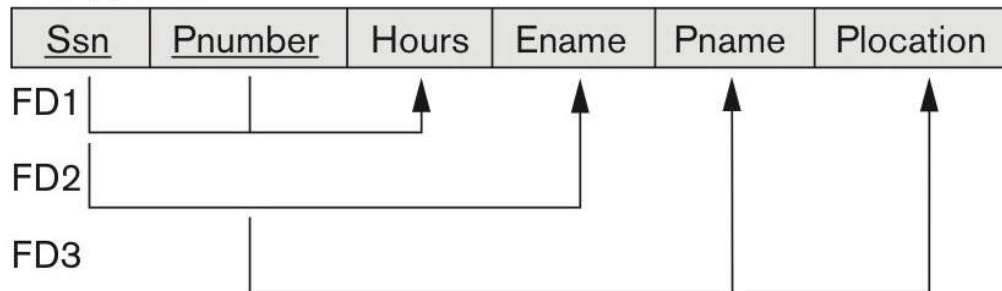
(a)

EMP_DEPT



(b)

EMP_PROJ



Guideline for Redundant Information in Tuples and Update Anomalies

- GUIDELINE 2:

- Design a schema that does not suffer from the insertion, deletion and update anomalies.
- If there are any anomalies present, then note them so that applications can be made to take them into account.

Null Values in Tuples

- GUIDELINE 3:

- Relations should be designed such that their tuples will have as few NULL values as possible
- Attributes that are NULL frequently could be placed in separate relations (with the primary key)
- Reasons for nulls:
 - Attribute not applicable or invalid
 - Attribute value unknown (may exist)
 - Value known to exist, but unavailable

Generation of Spurious Tuples

- Bad designs for a relational database may result in erroneous results for certain JOIN operations
- The "lossless join" property is used to guarantee meaningful results for join operations
- GUIDELINE 4:
 - The relations should be designed to satisfy the lossless join condition.
 - No spurious tuples should be generated by doing a natural-join of any relations.

Spurious Tuples

There are two important properties of decompositions:

- a) Non-additive or losslessness of the corresponding join
- b) Preservation of the functional dependencies.

Note that:

Property (a) is extremely important and cannot be sacrificed.
Property (b) is less stringent and may be sacrificed. (See Chapter 15).

Functional Dependencies

- Functional dependencies (FDs)
 - Are used to specify *formal measures* of the "goodness" of relational designs
 - And keys are used to define **normal forms** for relations
 - Are **constraints** that are derived from the *meaning* and *interrelationships* of the data attributes
- A set of attributes X *functionally determines* a set of attributes Y if the value of X determines a unique value for Y

Defining Functional Dependencies

- $X \rightarrow Y$ holds if whenever two tuples have the same value for X , they *must have* the same value for Y
 - For any two tuples t_1 and t_2 in any relation instance $r(R)$: If $t_1[X]=t_2[X]$, *then* $t_1[Y]=t_2[Y]$
- $X \rightarrow Y$ in R specifies a *constraint* on all relation instances $r(R)$
- Written as $X \rightarrow Y$; can be displayed graphically on a relation schema as in Figures. (denoted by the arrow:).
- FDs are derived from the real-world constraints on the attributes

Examples of FD Constraints

- Social security number determines employee name
 - $SSN \rightarrow ENAME$
- Project number determines project name and location
 - $PNUMBER \rightarrow \{PNAME, PLOCATION\}$
- Employee ssn and project number determines the hours per week that the employee works on the project
 - $\{SSN, PNUMBER\} \rightarrow HOURS$

Examples of FD Constraints

- An FD is a property of the attributes in the schema R
- The constraint must hold on *every* relation instance $r(R)$
- If K is a key of R , then K functionally determines all attributes in R
 - (since we never have two distinct tuples with $t_1[K] = t_2[K]$)

Figure 14.7 Ruling Out FDs

Note that given the state of the TEACH relation, we can say that the FD: Text \rightarrow Course may exist. However, the FDs Teacher \rightarrow Course, Teacher \rightarrow Text and Course \rightarrow Text are ruled out.

TEACH

Teacher	Course	Text
Smith	Data Structures	Bartram
Smith	Data Management	Martin
Hall	Compilers	Hoffman
Brown	Data Structures	Horowitz

Figure 14.8 What FDs may exist?

- A relation $R(A, B, C, D)$ with its extension.
- Which FDs may exist in this relation?

A	B	C	D
a1	b1	c1	d1
a1	b2	c2	d2
a2	b2	c2	d3
a3	b3	c4	d3

Normal Forms Based on Primary Keys

- Normalization of Relations
- Practical Use of Normal Forms
- Definitions of Keys and Attributes Participating in Keys
- First Normal Form
- Second Normal Form
- Third Normal Form

Normalization of Relations

- **Normalization:**

- The process of decomposing unsatisfactory "bad" relations by breaking up their attributes into smaller relations

- **Normal form:**

- Condition using keys and FDs of a relation to certify whether a relation schema is in a particular normal form

Normalization of Relations

- 2NF, 3NF, BCNF
 - based on keys and FDs of a relation schema
- 4NF
 - based on keys, multi-valued dependencies : MVDs;
- 5NF
 - based on keys, join dependencies : JDs
- Additional properties may be needed to ensure a good relational design (lossless join, dependency preservation; see Chapter 15)

Practical Use of Normal Forms

- **Normalization** is carried out in practice so that the resulting designs are of high quality and meet the desirable properties
- The practical utility of these normal forms becomes questionable when the constraints on which they are based are *hard to understand* or to *detect*
- The database designers *need not* normalize to the highest possible normal form
 - (usually up to 3NF and BCNF. 4NF rarely used in practice.)
- **Denormalization:**
- The process of storing the join of higher normal form relations as a base relation—which is in a lower normal form

Defining of Keys and Attributes Participating in Keys

- A **superkey** of a relation schema $R = \{A_1, A_2, \dots, A_n\}$ is a set of attributes S *subset-of* R with the property that no two tuples t_1 and t_2 in any legal relation state r of R will have $t_1[S] = t_2[S]$
- A **key** K is a **superkey** with the *additional property* that removal of any attribute from K will cause K not to be a superkey any more.

Definitions of Keys and Attributes Participating in Keys (2)

- If a relation schema has more than one key, each is called a **candidate** key.
 - One of the candidate keys is *arbitrarily* designated to be the **primary key**, and the others are called **secondary keys**.
- A **Prime attribute** must be a member of *some* candidate key
- A **Nonprime attribute** is not a prime attribute—that is, it is not a member of any candidate key.

First Normal Form 1NF


- Disallows
 - composite attributes
 - multivalued attributes
 - **nested relations**; attributes whose values for an *individual tuple* are non-atomic
- Considered to be part of the definition of a relation
- Most RDBMSs allow only those relations to be defined that are in First Normal Form

Figure 14.9 Normalization into 1NF

(a)

DEPARTMENT

Dname	<u>Dnumber</u>	Dmgr_ssn	Dlocations



(b)

DEPARTMENT

Dname	<u>Dnumber</u>	Dmgr_ssn	Dlocations
Research	5	333445555	{Bellaire, Sugarland, Houston}
Administration	4	987654321	{Stafford}
Headquarters	1	888665555	{Houston}

(c)

DEPARTMENT

Dname	<u>Dnumber</u>	Dmgr_ssn	<u>Dlocation</u>
Research	5	333445555	Bellaire
Research	5	333445555	Sugarland
Research	5	333445555	Houston
Administration	4	987654321	Stafford
Headquarters	1	888665555	Houston

Figure 14.10 Normalizing nested relations into 1NF

(a)

EMP_PROJ

		Projs	
Ssn	Ename	Pnumber	Hours

(b)

EMP_PROJ

Ssn	Ename	Pnumber	Hours
123456789	Smith, John B.	1	32.5
		2	7.5
666884444	Narayan, Ramesh K.	3	40.0
453453453	English, Joyce A.	1	20.0
		2	20.0
333445555	Wong, Franklin T.	2	10.0
		3	10.0
		10	10.0
		20	10.0
999887777	Zelaya, Alicia J.	30	30.0
		10	10.0
987987987	Jabbar, Ahmad V.	10	35.0
		30	5.0
987654321	Wallace, Jennifer S.	30	20.0
		20	15.0
888665555	Borg, James E.	20	NULL

(c)

EMP_PROJ1

<u>Ssn</u>	Ename
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EMP_PROJ2

<u>Ssn</u>	<u>Pnumber</u>	Hours
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Second Normal Form 2NF

- Uses the concepts of **FDs, primary key**
- Definitions
 - **Prime attribute:** An attribute that is member of the primary key K
 - **Full functional dependency:** a FD $Y \rightarrow Z$ where removal of any attribute from Y means the FD does not hold any more
- Examples:
 - $\{SSN, PNUMBER\} \rightarrow HOURS$ is a full FD since neither $SSN \rightarrow HOURS$ nor $PNUMBER \rightarrow HOURS$ hold
 - $\{SSN, PNUMBER\} \rightarrow ENAME$ is not a full FD (it is called a partial dependency) since $SSN \rightarrow ENAME$ also holds

Second Normal Form

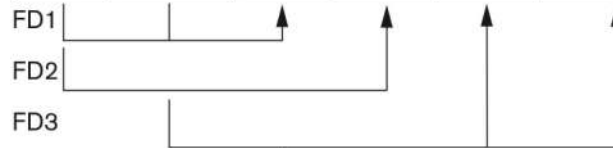
- A relation schema R is in **second normal form (2NF)** if every non-prime attribute A in R is fully functionally dependent on the primary key
- R can be decomposed into 2NF relations via the process of 2NF normalization or “second normalization”

Figure 14.11 Normalizing into 2NF and 3NF

(a)

EMP_PROJ

<u>Ssn</u>	<u>Pnumber</u>	Hours	Ename	Pname	Plocation
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2NF Normalization

EP1

<u>Ssn</u>	<u>Pnumber</u>	Hours
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EP2

<u>Ssn</u>	Ename
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EP3

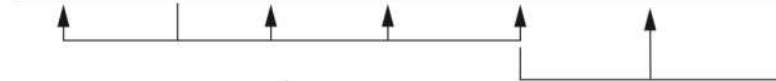
<u>Pnumber</u>	Pname	Plocation
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(b)

EMP_DEPT

Ename	<u>Ssn</u>	Bdate	Address	Dnumber	Dname	Dmgr_ssn
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3NF Normalization

ED1

Ename	<u>Ssn</u>	Bdate	Address	Dnumber
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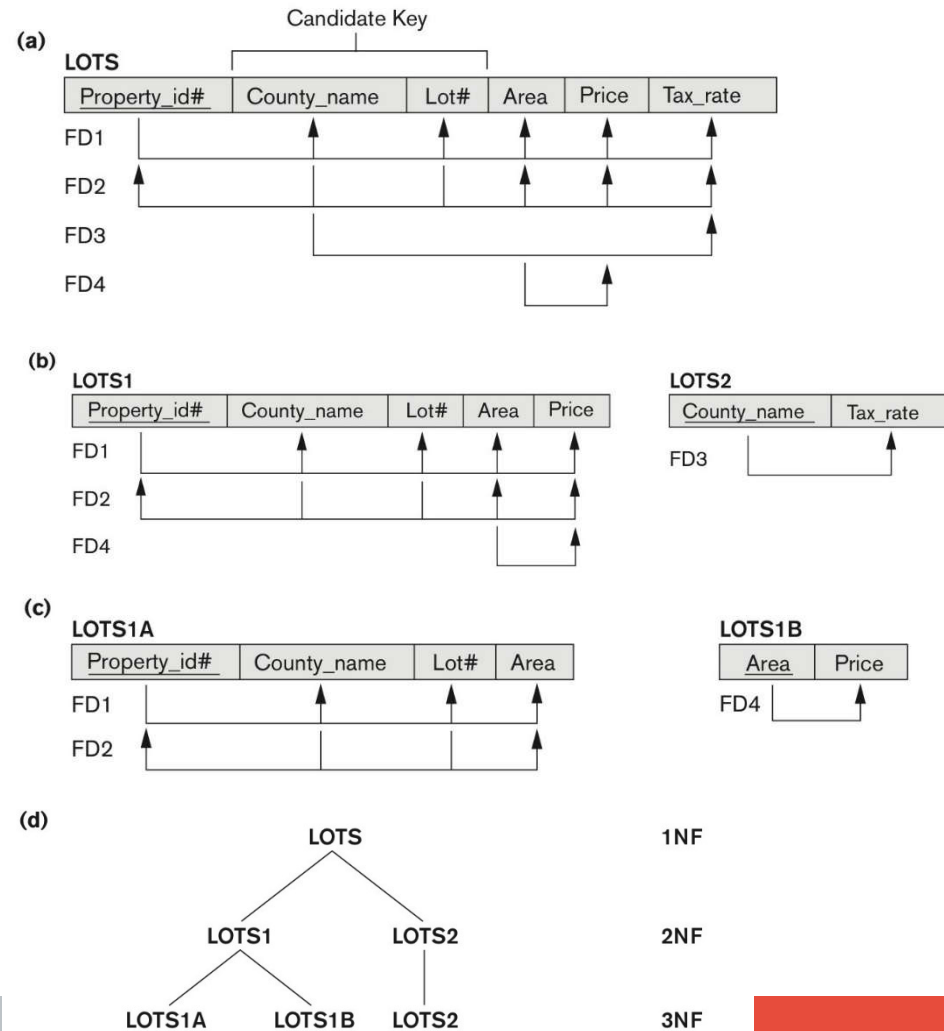


ED2

<u>Dnumber</u>	Dname	Dmgr_ssn
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Figure 14.12 Normalization into 2NF and 3NF



Third Normal Form

- Definition:
 - **Transitive functional dependency:** a FD $X \rightarrow Z$ that can be derived from two FDs $X \rightarrow Y$ and $Y \rightarrow Z$
- Examples:
 - $SSN \rightarrow DMGRSSN$ is a **transitive** FD
 - Since $SSN \rightarrow DNUMBER$ and $DNUMBER \rightarrow DMGRSSN$ hold
 - $SSN \rightarrow ENAME$ is **non-transitive**
 - Since there is no set of attributes X where $SSN \rightarrow X$ and $X \rightarrow ENAME$

Third Normal Form

- A relation schema R is in **third normal form (3NF)** if it is in 2NF *and* no non-prime attribute A in R is transitively dependent on the primary key
- R can be decomposed into 3NF relations via the process of 3NF normalization
- NOTE:
 - In $X \rightarrow Y$ and $Y \rightarrow Z$, with X as the primary key, we consider this a problem only if Y is not a candidate key.
 - When Y is a candidate key, there is no problem with the transitive dependency .
 - E.g., Consider EMP (SSN, Emp#, Salary).
 - Here, $SSN \rightarrow Emp\# \rightarrow Salary$ and $Emp\#$ is a candidate key.

Normal Forms Defined Informally

- 1st normal form
 - All attributes depend on **the key**
- 2nd normal form
 - All attributes depend on **the whole key**
- 3rd normal form
 - All attributes depend on **nothing but the key**

BCNF (Boyce-Codd Normal Form)

- A relation schema R is in **Boyce-Codd Normal Form (BCNF)** if whenever an **FD** $X \rightarrow A$ holds in R , then X is a **superkey** of R
- Each normal form is strictly stronger than the previous one
 - Every 2NF relation is in 1NF
 - Every 3NF relation is in 2NF
 - Every BCNF relation is in 3NF
- There exist relations that are in 3NF but not in BCNF
- Hence BCNF is considered a **stronger form of 3NF**
- The goal is to have each relation in BCNF (or 3NF)

Figure 14.13 Boyce-Codd normal form

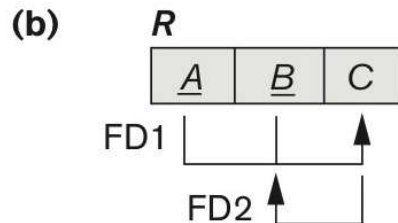
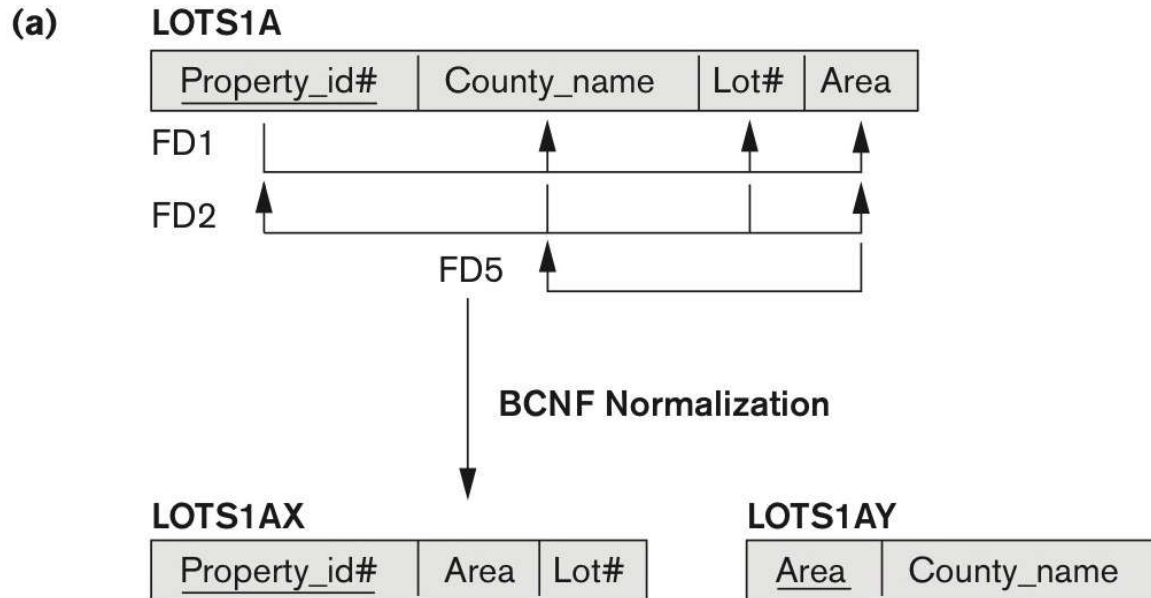


Figure 14.14 A relation TEACH that is in 3NF but not in BCNF

TEACH

Student	Course	Instructor
Narayan	Database	Mark
Smith	Database	Navathe
Smith	Operating Systems	Ammar
Smith	Theory	Schulman
Wallace	Database	Mark
Wallace	Operating Systems	Ahamad
Wong	Database	Omiecinski
Zelaya	Database	Navathe
Narayan	Operating Systems	Ammar

Achieving the BCNF by Decomposition

- Two FDs exist in the relation TEACH:
 - fd1: { student, course} \rightarrow instructor
 - fd2: instructor \rightarrow course
- {student, course} is a candidate key for this relation and that the dependencies shown follow the pattern in Figure 14.13 (b).
 - So this relation is in 3NF *but not in* BCNF

Achieving the BCNF by Decomposition

- Three possible decompositions for relation TEACH
 - D1: {student, instructor} and {student, course}
 - D2: {course, instructor} and {course, student}
 - D3: {instructor, course} and {instructor, student} ✓
- All three decompositions will lose fd1.
 - We have to settle for sacrificing the functional dependency preservation. But we cannot sacrifice the non-additivity property after decomposition.
- Out of the above three, only the 3rd decomposition will not generate spurious tuples after join. (and hence has the non-additivity property).

