

# Parameter sensitivity and identifiability for a biogeochemical model of hypoxia in the northern Gulf of Mexico<sup>☆</sup>

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## Abstract

Local sensitivity analyses and identifiable parameter subsets were used to describe numerical constraints of a hypoxia model for bottom waters of the northern Gulf of Mexico. The sensitivity of state variables differed considerably with parameter changes, although most variables were responsive to changes in parameters that influenced planktonic growth rates and less sensitive to physical or chemical parameters. Variation in sensitivity had a direct correspondence with identifiability, such that only small subsets of the complete parameter set had unique effects on the model output. Selecting parameters by decreasing sensitivity demonstrated that only eight of 51 total parameters had a sufficiently unique effect on model output for precise calibration. As a result, parameter selection heuristics were used to identify parameters for model calibration that depended on combined effects on output, relative

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sensitivity of each parameter, and ecological categories for the biogeochemical equations. The calibrated zero-dimensional (0-D) unit of the hypoxia model had improved precision if sensitive parameters were included in an identifiable subset. Extension of results to a three-dimensional grid of the Gulf of Mexico showed that sensitive parameters for the 0-D model translated to non-trivial changes in the areal estimates of hypoxia.

*Keywords:* Coastal General Ecosystem Model (CGEM), Gulf of Mexico (GOM), Hypoxia, Identifiability, Sensitivity

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## 1. Introduction

Hypoxia formation in bottom waters of coastal oceans occurs primarily from excess nutrient inputs from land-based sources (Justić et al., 1987; Diaz and Rosenberg, 1995; Howarth et al., 1996). These events are detrimental to aquatic organisms and have significant negative effects on economic resources derived from coastal ecosystems (Lipton and Hicks, 2003; Diaz and Rosenberg, 2011). An understanding of the biological, physical, and chemical processes that influence hypoxic areas is a critical concern for mitigating and preventing these negative impacts. Numerical ecosystem models are important tools that synthesize knowledge of ecosystem processes that contribute to hypoxia formation and for predicting the effects of proposed management activities or future scenarios (Scavia et al., 2004; Hagy and Murrell, 2007; Pauer et al., 2016). Unlike statistical models with more generic structures, simulation and process-based models include explicit descriptions of relevant processes that are constrained by empirical or observational data relevant to the system of interest (e.g. Omlin et al., 2001b; Eldridge and Roelke, 2010). These models are often coupled with hydrodynamic grids to provide spatially-explicit representations of patterns in three dimensions (Warner et al., 2005; Zhao et al., 2010; Ganju et al., 2016). Combined hydrodynamic and

bio-geo-chemical models have been developed specifically to describe hypoxic conditions on the Louisiana continental shelf (LCS) in the northern Gulf of Mexico (GOM) (Fennel et al. 2013; Obenour et al. 2015; Pauer et al. 2016, Lehrter et al. in press). This area drains a significant portion of the continental United States through the Mississippi-Atchafalaya River Basin (MARB) and is the second largest hypoxic area in the world (Rabalais et al., 2002). Understanding processes that contribute to the frequency and duration of hypoxic events remains a critical research goal for the region.

The development of a model represents a tradeoff between characteristics expected from the output and information represented by the structural components. An ideal model is sufficiently generalizable across systems, provides results that are precise given the inputs, and includes components that are realistic descriptions of actual processes (Levins, 1966). Given that these characteristics cannot be simultaneously achieved, models are developed in partial dependence of reality and theoretical constructs, completely separate from both, or dependent on one or the other (Morrison and Morgan, 1999; Ganju et al., 2016). These challenges are analagous to the well-known bias-variance tradeoff in statistical models that balances the competing objectives of over- and under-fitting to an observed dataset. Process-based models are more commonly imbalanced between reality and theory, such that most are over-parameterized in an attempt to completely describe reality (Denman, 2003; Nossent and Bauwens, 2012; Petrucci and Bonhomme, 2014). Quantitative limitations of over-parameterization are analagous to degrees of freedom in standard statistical models as free parameters cannot be numerically estimated when constrained to an observed dataset (Kirchner, 2006). More importantly, over-parameterization can limit use across systems outside of the data domain and impose uncertainty in model predictions as realistic values

for every variable may not be known or inaccurately applied from existing studies (Durand et al., 2002; Refsgaard et al., 2007; Wade et al., 2008).

Model precision can be evaluated relative to the effects of initial conditions or the observed data used for calibration, changes in parameter values, or variation in the structural components (i.e., observational, parameter, or structural uncertainty) (Beck, 1987). Evaluating effects of parameter changes is by far the most common and simplest approach. Although sensitivity analyses should be integrated with model development, parameters are often evaluated post-hoc as a form of ‘damage control’ for further calibration. This approach is sometimes called inverse modelling where results from sensitivity analyses are used to guide calibration or fit of the developed model to observations (Soetaert and Petzoldt 2010, or confronting models with data, *sensu* Hilborn and Mangel 1997). Parameter sensitivity analysis combined with inverse modelling necessarily involves questions of parameter ‘identifiability’. Redundancies in parameter effects lead to unidentifiable models where calibration is empirically impossible (i.e., standard algorithms will not converge) or parameter values may be non-unique leading to the right answer for the wrong reason (Kirchner, 2006). Unidentifiable parameter sets have effects on model output that can be undone or compensated for by alteration of other parameters. Identifiability issues are not foreign to hypoxia or eutrophication models (Omlin et al., 2001a; Estrada and Diaz, 2010; Mateus and Franz, 2015), although there is a clear need for greater integration of these concepts in practice (Fasham et al., 2006).

This study describes a sensitivity and identifiability analysis of a zero-dimensional (0-D) unit of a larger spatial-temporal model of hypoxia dynamics on the LCS. The objectives were to provide a statistical approach that demonstrates numerical limitations of parameter

sets for model calibration and provide a framework for selecting parameters within the identifiability constraints. The specific goals were to 1) identify the parameters that have the greatest influence on state variables using local sensitivity analysis, 2) quantify the identifiability of subsets of the total parameter space based on sensitivity, 3) and provide a set of heuristics for choosing parameters based on sensitivity, identifiability, and parameter categories. The 0-D model was calibrated with selected parameter subsets to demonstrate use of the selection heuristics to improve model precision. Sensitive parameters for the 0-D model were also varied in the larger 3-dimensional model to demonstrate scalability the results. In addition to dissolved oxygen ( $O_2$ ), other state variables that were evaluated included ammonium, chlorophyll *a* (chl-*a*), irradiance, nitrate, particulate organic matter (POM), dissolved organic matter (DOM), and phosphorus. In general, we provide empirical results to support the assumption that models are generally over-parameterized and only a finite and smaller subset of the complete parameter set can be optimized.

## 2. Methods

### 2.1. Model description

Hypoxic events, defined as  $<2 \text{ mg L}^{-1}$  of  $O_2$  ( $< 64 \text{ mmol m}^{-3}$ ), occur seasonally in bottom waters in the northern GOM. The hypoxic area averages  $15,540 \text{ km}^2$  annually (1993-2015) with minimum concentrations observed from late spring to early fall. Seasonal variation is strongly related to carbon and nutrient export from the MARB (Lohrenz et al., 2008; Bianchi et al., 2010), whereas hydrologic variation, currents, and wind patterns can affect vertical salinity gradients that contribute to hypoxia formation (Wiseman et al., 1997; Paerl et al., 1998; Obenour et al., 2015). The Coastal General Ecosystem Model (CGEM) was developed to describe hypoxia dynamics on the LCS and includes elements from the Navy Coastal Ocean

Model ([Martin, 2000](#)) for hydrodynamics and a biogeochemical model with multiple plankton groups, water-column metabolism, and sediment diagenesis (Fig. 1, [Eldridge and Roelke, 2010](#)). The hydrodynamic component of CGEM provides a spatially-explicit description of hypoxia using an orthogonal grid with an approximate horizontal resolution of 1.9 km<sup>2</sup> and twenty equally-spaced vertical sigma layers on the shelf. The biogeochemical component includes equations for 36 state variables including six phytoplankton groups (with nitrogen and phosphorus quotas for each), two zooplankton groups, nitrate, ammonium, phosphate, dissolved inorganic carbon, oxygen, silica, and multiple variables for dissolved and particulate organic matter from different sources.

The core unit of CGEM is FishTank, a 0-D model that implements the biogeochemical equations in [Eldridge and Roelke \(2010\)](#) and does not include any advection, mixing, or sediment diagenesis. Although FishTank was developed for specific application in CGEM, it can easily be applied to other hydrodynamic grids. Results are based on time-dependent differential equations that describe energy flow between phytoplankton and zooplankton groups given nutrient uptake rates, organic matter inputs and losses, inherent optical properties, and temperature ([Penta et al. 2008](#); [Eldridge and Roelke 2010](#), see appendix in [Lehrter et al. in press](#)). A total of 108 equations are estimated at each time step to return values for each of the 36 state variables described by the model. In addition to the initial conditions, 251 parameter values for each of the equations are also supplied at model execution. Values for each of the parameters were based on estimates from the literature, field or laboratory-based measurements, or expert knowledge in absence of the former. As such, a sensitivity analysis of parameter values is warranted given that, for example, literature or field-based estimates may not apply under all scenarios or expert knowledge is not completely certain ([Refsgaard](#)

et al., 2007).

The sensitivity of state variables to perturbations of all relevant parameters for the 108 equations was estimated using a five minute timestep with daily output from January 1<sup>st</sup> 111 to December 31<sup>st</sup>, 2006. Irrelevant parameters were removed for several reasons; parameters 112 were not relevant for the 0-D model (i.e., hydrodynamic parameters), were considered 113 physical constants, or had no effect given initial conditions. Additionally, FishTank includes 114 six phytoplankton and two zooplankton groups to add complexity in community structure 115 and foodweb dynamics. To remove obvious redundancies, the sensitivity analyses were conducted 116 using only one phytoplankton and one zooplankton group. The final set that was 117 evaluated included 51 parameters that were further grouped into one of six categories based 118 on applicable biogeochemical components of the model: optics ( $n = 4$  parameters), organic 119 matter (12), phytoplankton (22), temperature (2), and zooplankton (11). A full description 120 of the model parameters is available as an appendix in [Lehrter et al. in press](#). 121

## 2.2. Local sensitivity analysis

A local sensitivity analysis was performed by evaluating the change in state variables 123 following perturbation of each parameter from its original value ([Soetaert and Petzoldt, 124 2010; RDCT \(R Development Core Team\), 2017](#)). Parameters were individually perturbed 125 by a 50% increase of the original values and sensitivity  $S$  was estimated for each time step 126  $i$  given a change for parameter  $j$  as:

$$S_{ij} = \frac{\partial y_i}{\partial \Theta_j} \cdot \frac{w_{\Theta_j}}{w_{y_i}} \quad (1)$$

where the estimate is based on the change in the predicted value for response variable  $y$  128 divided by the change in the parameter  $\Theta_j$  multiplied by the quotient of scaling factors  $w$  129

for each. The scaling factors,  $w_{\Theta_j}$  for the parameter  $\Theta_j$  and  $w_{y_i}$  for response variable  $y_i$ , were set as the default value of the unperturbed parameter and the predicted value of  $y_i$  after perturbation (Soetaert and Petzoldt, 2010). Scaling makes the estimates unitless to compare model sensitivity to parameters and state variables that differ in relative magnitude. Sensitivity values for all  $j$  parameters were summarized as a single value across the time series from  $i = 1$  to  $n$  as  $L1$ :

$$L1 = \sum |S_{ij}|/n \quad (2)$$

All parameters for each of the six equation categories (optics, organic matter, phytoplankton, temperature, and zooplankton) that had non-zero  $L1$  were retained for identifiability analysis.

### 2.3. Identifiability and selecting parameter subsets

The collinearity index  $\gamma$  provides a measure of potential redundancies in the response of a state variable to changes in parameter values. The index measures the linear dependence between sensitivity functions (i.e.,  $S_i$  for  $j$  parameters) described above for parameter subsets and was estimated from the minimum eigenvector of the cross-product of a selected sensitivity matrix (Brun et al., 2001; Omlin et al., 2001a):

$$\gamma = \frac{1}{\sqrt{\min(\text{EV}[\hat{S}^\top \hat{S}])}} \quad (3)$$

where  $\gamma$  ranges from one to infinity for perfectly identifiable (orthogonal) or unidentifiable (perfectly collinear) parameter sets. The sensitivity functions were supplied as a matrix  $\hat{S}$  with rows  $i$  and columns  $j$  (eq. (1)) that described deviations of predicted  $\text{O}_2$  following



perturbations of each parameter. Thus,  $\gamma$  can be estimated from results for any subset of  
 parameter combinations. Sensitivity matrices were first normalized by dividing by the square  
 root of the summed residuals (Omlin et al., 2001a; Soetaert and Petzoldt, 2010). Estimates  
 of  $\gamma$  greater than 10-15 suggest parameter sets are poorly identifiable (Brun et al., 2001;  
 Omlin et al., 2001a), meaning parameter values that maximize precision on a calibration  
 dataset are inestimable by conventional optimization algorithms. An intuitive interpretation  
 of  $\gamma$  is provided by Brun et al. (2001), such that a change in a state variable caused by a  
 change in one parameter can be offset by the fraction  $1 - 1/\gamma$  by the remaining parameters.  
 That is,  $\gamma = 10$  suggests the relative change in  $O_2$  for an arbitrary parameter in the selected  
 set can be compensated for by 90% with changes in the other parameters.

Parameter selection for model calibration must consider the competing objectives of in-  
 creased precision with parameter inclusion and reduced identifiability as it relates to opti-  
 mization. An additional challenge is a large number of combinations of parameter sets, which  
 complicates selection given sensitivity differences and desired ecological categories of each  
 parameter (e.g., parameters for a group of related structural equations could be of interest).  
 Fig. 2 provides a simple graphic of the unique number of combinations that are possible for  
 different subsets of ‘complete’ parameter sets of different sizes (i.e.,  $n$  choose  $k$  combinations,  
 $n!/(k!(n-k)!)$ ). The number of unique combinations increases with the total parameters  
 in the set and is also maximized for moderate selections (e.g., selecting half the total). For  
 example, over  $10^{14}$  combinations are possible by selecting 25 parameters from a set of 50.

A set of heuristics was developed that addresses the tradeoff in model complexity and  
 identifiability given the challenges described above (see also Wagener et al., 2001). These  
 rulesets were developed to select parameters with preference for those with high sensitiv-

ity and identifiability based on  $\gamma < 15$  as an acceptable threshold for subsets (e.g., 93% accountability between parameters). Selection heuristics also recognized that parameter categories (i.e., optics, organic matter, phytoplankton, temperature, zooplankton) may have unequal preferences by users given desired application of the model. For all selection heuristics, parameters were selected by decreasing sensitivity starting with the most sensitive until identifiability did not exceed  $\gamma = 15$  where selections were 1) blocked within each of five parameter categories, 2) independent of parameter category, 3) or considering all categories equally.

#### *2.4. Model calibration and scalability*

Selected parameter subsets from the seven heuristics were used to calibrate the 0-D model. This analysis demonstrated that different parameter sets can produce model output with differing precision and calibration effort given 1) differences in variable sensitivity to parameters in each subset, 2) differences in the parameters selected from different categories (heuristic difference), and 3) differences in identifiability values. Generally, this analysis was a proof of concept that the selection heuristics can lead to an ‘optimal’ model by maximizing the balance between sensitivity and identifiability.

A time series of  $O_2$  from Weeks Bay, Alabama was used for model calibration. Daily observations from January 1<sup>st</sup>, 2006 to January 1<sup>st</sup>, 2007 at the Weeks Bay station of the Weeks Bay National Estuarine Reserve were used (Wenner et al., 2004). We chose this location because of the availability of data for model calibration compared to bottom waters in the northern GOM and the system exhibits hypoxia from eutrophication. This application also provided a practical example of how the FishTank model could be calibrated using data from alternative locations. Initial conditions for model input were modified to match

conditions in Weeks Bay using observed water quality and nutrient data (all data from <http://cdmo.baruch.sc.edu/>). The O<sub>2</sub> time series was filtered to reduce physical effects of the tidal advection component on the observed data (*sensu* Beck et al. 2015). As such, the filtered data were comparable to a time series with no physical advection to match conditions of the 0-D FishTank model with no hydrodynamic component.

Each parameter subset was calibrated to most closely match the model output to the observed time series. Parameter values were searched using the `optim` function in R that implemented the limited memory modification of the BFGS quasi-Newton method (Byrd et al., 1995; Nocedal and Wright, 2006; RDCT (R Development Core Team), 2017). This optimization scheme searches for values within the user-defined lower and upper bounds of each parameter. We set the algorithm to search within +/- 50% of the default parameter values. While we recognize that ‘actual’ parameter values could possibly extend beyond this range, constraining the values to the range tested herein was expected to produce output that was more interpretable within the context of the sensitivity functions defined above. Moreover, precise limits on each parameter were less of a concern for the current analysis as our primary goal was to demonstrate differences in precision as a function of sensitivity and identifiability. The optimal values for each parameter were identified based on convergence of the model results as a minimization of the root mean squared error (*RMSE*) between the observed and modelled data.

As a final analysis, effects of parameter changes on the larger 3-dimensional model were evaluated to demonstrate that results from the 0-D FishTank model are scalable. For simplicity, only the most sensitive parameter in each category was selected. The CGEM model was run for one year using the default parameter conditions and by increasing each of the

selected parameters by 50%. This produced six spatially-referenced time series (one default, five for each parameter change) from which changes in the daily hypoxic area (number of cells  $< 64$  mmol  $O_2$ ) were estimated.

### 3. Results

#### 3.1. Local sensitivity analysis

Local sensitivity analyses showed that  $O_2$  was sensitive to perturbations in 38 of the 51 (75% of total) parameters that were evaluated in FishTank (Fig. 3, Table 1). Within each parameter category,  $O_2$  was sensitive to three parameters for optics (75% of all optic parameters), eight for organic matter (67%), 16 for phytoplankton (73%), one for temperature (50%), and 10 for zooplankton (91%). Although  $O_2$  had the greatest sensitivity to parameters in the zooplankton category (as percentage of total), the relative effects varied. Among all parameters, average sensitivity was  $L1 = 9.2 \times 10^{-3}$  with values ranging from  $L1 = 8.34 \times 10^{-8}$  for  $QminP$  (phytoplankton) to 0.05 for  $umax$  (phytoplankton). Within categories (excluding temperature with one sensitive parameter), sensitivity ranged from  $4.39 \times 10^{-5}$  ( $astarOMA$ ) to  $7.51 \times 10^{-4}$  ( $astar490$ ) for optics,  $4.17 \times 10^{-4}$  ( $KNH4$ ) to  $6.15 \times 10^{-3}$  ( $KG1$ ) for organic matter,  $8.34 \times 10^{-8}$  ( $QminP$ ) to 0.05 ( $umax$ ) for phytoplankton, and  $3.69 \times 10^{-5}$  ( $ZQp$ ) to 0.05 ( $ZKa$ ) for zooplankton (Table 1). Average sensitivity values in each category were  $L1 = 2.81 \times 10^{-4}$  for optics,  $2.17 \times 10^{-3}$  for organic matter, 0.02 for temperature, 0.01 for phytoplankton, and 0.01 for zooplankton.

Local sensitivity analyses for the additional state variables (ammonium, chl-*a*, irradiance, nitrate, POM, DOM, and phosphorus) had similar results as  $O_2$  with some exceptions (Fig. 3 and Tables S1 to S7). All variables were sensitive to the same parameters as  $O_2$  (38 of 51 evaluated), although average sensitivity differed between variables. Average  $L1$  ranged from

0.02 for irradiance (Table S3) to 0.71 for DOM (Table S6). All average sensitivity values for the state variables were higher than the average for  $O_2$  ( $L1 = 9.2 \times 10^{-3}$ ). For each variable,  $L1$  ranged from  $2.24 \times 10^{-6}$  ( $QminP$ ) to 8.49 ( $mA$ ) for ammonium (Table S1),  $1.38 \times 10^{-6}$  ( $QminP$ ) to 13.94 ( $mA$ ) for chl-*a* (Table S2),  $1.92 \times 10^{-7}$  ( $QminP$ ) to 0.13 ( $ZKa$ ) for irradiance (Table S3),  $6.67 \times 10^{-7}$  ( $QminP$ ) to 8.49 ( $umax$ ) for nitrate (Table S4),  $6.41 \times 10^{-5}$  ( $KNH_4$ ) to 7.22 ( $mA$ ) for POM (Table S5),  $7.41 \times 10^{-5}$  ( $KNH_4$ ) to 14.25 ( $mA$ ) for DOM (Table S6), and  $8.21 \times 10^{-7}$  ( $QminP$ ) to 1.47 ( $ZKa$ ) for phosphate (Table S7). For the parameter categories, ammonium was most sensitive to phytoplankton parameters (average  $L1 = 0.8$  across all parameters in the category), chl-*a* to phytoplankton ( $L1 = 1.14$ ), irradiance to zooplankton ( $L1 = 0.03$ ), nitrate to zooplankton ( $L1 = 1.06$ ), POM to temperature ( $L1 = 0.86$ ), DOM to temperature ( $L1 = 1.48$ ), and phosphate to zooplankton ( $L1 = 0.31$ ). Finally, average sensitivity between parameter categories independent of the state variables ranged from  $8.38 \times 10^{-3}$  for optics (average  $L1$  across all variables) to 0.62 for phytoplankton.

### 3.2. Identifiability of parameter subsets and selection rules

The identifiability analyses suggested that many parameter subsets exceeded the thresholds of  $\gamma = 10, 15$ . Parameter identifiability for  $O_2$  decreased (increasing  $\gamma$ ) at different rates with increasing size of parameter subsets depending on the parameter category or the number of top parameters that were selected (Fig. 4). By category, identifiability was lowest for all combinations of parameter subsets in the phytoplankton (60% of subsets less than  $\gamma = 15$ , 43% less than  $\gamma = 10$ ) and zooplankton categories (53.1% less than  $\gamma = 15$ , 40% less than  $\gamma = 10$ ), whereas all combinations were identifiable for optics (100% less than  $\gamma = 15, 10$ ) and a majority identifiable for organic matter (91.9% less than  $\gamma = 15$ , 76.5% less than  $\gamma = 10$ ).

Identifiability for parameters in the temperature category was not evaluated because  $O_2$  was sensitive to only one parameter (i.e.,  $\gamma = 1$ ). Parameter combinations for choosing from the top, top two, top three, and top four parameters in each category together had decreasing identifiability with the increasing size of the selection pool (e.g., top one versus top four parameters, Fig. 4). The percentage of parameter subsets that were below the acceptable thresholds for identifiability was 100% less than  $\gamma = 15, 10$  for the top parameter in each category, 90.6% and 80.7% for the top two, 80.7% and 70.9% for the top three, and 55.8% and 45.7% for the top four. Results for the remaining state variables had similar patterns in identifiability with increasing size of parameter subsets and selection categories, although differences in identifiability between state variables was observed (Fig. 5). Most notably, nitrate was consistently the least identifiable variable (highest overall  $\gamma$ ), whereas  $O_2$  was most identifiable.

An evaluation of the effects of individual parameters on  $\gamma$  suggested that some parameters had disproportionate effects on identifiability. Based on  $\gamma = 15$ , Fig. 4 suggests that most parameter sets for organic matter were identifiable, regardless of how many parameters were selected (i.e., two through eight). However, some subsets were not identifiable such that identification of one or more redundant parameters that are inflating  $\gamma$  values could provide useful information. Fig. 6 shows an alternative view of identifiability of  $O_2$  with exclusion and inclusion of individual parameters in different sets for the organic matter category. As before, collinearity increases with more parameters in a subset, although the increase varies depending on which parameter was included or excluded from the set. For example, inclusion of *KNO3* in a parameter set almost always inflated  $\gamma$ . All parameter subsets that did not include *KNO3* were well below  $\gamma = 15$ , suggesting that exclusion of this parameter improves

286 identifiability. Interestingly, the inclusion of some parameters caused a reduction in  $\gamma$ , which  
287 contradicts the general rule that more parameters caused reduced identifiability. For example,  
288 parameter sets that included *KGcdom* generally had lower  $\gamma$  values relative to those that  
289 excluded the parameter.

290 Results for each of the three selection heuristics (blocked by parameter category, indepen-  
291 dent of category, all categories equally) applied to each state variable differed in the number  
292 of selected parameters and distribution of parameters within each category (Tables 2 to 4).  
293 In general, a correspondence was observed between the number of parameters that were  
294 selected given the threshold of  $\gamma = 15$  and relative identifiability between the state variables.  
295 As noted above, nitrate was the least identifiable variable (Fig. 5), whereas other variables  
296 (e.g.,  $O_2$ , irradiance) were more identifiable. The constraints on identifiability between vari-  
297 ables were demonstrated with the selection heuristics. For example, heuristics for nitrate  
298 typically selected only one or two parameters that met the criteria as compared to more  
299 identifiable variables that included several parameters. Overall, the first selection heuristic  
300 demonstrated that the number of parameters chosen by parameter category differed indepen-  
301 dently of the state variables (Table 2). The number of selected parameters averaged across  
302 state variables in decreasing order was 4.25 parameters from the phytoplankton category,  
303 3.5 from organic matter, 2.75 from optics, and 2.38 from zooplankton. The second and third  
304 selection heuristics (Tables 3 and 4) were similar, although more parameters were generally  
305 selected for the third heuristic given equal importance between categories.

### 306 3.3. Model calibration and scalability

307 Calibration of parameter values for each of the seven selection heuristics (Tables 2 to 4)  
308 produced model output that varied in precision and computational effort required to identify

309 optimal values (Table 5). As expected, the number of required iterations of the optimiza-  
 310 tion algorithm to minimize *RMSE* of observed O<sub>2</sub> and model output varied in proportion  
 311 to the number of parameters in a subset. For example, only six iterations were required to  
 312 optimize the single parameter selected for the temperature category, whereas 1530 iterations  
 313 were required for the eight parameters selected independent of category. No association  
 314 was observed between collinearity ( $\gamma$ ) and number of iterations or calibration. Of the seven  
 315 parameter subsets, selection independent of parameter category and equally within each  
 316 category produced the largest reduction in *RMSE* values from the default output (start-  
 317 ing *RMSE* 72.14, reduction to 66.77, 67.44, respectively), whereas the optimal values for  
 318 parameters in the Optics category had the smallest reduction (72.12). Lower *RMSE* was  
 319 associated with higher average sensitivity of a parameter subset. Parameters selected only  
 320 in the optics category had the highest *RMSE* and lowest average L1 ( $2.81 \times 10^{-4}$ , three  
 321 parameters), whereas parameters selected independent of category had the lowest *RMSE*  
 322 and highest average L1 (0.03, eight parameters, Table 5).

323 The estimated areal extent of bottom-water hypoxia using default parameter values for  
 324 the 3-dimensional model peaked on August, 28<sup>th</sup> at  $1.19 \times 10^4$  km<sup>2</sup> (Fig. 7a, August mean area  
 325  $8988 \pm 551$  km<sup>2</sup>, Fig. 7b). Increases in the top sensitive parameters for O<sub>2</sub> in each category  
 326 (Table 1) increased the estimated areal extent of hypoxia (Figs. 7c, 7e), with the exception  
 327 of the parameter for optimum temperature of growth ( $T_{ref}(nospA+nospZ)_{p1}$ ), which caused  
 328 a decrease (mean difference from July default area  $-1070 \pm 1161$  km<sup>2</sup>, Fig. 7d). The largest  
 329 increase in area was caused by an increase in the maximum growth rate of phytoplankton  
 330 ( $u_{max}$ ), with the greatest increase occurring in July (monthly mean increase of  $4109 \pm 1085$   
 331 km<sup>2</sup>, Fig. 7d). Overall, changes in hypoxia extent were largest for parameters with large



sensitivity values (i.e.,  $L1 = 0.05$  for *ZKa*,  $L1 = 0.05$  for *umax*).

#### 4. Discussion

Common goals in the application of biogeochemical models are to 1) accurately describe the system by matching predictions with observed data (Reckhow et al., 1990), and 2) provide a means of forecasting ecosystem condition with hypothesized management or environmental scenarios (Clark et al., 2001). Although these objectives are the focus of most applications, the structural components and associated parameters of process-based models should secondarily provide insight of ecosystem processes that are driving observed changes. This latter objective represents a more generic scientific purpose of modelling that extends beyond the benefits of describing and predicting change. Modelers aim to identify universal principles that govern dynamics across systems and the constraint of model parameters to observations provides a means of supporting or refuting hypotheses (Hilborn and Mangel, 1997; Kirchner, 2006). Accordingly, this study provided a simple approach to use the effects of parameter perturbations on state variables to characterize identifiable parameter subsets that varied by selection criteria. By doing so, we provided a simple and preliminary approach towards improved model refinement that begins to address more general purposes of model applications. Our specific results demonstrated that small parameter subsets relative to all sensitive parameters were within the identifiability thresholds described in the literature. The identifiable parameter subsets varied considerably between state variables and the method for parameter selection. Use of identifiable parameter subsets with sensitive parameters improved model precision and results for the smaller model were scalable to the 3-dimensional model. In general, these results provide justification for the use of explicit parameter selection heuristics to improve model precision.

State variables were most sensitive to parameters in the phytoplankton and zooplankton categories, particularly the maximum growth rates ( $umax$  for phytoplankton,  $Zumax$  for zooplankton), mortality coefficient for phytoplankton ( $mA$ ), and the zooplankton half saturation coefficient for grazing ( $ZKa$ ). An increase in the growth rate of primary producers has the potential to increase oxygen concentration through photosynthetic processes, although increased production of organic matter is balanced with respiration and bacterial decomposition that reduce  $O_2$  in the water column. Similarly, increases in zooplankton abundance with increased growth rates causes a reduction in phytoplankton biomass through grazing, which is expected to further deplete pools of organic matter from algal sources. Most variables were also sensitive to variation in the half-saturation grazing coefficient which moderates the concentration of nutrients that support half the maximum grazing rate. Although the tradeoff between abundance, grazing, and decomposition is complex, the sensitivity of model state variables to parameters that directly control the abundance of primary producers is in agreement with empirical observations of factors that influence hypoxia dynamics on the LCS (Fahnenstiel et al., 1995; Roelke, 2000; Eldridge and Roelke, 2010). The sensitivity of the model output to variation in other parameters that relate to physical and chemical properties of the system was of secondary importance to biological relationships. That is, state variables were sensitive to changes in light and temperature parameters, although to a lesser extent than phytoplankton and zooplankton parameters. As such, the differing sensitivities of state variables to parameters in each of the categories was not unexpected given general ecological relationships that are well understood and described by the model.

A general conclusion from the identifiability analyses is that only limited subsets of parameters were identifiable within the constraints of local sensitivity analyses. These results

support previous studies that have suggested similarly small subsets of parameters can be identified using traditional calibration schemes (e.g., [Wheater et al., 1986](#); [Ye et al., 1997](#); [Omlin et al., 2001a](#)). In addition to CGEM, these conclusions have relevance for other biogeochemical models that include numerous parameters and structural equations to characterize processes in the model domain. A general conclusion is that less complex models could potentially be beneficial given that only a small subset of parameters is identifiable and that ecosystem processes may in fact be sufficiently characterized with few parameters ([Ye et al., 1997](#)). Conversely, others have argued that model complexity is not in itself a disadvantage when parsimony is not the sole arbitrator of model structure ([Reichert and Omlin, 1997](#)). Over-parameterization can be useful if processes have importance that were not evaluated during model identification. Single objective functions that maximize model precision with identifiable parameters may also provide an incomplete characterization of model worth, which has prompted the development of probability-based models of hypoxia that explicitly include uncertainty in model components (e.g. [Obenour et al., 2015](#)). Our results demonstrated that approximately 75% of the evaluated parameters had an effect on the eight state variables, whereas CGEM includes a total of 36 variables and multiple plankton groups, not all of which have immediate concern for understanding hypoxia. The redundancies identified with the sensitivity analyses are only problematic if the primary interest is, for example,  $O_2$  dynamics. Moreover, the proposed selection heuristics provide flexibility for choosing different parameters with the assumption that those chosen depend on the research or management question.

Results from the identifiability analyses provided additional insight into the interactions of parameters in large biogeochemical models. First, identifiability of parameter subsets

was not related to the sensitivity of individual variables. As noted above, an identifiable parameter is one that has a unique effect on model predictions that cannot be compensated for or undone by changing other parameters. The magnitude of the effect of a parameter has no bearing on identifiability, which further complicates the selection of parameters for calibration. Although identifiability is the primary limiting factor in choosing a set, the relative sensitivities are more important for the decision to include or exclude individual parameters. For example, Table 5 and Fig. 7 demonstrated that parameter sets with sensitive parameters had improved model precision and that these parameters had affects that translated to the larger model. Our analysis addressed this challenge by presenting multiple selection criteria for identifiable parameter sets that prioritized the most sensitive parameters during the selection process. Similarly, identifiability was not always related to the number of parameters in a set. Although the overwhelming trend was decreasing identifiability with more parameters, the unique effects of including an individual parameter with an existing set often reduced the  $\gamma$  estimate. For example, Fig. 6 showed that including *KGc-dom*, *KO2*, or *nitmax* in parameter sets more often reduced  $\gamma$  relative to sets that excluded the parameters. These examples demonstrate the complex interactions of parameter changes on variable response, highlighting the need to consider the combined and individual effects of parameters on identifiability. The selection criteria proposed in our above analyses can facilitate parameter selection and also provide diagnostic tools to identify parameters with disproportionate effects on  $\gamma$ .

#### 4.1. Recommendations and conclusions

An evaluation of sensitivity and identifiability of relevant parameter sets is a preliminary and simplistic approach to improving model predictions. In general, uncertainty analy-

ses that lead to improved models are ultimately expected to increase our understanding of properties defining ecological relationships. The extension of simple parameter sensitivity analyses to the generalization of ecosystem properties requires additional analysis and model refinement. Further, the utility of a specific model depends on the question and objective for application to a specific system. For the above analysis, the FishTank model, as part of the larger CGEM application, was evaluated in the context of hypoxia effects on ecosystem condition and function. Our results have shown that relatively small subsets of parameters are identifiable given the complexity of the model, and as a result, we have provided a general approach to select parameter subsets depending on the ecological context (i.e., selection by parameter category, selection for specific state variables). We further demonstrated the effects of selected subsets on model precision and the potential for scalability to larger spatial-temporal models. Thus, the results described above have relevance for further model refinement with the specific goal of better understanding ecological dynamics that moderate hypoxia on the northern GOM. However, the general principles of sensitivity and parameter identifiability have broad applicability beyond this context and we argue that such methods should be more universally applied as an initial approach to quantify numerical constraints of biogeochemical models.

Specific approaches can be used to improve and build on the results presented herein, in addition to the more general considerations above. The effects of structural or observational uncertainty could be evaluated as an extension of the analyses presented above. For example, the sensitivity of  $O_2$  to variation in the half-saturation constants for phytoplankton (the concentration supporting half the maximum uptake rate of nutrients) could vary given the initial nutrient concentrations (Eppley et al., 1969). Further, changes in the ratio between

nitrogen and phosphorus could affect the sensitivity of state variables to parameter changes depending on the limiting nutrient. A more challenging analysis is an evaluation of the effects of structural components on model output, which requires exclusion or inclusion of explicit biogeochemical equations. Fortunately, the FishTank model includes several ‘switches’ that allow users to change the governing equations that estimate state variables, such as switches that ‘turn on’ different structural equations for light attenuation in the water column. This design is uncommon in biogeochemical models and could be leveraged for an evaluation of structural uncertainty. As such, our analysis of parameter sensitivity and identifiability could be combined with an evaluation of observational and structural uncertainty for a more complete characterization of the model, having implications for understanding drivers of hypoxia in coastal waters.

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Table 1: Sensitivity of O<sub>2</sub> to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where *L1* summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect O<sub>2</sub> are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
<b>Optics</b>		
Chla specific absorption at 490 nm	<i>astar490</i>	$7.51 \times 10^{-4}$
OMZ specific absorption at 490 nm	<i>astarOMZ</i>	$4.92 \times 10^{-5}$
OMA specific absorption at 490 nm	<i>astarOMA</i>	$4.39 \times 10^{-5}$
<b>Temperature</b>		
Optimum temperature for growth(C)	<i>Tref(nospA+nospZ)<sub>p1</sub></i>	0.02
<b>Phytoplankton</b>		
maximum growth rate	<i>umax</i>	0.05
mortality coefficient	<i>mA</i>	0.02
initial slope of the photosynthesis-irradiance relationship	<i>alpha</i>	0.02
edibility vector for Z1	<i>ediblevector(Z1)</i>	0.02
phytoplankton carbon/cell	<i>Qc</i>	0.01
phytoplankton growth respiration coefficient	<i>respg</i>	$8.36 \times 10^{-3}$
N-uptake rate measured at umax	<i>vmaxN</i>	$8.12 \times 10^{-3}$
phytoplankton basal respiration coefficient	<i>respb</i>	$6.94 \times 10^{-3}$
Phytoplankton threshold for grazing, is multiplied by VOLcell	<i>Athresh</i>	$4.57 \times 10^{-3}$
minimum N cell-quota	<i>QminN</i>	$4.32 \times 10^{-3}$
P-uptake rate measured at umax	<i>vmaxP</i>	$4.27 \times 10^{-3}$
coefficient for non-limiting nutrient	<i>aN</i>	$4.23 \times 10^{-3}$
phytoplankton volume/cell	<i>volcell</i>	$4.13 \times 10^{-3}$
half-saturation constant for P	<i>Kp</i>	$2.9 \times 10^{-3}$
half-saturation constant for N	<i>Kn</i>	$2.77 \times 10^{-4}$
minimum P cell-quota	<i>QminP</i>	$8.34 \times 10^{-8}$
<b>Zooplankton</b>		
half saturation coefficient for grazing	<i>ZKa</i>	0.05
zooplankton nitrogen/individual	<i>ZQn</i>	0.02
Zooplankton mortality constant for quadratic mortality	<i>Zm</i>	0.02
maximum growth rate of zooplankton	<i>Zumax</i>	0.02
assimilation efficiency as a fraction of ingestion	<i>Zeffic</i>	0.01
proportion of grazed phytoplankton lost to sloppy feeding	<i>Zslop</i>	$7.78 \times 10^{-3}$
Zooplankton growth-dependent respiration factor	<i>Zrespg</i>	$5.32 \times 10^{-3}$
Zooplankton biomass-dependent respiration factor	<i>Zrespb</i>	$2.96 \times 10^{-3}$
zooplankton carbon/individual	<i>ZQc</i>	$9.38 \times 10^{-5}$
zooplankton phosphorus/individual	<i>ZQp</i>	$3.69 \times 10^{-5}$
<b>Organic Matter</b>		
turnover rate for OM1A and OM1Z	<i>KG1</i>	$6.15 \times 10^{-3}$
turnover rate for OM2A and OM2Z	<i>KG2</i>	$3.14 \times 10^{-3}$
O2 concentration that inhibits denitrification	<i>KstarO2</i>	$3.04 \times 10^{-3}$
decay rate of CDOM, 1/day	<i>KGcdom</i>	$2.98 \times 10^{-3}$
half-saturation concentration for O2 utilization	<i>KO2</i>	$5.85 \times 10^{-4}$
half-saturation concentration for NO3 used in denitrification	<i>KNO3</i>	$5.8 \times 10^{-4}$
maximum rate of nitrification per day	<i>nitmax</i>	$4.99 \times 10^{-4}$
NH4 rate constant for nitrification	<i>KNH4</i>	$4.17 \times 10^{-4}$

\*Temperature parameters apply separately to phytoplankton (*p1*, one group) or zooplankton (*z1*, one group), denoted by subscripts

Table 2: Parameter identifiability (as  $\gamma$ , eq. (3)) by category for relevant state variables. Selections followed the first heuristic where parameters were selected within categories from most to least sensitive until  $\gamma > 15$ . Rank describes the relative parameter sensitivity in each category for each state variable. Duplicate parameters and ranks in the first two columns apply only to  $\gamma$  values in the same row (i.e., parameter ranks vary for each variable).

Parameter	Rank	Ammonium	Chl- <i>a</i>	O <sub>2</sub>	Irradiance	Nitrate	POM	DOM	Phosphate
<b>Optics</b>									
<i>astar490</i>	1	1	1	1	1	1	1	1	1
<i>astarOMA</i>	2	7.33	5.42	-	5.36	-	7.78	7.87	-
<i>astarOMZ</i>	2	-	-	1.39	-	-	-	-	4.73
<i>astarOMA</i>	3	-	-	3.87	-	-	-	-	10.04
<i>astarOMZ</i>	3	7.58	5.51	-	6.02	-	7.91	7.87	-
<b>Organic Matter</b>									
<i>KG1</i>	1	-	-	1	-	-	1	-	1
<i>KG2</i>	1	-	-	-	-	-	-	1	-
<i>KGcdom</i>	1	-	1	-	1	-	-	-	-
<i>KstarO2</i>	1	-	-	-	-	1	-	-	-
<i>nitmax</i>	1	1	-	-	-	-	-	-	-
<i>KG1</i>	2	-	1.12	-	1.93	-	-	-	-
<i>KG2</i>	2	-	-	6	-	-	-	-	13.43
<i>KGcdom</i>	2	-	-	-	-	-	1.47	1.39	-
<i>KNH<sub>4</sub></i>	2	4.03	-	-	-	-	-	-	-
<i>KG1</i>	3	4.09	-	-	-	-	-	-	-
<i>KG2</i>	3	-	-	-	8.19	-	-	-	-
<i>KGcdom</i>	3	-	-	-	-	-	-	-	13.75
<i>KO2</i>	3	-	-	-	-	-	14.07	11.96	-
<i>KstarO2</i>	3	-	-	6.04	-	-	-	-	-
<i>KGcdom</i>	4	4.19	-	6.12	-	-	-	-	-
<i>KO2</i>	4	-	-	-	-	-	-	-	14.68
<i>KstarO2</i>	4	-	-	-	10.65	-	14.08	-	-
<i>KO2</i>	5	9.47	-	8.61	-	-	-	-	-
<b>Phytoplankton</b>									
<i>mA</i>	1	1	1	-	-	-	1	1	-
<i>umax</i>	1	-	-	1	1	1	-	-	1
<i>ediblevector(Z1)</i>	2	1.13	1.17	-	-	-	1.15	-	-
<i>mA</i>	2	-	-	1.19	1.29	-	-	-	-
<i>Qc</i>	2	-	-	-	-	11.57	-	-	-
<i>umax</i>	2	-	-	-	-	-	-	1.21	-
<i>vmaxP</i>	2	-	-	-	-	-	-	-	7.45
<i>alpha</i>	3	-	-	1.44	1.98	-	-	-	-
<i>ediblevector(Z1)</i>	3	-	-	-	-	-	-	2.9	-
<i>umax</i>	3	2.73	2.11	-	-	-	3.26	-	-
<i>alpha</i>	4	3.55	4.57	-	-	-	-	-	-
<i>ediblevector(Z1)</i>	4	-	-	2.09	4.09	-	-	-	-
<i>Qc</i>	4	-	-	-	-	-	4.98	-	-
<i>vmaxN</i>	4	-	-	-	-	-	-	4.9	-
<i>alpha</i>	5	-	-	-	-	-	10.11	-	-
<i>Qc</i>	5	-	-	2.9	-	-	-	-	-
<i>vmaxN</i>	5	8.14	-	-	-	-	-	-	-
<i>Athresh</i>	6	11.27	-	-	-	-	-	-	-
<i>respg</i>	6	-	-	3.41	-	-	-	-	-
<i>vmaxN</i>	7	-	-	3.97	-	-	-	-	-
<b>Zooplankton</b>									
<i>ZKa</i>	1	-	-	1	1	1	-	-	1
<i>Zumax</i>	1	1	1	-	-	-	1	1	-
<i>ZKa</i>	2	-	4.31	-	-	-	7.3	5.43	-
<i>ZQn</i>	2	-	-	3.18	6.32	9.76	-	-	8.54
<i>Zm</i>	3	-	-	4.57	-	-	-	-	-
<i>Zumax</i>	3	-	-	-	6.93	-	-	-	-
<i>Zm</i>	4	-	-	-	11.86	-	-	-	-
<i>Zumax</i>	4	-	-	5.2	-	-	-	-	-

Table 3: Parameter identifiability (as  $\gamma$ , eq. (3)) for relevant state variables. Selections followed the second heuristic where parameters were selected independent of category from most to least sensitive (L1, eq. (2)), until  $\gamma > 15$ . Rank describes the relative parameter sensitivity in each category for each state variable (O: optics, OM: organic matter, P: phytoplankton, T: temperature, Z: zooplankton).

Selections by state variable	Parameter	L1	Rank	$\gamma$
<b>Ammonium</b>				
1	$mA$	8.49	1 <sub>P</sub>	1
2	$nitmax$	1.54	1 <sub>OM</sub>	1.16
3	$Zumax$	1.42	1 <sub>Z</sub>	2.9
<b>Chlorophyll</b>				
1	$mA$	13.94	1 <sub>P</sub>	1
2	$Zumax$	1.02	1 <sub>Z</sub>	1.18
<b>Dissolved Oxygen</b>				
1	$umax$	0.05	1 <sub>P</sub>	1
2	$ZKa$	0.05	1 <sub>Z</sub>	2.17
3	$mA$	0.02	2 <sub>P</sub>	2.31
4	$Tref(nospA+nospZ)_{p1}$	0.02	1 <sub>T</sub>	2.37
5	$ZQn$	0.02	2 <sub>Z</sub>	4.69
6	$alpha$	0.02	3 <sub>P</sub>	4.91
7	$Zm$	0.02	3 <sub>Z</sub>	6.73
8	$Zumax$	0.02	4 <sub>Z</sub>	6.81
<b>DOM</b>				
1	$mA$	14.25	1 <sub>P</sub>	1
2	$Tref(nospA+nospZ)_{p1}$	1.48	1 <sub>T</sub>	1.05
3	$umax$	1.11	2 <sub>P</sub>	2.46
4	$Zumax$	1.01	1 <sub>Z</sub>	2.91
<b>Irradiance</b>				
1	$ZKa$	0.13	1 <sub>Z</sub>	1
2	$umax$	0.09	1 <sub>P</sub>	4.41
3	$ZQn$	0.06	2 <sub>Z</sub>	7.54
4	$mA$	0.05	2 <sub>P</sub>	8.17
5	$KGcdom$	0.05	1 <sub>OM</sub>	9.44
6	$alpha$	0.04	3 <sub>P</sub>	9.66
7	$Zumax$	0.04	3 <sub>Z</sub>	10.79
<b>Nitrate</b>				
1	$umax$	8.49	1 <sub>P</sub>	1
<b>Phosphate</b>				
1	$ZKa$	1.47	1 <sub>Z</sub>	1
2	$umax$	0.78	1 <sub>P</sub>	11.45
3	$vmaxP$	0.59	2 <sub>P</sub>	11.48
4	$ZQn$	0.5	2 <sub>Z</sub>	13.74
<b>POM</b>				
1	$mA$	7.22	1 <sub>P</sub>	1
2	$Zumax$	0.96	1 <sub>Z</sub>	1.15
3	$KG1$	0.92	1 <sub>OM</sub>	3.87



Table 4: Parameter identifiability (as  $\gamma$ , eq. (3)) for relevant state variables. Selections followed the third heuristic where parameters were selected equally within each category from most to least sensitive (L1, eq. (2)), until  $\gamma > 15$ . Rank describes the relative parameter sensitivity in each category for each state variable (O: optics, OM: organic matter, P: phytoplankton, T: temperature, Z: zooplankton).

Selections by state variable	Parameter	L1	Rank	$\gamma$
<b>Ammonium</b>				
1	$mA$	8.49	1 <sub>P</sub>	1
2	$nitmax$	1.54	1 <sub>OM</sub>	1.16
3	$Zumax$	1.42	1 <sub>Z</sub>	2.9
4	$Tref(nospA+nospZ)_{p1}$	0.79	1 <sub>T</sub>	3.46
5	$astar490$	0.03	1 <sub>O</sub>	4.25
<b>Chlorophyll</b>				
1	$mA$	13.94	1 <sub>P</sub>	1
2	$Zumax$	1.02	1 <sub>Z</sub>	1.18
3	$Tref(nospA+nospZ)_{p1}$	0.6	1 <sub>T</sub>	2.62
4	$KGcdom$	0.07	1 <sub>OM</sub>	3.24
5	$astar490$	0.02	1 <sub>O</sub>	5.98
<b>Dissolved Oxygen</b>				
1	$umax$	0.05	1 <sub>P</sub>	1
2	$ZKa$	0.05	1 <sub>Z</sub>	2.17
3	$Tref(nospA+nospZ)_{p1}$	0.02	1 <sub>T</sub>	2.29
4	$KG1$	$6.15 \times 10^{-3}$	1 <sub>OM</sub>	3.85
5	$astar490$	$7.51 \times 10^{-4}$	1 <sub>O</sub>	3.89
6	$mA$	0.02	2 <sub>P</sub>	4.42
7	$ZQn$	0.02	2 <sub>Z</sub>	5.22
<b>DOM</b>				
1	$mA$	14.25	1 <sub>P</sub>	1
2	$Tref(nospA+nospZ)_{p1}$	1.48	1 <sub>T</sub>	1.05
3	$Zumax$	1.01	1 <sub>Z</sub>	2.61
4	$KG2$	0.94	1 <sub>OM</sub>	3.39
5	$astar490$	0.04	1 <sub>O</sub>	4.46
6	$umax$	1.11	2 <sub>P</sub>	6.02
7	$ZKa$	0.88	2 <sub>Z</sub>	9.21
<b>Irradiance</b>				
1	$ZKa$	0.13	1 <sub>Z</sub>	1
2	$umax$	0.09	1 <sub>P</sub>	4.41
3	$KGcdom$	0.05	1 <sub>OM</sub>	4.5
4	$Tref(nospA+nospZ)_{p1}$	0.03	1 <sub>T</sub>	4.5
5	$astar490$	0.02	1 <sub>O</sub>	6.9
6	$ZQn$	0.06	2 <sub>Z</sub>	10.63
7	$mA$	0.05	2 <sub>P</sub>	11.21
8	$KG1$	$3.96 \times 10^{-3}$	2 <sub>OM</sub>	14.65
9	$astarOMA$	$1.47 \times 10^{-3}$	2 <sub>O</sub>	14.72
<b>Nitrate</b>				
1	$umax$	8.49	1 <sub>P</sub>	1
<b>Phosphate</b>				
1	$ZKa$	1.47	1 <sub>Z</sub>	1
2	$umax$	0.78	1 <sub>P</sub>	11.45
3	$Tref(nospA+nospZ)_{p1}$	0.16	1 <sub>T</sub>	13.71
4	$KG1$	0.14	1 <sub>OM</sub>	14.64
<b>POM</b>				
1	$mA$	7.22	1 <sub>P</sub>	1
2	$Zumax$	0.96	1 <sub>Z</sub>	1.15
3	$KG1$	0.92	1 <sub>OM</sub>	3.87
4	$Tref(nospA+nospZ)_{p1}$	0.86	1 <sub>T</sub>	3.93
5	$astar490$	0.03	1 <sub>O</sub>	5.81

Table 5: Results of model calibration to observed  $O_2$  for each of seven parameter subsets selected by sensitivity within each parameter category (first), independent of category (second), and equally within each category (third). The collinearity values ( $\gamma$ ) and parameters of each subset are from Tables 2 to 4. Mean L1 is the average of sensitivity values (eq. (2)) for the subset.  $RMSE$  shows the final error comparing observed and model output after the specified number of iterations for optimization.

Selection heuristic	$\gamma$	$n$ parameters	mean L1	Iterations	$RMSE^*$
<b>1</b>					
Optics	3.87	3	$2.81 \times 10^{-4}$	49	72.12
Organic Matter	8.61	5	$3.18 \times 10^{-3}$	154	68.7
Phytoplankton	3.97	7	0.02	1725	68.3
Temperature	1	1	0.02	6	71.76
Zooplankton	5.2	4	0.03	279	71.22
<b>2</b>					
Independent of category	6.81	8	0.03	1530	66.77
<b>3</b>					
Equally within category	5.22	7	0.03	1005	67.44

\*Starting  $RMSE = 72.140$

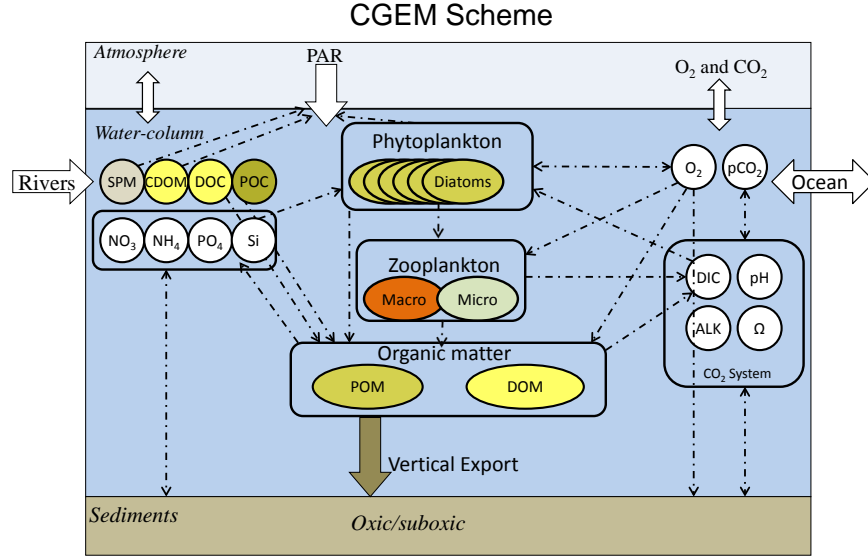


Fig. 1: Conceptual representation of biogeochemical components modelled in CGEM (complete equations [Eldridge and Roelke 2010](#)). FishTank implements a 0-D version of the model that does not include any advection, mixing, or sediment diagenesis.

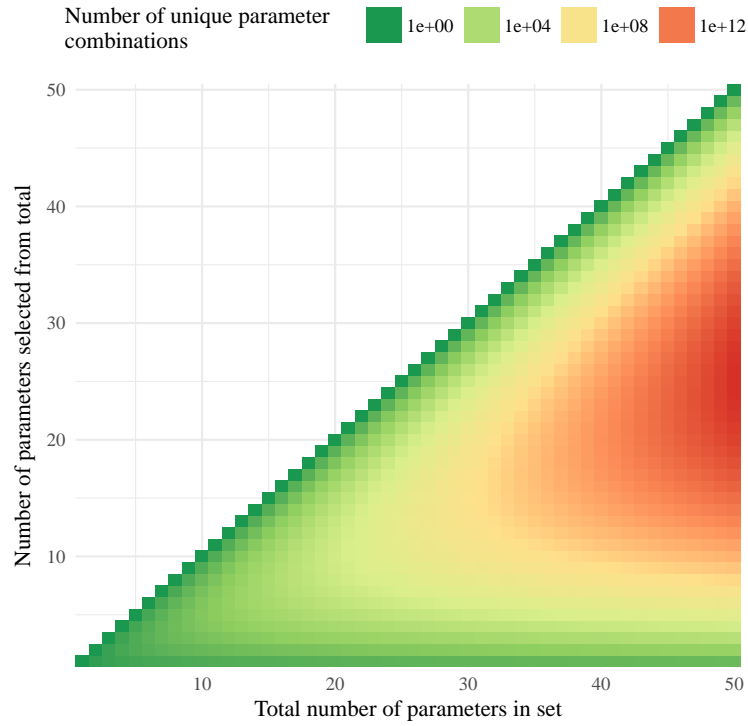


Fig. 2: Examples of unique parameter combinations from different parameter sets and number of selected parameters. The number of combinations are shown for increasing numbers of selected parameters from the total in the set, where 50 parameter sets are shown each with one through 50 total parameters. Note that the number of unique combinations is shown as the natural-log.

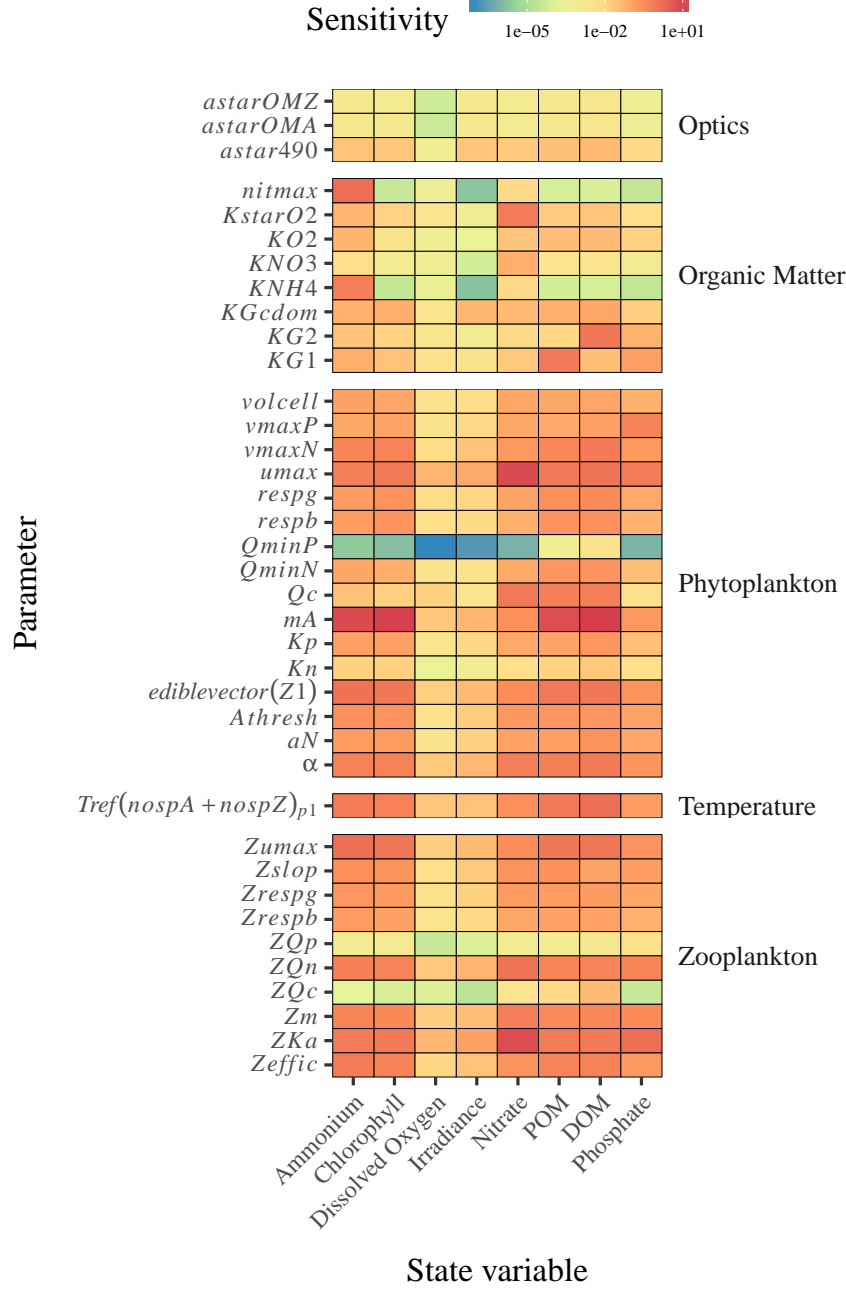


Fig. 3: Sensitivity values (L1, eq. (2)) of all state variables to changes in a 50% increase in parameter values. Parameters are grouped by category: optics, organic matter, phytoplankton, zooplankton, temperature, and zoplankton. See Table 1 for L1 values for O<sub>2</sub> and Tables S1 to S7 for the other state variables.

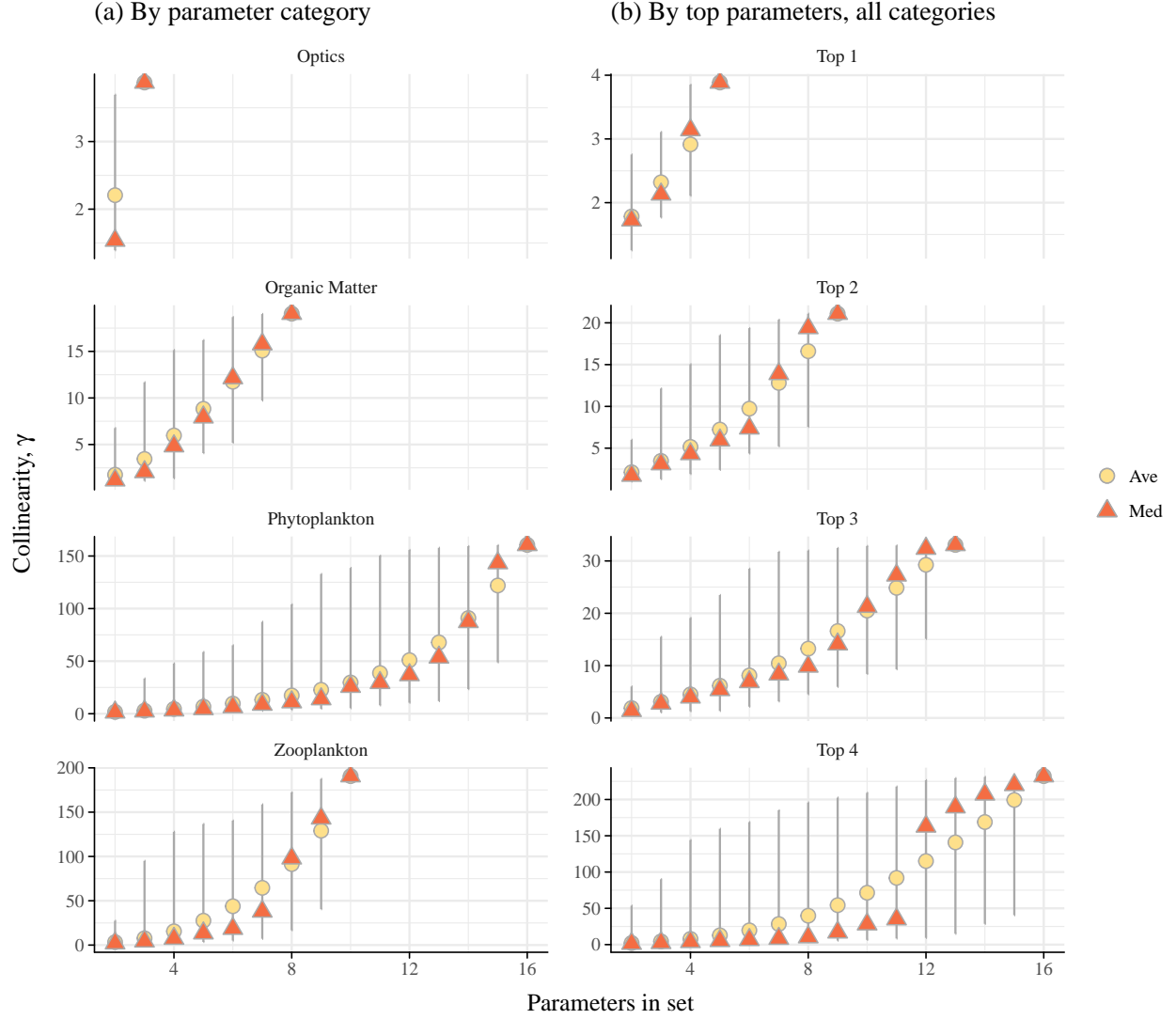


Fig. 4: Collinearity ( $\gamma$  as a measure of identifiability, eq. (3)) of parameter subsets for  $O_2$ . Plots in (a) show collinearity by parameter categories and (b) shows collinearity by selecting the top 1 through 4 parameters in all categories. Lines represent collinearity ranges for the possible combinations given the number of parameters in the set. The temperature category is not shown because  $O_2$  was sensitive to only one parameter (i.e.,  $\gamma = 1$ ).

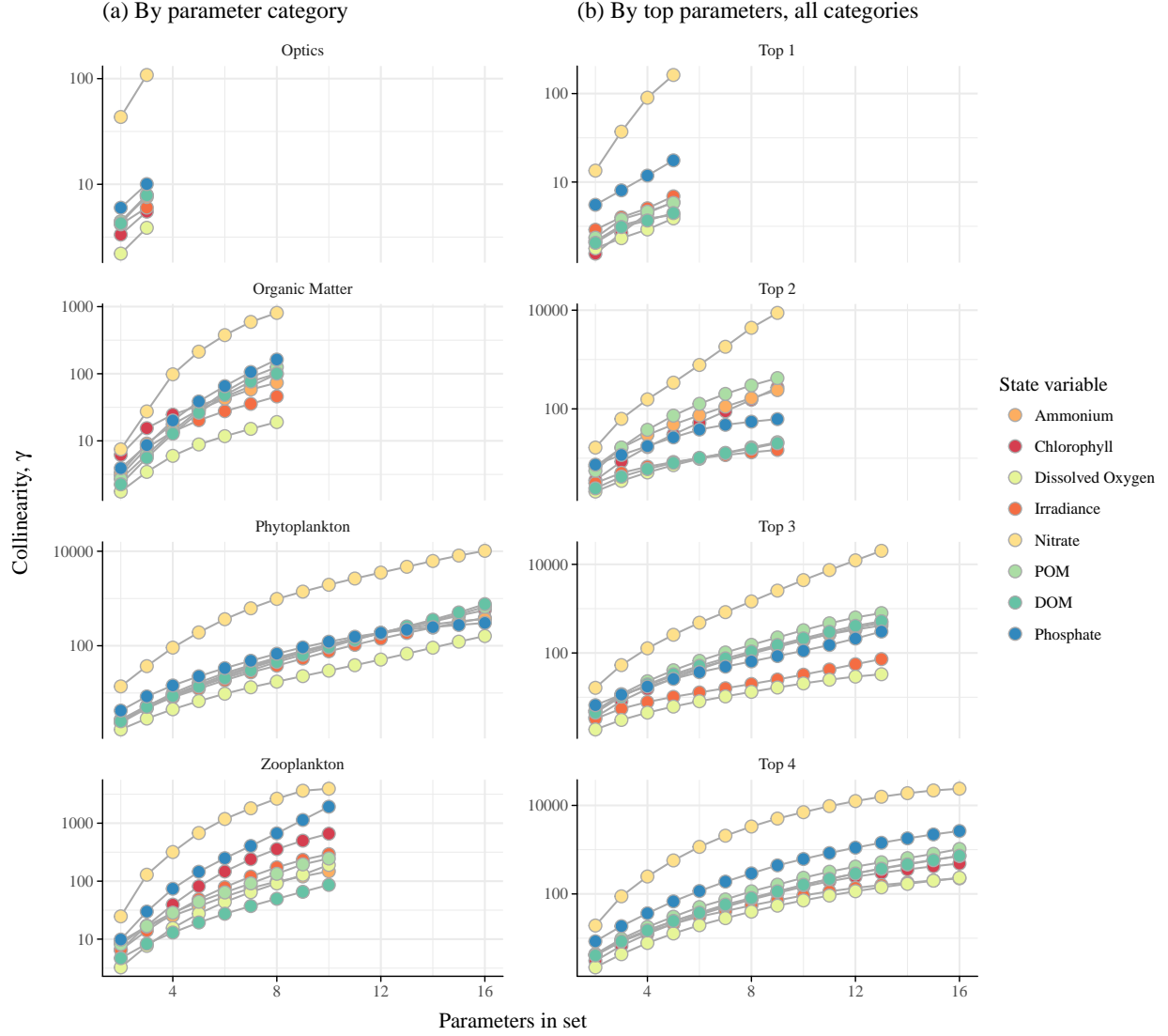


Fig. 5: Average collinearity ( $\gamma$  as a measure of identifiability, eq. (3)) of parameter subsets for all state variables. Plots in (a) show collinearity by parameter categories and (b) shows collinearity by selecting the top 1 through 4 parameters in all categories. Collinearity was averaged for all combinations in a parameter set to evaluate relative differences between state variables. The temperature category is not shown because all state variables were sensitive to only one parameter (i.e.,  $\gamma = 1$ ).

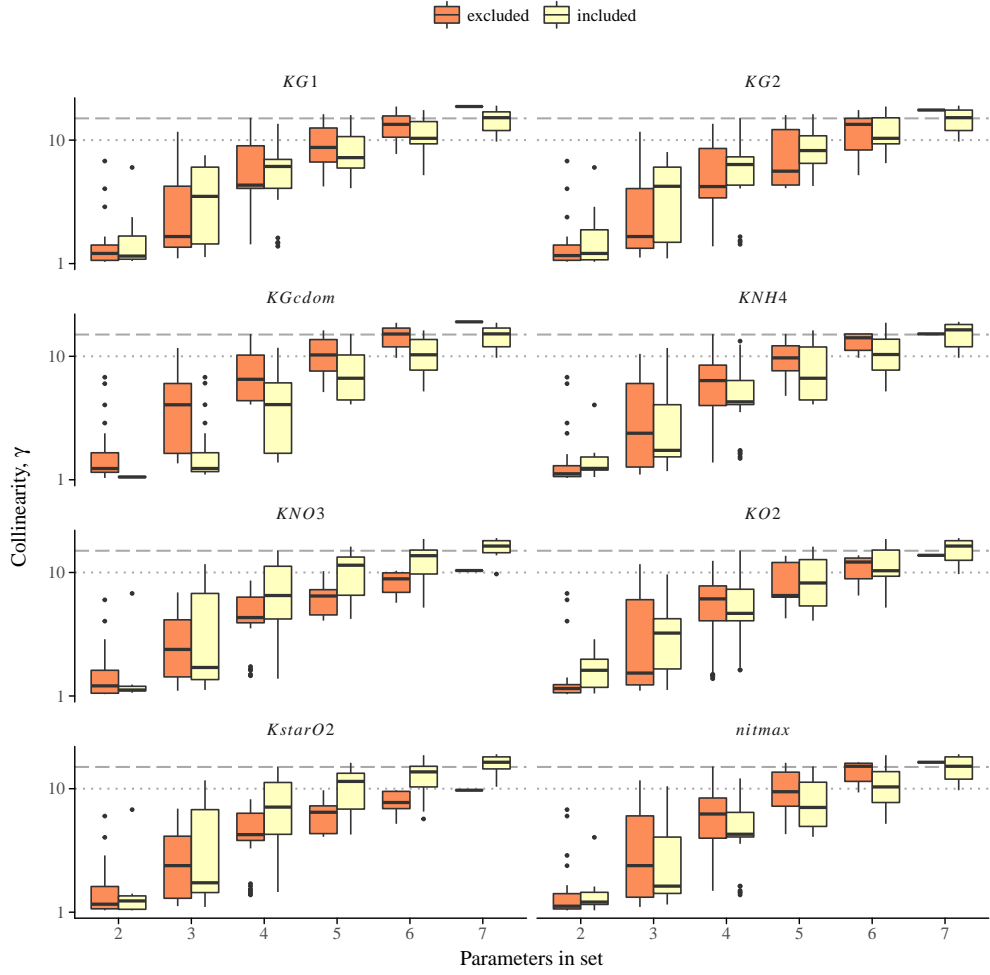


Fig. 6: Collinearity ( $\gamma$  as a measure of identifiability, eq. (3)) for  $O_2$  of organic matter parameters for subset combinations in Fig. 4. Collinearity is evaluated for subsets that excluded and included the parameters at the top of each plot. Collinearity of including all eight parameters is in Fig. 4. Grey lines indicate potential thresholds at  $\gamma = 10, 15$  for maximum acceptable collinearity.

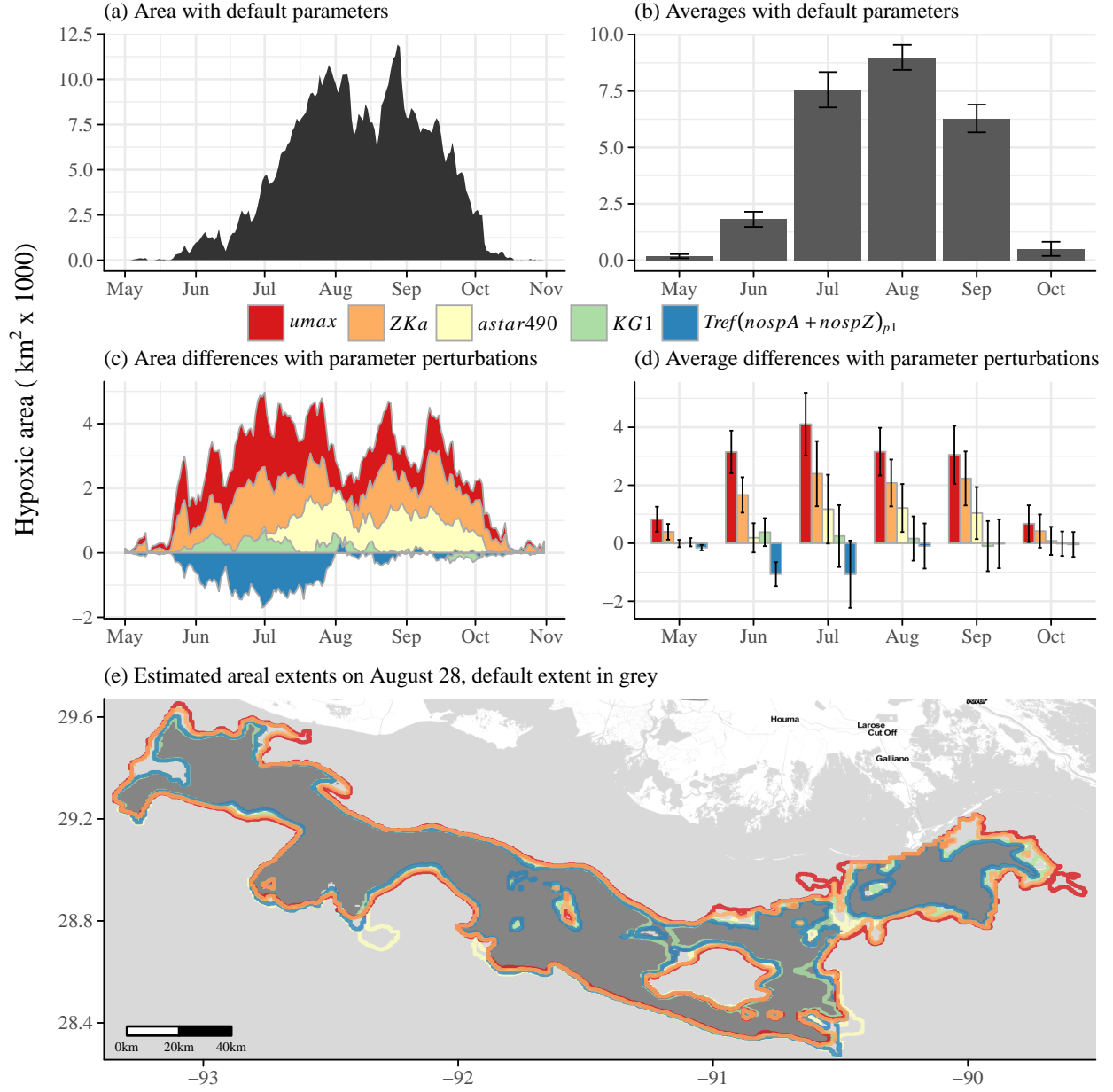


Fig. 7: Estimated hypoxic area and monthly averages (km<sup>2</sup> × 1000) using the default parameter settings (a, b) and the differences using a 50% increase in each parameter (c, d). The selected parameters were the top sensitive in each parameter category for O<sub>2</sub> in Fig. 3 and Table 1. Error bars are 95% confidence intervals for the monthly averages in (b) and the difference in monthly averages (d) from the perturbed and default results. Areal extent of estimated hypoxia on August 28<sup>th</sup> using the default parameters (grey) and estimated changes with parameter perturbations is shown in (e).



Table S1: Sensitivity of ammonium to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where  $L1$  summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect ammonium are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
<b>Optics</b>		
Chla specific absorption at 490 nm	<i>astar490</i>	0.03
OMA specific absorption at 490 nm	<i>astarOMA</i>	$1.63 \times 10^{-3}$
OMZ specific absorption at 490 nm	<i>astarOMZ</i>	$1.5 \times 10^{-3}$
<b>Temperature</b>		
Optimum temperature for growth(C)	<i>Tref(nospA+nospZ)<sub>p1</sub></i>	0.79
<b>Phytoplankton</b>		
mortality coefficient	<i>mA</i>	8.49
edibility vector for Z1	<i>ediblevector(Z1)</i>	1.32
maximum growth rate	<i>umax</i>	0.65
initial slope of the photosynthesis-irradiance relationship	<i>alpha</i>	0.6
N-uptake rate measured at umax	<i>vmaxN</i>	0.46
Phytoplankton threshold for grazing, is multiplied by VOLcell	<i>Athresh</i>	0.29
coefficient for non-limiting nutrient	<i>aN</i>	0.17
phytoplankton growth respiration coefficient	<i>respg</i>	0.16
phytoplankton basal respiration coefficient	<i>respb</i>	0.15
half-saturation constant for P	<i>Kp</i>	0.14
phytoplankton volume/cell	<i>volcell</i>	0.14
minimum N cell-quota	<i>QminN</i>	0.1
P-uptake rate measured at umax	<i>vmaxP</i>	0.1
phytoplankton carbon/cell	<i>Qc</i>	0.03
half-saturation constant for N	<i>Kn</i>	0.01
minimum P cell-quota	<i>QminP</i>	$2.24 \times 10^{-6}$
<b>Zooplankton</b>		
maximum growth rate of zooplankton	<i>Zumax</i>	1.42
assimilation efficiency as a fraction of ingestion	<i>Zeffic</i>	0.76
half saturation coefficient for grazing	<i>ZKa</i>	0.74
zooplankton nitrogen/individual	<i>ZQn</i>	0.62
Zooplankton mortality constant for quadratic mortality	<i>Zm</i>	0.5
proportion of grazed phytoplankton lost to sloppy feeding	<i>Zslop</i>	0.3
Zooplankton growth-dependent respiration factor	<i>Zrespg</i>	0.22
Zooplankton biomass-dependent respiration factor	<i>Zrespb</i>	0.16
zooplankton phosphorus/individual	<i>ZQp</i>	$1.07 \times 10^{-3}$
zooplankton carbon/individual	<i>ZQc</i>	$1.44 \times 10^{-4}$
<b>Organic Matter</b>		
maximum rate of nitrification per day	<i>nitmax</i>	1.54
NH4 rate constant for nitrification	<i>KNH4</i>	0.66
turnover rate for OM1A and OM1Z	<i>KG1</i>	0.07
decay rate of CDOM, 1/day	<i>KGcdom</i>	0.07
half-saturation concentration for O2 utilization	<i>KO2</i>	0.06
O2 concentration that inhibits denitrification	<i>KstarO2</i>	0.05
turnover rate for OM2A and OM2Z	<i>KG2</i>	0.03
half-saturation concentration for NO3 used in denitrification	<i>KNO3</i>	$7.55 \times 10^{-3}$

Table S2: Sensitivity of chl-*a* to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where *L1* summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect chl-*a* are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
<b>Optics</b>		
Chla specific absorption at 490 nm	<i>astar490</i>	0.02
OMA specific absorption at 490 nm	<i>astarOMA</i>	$1.45 \times 10^{-3}$
OMZ specific absorption at 490 nm	<i>astarOMZ</i>	$1.13 \times 10^{-3}$
<b>Temperature</b>		
Optimum temperature for growth(C)	<i>Tref(nospA+nospZ)<sub>p1</sub></i>	0.6
<b>Phytoplankton</b>		
mortality coefficient	<i>mA</i>	13.94
edibility vector for Z1	<i>ediblevector(Z1)</i>	0.95
maximum growth rate	<i>umax</i>	0.85
initial slope of the photosynthesis-irradiance relationship	<i>alpha</i>	0.62
N-uptake rate measured at umax	<i>vmaxN</i>	0.53
phytoplankton growth respiration coefficient	<i>respg</i>	0.26
Phytoplankton threshold for grazing, is multiplied by VOLcell	<i>Athresh</i>	0.25
phytoplankton basal respiration coefficient	<i>respb</i>	0.24
coefficient for non-limiting nutrient	<i>aN</i>	0.17
half-saturation constant for P	<i>Kp</i>	0.14
P-uptake rate measured at umax	<i>vmaxP</i>	0.12
phytoplankton volume/cell	<i>volcell</i>	0.1
minimum N cell-quota	<i>QminN</i>	0.07
phytoplankton carbon/cell	<i>Qc</i>	0.02
half-saturation constant for N	<i>Kn</i>	0.01
minimum P cell-quota	<i>QminP</i>	$1.38 \times 10^{-6}$
<b>Zooplankton</b>		
maximum growth rate of zooplankton	<i>Zumax</i>	1.02
half saturation coefficient for grazing	<i>ZKa</i>	0.85
assimilation efficiency as a fraction of ingestion	<i>Zeffic</i>	0.57
zooplankton nitrogen/individual	<i>ZQn</i>	0.52
Zooplankton mortality constant for quadratic mortality	<i>Zm</i>	0.41
proportion of grazed phytoplankton lost to sloppy feeding	<i>Zslop</i>	0.23
Zooplankton growth-dependent respiration factor	<i>Zrespg</i>	0.17
Zooplankton biomass-dependent respiration factor	<i>Zrespb</i>	0.14
zooplankton phosphorus/individual	<i>ZQp</i>	$1.29 \times 10^{-3}$
zooplankton carbon/individual	<i>ZQc</i>	$7.55 \times 10^{-5}$
<b>Organic Matter</b>		
decay rate of CDOM, 1/day	<i>KGcdom</i>	0.07
turnover rate for OM1A and OM1Z	<i>KG1</i>	0.03
turnover rate for OM2A and OM2Z	<i>KG2</i>	0.01
O2 concentration that inhibits denitrification	<i>KstarO2</i>	0.01
half-saturation concentration for O2 utilization	<i>KO2</i>	$3.35 \times 10^{-3}$
half-saturation concentration for NO3 used in denitrification	<i>KNO3</i>	$1.19 \times 10^{-3}$
maximum rate of nitrification per day	<i>nitmax</i>	$3.4 \times 10^{-5}$
NH4 rate constant for nitrification	<i>KNH4</i>	$2.97 \times 10^{-5}$

Table S3: Sensitivity of irradiance to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where  $L1$  summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect irradiance are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
<b>Optics</b>		
Chla specific absorption at 490 nm	<i>astar490</i>	0.02
OMA specific absorption at 490 nm	<i>astarOMA</i>	$1.47 \times 10^{-3}$
OMZ specific absorption at 490 nm	<i>astarOMZ</i>	$1.34 \times 10^{-3}$
<b>Temperature</b>		
Optimum temperature for growth(C)	<i>Tref(nospA+nospZ)<sub>p1</sub></i>	0.03
<b>Phytoplankton</b>		
maximum growth rate	<i>umax</i>	0.09
mortality coefficient	<i>mA</i>	0.05
initial slope of the photosynthesis-irradiance relationship	<i>alpha</i>	0.04
edibility vector for Z1	<i>ediblevector(Z1)</i>	0.04
N-uptake rate measured at umax	<i>vmaxN</i>	0.03
Phytoplankton threshold for grazing, is multiplied by VOLcell	<i>Athresh</i>	0.02
coefficient for non-limiting nutrient	<i>aN</i>	0.01
phytoplankton growth respiration coefficient	<i>respg</i>	0.01
half-saturation constant for P	<i>Kp</i>	0.01
P-uptake rate measured at umax	<i>vmaxP</i>	$9.48 \times 10^{-3}$
phytoplankton basal respiration coefficient	<i>respb</i>	$9.38 \times 10^{-3}$
phytoplankton volume/cell	<i>volcell</i>	$8.1 \times 10^{-3}$
minimum N cell-quota	<i>QminN</i>	$5.75 \times 10^{-3}$
phytoplankton carbon/cell	<i>Qc</i>	$3.78 \times 10^{-3}$
half-saturation constant for N	<i>Kn</i>	$9.81 \times 10^{-4}$
minimum P cell-quota	<i>QminP</i>	$1.92 \times 10^{-7}$
<b>Zooplankton</b>		
half saturation coefficient for grazing	<i>ZKa</i>	0.13
zooplankton nitrogen/individual	<i>ZQn</i>	0.06
maximum growth rate of zooplankton	<i>Zumax</i>	0.04
Zooplankton mortality constant for quadratic mortality	<i>Zm</i>	0.04
assimilation efficiency as a fraction of ingestion	<i>Zeffic</i>	0.03
proportion of grazed phytoplankton lost to sloppy feeding	<i>Zslop</i>	0.02
Zooplankton growth-dependent respiration factor	<i>Zrespg</i>	0.01
Zooplankton biomass-dependent respiration factor	<i>Zrespb</i>	$9.67 \times 10^{-3}$
zooplankton phosphorus/individual	<i>ZQp</i>	$9.34 \times 10^{-5}$
zooplankton carbon/individual	<i>ZQc</i>	$1.99 \times 10^{-5}$
<b>Organic Matter</b>		
decay rate of CDOM, 1/day	<i>KGcdom</i>	0.05
turnover rate for OM1A and OM1Z	<i>KG1</i>	$3.96 \times 10^{-3}$
turnover rate for OM2A and OM2Z	<i>KG2</i>	$9.88 \times 10^{-4}$
O2 concentration that inhibits denitrification	<i>KstarO2</i>	$7.2 \times 10^{-4}$
half-saturation concentration for O2 utilization	<i>KO2</i>	$3.54 \times 10^{-4}$
half-saturation concentration for NO3 used in denitrification	<i>KNO3</i>	$6.18 \times 10^{-5}$
maximum rate of nitrification per day	<i>nitmax</i>	$1.72 \times 10^{-6}$
NH4 rate constant for nitrification	<i>KNH4</i>	$1.48 \times 10^{-6}$

Table S4: Sensitivity of nitrate to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where  $L1$  summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect nitrate are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
<b>Optics</b>		
Chla specific absorption at 490 nm	<i>astar490</i>	0.02
OMZ specific absorption at 490 nm	<i>astarOMZ</i>	$1.27 \times 10^{-3}$
OMA specific absorption at 490 nm	<i>astarOMA</i>	$1.19 \times 10^{-3}$
<b>Temperature</b>		
Optimum temperature for growth(C)	<i>Tref(nospA+nospZ)<sub>p1</sub></i>	0.3
<b>Phytoplankton</b>		
maximum growth rate	<i>umax</i>	8.49
phytoplankton carbon/cell	<i>Qc</i>	0.89
initial slope of the photosynthesis-irradiance relationship	<i>alpha</i>	0.7
edibility vector for Z1	<i>ediblevector(Z1)</i>	0.33
mortality coefficient	<i>mA</i>	0.27
Phytoplankton threshold for grazing, is multiplied by VOLcell	<i>Athresh</i>	0.2
N-uptake rate measured at umax	<i>vmaxN</i>	0.19
coefficient for non-limiting nutrient	<i>aN</i>	0.13
phytoplankton growth respiration coefficient	<i>respg</i>	0.11
phytoplankton volume/cell	<i>volcell</i>	0.1
P-uptake rate measured at umax	<i>vmaxP</i>	0.1
half-saturation constant for P	<i>Kp</i>	0.09
minimum N cell-quota	<i>QminN</i>	0.09
phytoplankton basal respiration coefficient	<i>respb</i>	0.07
half-saturation constant for N	<i>Kn</i>	$7.06 \times 10^{-3}$
minimum P cell-quota	<i>QminP</i>	$6.67 \times 10^{-7}$
<b>Zooplankton</b>		
half saturation coefficient for grazing	<i>ZKa</i>	7.59
zooplankton nitrogen/individual	<i>ZQn</i>	1.17
Zooplankton mortality constant for quadratic mortality	<i>Zm</i>	0.7
maximum growth rate of zooplankton	<i>Zumax</i>	0.34
proportion of grazed phytoplankton lost to sloppy feeding	<i>Zslop</i>	0.26
assimilation efficiency as a fraction of ingestion	<i>Zeffic</i>	0.25
Zooplankton growth-dependent respiration factor	<i>Zrespg</i>	0.17
Zooplankton biomass-dependent respiration factor	<i>Zrespb</i>	0.1
zooplankton carbon/individual	<i>ZQc</i>	$3.8 \times 10^{-3}$
zooplankton phosphorus/individual	<i>ZQp</i>	$8.59 \times 10^{-4}$
<b>Organic Matter</b>		
O2 concentration that inhibits denitrification	<i>KstarO2</i>	0.78
half-saturation concentration for NO3 used in denitrification	<i>KNO3</i>	0.07
decay rate of CDOM, 1/day	<i>KGcdom</i>	0.04
half-saturation concentration for O2 utilization	<i>KO2</i>	0.03
turnover rate for OM1A and OM1Z	<i>KG1</i>	0.02
turnover rate for OM2A and OM2Z	<i>KG2</i>	0.01
maximum rate of nitrification per day	<i>nitmax</i>	$9.96 \times 10^{-3}$
NH4 rate constant for nitrification	<i>KNH4</i>	$9.87 \times 10^{-3}$

Table S5: Sensitivity of POM to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where  $L1$  summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect POM are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
<b>Optics</b>		
Chla specific absorption at 490 nm	$astar490$	0.03
OMA specific absorption at 490 nm	$astarOMA$	$1.73 \times 10^{-3}$
OMZ specific absorption at 490 nm	$astarOMZ$	$1.49 \times 10^{-3}$
<b>Temperature</b>		
Optimum temperature for growth(C)	$Tref(nospA + nospZ)_{p1}$	0.86
<b>Phytoplankton</b>		
mortality coefficient	$mA$	7.22
edibility vector for Z1	$ediblevector(Z1)$	0.9
maximum growth rate	$umax$	0.89
phytoplankton carbon/cell	$Qc$	0.67
initial slope of the photosynthesis-irradiance relationship	$alpha$	0.67
N-uptake rate measured at $umax$	$vmaxN$	0.45
phytoplankton growth respiration coefficient	$respg$	0.29
phytoplankton basal respiration coefficient	$respb$	0.24
Phytoplankton threshold for grazing, is multiplied by VOLcell	$Athresh$	0.22
minimum N cell-quota	$QminN$	0.21
coefficient for non-limiting nutrient	$aN$	0.14
half-saturation constant for P	$Kp$	0.11
phytoplankton volume/cell	$volcell$	0.1
P-uptake rate measured at $umax$	$vmaxP$	0.09
half-saturation constant for N	$Kn$	0.01
minimum P cell-quota	$QminP$	$7.35 \times 10^{-4}$
<b>Zooplankton</b>		
maximum growth rate of zooplankton	$Zumax$	0.96
half saturation coefficient for grazing	$ZKa$	0.79
assimilation efficiency as a fraction of ingestion	$Zeffic$	0.54
zooplankton nitrogen/individual	$ZQn$	0.49
Zooplankton mortality constant for quadratic mortality	$Zm$	0.39
proportion of grazed phytoplankton lost to sloppy feeding	$Zslop$	0.27
Zooplankton growth-dependent respiration factor	$Zrespg$	0.16
Zooplankton biomass-dependent respiration factor	$Zrespb$	0.12
zooplankton carbon/individual	$ZQc$	$9.64 \times 10^{-3}$
zooplankton phosphorus/individual	$ZQp$	$1.06 \times 10^{-3}$
<b>Organic Matter</b>		
turnover rate for OM1A and OM1Z	$KG1$	0.92
decay rate of CDOM, 1/day	$KGcdom$	0.07
half-saturation concentration for O2 utilization	$KO2$	0.04
O2 concentration that inhibits denitrification	$KstarO2$	0.02
turnover rate for OM2A and OM2Z	$KG2$	0.01
half-saturation concentration for NO3 used in denitrification	$KNO3$	$3.72 \times 10^{-3}$
maximum rate of nitrification per day	$nitmax$	$6.98 \times 10^{-5}$
NH4 rate constant for nitrification	$KNH4$	$6.41 \times 10^{-5}$

Table S6: Sensitivity of dissolved organic matter to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where  $L1$  summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect dissolved organic matter are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
<b>Optics</b>		
Chla specific absorption at 490 nm	<i>astar490</i>	0.04
OMA specific absorption at 490 nm	<i>astarOMA</i>	$2.48 \times 10^{-3}$
OMZ specific absorption at 490 nm	<i>astarOMZ</i>	$2.04 \times 10^{-3}$
<b>Temperature</b>		
Optimum temperature for growth(C)	<i>Tref(nospA+nospZ)<sub>p1</sub></i>	1.48
<b>Phytoplankton</b>		
mortality coefficient	<i>mA</i>	14.25
maximum growth rate	<i>umax</i>	1.11
edibility vector for Z1	<i>ediblevector(Z1)</i>	0.94
N-uptake rate measured at umax	<i>vmaxN</i>	0.86
initial slope of the photosynthesis-irradiance relationship	<i>alpha</i>	0.85
phytoplankton carbon/cell	<i>Qc</i>	0.67
phytoplankton growth respiration coefficient	<i>respg</i>	0.36
phytoplankton basal respiration coefficient	<i>respb</i>	0.29
coefficient for non-limiting nutrient	<i>aN</i>	0.25
minimum N cell-quota	<i>QminN</i>	0.24
Phytoplankton threshold for grazing, is multiplied by VOLcell	<i>Athresh</i>	0.22
half-saturation constant for P	<i>Kp</i>	0.2
P-uptake rate measured at umax	<i>vmaxP</i>	0.14
phytoplankton volume/cell	<i>volcell</i>	0.1
half-saturation constant for N	<i>Kn</i>	0.02
minimum P cell-quota	<i>QminP</i>	$4.37 \times 10^{-3}$
<b>Zooplankton</b>		
maximum growth rate of zooplankton	<i>Zumax</i>	1.01
half saturation coefficient for grazing	<i>ZKa</i>	0.88
assimilation efficiency as a fraction of ingestion	<i>Zeffic</i>	0.58
zooplankton nitrogen/individual	<i>ZQn</i>	0.54
Zooplankton mortality constant for quadratic mortality	<i>Zm</i>	0.41
Zooplankton growth-dependent respiration factor	<i>Zrespg</i>	0.17
Zooplankton biomass-dependent respiration factor	<i>Zrespb</i>	0.13
proportion of grazed phytoplankton lost to sloppy feeding	<i>Zslop</i>	0.12
zooplankton carbon/individual	<i>ZQc</i>	0.04
zooplankton phosphorus/individual	<i>ZQp</i>	$1.69 \times 10^{-3}$
<b>Organic Matter</b>		
turnover rate for OM2A and OM2Z	<i>KG2</i>	0.94
decay rate of CDOM, 1/day	<i>KGcdom</i>	0.1
half-saturation concentration for O2 utilization	<i>KO2</i>	0.04
turnover rate for OM1A and OM1Z	<i>KG1</i>	0.04
O2 concentration that inhibits denitrification	<i>KstarO2</i>	0.03
half-saturation concentration for NO3 used in denitrification	<i>KNO3</i>	$3.16 \times 10^{-3}$
maximum rate of nitrification per day	<i>nitmax</i>	$8.44 \times 10^{-5}$
NH4 rate constant for nitrification	<i>KNH4</i>	$7.41 \times 10^{-5}$

Table S7: Sensitivity of phosphate to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where  $L1$  summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect phosphate are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
<b>Optics</b>		
Chla specific absorption at 490 nm	<i>astar490</i>	$9.01 \times 10^{-3}$
OMZ specific absorption at 490 nm	<i>astarOMZ</i>	$5.21 \times 10^{-4}$
OMA specific absorption at 490 nm	<i>astarOMA</i>	$5.13 \times 10^{-4}$
<b>Temperature</b>		
Optimum temperature for growth(C)	<i>Tref(nospA+nospZ)<sub>p1</sub></i>	0.16
<b>Phytoplankton</b>		
maximum growth rate	<i>umax</i>	0.78
P-uptake rate measured at umax	<i>vmaxP</i>	0.59
edibility vector for Z1	<i>ediblevector(Z1)</i>	0.25
initial slope of the photosynthesis-irradiance relationship	<i>alpha</i>	0.23
mortality coefficient	<i>mA</i>	0.2
N-uptake rate measured at umax	<i>vmaxN</i>	0.18
Phytoplankton threshold for grazing, is multiplied by VOLcell	<i>Athresh</i>	0.13
coefficient for non-limiting nutrient	<i>aN</i>	0.11
phytoplankton growth respiration coefficient	<i>respg</i>	0.09
phytoplankton volume/cell	<i>volcell</i>	0.06
phytoplankton basal respiration coefficient	<i>respb</i>	0.06
minimum N cell-quota	<i>QminN</i>	0.04
half-saturation constant for P	<i>Kp</i>	0.03
half-saturation constant for N	<i>Kn</i>	$6.97 \times 10^{-3}$
phytoplankton carbon/cell	<i>Qc</i>	$6.68 \times 10^{-3}$
minimum P cell-quota	<i>QminP</i>	$8.21 \times 10^{-7}$
<b>Zooplankton</b>		
half saturation coefficient for grazing	<i>ZKa</i>	1.47
zooplankton nitrogen/individual	<i>ZQn</i>	0.5
Zooplankton mortality constant for quadratic mortality	<i>Zm</i>	0.35
maximum growth rate of zooplankton	<i>Zumax</i>	0.26
assimilation efficiency as a fraction of ingestion	<i>Zeffic</i>	0.19
proportion of grazed phytoplankton lost to sloppy feeding	<i>Zslop</i>	0.15
Zooplankton growth-dependent respiration factor	<i>Zrespg</i>	0.1
Zooplankton biomass-dependent respiration factor	<i>Zrespb</i>	0.06
zooplankton phosphorus/individual	<i>ZQp</i>	$6.43 \times 10^{-3}$
zooplankton carbon/individual	<i>ZQc</i>	$3.38 \times 10^{-5}$
<b>Organic Matter</b>		
turnover rate for OM1A and OM1Z	<i>KG1</i>	0.14
turnover rate for OM2A and OM2Z	<i>KG2</i>	0.06
decay rate of CDOM, 1/day	<i>KGcdom</i>	0.02
half-saturation concentration for O2 utilization	<i>KO2</i>	0.01
O2 concentration that inhibits denitrification	<i>KstarO2</i>	$7.29 \times 10^{-3}$
half-saturation concentration for NO3 used in denitrification	<i>KNO3</i>	$1.19 \times 10^{-3}$
maximum rate of nitrification per day	<i>nitmax</i>	$2.7 \times 10^{-5}$
NH4 rate constant for nitrification	<i>KNH4</i>	$2.64 \times 10^{-5}$