# Parameter sensitivity and identifiability for a biogeochemical model of hypoxia in the northern Gulf of Mexico

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Abstract

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Bio-geo-chemical models are useful tools in environmental sciences that can guide management and policy-making. Consequently, significant time and resources are spent developing these models in system-specific contexts. The optimization of model parameters to maximize precision, including transferability of these models to different systems, are fundamental concerns in the development and application of these tools. This study provides a context for understanding quantitative limitations of coupled hydrodynamic-ecological models by evaluating parameter sensitivity and identifability of a zero-dimensional (0-D) unit of a larger spatio-temporal model of hypoxia on the Louisiana continental shelf of Gulf of Mexico. The analysis provides a contrast of numeric and ecological certainty in parameter subsets using a systematic framework to infer larger trends in dissolved oxygen dynamics over time, having implications for understanding factors that contribute to environmental conditions that are detrimental to aquatic resources. In particular, we focus on issues of parameter identifiability using local sensitivity analyses to provide quantitative descriptions of numerical constraints on model precision. The sensitivity of state variables differed considerably with parameter changes, although most variables were responsive to changes in parameters that influenced planktonic growth rates. Variation in sensitivity had a direct correspondence with identifiability, such that only small subsets of the complete parameter set were characterized as having unique effects on the model output. As a result, we provide a set of parameter selection heuristics that can be used to identify parameters for model calibration that depend on relative sensitivity and ecological categories within the biogeochemical equations. Although these concerns have been expressed in the literature, they are rarely explicitly addressed or included in evaluations of water quality models. In addition to immediate implications for regional models, we provide a framework for describing the effects of parameter uncertainty and identifiability that can be applied to similar models to better inform environmental management.

# 1 Introduction

Hypoxia formation in bottom waters of coastal oceans occurs primarily from excess nutrient inputs from land-based sources (Justíc et al. 1987, Diaz and Rosenberg 1995, Howarth et al. 1996). These events are detrimental to aquatic organisms and have significant negative effects on economic resources derived from coastal ecosystems (Lipton and Hicks 2003, Diaz and

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Rosenberg 2011). An understanding of the biological, physical, and chemical processes that
   contribute to the growth of hypoxic areas is a critical concern for mitigating and preventing these
   negative impacts. Numerical ecosystem models are important tools that synthesize knowledge of
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   ecosystem processes that contribute to hypoxia formation and for predicting the effects of
   proposed management activities or future scenarios (Scavia et al. 2004, Hagy and Murrell 2007,
   Pauer et al. 2016). Unlike statistical models with more generic structures, simulation and
   process-based models include explicit descriptions of relevant processes that are constrained by
   empirical or observational data relevant to the system of interest (e.g. Omlin et al. 2001b,
   Eldridge and Roelke 2010). These models are often coupled with hydrodynamic grids to provide
   spatially-explicit representations of patterns in three dimensions (Warner et al. 2005, Zhao et al.
   2010, Ganju et al. 2016). Combined hydrodynamic and bio-geo-chemical models have been
   developed specifically to describe hypoxic conditions on the \texttt{Louisiana} continental shelf (LCS) in
   the northern Gulf of Mexico (GOM) (Fennel et al. 2013, Obenour et al. 2015, Pauer et al. 2016,
   Lehrter et al. in press). This area drains a significant portion of the continental United States
   through the Mississippi-Atchafalaya River Basin (MARB) and is the second largest hypoxic area
   in the world (Rabalais et al. 2002). Understanding processes that contribute to the frequency and
   duration of hypoxic events remains a critical research goal for the region, including the
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   application of process-based models to characterize the current knowledge domain.
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           The development and application of a model represents a tradeoff between characteristics
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   expected from the output or provided by the structural components. An idealized model is
   sufficiently generalizable across systems, provides results that are precise given the inputs, and
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   includes components that are realistic descriptions of actual processes (Levins 1966). Given that
   these characteristics cannot be simultaneously achieved, models are developed in partial
   dependence of reality and theoretical constructs, completely separate from both, or dependent on
   one or the other (Morrison and Morgan 1999, Ganju et al. 2016). These challenges are analagous
   to the well-known bias-variance tradeoff in statistical models that balances the competing
   objectives of over- and under-fitting to an observed dataset. Process-based models are more
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   commonly imbalanced between reality and theory, such that most are over-parameterized in an
   attempt to completely describe reality (Denman 2003, Nossent and Bauwens 2012, Petrucci and
   Bonhomme 2014). Such over-parameterization, including use of many structural equations, can
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have serious implications for practical applications. Quantitative limitations of over-parameterization are analagous to degrees of freedom in standard statistical models as free parameters cannot be numerically estimated when constrained to an observed dataset (Kirchner 67 2006). More importantly, over-parameterization can limit use across systems outside of the data domain and impose uncertainty in model predictions as realistic values for every variable may not be known or inaccurately applied from existing studies (Durand et al. 2002, Refsgaard et al. 2007, Wade et al. 2008). The application of process-based models to describe hypoxia dynamics has not been immune to these challenges and comprehensive approaches are needed to develop models that more carefully balance theory with reality (e.g., Snowling and Kramer 2001). Standard approaches for uncertainty analysis can be used to begin addressing model 74 complexity issues. In the most general sense, uncertainty is evaluated relative to the effects of input conditions or the observed data used to calibrate a model, changes in parameter values, or variation in the structural components (i.e., observational, parameter, or structural uncertainty) 77 (Beck 1987). Evaluating parameter uncertainty is by far the most common and simplest means of 78 evaluating model behavior. Although uncertainty analyses should be integrated throughout model development and application, parameters are more often evaluated post-hoc as a form of 'damage control' for further calibration. This approach is sometimes called inverse modelling where 81 results from sensitivity analyses are used to guide calibration or fit of the developed model to observations (Soetaert and Petzoldt 2010, or confronting models with data, sensu Hilborn and 83 Mangel 1997). Parameter sensitivity analysis combined with inverse modelling necessarily involves questions of parameter 'identifiability', where only a subset of parameters can be numerically constrained to the data as compared to the entire parameter set. Redundancies in parameter effects lead to unidentifiable models where optimal solutions may be empirically 87 impossible (i.e., standard algorithms will not converge) or parameter values may be non-unique leading to the right answer for the wrong reason (Kirchner 2006). An unidentifiable parameter or parameter set has effects on model output that can be undone or compensated for by alteration of 90 other parameters. The concept of identifiable parameter subsets is not foreign to hypoxia or eutrophication models (Omlin et al. 2001a, Estrada and Diaz 2010, Mateus and Franz 2015), although there is a clear need for greater integration of these concepts in model development (Fasham et al. 2006). Moreover, the inclusion of sensitivity and identifiability analyses in model

tuning will require the adoption of conservative selection rules for parameters to calibrate given the number of unique combinations of parameter subsets for most models (e.g., Wagener et al. 2001a,b).

This study describes a parameter sensitivity analysis to evaluate identifiability of 98 parameter subsets for a bio-geo-chemical model of hypoxia for the northern GOM. We evaluate a simple zero-dimensional (0-D) unit of a larger spatial-temporal model to explore relationships 100 between multiple parameter sets and hypoxia dynamics on the LCS. Specifically, we provide 101 empirical results to support the assumption that models are generally over-parameterized and only 102 a finite and smaller subset of the larger parameter set can be optimized for a given research 103 question or dataset. We provide explicit guidance for choosing such subsets of the parameter space given constraints on identifiability as directly related to sensitivity analyses. The objectives 105 are to 1) identify the parameters that have the greatest influence on dissolved oxygen  $(O_2)$  using 106 local sensitivity analysis, 2) quantify the identifiability of subsets of the total parameter space 107 based on sensitivity, 3) and provide a set of heuristics for choosing parameters based on 108 sensitivity, identifiability, and parameter categories. These principles were also applied to other state variables predicted by the model (ammonium, chlorophyll a (chl-a), irradiance, nitrate, acro:pom 110 particulate organic matter (POM), dissolved organic matter (DOM), and phosphorus). A final 111 analysis evaluated identifiability relative to structural uncertainty to provide an example of 112 extending these methods to more complex uncertainty assessments. Throughout, the optimum 113 parameter set is defined as the chosen subset that represents the maximum number of identifiable parameters. 'Optimum' is both a qualitative description based on a research question or 115 management goal and a quantitative objective based on numerical optimization criteria for fitting 116 model output to a calibration dataset. These results can be used to refine existing models or guide 117 application of models to novel contexts, such as downscaling or application to new environments. 118 We conclude with a discussion of the implications for hypoxia formation in coastal regions, including management strategies for nutrient reduction and use of mechanistic models to inform decision-making.

### 2 Methods

#### 2.1 Model description

Hypoxic events, defined as <2 mg L<sup>-1</sup> of O<sub>2</sub> (< 64 mmol m<sup>-3</sup>), occur seasonally in bottom waters in the northern GOM. The LCS receives high nutrient loads from the MARB that drains a significant portion of the continental United States. Nutrient-stimulated primary production in surface waters increases biological oxygen demand in bottom waters as sinking organic matter is decomposed (Bierman et al. 1994, Murrell et al. 2013). The hypoxic area averages 15,540 km<sup>2</sup> annually (1993-2015) with minimum concentrations observed from late spring to early fall. Seasonal variation is strongly related to carbon and nutrient export from the MARB (Lohrenz et al. 2008, Bianchi et al. 2010), whereas hydrologic variation, currents, and wind patterns can affect vertical salinity gradients that contribute to the formation of hypoxia (Wiseman et al. 1997, Paerl et al. 1998, Obenour et al. 2015).

This study evaluated the core unit of a recently developed hydrodynamic and ecological model that describes horizontal and vertical transport and mixing of state variables relevant for hypoxia in the northern GOM. The Coastal General Ecosystem Model (CGEM) includes elements from the Navy Coastal Ocean Model (Martin 2000) for hydrodynamics on the LCS and a biogeochemical model with multiple plankton groups, water-column metabolism, and sediment diagenesis (Eldridge and Roelke 2010). The hydrodynamic component of CGEM provides a spatially-explicit description of hypoxia using an orthogonal grid with an approximate horizontal resolution of 1.9 km² and twenty equally-spaced vertical sigma layers on the shelf (depth ≤ 100 m, with additional hybrid layers at deeper depths). The biogeochemical component includes equations for 36 state variables including six phytoplankton groups (with nitrogen and phosophorus quotas for each), two zooplankton groups, nitrate, ammonium, phosphate, dissolved inorganic carbon, oxygen, silica, and multiple variables for dissolved and particulate organic matter from different sources. Atmospheric and hydrological boundary conditions described in Hodur (1997) and Lehrter et al. (2013) are also included in CGEM.

The core unit of CGEM is FishTank, a 0-D model that implements the biogeochemical equations in Eldridge and Roelke (2010) and does not include any form of physical transport (i.e., advection, mixing, or surface flux) nor sediment diagenesis. Although FishTank was developed

for specific application in CGEM, it can easily be applied to other hydrodynamic grids.

Accordingly, the sensitivity and identifiability analyses described below are informative for both
the LCS gridded model as well as potential applications to different systems. The FishTank model
provides estimates for the 36 state variables described above using a 0-D parcel that is uniformly
mixed as a closed system. A set of initial conditions is provided on execution of the model that is
based on observations of relevant variables obtained from research cruises in the northern GOM
during April, June, and September of 2006 (Table 1 in Murrell et al. 2014).

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Results from FishTank are based on time-dependent differential equations that describe energy flow between phytoplankton and zooplankton groups as affected by nutrient uptake rates, organic matter inputs and losses, inherent optical properties, and temperature (Penta et al. 2008, Eldridge and Roelke 2010, see appendix in Lehrter et al. in press). A total of 108 equations are estimated at each time step to return a value for each of the 36 state variables described by the model. In addition to the initial conditions, 251 parameter values for each of the equations are also supplied at model execution. These parameters define relationships among fixed effects in the equations and represent ecological properties described by the model that influence hypoxia formation. Values for each of the parameters were based on estimates from the literature, field or laboratory-based measurements, or expert knowledge in absence of the former. As such, a sensitivity analysis of parameter values is warranted given that, for example, literature or field-based estimates may not apply under all scenarios or expert knowledge is not completely certain (Refsgaard et al. 2007).

The sensitivity of O<sub>2</sub> to perturbations of all relevant parameters for the 108 equations was 171 estimated using a five minute timestep of FishTank simulations from January 1st to December 172 31st, 2006. Irrelevant parameters were removed for several reasons; parameters were not relevant 173 for the 0-D model (i.e., hydrodynamic parameters), were considered physical constants, or had no 174 effect given initial conditions. Additionally, FishTank includes six phytoplankton and two zooplankton groups to describe complexity in community structure and foodweb dynamics. However, structural equations for each group are identical such that chosen parameter values 177 primarily control differences between the groups, e.g., large-bodied or small-bodied plankton, 178 slow-growing or fast-growing plankton, etc. Initial analyses indicated that parameter sensitivity of dissolved oxygen was identical within the six phytoplankton and zooplankton groups. To remove

obvious redundancies in the model, the sensitivity analyses were conducted using only one phytoplankton and one zooplankton group. The final parameter set that was evaluated included 51 parameters that were further grouped into one of six categories based on applicable biogeochemical components of the model: optics (n = 4 parameters), organic matter (12), phytoplankton (22), temperature (2), and zooplankton (11). A full description of the model parameters is available as an appendix in Lehrter et al. in press.

#### 2.2 Local sensitivity analysis

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The analysis focused on sensitivity of  $O_2$  and other state variables (noted below) in the 188 0-D FishTank model to identify parameters that may affect spatial and temporal variation of hypoxia in the larger model. A local sensitivity analysis was performed by evaluating the change 190 in O<sub>2</sub> following perturbation of each parameter from its original value. The analyses relied 191 exclusively on concepts used in the FME package developed for the R statistical programming 192 language (Soetaert and Petzoldt 2010, RDCT (R Development Core Team) 2016). Parameters 193 were individually perturbed by 50% of the original values and the model was executed to obtain an estimate of  $O_2$  sensitivity. For each perturbation, a sensitivity value S was estimated for each 195 time step i given a change for parameter j as: 196

$$S_{ij} = \frac{\partial y_i}{\partial \Theta_i} \cdot \frac{w_{\Theta_j}}{w_{u_i}} \tag{1}$$

where the estimate depended on the change in the predicted value for response variable y divided by the change in the parameter  $\Theta_j$  multiplied by the quotient of scaling factors w for each. The scaling factors,  $w_{\Theta_j}$  for the parameter  $\Theta_j$  and  $w_{y_i}$  for response variable  $y_i$ , were set as the default value of the unperturbed parameter and the predicted value of  $y_i$  after perturbation (Soetaert and Petzoldt 2010). The scaling ensures the estimates are unitless such that the relative magnitudes allow comparisons of model sensitivity to parameters and state variables that differ in scale. Sensitivity values for all j parameters were summarized across the time series from i=1 to n as L1:

$$L1 = \sum |S_{ij}|/n \tag{2}$$

The L1 value for each parameter was used as the primary measure of sensitivity for the

state variables. All parameters for each of the six equation categories (optics, organic matter, phytoplankton, temperature, and zooplankton) that had non-zero L1 (suggesting sensitivity) were retained for identifiability analysis.

#### 2.3 Identifiability and selecting parameter subsets

Identifiability of parameter subsets was estimated from the minimum eigenvector of the cross-product of a selected sensitivity matrix (Brun et al. 2001, Omlin et al. 2001a):

$$\gamma = \frac{1}{\sqrt{\min\left(\text{EV}[\hat{S}^{\top}\hat{S}]\right)}}$$
 games (3)

where  $\gamma$  ranges from one to infinity for perfectly identifiable (orthogonal) or unidentifiable (perfectly collinear) results for parameters in a sensitivity matrix S. The sensitivity functions were supplied as a matrix  $\hat{S}$  with rows i and columns j (eq. (1)) that described deviations of predicted  $O_2$  from the default parameter values. Thus,  $\gamma$  can be estimated for any subset of parameter combinations using the change in model output for perturbations of individual parameters. Sensitivity matrices were first normalized by dividing by the square root of the summed residuals (Omlin et al. 2001a, Soetaert and Petzoldt 2010).

The collinearity index  $\gamma$  provides a measure of the linear dependence between sensitivity functions (i.e.,  $S_i$  for j parameters) described above for subsets of parameters. Estimates of  $\gamma$  greater than 10-15 suggest parameter sets are poorly identifiable (Brun et al. 2001, Omlin et al. 2001a), meaning parameter values that maximize precision on a calibration dataset are inestimable by conventional optimization algorithms given similar effects of the selected parameters on the estimated state variable. Greater sensitivity of a state variable to a subset of parameters does not always imply better identifiability if the effects of individual parameters are similar. An intuitive interpretation of  $\gamma$  is provided by Brun et al. (2001) such that a change in a state variable caused by a change in one parameter can be offset by the fraction  $1-1/\gamma$  by the remaining parameters. That is,  $\gamma=10$  suggests the relative change in  $O_2$  for an arbitrary parameter in the selected set can be compensated for by 90% with changes in the other parameters.

Initial analyses suggested that considerably limited subsets of parameters were identifiable of the 51 evaluated for the FishTank model. Given this limitation, parameter selection must

consider the competing objectives of increased precision with parameter inclusion and reduced identifability as it relates to optimization. An additional challenge is the excessively high number of combinations of parameter sets, which complicates selection given sensitivity differences and desired ecological categories of each parameter (e.g., practitioners may only be interested in optics parameters). For example, Fig. 1 provides a simple graphic of the unique number of combinations that are possible for different subsets of 'complete' parameter sets of different sizes (i.e., based on n choose k combinations equal to n!/(k!(n-k)!)). The number of unique combinations increases with the total parameters in the set and is also maximized for moderate selections (e.g., selecting half the total). For example, over 10<sup>14</sup> combinations are possible by selecting 25 parameters from a set of 50. Accordingly, parameter selection is complicated by differing sensitivity, identifiability limits for parameter subsets, and the difficulty of choosing from many combinations. 

A set of heuristics was developed that address the tradeoff in model complexity and identifiability given the challenges described above (see also Wagener et al. 2001a). These rulesets were developed with the assumption that parameters will be selected with preference for those with high sensitivity and identifability based on  $\gamma < 15$  as an acceptable threshold for subsets (e.g., 93% accountability). Selection heurestics also recognized that parameter categories (i.e., optics, organic matter, phytoplankton, temperature, zooplankton) may have unequal preferences by model users given questions of interest. In all selection scenarios, parameters were selected by decreasing sensitivity starting with the most sensitive until identifiability did not exceed  $\gamma = 15$  where selections were 1) blocked within parameter category, 2) independent of parameter category, 3) or considering all categories equally. The selection rules produced seven subsets of parameters that could further be used to optimize model calibration.

# 2.4 Observational and structural uncertainty

In addition to parameter uncertainty, the effects of observational and structural uncertainty on the sensitivity analyses were evaluated by changing the initial conditions and structural components, respectively, from the default model setup. First, observational uncertainty (i.e., effects of observed data on model output) was evaluated by varying the initial conditions that were based on observational data from research cruises in the northern GOM (Murrell et al. 2014). Uncertainty in these data translates directly to uncertainty that can influence results of the

sensitivity analysis. For example, the sensitivity of O<sub>2</sub> to variation in the half-saturation constants for phytoplankton (the concentration supporting half the maximum uptake rate of nutrients) will vary given the initial nutrient concentrations (Eppley et al. 1969). Further, changes in the ratio between nitrogen and phosphorus could affect sensitivity depending on the limiting nutrient.

Parameter sensitivity was re-evaluated by varying all initial conditions that were non-zero by different seasonal means based on averages of water quality data across stations and years. April and September seasonal averages of the observed data were used to evaluate the effects of conditions that were typical of spring and late summer on the LCS (Table 1).

The effects of model structure on parameter sensitivity (i.e., structural uncertainty) were evaluated by changing specific components of the model. The FishTank model includes several ecosystem processes or characteristics that can be included based on expected conditions, available data, or desired complexity. These 'switches' are conceptually different from model parameters as they allow the inclusion or exclusion of explicit equations or processes. Switches in FishTank include different structural equations for the vertical attenuation of light through the water column (inherent or apparent optical properties, Penta et al. 2009, Eldridge and Roelke 2010) and chlorophyll to carbon ratio models (fixed or dynamic given light and nutrients, Cloern et al. 1995). Several switches also affect phytoplankton growth including different models for specific growth and effects of temperature, light dependence, nutrient uptake, and internal cell quotas (Lehrter et al. in press, references therein).

Parameter sensitivity was evaluated by comparing the results from the default model setup to a more complex setup with alternative switches (Table 2). The scenarios used switches for different equations to represent structural relationships of phytoplankton growth patterns with temperature, nutrient uptake, cell quotas, chl-*a* to carbon ratios, photosynthesis dynamics, and specific growth limits. The default scenario modelled phytoplankton growth with temperature as a sigmoidal function (Eldridge and Roelke 2010), nutrient uptake as Michaelis-Menten kinetics (Dugdale and Goering 1967), internal cell quotas following Droop (1973), chl-*a* to carbon ratios as a simple regression (Murrell et al. 2014), light-dependence of photosynthesis with photoinhibition (Platt et al. 1980), and a specific growth rate following Leibig's law of the minimum. Conversely, the complex scenario used switches that modelled relationships between phytoplankton growth with temperature using the Arrhenius model (Geider et al. 1997), nutrient

uptake as proposed by Lehman et al. (1975) and modified in Geider et al. (1998), internal cell quotas following Flynn (2003), chl-*a* to carbon ratios following Cloern et al. (1995), light-dependence of photosynthesis that is nutrient dependent (Flynn 2003), and a specific growth rate that is nutrient dependent. Complete details of model switches are provided as supplementary material to Lehrter et al. in press.

#### 2.5 Extension to other state variables

The above analyses were repeated for additional state variables estimated by FishTank to provide further descriptions of ecological dynamics that are relevant for hypoxia. In addition to O<sub>2</sub>, other state variables that were evaluated were ammonium, chl-*a*, irradiance, nitrate, POM, DOM, and phosphorus. Particulate and dissolved organic matter were estimated as the summation of the respective outputs for organic matter from phytoplankon (*OM1* A, *OM2* A) and fecal pellets from zooplankton (*OM1* Z, *OM2* Z, see Lehrter et al. in press).

## 305 3 Results

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#### 3.1 Local sensitivity analysis

Local sensitivity analyses showed that O<sub>2</sub> was sensitive to perturbations in 38 of the 51 307 (75% of total) parameters that were evaluated in FishTank (default panel Fig. 2, Table 3). Within 308 each parameter category, O<sub>2</sub> was sensitive to three parameters for optics (75% of all optic 309 parameters), eight for organic matter (67%), 16 for phytoplankton (73%), one for temperature 310 (50%), and 10 for zooplankton (91%). Although  $O_2$  had the greatest sensitivity to parameters in 311 the zooplankton category (as percentage of total), the relative effects varied. Among all parameters, sensitivity values ranged from  $L1 = 8.34 \times 10^{-8}$  for QminP (phytoplankton) to 0.05313 for umax (phytoplankton), whereas average sensitivity among all parameters was L1 =314  $9.2 \times 10^{-3}$ . Within categories (excluding temperature with one sensitive parameter), sensitivity 315 ranged from  $4.39 \times 10^{-5}$  (astarOMA) to  $7.51 \times 10^{-4}$  (astar490) for optics,  $4.17 \times 10^{-4}$  (KNH4) 316 to  $6.15 \times 10^{-3}$  (KG1) for organic matter,  $8.34 \times 10^{-8}$  (QminP) to 0.05 (umax) for phytoplankton, and  $3.69 \times 10^{-5}$  (ZQp) to 0.05 (ZKa) for zooplankton (Table 3). Average sensitivity values in 318 each category were  $L1 = 2.81 \times 10^{-4}$  for optics,  $2.17 \times 10^{-3}$  for organic matter, 0.02 for 319 temperature, 0.01 for phytoplankton, and 0.01 for zooplankton. 320

Local sensitivity analyses for the additional state variables (ammonium, chl-a, irradiance,

nitrate, POM, DOM, and phosphorus) had similar results as O2 with some exceptions (Fig. 2 and Tables S1 to S7). All variables were sensitive to the same parameters as  $O_2$  (38 of 51 323 evaluated), although average sensitivity differed between variables. Average L1 ranged from 0.02 324 for irradiance (Table S3) to 0.71 for DOM (Table S6). All average sensitivity values for the state 325 variables were higher than the average for  $O_2$  ( $L1 = 9.2 \times 10^{-3}$ ). For each variable, L1 ranged from  $2.24 \times 10^{-6}$  (*QminP*) to 8.49 (*mA*) for ammonium (Table S1),  $1.38 \times 10^{-6}$  (*QminP*) to 13.94(mA) for chl-a (Table S2),  $1.92 \times 10^{-7}$  (QminP) to 0.13 (ZKa) for irradiance (Table S3), 328  $6.67 \times 10^{-7}$  (*QminP*) to 8.49 (*umax*) for nitrate (Table S4),  $6.41 \times 10^{-5}$  (*KNH4*) to 7.22 (*mA*) for POM (Table S5),  $7.41 \times 10^{-5}$  (KNH4) to 14.25 (mA) for DOM (Table S6), and  $8.21 \times 10^{-7}$ (QminP) to 1.47 (ZKa) for phosphate (Table S7). For the parameter categories, ammonium was most sensitive to phytoplankton parameters (average L1 = 0.8 across all parameters in the category), chl-a to phytoplankton (L1 = 1.14), irradiance to zooplankton (L1 = 0.03), nitrate to 333 zooplankton (L1 = 1.06), POM to temperature (L1 = 0.86), DOM to temperature (L1 = 1.48), and 334 phosphate to zooplankton (L1 = 0.31). Finally, average sensitivity between parameter categories 335 independent of the state variables ranged from  $8.38 \times 10^{-3}$  for optics (average L1 across all variables) to 0.62 for phytoplankton. 337

# 3.2 Subset identifiability

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The identifiability analyses suggested that many parameter subsets exceeded the 339 thresholds of  $\gamma = 10, 15$ , providing further justification for using selection heuristics for parameter optimization. Results for O<sub>2</sub> are provided first to demonstrate general concepts for the 341 identifiability analyses, followed by an extension to the remaining state variables. Parameter 342 identifiability for  $O_2$  decreased (increasing  $\gamma$ ) at different rates with increasing size of parameter 343 subsets depending on the parameter category or the number of top parameters that were selected (Fig. 3). By category, identifiability was lowest for all combinations of parameter subsets in the phytoplankton (60% of subsets less than  $\gamma = 15$ , 43% less than  $\gamma = 10$ ) and zooplankton 346 categories (53.1% less than  $\gamma = 15$ , 40% less than  $\gamma = 10$ ), whereas all combinations were 347 identifiable for optics (100% less than  $\gamma = 15, 10$ ) and a majority identifiable for organic matter  $(91.9\% \text{ less than } \gamma = 15, 76.5\% \text{ less than } \gamma = 10)$ . Identifiability for parameters in the temperature category was not evaluated because O2 was sensitive to only one parameter (i.e., 350  $\gamma = 1$ ). Parameter combinations for choosing from the top, top two, top three, and top four 35

parameters in each category together had decreasing identifability with the increasing size of the selection pool (e.g., top one versus top four parameters, Fig. 3). The percentage of parameter subsets that were below the acceptable thresholds for identifiability was 100% less than  $\gamma = 15, 10$ for the top parameter in each category, 90.6% and 80.7% for the top two, 80.7% and 70.9% for the top three, and 55.8% and 45.7% for the top four. Results for the remaining state variables had similar patterns in identifiability with increasing size of parameter subsets and selection categories, although differences in identifiability between state variables was observed (Fig. 4). Most notably, nitrate was consistently the least identifiable variable (highest overall  $\gamma$ ), whereas  $O_2$  was most identifiable. 

An alternative view of the results in Fig. 3 can be used to demonstrate the effects of parameter selection criteria and number of parameters in the selection pool on identifiability. Fig. 5 shows the percentage of identifiable parameter sets for  $O_2$  using the same selection criteria in Fig. 3, i.e., selection of parameters only within parameter categories and selection of the top sensitive parameters regardless of category. Fig. 5 is similar to Fig. 3, with the added effect of a chosen  $\gamma$  threshold on identifability. Previous studies have provided only general rules for  $\gamma$  thresholds (Brun et al. 2001, Omlin et al. 2001a), such that exact values for which parameter sets are inestimable likely vary between models and optimization methods. As such, multiple values are shown in Fig. 5 given that actual thresholds could vary in practice. In general, identifiability decreased with the addition of parameters, although the rate of decrease depended on the selected threshold for  $\gamma$ . More conservative values for  $\gamma$  (e.g.,  $\gamma = 5$ ) were more sensitive to the number of parameters in a subset, that is, identifiability decreased more quickly with the addition of parameters at lower  $\gamma$  thresholds as compared to higher  $\gamma$ . Notable differences in identifiability were also observed by parameter selection criteria (within categories or top parameters only), which further supports results in Figs. 3 and 4.

An evaluation of the effects of individual parameters on  $\gamma$  suggested that some parameters had disproportionate effects on identifiability. Based on  $\gamma=15$ , Fig. 3 suggests that most parameter sets for organic matter were identifiable, regardless of how many parameters were selected (i.e., two through eight). However, some subsets were not identifiable such that identification of one or more redundant parameters that are inflating  $\gamma$  values could provide useful information. Fig. 6 shows an alternative view of identifiability of  $O_2$  with exclusion and inclusion

of individual parameters in different sets for the organic matter category. As before, collinearity increases with more parameters in a subset, although the increase varies depending on which parameter was included or excluded from the set. For example, inclusion of KNO3 in a parameter set almost always inflated  $\gamma$ . All parameter subsets that did not include KNO3 were well below  $\gamma = 15$ , suggesting that removal of this parameter improves identifiability. Interestingly, the inclusion of some parameters caused a reduction in  $\gamma$ , which contradicts the general rule that more parameters caused reduced identifiability. For example, parameter sets that included KGcdom generally had lower  $\gamma$  values relative to those that excluded the parameter.

#### 3.3 Parameter selection

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The above results demonstrated that state variables differed in the magnitudes of 391 sensitivity for each parameter and the number of identifiable subsets, where the latter varied by  $\gamma$ thresholds and parameter selection criteria. Results for each of the three selection heuristics (blocked by parameter category, independent of category, all categories equally) applied to each state variable differed in the number of selected parameters and distribution of parameters within each category (Tables 4 to 6). In general, a corresponendence was observed between the number 396 of parameters that were selected given the threhold of  $\gamma = 15$  and relative identifiability between the state variables. As noted above, nitrate was the least identifiable variable (Fig. 4), whereas 398 other variables (e.g., O<sub>2</sub>, irradiance) were more identifiable. The constraints on identifiability between variables were demonstrated with the selection heuristics. For example, heuristics for nitrate typically selected only one or two parameters that met the criteria as compared to more identifiable variables that included several parameters. Overall, the first selection heuristic 402 demonstrated that the number of parameters chosen by parameter category differed independently 403 of the state variables (Table 4). The number of selected parameters averaged across state variables 404 in decreasing order was 4.25 parameters from the phytoplankton category, 3.5 from organic 405 matter, 2.75 from optics, and 2.38 from zooplankton. The second and third selection heuristics 406 (Tables 5 and 6) were similar, although more parameters were generally selected for the third heuristic given equal importance between categories.

Fig. 7 demonstrates parameter selection for all state variables following the second heuristic where parameters were chosen by decreasing sensitivity independent of parameter categories (exact values are shown in Table 5). The y-axis shows the relative identifiability with

the addition of parameters from one to many on the x-axis (from left to right). The second to last parameter for each variable is the last parameter selected within the potential threshold of  $\gamma = 15$ . 413 Interestingly, the last parameter shown for most of the state variables caused a relatively large 414 increase in  $\gamma$  that was disproportionate to the combined identifiability of the preceding parameter 415 set. For most variables, the phytoplankton edibility vector for zooplankton (ediblevector(Z1)) caused a dramatic increase in  $\gamma$  with inclusion in the parameter set. In addition to demonstrating the approach for selection with the second heuristic, Fig. 7 provides an alternative method of 418 identifying parameters that are disproportionately redundant within a given parameter set (i.e., 419 large contribution to  $\gamma$ ). This infomation is useful if additional parameter selection rules are 420 developed independently of those proposed herein. 421

### 3.4 Observational and structural uncertainty

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Both the relative L1 estimates and number of parameters that affected state variables were 423 sensitive to variation in the initial conditions (observation effects) and structural changes in the 424 model. Visual comparison of sensitivity values (L1) for the default model setup showed that all 425 state variables were sensitive to *vmaxSi* after changing the initial conditions to April or September 426 conditions (Fig. 2). State variables were also sensitive to Ksi for only the September conditions. 427 Changing the model structure from the default (simple) to the complex setup showed state 428 variables were also sensitive to KQn and  $Tref(nospA+nospZ)_{z1}$ . Changes in the sensitivity of 429 individual parameters were also observed, most notably as a disproportionate increase in L1 for 430 ammonium, chl-a, POM, and DOM to mA and  $Tref(nospA + nospZ)_{p1}$  using the complex model 431 setup. Summaries by parameter categories of the effects of initial conditions and structural 432 changes are shown in Table 7 and Fig. 8. Changes in average sensitivity using April and 433 September initial conditions showed most variables were less sensitive to parameters in the 434 optics, temperature, and zooplankton categories, whereas increased sensitivity was generally 435 observed for parameters in the organic matter and phytoplankton categories. Some exceptions 436 were observed, such as a decrease in nitrogen sensitivity to phytoplankton parameters (Table 7). 437 Effects of structural complexity were most apparent as an increase in sensitivity of state variables 438 to phytoplankton and temperature parameters, as noted for the individual variables in Fig. 2.

### 4 Discussion

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#### 4.1 Implications of sensitivity and identifiability analyses

Common goals in the application of biogeochemical models of ecosystem processes are to 1) accurately describe the system by matching predictions with observed data (Reckhow et al. 443 1990), and 2) provide a means of forecasting ecosystem condition with hypothesized 444 management or environmental scenarios (Clark et al. 2001). Although these objectives are the 445 focus of most applications, the structural components of process-based models should secondarily 446 provide inference into which ecosystem processes and functions are driving observed changes. This latter objective represents a more generic scientific purpose of biogeochemical models that 448 extends beyond the applied benefits of describing and predicting change in a particular system. 449 Modelers often hope to identify universal principles that govern dynamics across systems and the 450 constraint of model parameters to observations provides a means of supporting or refuting 451 hypotheses (Kirchner 2006). Extension of these principles to test the effects of structural changes 452 and observation uncertainty on model predictions provides further information to support 453 validation of model components. This study provided a simple approach to use the effects of 454 parameter perturbations on model state variables to characterize identifiable parameter subsets 455 that vary by parameter selection criteria. By doing so, we demonstrated that small parameter 456 subsets relative to all sensitive parameters were within the identifiabilty thresholds described in 457 the literature. The identifiable parameter subsets varied considerably between state variables and 458 the method for parameter selection. We further demonstrated that changes in the model structure 459 and variation in the initial conditions had an effect on sensitivity which has direct implications for 460 identifiability. In general, these results provide justification for the use of explicit parameter selection heuristics that practitioners should adopt to facilitate model calibration. 462

Although the results were specific to individual variables, some generalities about hypoxia dynamics can be inferred from the sensitivity analyses. State variables were most sensitive to parameters in the phytoplankton and zooplankton categories, particularly the maximum growth rates (*umax* for phytoplankton, *Zumax* for zooplankton), mortality coefficient for phytoplankton (*mA*), and the zooplankton half saturation coefficient for grazing (*ZKa*). An increase in the growth rate of primary producers has the potential to increase oxygen concentration through

photosynthetic processes, although increased production of organic matter is balanced with respiration and bacterial decomposition that reduce O2 in the water column. Similarly, increases in zooplankton abundance with increased growth rates causes a reduction in phytoplankton biomass through grazing, which is expected to further deplete pools of organic matter. Most variables were also sensitive to variation in the half-saturation grazing coefficient which moderates the concentration of nutrients that support half the maximum grazing rate. Although the tradeoff between abundance, grazing, and decomposition is complex, the sensitivity of model state variables to parameters that directly control the abundance of primary producers is in agreement with empirical observations of factors that influence hypoxia dynamics on the LCS (Fahnenstiel et al. 1995, Roelke 2000, Eldridge and Roelke 2010). The sensitivity of the model output to variation in other parameters that relate to physical and chemical properties of the system was of secondary importance to biological relationships. That is, state variables were sensitive to changes in light and temperature parameters, although to a lesser extent than phytoplankton and zooplankton parameters. As such, the differing sensitivities of state variables to parameters in each of the categories was not unexpected given general ecological relationships that are well understood and described by the model. 

The overwhelming conclusion from the identifiability analyses is that only limited subsets of parameters were identifiable within the constraints of local sensitivity analyses. Although we have not attempted actual model calibration (see recommendations below), these results support previous studies that have suggested similarly small subsets of parameters can be identified using traditional calibration schemes (e.g., Wheater et al. 1986, Ye et al. 1997, Omlin et al. 2001a). In addition to CGEM, these conclusions have relevance for many biogeochemical models that include numerous parameters and structural equations to characterize processes in the model domain. A general conclusion is that perhaps a trend towards less complex models could be beneficial given that only a small subset of parameters is identifiable and that ecosystem processes may in fact be sufficiently characterized with few parameters (Ye et al. 1997). Conversely, others have argued that model complexity is not in itself a disadvantage when parsimony is not the sole arbitrator of model structure (Reichert and Omlin 1997). Over-parameterization can be useful if processes have importance that were not evaluated during model identification. Single objective functions that maximize model precision with identifiable parameters may also provide an

incomplete characterization of model worth, which has prompted the development of probability-based models of hypoxia that explicitly include uncertainty in model components 500 (e.g. Obenour et al. 2015). Our results demonstrated that approximately 75% of the evaluated 501 parameters had an effect on the eight state variables, whereas CGEM includes a total of 36 502 variables and multiple plankton groups, not all of which have immediate concern for 503 understanding hypoxia. The redundancies identified with the sensitivity analyses are only 504 problematic if the primary interest is, for example, O<sub>2</sub> dynamics. Moreover, the proposed 505 selection heuristics provide flexibility for choosing different parameters with the assumption that 506 those chosen depend on the research or management question. 507

Results from the identifiability analyses provided additional insight into the interactions of 508 parameters in large biogeochemical models. First, identifiability of parameter subsets was not 509 related to the sensitivity of individual variables. As noted above, an identifiable parameter is one 510 that has a unique effect on model predictions that cannot be compensated for or undone by 511 changing other parameters. The magnitude of the effect of a parameter has no bearing on 512 identifiability, which further complicates the selection of parameters for calibration. Although identifiability is the primary limiting factor in choosing a set, the relative sensitivities are more important for the decision to include or exclude individual parameters. Our analysis addressed 515 this challenge by presenting multiple selection criteria for identifiable parameter sets that 516 prioritized the most sensitive parameters during the selection process. Similarly, identifability was 517 not always related to the number of parameters in a set. Although the overwhelming trend was decreasing identifiability with more parameters, the unique effects of including an individual 519 parameter with an existing set often reduced the  $\gamma$  estimate. For example, Fig. 6 shows that 520 including KGcdom, KO2, or nitmax in parameter sets more often reduced  $\gamma$  relative to sets that 521 excluded the parameters. Conversely, Fig. 7 showed that the inclusion of a specific parameters 522 often caused a disproportionate increase in  $\gamma$  (e.g., ediblevector(Z1)). These examples demonstrate the complex interactions of parameter changes on variable response, highlighting the need to consider the combined and individual effects of parameters on identifiability. The 525 selection criteria proposed in our above analyses can facilitate parameter selection and also provide diagnostic tools to identify parameters with disproportionate effects on  $\gamma$ .

#### 4.2 Recommendations and conclusions

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An evaluation of parameter uncertainty and identifiability of relevant parameter sets is a 529 preliminary and simplistic approach to improving model predictions. In general, uncertainty 530 analyses that lead to improved models are ultimately expected to increase our understanding of 531 properties defining ecological relationships. The extension of simple parameter sensitivity 532 analyses to the generalization of ecosystem properties requires additional analysis and potential 533 model refinement, at the core of which is the balance between generality and precision. We 534 emphasize that the utility of a specific model depends on the question and objective for 535 application to a specific system. For the above analysis, the FishTank model, as part of the larger CGEM application, was evaluated in the context of hypoxia effects on ecosystem condition and function. At the core of the simple model is a set of biogeochemical equations that characterize 538 the system in relation to planktonic groups, nutrient requirements, and water-column metabolism. 539 Our results have shown that relatively small subsets of parameters are identifiable given the complexity of the model, and as a result, we have provided a general approach to select parameter subsets depending on the ecological context (i.e., selection by parameter category, selection for specific state variables). Thus, the results described above have relevance for further model 543 refinement with the specific goal of better understanding ecological dynamics that moderate 544 hypoxia on the northern GOM. However, the general principles of sensitivity and parameter 545 identifiability have broad applicability beyond this context and we argue that such methods should be more universally applied as an initial approach to quantify numerical constraints of biogeochemical models. 548

Specific approaches can be used to improve and build on the results presented herein, in addition to the more general considerations noted above. An evaluation of model precision following calibration with relevant parameter subsets could provide additional information that supports results from the sensitivity analyses. For simplicity, our analysis did not calibrate model parameters and an explicit assumption was that parameter subsets with  $\gamma$  below 10 or 15 were identifiable. To our knowledge, this threshold has not been rigorously evaluated and it is likely to vary between parameter subsets and the chosen calibration method. Variation in parameter estimates given the calibration method and different identifiability thresholds could affect the interpration of model output. Further, the extent to which results for the 0-D model extrapolate to

the larger three-dimensional model should be evaluated. Although the above analyses were facilitated using the 0-D model (i.e, quick execution times, ease of changing model parameters), 559 lack of physical transport or spatial components potentially limits extrapolation of the results. 560 Uncertainy in parameter estimates at lower dimensions could be magnified as errors propagate to 561 larger scales or site-specific observations for model calibration are not appropriate across a 562 hydrodynamic grid (Harvey 2000, Lehrter and Cebrian 2010). The effects of structural or 563 observational uncertainty should also be evaluated in the context of the larger model. Our simple 564 approach to examine changes in the initial conditions and switches used in the model showed that 565 sensitivity estimates of individual parameters differed relative to the original model configuration, 566 having further implications for characterizing identifiability.

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Table 1: Initial conditions that were varied to evaluate effects of observational uncertainty on parameter sensitivity. April and September values are based on seasonal averages from water quality samples of the LCS. All units are  $\mu$ mol  $L^{-1}$ .

Variables	Default	April	September
Dissolved Inorganic Carbon	$2.13 \times 10^{3}$	$2.1 \times 10^{3}$	$2.13 \times 10^{3}$
Ammonium	1.09	1.79	0.35
Nitrate	71.4	3.75	2.04
Dissolved Oygen	172	194.47	152.57
Phosphate	1.81	0.23	0.42
Silica	71.4	5.84	9.77

Table 2: Model switches that were used to evaluate effects of structural uncertainty on parameter sensitivity. Complete details and equations are provided as supplementary material to Lehrter et al. in press.

Switch type	Default	Complex
Temperature	sigmoidal (Eldridge and Roelke 2010)	Arrenhius (Geider et al. 1997)
Uptake	Michaelis-Menten (Dugdale and Goering 1967)	Geider (Lehman et al. 1975, Geider et al. 1998)
Quota	Droop (Droop 1973)	Flynn (Flynn 2003)
Chla:C	regression (Murrell et al. 2014)	Cloern (Cloern et al. 1995)
Photosynthesis	photoinhibition (Platt et al. 1980)	nutrient dependent
Specific growth rate	Leibig's minimum	nutrient dependent

Table 3: Sensitivity of  $O_2$  to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where L1 summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect  $O_2$  are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
Optics		
Chla specific absorption at 490 nm	astar490	$7.51\times10^{-4}$
OMZ specific absorption at 490 nm	astarOMZ	$4.92\times10^{-5}$
OMA specific absorption at 490 nm	astarOMA	$4.39\times10^{-5}$
Temperature		
Optimum temperature for growth(C)	$Tref(nospA + nospZ)_{p1}$	0.02
Phytoplankton		
maximum growth rate	umax	0.05
mortality coefficient	mA	0.02
initial slope of the photosynthesis-irradiance relationship	alpha	0.02
edibility vector for Z1	ediblevector(Z1)	0.02
phytoplankton carbon/cell	Qc	0.01
phytoplankton growth respiration coefficient	respg	$8.36  imes 10^{-3}$
N-uptake rate measured at umax	vmaxN	$8.12 \times 10^{-3}$
phytoplankton basal respiration coefficient	respb	$6.94 \times 10^{-3}$
Phytoplankton threshold for grazing, is multiplied by VOLcell	Athresh	$4.57 \times 10^{-3}$
minimum N cell-quota	<i>QminN</i>	$4.32 \times 10^{-3}$
P-uptake rate measured at umax	vmaxP	$4.27 \times 10^{-3}$
coefficient for non-limiting nutrient	aN	$4.23\times10^{-3}$
phytoplankton volume/cell	volcell	$4.13\times10^{-3}$
half-saturation constant for P	Kp	$2.9\times10^{-3}$
half-saturation constant for N	Kn	$2.77\times10^{-4}$
minimum P cell-quota	QminP	$8.34 \times 10^{-8}$
Zooplankton		
half saturation coefficient for grazing	ZKa	0.05
zooplankton nitrogen/individual	ZQn	0.02
Zooplankton mortality constant for quadratic mortality	Zm	0.02
maximum growth rate of zooplankton	Zumax	0.02
assimilation efficiency as a fraction of ingestion	Zeffic	0.01
proportion of grazed phytoplankton lost to sloppy feeding	Zslop	$7.78 \times 10^{-3}$
Zooplankton growth-dependent respiration factor	Zrespg	$5.32\times10^{-3}$
Zooplankton biomass-dependent respiration factor	Zrespb	$2.96\times10^{-3}$
zooplankton carbon/individual	ZQc	$9.38 \times 10^{-5}$
zooplankton phosphorus/individual	$\widetilde{ZQp}$	$3.69 \times 10^{-5}$
Organic Matter	~1	
turnover rate for OM1A and OM1Z	KG1	$6.15\times10^{-3}$
turnover rate for OM2A and OM2Z	KG2	$3.14\times10^{-3}$
O2 concentration that inhibits denitrification	KstarO2	$3.04\times10^{-3}$
decay rate of CDOM, 1/day	KGcdom	$2.98 \times 10^{-3}$
half-saturation concentration for O2 utilization	KO2	$5.85 \times 10^{-4}$
half-saturation concentration for NO3 used in denitrification	KNO3	$5.8 \times 10^{-4}$
maximum rate of nitrification per day	nitmax	$4.99 \times 10^{-4}$
NH4 rate constant for nitrification	KNH4	$4.17 \times 10^{-4}$

<sup>\*</sup>Temperature parameters apply separately to phytoplankton (p1, one group) or zooplankton (z1, one group), denoted by subscripts

Table 4: Parameter identifiability (as  $\gamma$ , eq. (3)) by category for relevant state variables. Selections followed the first heuristic where parameters were selected within categories from most to least sensitive until  $\gamma > 15$ . Rank describes the relative parameter sensitivity in each category for each state variable. Duplicate parameters and ranks in the first two columns apply only to  $\gamma$  values in the same row (i.e., parameter ranks vary for each variable).

Parameter	Rank	Ammonium	Chl-a	$O_2$	Irradiance	Nitrate	POM	DOM	Phosphate
Optics									
astar490	1	1	1	1	1	1	1	1	1
astarOMA	2	7.33	5.42	-	7.87	5.36	-	-	7.78
astarOMZ	2	-	-	1.39	-	-	-	4.73	-
astarOMA	3	-	-	3.87	-	-	-	10.04	-
astarOMZ	3	7.58	5.51	-	7.87	6.02	-	-	7.91
Organic Matter									
KG1	1	_	_	1	_	_	-	1	1
KG2	1	_	_	_	1	_	_	_	_
KGcdom	1	_	1	_	-	1	_	_	_
KstarO2	1	_	-	_	_	-	1	_	_
nitmax	1	1		_	_	_	-	_	_
KG1	$\overset{1}{2}$	-	1.12	-	-	1.93	-	-	-
KG1 KG2	$\frac{2}{2}$	-	1.12	6	-	1.93	-	13.43	-
				-		-			
KGcdom	2	-	-		1.39	-	-	-	1.47
KNH4	2	4.03	-	-	-	-	-	-	-
KG1	3	4.09	-	-	-	-	-	-	-
KG2	3	-	-	-	-	8.19	-	-	-
KGcdom	3	-	-	-	-	-	-	13.75	-
KO2	3	-	-	-	11.96	-	-	-	14.07
KstarO2	3	-	-	6.04	-	-	-	-	-
KGcdom	4	4.19	-	6.12	-	-	-	-	-
KO2	4	-	-	-	-	-	-	14.68	-
KstarO2	4	-	-	-	-	10.65	-	-	14.08
KO2	5	9.47	-	8.61	-	-	-	-	-
Phytoplankton									
mA	1	1	1	-	1	_	-	_	1
umax	1	_	_	1	_	1	1	1	_
ediblevector(Z1)	$\overset{-}{2}$	1.13	1.17	_	_	_	_	_	1.15
mA	2	-	-	1.19	_	1.29	_	_	-
Qc	2	_	_	-	_	-	11.57	_	_
umax	2	_	_	_	1.21	_	-	_	_
vmaxP	$\frac{2}{2}$	_	_	-	-	_	_	7.45	-
	3	-	-	1.44	-	1.98	-	-	-
alpha			-	1.44		1.98			
ediblevector(Z1)	3	- 0.70	- 0.11		2.9		-	-	- 0.00
umax	3	2.73	2.11	-	-	-	-	-	3.26
alpha	4	3.55	4.57	-	-	-	-	-	-
ediblevector(Z1)	4	-	-	2.09	-	4.09	-	-	-
Qc	4	-	-	-	-	-	-	-	4.98
vmaxN	4	-	-	-	4.9	-	-	-	-
alpha	5	-	-	-	-	-	-	-	10.11
Qc	5	-	-	2.9	-	-	-	-	-
vmaxN	5	8.14	-	-	-	-	-	-	-
Athresh	6	11.27	-	-	-	-	-	-	-
respg	6	-	-	3.41	-	-	-	-	-
vmaxN	7	-	-	3.97	-	-	-	-	-
Zooplankton									
ZKa	1	_	-	1	_	1	1	1	_
Zumax	1	1	1	-	1	-	-	-	1
ZKa	2	-	4.31	_	5.43	_	_	_	7.3
ZQn	$\frac{2}{2}$	_	-	3.18	-	6.32	9.76	8.54	-
Zgn Zm	3	_	_	4.57	-	-	9.10 -	-	_
	3	-	-	4.57	=	6.93	-	-	-
Zumax		-	-		-			-	-
Zm	4	-	-	-	-	11.86	-	-	-
Zumax	4	-	-	5.2	-	-	-	-	-

Table 5: Parameter identifiability (as  $\gamma$ , eq. (3)) for relevant state variables. Selections followed the second heuristic where parameters were selected independent of category from most to least sensitive (L1, eq. (2)), until  $\gamma > 15$ . Rank describes the relative parameter sensitivity in each category for each state variable (O: optics, OM: organic matter, P: phytoplankton, T: temperature, Z: zooplankton). See Fig. 7 for a graphical illustration.

Selections by state variable	Parameter	L1	Rank	$\overline{\gamma}$
Ammonium				· · ·
1	mA	8.49	$1_{\rm P}$	1
2	nitmax	1.54	$1_{\text{OM}}$	1.16
3	Zumax	1.42	$1_{\rm Z}$	2.9
Chlorophyll				
1	mA	13.94	$1_{P}$	1
2	Zumax	1.02	$1_{\rm Z}$	1.18
Dissolved Oxygen				
1	umax	0.05	$1_{\mathbf{P}}$	1
2	ZKa	0.05	$1_{\mathbf{Z}}$	2.17
3	mA	0.02	$2_{\rm P}$	2.31
4	$Tref(nospA+nospZ)_{D1}$	0.02	$1_{\mathrm{T}}$	2.37
5	ZQn	0.02	$2_{\mathbb{Z}}$	4.69
6	alpha	0.02	$3_{\rm P}$	4.91
7	Zm	0.02	$3_{\mathbb{Z}}$	6.73
8	Zumax	0.02	$4_{\rm Z}$	6.81
DOM				
1	mA	14.25	$1_{\mathbf{P}}$	1
2	$Tref(nospA+nospZ)_{p1}$	1.48	$1_{\mathrm{T}}$	1.05
3	umax	1.11	$2_{\rm P}$	2.46
4	Zumax	1.01	$1_{\mathbb{Z}}$	2.91
Irradiance				
1	ZKa	0.13	$1_{\mathbb{Z}}$	1
2	umax	0.09	$1_{\mathrm{P}}$	4.41
3	ZQn	0.06	$2_{\rm Z}$	7.54
4	mA	0.05	$2_{\rm P}$	8.17
5	KGcdom	0.05	$1_{\text{OM}}$	9.44
6	alpha	0.04	$3_{\rm P}$	9.66
7	Zumax	0.04	$3_{\mathbb{Z}}$	10.79
Nitrate				
1	umax	8.49	$1_{\mathrm{P}}$	1
Phosphate				
1	ZKa	1.47	$1_{\mathbb{Z}}$	1
2	umax	0.78	$1_{\mathbf{P}}$	11.45
3	vmaxP	0.59	$2_{\rm P}$	11.48
4	ZQn	0.5	$2_{\mathbb{Z}}$	13.74
POM	<u> </u>			
1	mA	7.22	$1_{\mathbf{P}}$	1
2	Zumax	0.96	$1_{\mathbb{Z}}$	1.15
3	KG1	0.92	$1_{OM}$	3.87

Table 6: Parameter identifiability (as  $\gamma$ , eq. (3)) for relevant state variables. Selections followed the third heuristic where parameters were selected equally within each category from most to least sensitive (L1, eq. (2)), until  $\gamma > 15$ . Rank describes the relative parameter sensitivity in each category for each state variable (O: optics, OM: organic matter, P: phytoplankton, T: temperature, Z: zooplankton).

Selections by state variable	Parameter	L1	Rank	$\gamma$
Ammonium				
1	mA	8.49	$1_{\mathbf{P}}$	1
2	nitmax	1.54	$1_{\text{OM}}$	1.16
3	Zumax	1.42	$1_{\mathbb{Z}}$	2.9
4	$Tref(nospA+nospZ)_{p1}$	0.79	$1_{\mathrm{T}}$	3.46
5	astar490	0.03	$1_{\rm O}$	4.25
Chlorophyll				
1	mA	13.94	$1_{\rm P}$	1
2	Zumax	1.02	$1_{\mathbf{Z}}$	1.18
3	$Tref(nospA+nospZ)_{p1}$	0.6	$1_{\mathrm{T}}$	2.62
4	KGcdom	0.07	$1_{\text{OM}}$	3.24
5	astar490	0.02	1 <sub>0</sub>	5.98
Dissolved Oxygen				
1	umax	0.05	$1_{\mathrm{P}}$	1
2	ZKa	0.05	$1_{\mathbb{Z}}$	2.17
3	$Tref(nospA+nospZ)_{p1}$	0.02	$1_{\mathrm{T}}$	2.29
4	KG1	$6.15 \times 10^{-3}$	$1_{\text{OM}}$	3.85
5	astar490	$7.51 \times 10^{-4}$	$1_{\rm O}$	3.89
6	mA	0.02	$2_{\rm P}$	4.42
7	ZQn	0.02	$2_{\mathbb{Z}}$	5.22
DOM				
1	mA	14.25	$1_{\mathbf{P}}$	1
2	$Tref(nospA+nospZ)_{p1}$	1.48	$1_{\mathrm{T}}$	1.05
3	Zumax	1.01	$1_{\rm Z}$	2.61
4	KG2	0.94	$1_{\text{OM}}$	3.39
5	astar490	0.04	$1_{\rm O}$	4.46
6	umax	1.11	$2_{\rm P}$	6.02
7	ZKa	0.88	$2_{\mathbb{Z}}$	9.21
Irradiance	717	0.19	4	4
1	ZKa	0.13	$1_{\rm Z}$	1
2	umax	0.09	$1_{\mathrm{P}}$	4.41
3 4	KGcdom	0.05	$1_{\text{OM}}$	4.5
5	$Tref(nospA+nospZ)_{p1}$ astar490	0.03	$1_{\mathrm{T}}$	$4.5 \\ 6.9$
6		$0.02 \\ 0.06$	$\frac{1}{2}$	10.63
7	ZQn mA	0.05	$rac{2_{ m Z}}{2_{ m P}}$	10.03 $11.21$
8	KG1	$3.96 \times 10^{-3}$	-	14.65
9	astarOMA	$1.47 \times 10^{-3}$	$\frac{2_{\mathrm{OM}}}{2_{\mathrm{O}}}$	14.05 $14.72$
Nitrate	usiurOMA	1.47 × 10	20	14.12
Nitrate 1	umax	8.49	$1_{\rm P}$	1
Phosphate	инил	0.40	1P	1
1	ZKa	1.47	$1_{\mathbb{Z}}$	1
2	umax	0.78	$1_{ m P}$	11.45
3	$Tref(nospA+nospZ)_{D1}$	0.16	$1_{ m T}$	13.71
4	KGl	0.14	$1_{\rm OM}$	14.64
POM		J.11	±UM	11.01
1 OW1	mA	7.22	$1_{\mathrm{P}}$	1
2	Zumax	0.96	$1_{ m Z}$	1.15
3	KG1	0.92	$1_{\rm OM}$	3.87
4	$Tref(nospA+nospZ)_{D1}$	0.86	$1_{\mathrm{T}}$	3.93
5	astar490	0.03	1 <sub>0</sub>	5.81
		0.00	-0	3.01

Table 7: Changes in mean sensitivity of state variables by parameter categories to different initial conditions and structural components of the model. Changes show the difference in average sensitivity from results using the default model setup. Sensitivities are based on average L1 (see eq. (2)) values of the state variables to changes in parameters in each parameter category. Increases in average sensitivity are in bold. Medians and ranges of sensitivity values for the different conditions are shown in Fig. 8.

State variables by parameter category	<u> </u>		Change	
	Default sensitivity	Initial: April	Initial: September	Structure: complex
Optics				
Ammonium	0.01	$-9.13 \times 10^{-3}$	$-8.37 \times 10^{-3}$	$-7.7 \times 10^{-3}$
Chlorophyll	$8.77 \times 10^{-3}$	$-6.79 \times 10^{-3}$	$-6.3 \times 10^{-3}$	$-7.33 \times 10^{-3}$
Dissolved Oxygen	$2.81 \times 10^{-4}$	$-2.11 \times 10^{-4}$	$-1.46 \times 10^{-4}$	$-1.93 \times 10^{-4}$
Irradiance	$9.1 \times 10^{-3}$	$2.56  imes 10^{-3}$	$3.1  imes 10^{-3}$	$1.57  imes 10^{-3}$
Nitrate	$7.72 \times 10^{-3}$	$-6.46 \times 10^{-3}$	$-6.2 \times 10^{-3}$	$-6.8 \times 10^{-3}$
POM	0.01	$-9.06 \times 10^{-3}$	$-8.49 \times 10^{-3}$	$-8.56 \times 10^{-3}$
DOM	0.02	-0.01	-0.01	-0.01
Phosphate	$3.35 \times 10^{-3}$	$-2.53 \times 10^{-3}$	$-2.15 \times 10^{-3}$	$-3.04 \times 10^{-3}$
Organic Matter				
Ammonium	0.31	0.08	0.04	$-2.22 \times 10^{-4}$
Chlorophyll	0.02	0.12	0.14	-0.01
Dissolved Oxygen	$2.17 \times 10^{-3}$	$-6.75 \times 10^{-4}$	$2.32  imes 10^{-4}$	$-1.05 \times 10^{-3}$
Irradiance	$6.63 \times 10^{-3}$	$5.34  imes 10^{-3}$	$6.79 \times 10^{-3}$	$-2.99 \times 10^{-4}$
Nitrate	0.12	0.06	0.09	-0.1
POM	0.13	0.15	0.12	0.04
DOM	0.14	0.07	0.17	0.05
Phosphate	0.03	0.04	0.06	-0.02
Phytoplankton	0.00	0.01	0.00	0.02
Ammonium	0.8	-0.02	0.3	65.98
Chlorophyll	1.14	1.23	4.38	104.24
Dissolved Oxygen	0.01	$-4.58 \times 10^{-4}$	$2.31 \times 10^{-3}$	$3.44 \times 10^{-4}$
Irradiance	0.02	$-2.04 \times 10^{-3}$	$1.83 \times 10^{-3}$	$7.53 \times 10^{-3}$
Nitrate	0.74	$-2.04 \times 10$ -0.43	-0.45	-0.64
POM	0.74	-0.43 0.17	0.46	-0.04 <b>55.11</b>
DOM	1.28	0.17	1.15	128.93
Phosphate	0.17	0.34 $0.03$	0.05	-0.14
Temperature	0.17	0.05	0.00	-0.14
Ammonium	0.79	-0.69	-0.69	272.31
	0.79			
Chlorophyll		-0.47	-0.45	114.51
Dissolved Oxygen	0.02	-0.02	-0.02	-0.01
Irradiance	0.03	-0.02	-0.02	0.01
Nitrate	0.3	-0.15	-0.16	-0.19
POM	0.86	-0.68	-0.69	215.17
DOM	1.48	-1.21	-1.2	900.26
Phosphate	0.16	-0.11	-0.09	-0.11
Zooplankton	0.45	0.45	0.44	0.10
Ammonium	0.47	-0.45	-0.44	-0.16
Chlorophyll	0.39	-0.26	-0.23	-0.2
Dissolved Oxygen	0.01	-0.01	$-8.68 \times 10^{-3}$	$-6.96 \times 10^{-3}$
Irradiance	0.03	-0.02	-0.02	-0.01
Nitrate	1.06	-1.02	-1.02	-0.98
POM	0.37	-0.27	-0.28	-0.18
DOM	0.39	-0.3	-0.28	-0.18
Phosphate	0.31	-0.19	-0.17	-0.27

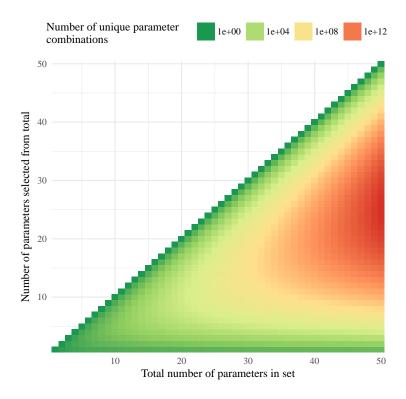


Fig. 1: Examples of unique parameter combinations from different parameter sets and number of selected parameters. The number of combinations are shown for increasing numbers of selected parameters from the total in the set, where 50 parameter sets are shown each with one through 50 total parameters. Note that the number of unique combinations is shown as the natural log mbnex

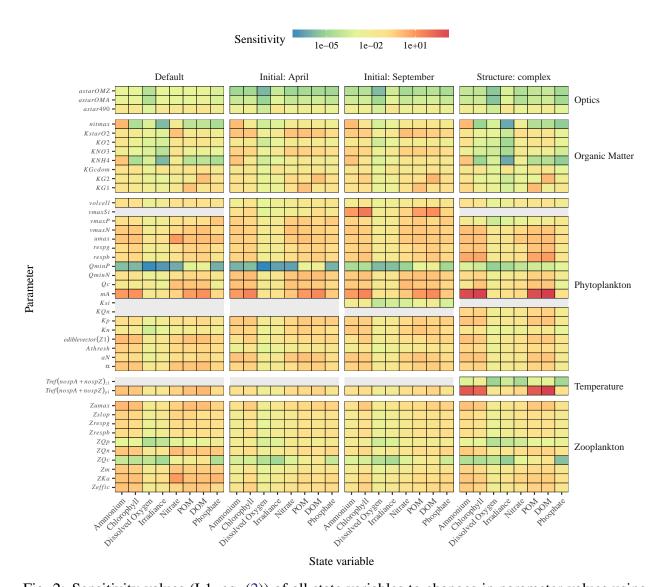


Fig. 2: Sensitivity values (L1, eq. (2)) of all state variables to changes in parameter values using default conditions, changes in initial conditions (April, September seasonal means, Table 1), and changes in structural complexity (Table 2). Parameters are grouped by category: optics, organic matter, phytoplankton, zooplankton, temperature, and zoplankton. See Table 3 for L1 values for  $O_2$  and Tables S1 to S7 for the other state variables.

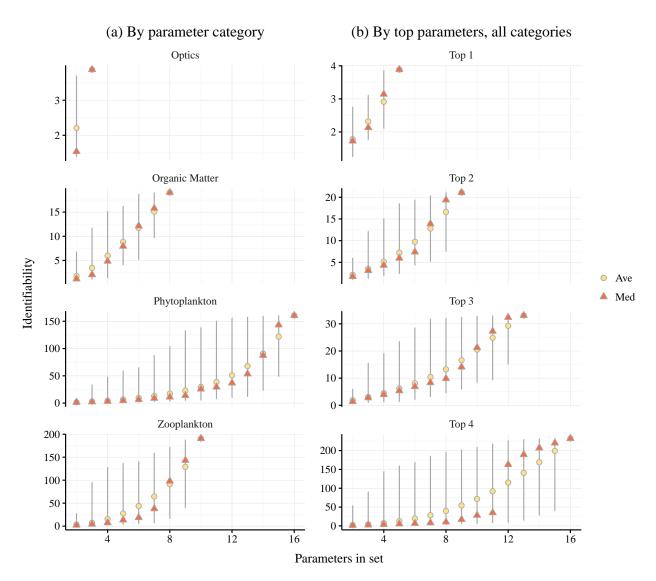


Fig. 3: Identifiability (as  $\gamma$ , eq. (3)) of parameter subsets for  $O_2$ . Plots in (a) show identifiability by parameter categories and (b) shows identifiability by selecting the top 1 through 4 parameters in all categories. Lines represent identifiability ranges for the possible combinations given the number of parameters in the set. The temperature category is not shown because  $O_2$  was sensitive to only one parameter (i.e.,  $\gamma = 1$ ).

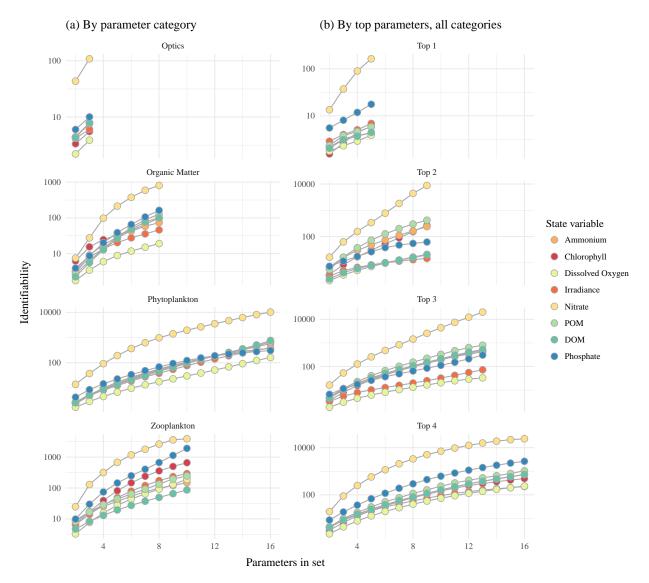


Fig. 4: Average identifiability (as  $\gamma$ , eq. (3)) of parameter subsets for all state variables. Plots in (a) show identifiability by parameter categories and (b) shows identifiability by selecting the top 1 through 4 parameters in all categories. Identifiability was averaged for all combinations in a parameter set to evaluate relative differences between state variables. The temperature category is not shown because all state variables were sensitive to only one parameter (i.e<sub>f</sub>:  $\gamma$  = 1dentploal1

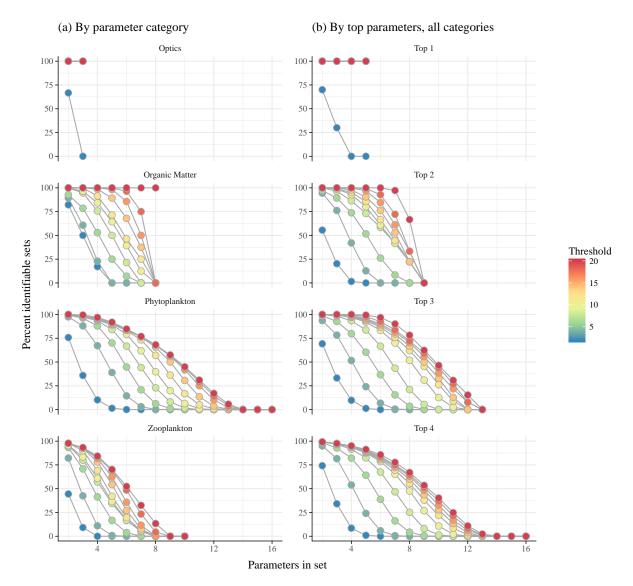


Fig. 5: Percent of identifiable parameter sets for  $O_2$  at different  $\gamma$  thresholds, selection criteria, and total number of parameters in the set. Thresholds varied from  $\gamma=2$  to 20 such that sets with  $\gamma$  below a threshold were considered identifiable relative to the value. Plots in (a) show percent of identifiable sets by selecting parameters within categories and (b) shows percent identifiable by selecting from the top 1 through 4 parameters in all categories. Percent identifiable was based on all sets in Fig. 3.

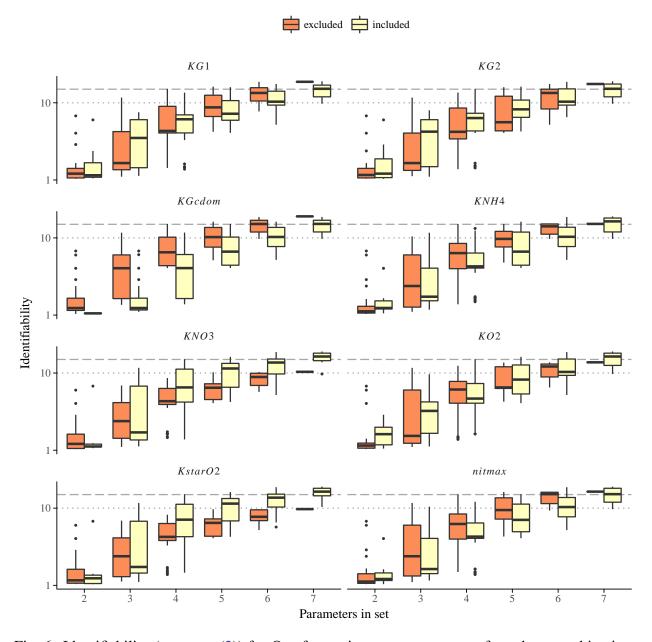


Fig. 6: Identifiability (as  $\gamma$ , eq. (3)) for  $O_2$  of organic matter parameters for subset combinations in Fig. 3. Identifiability is evaluated for subsets that excluded and included the parameters at the top of each plot. Identifiability of including all eight parameters is in Fig. 3. Grey lines indicate potential thresholds at  $\gamma=10,15$  for maximum acceptable identifiability.

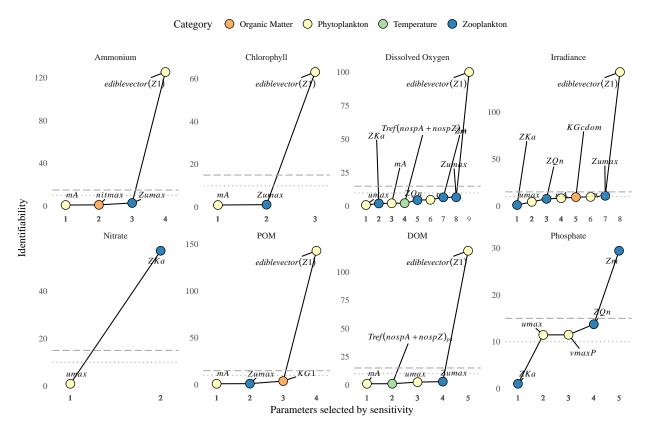


Fig. 7: Identifiability (as  $\gamma$ , eq. (3)) of selecting parameters for all state variables. Parameters are selected by decreasing sensitivity independent of parameter categories. Grey lines indicate potential thresholds at  $\gamma=10,15$  for maximum acceptable identifiability. Selection stops after  $\gamma>15$ .

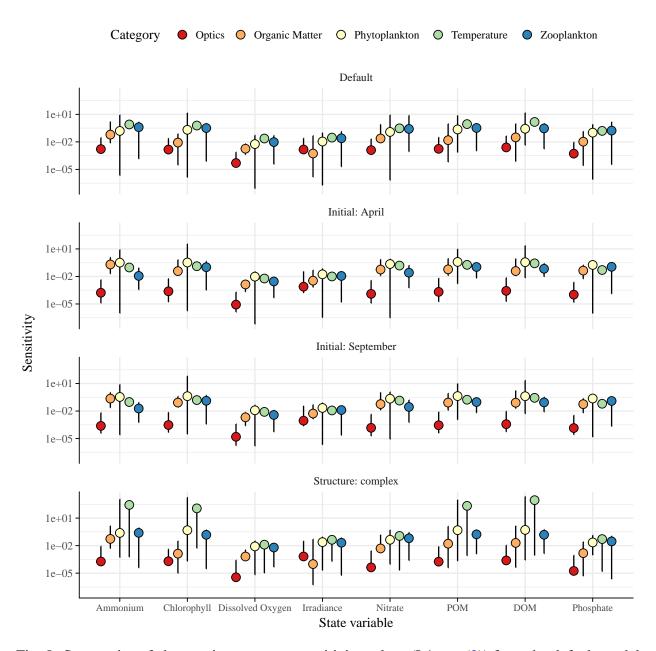


Fig. 8: Summaries of changes in parameter sensitivity values (L1, eq. (2)) from the default model conditions. Sensitivity was re-evaluated using initial conditions as seasonal means for April and September, and added structural complexity. Sensitivity is summarized as the minimum, median, and maximum for each state variable separated by parameter categories. Changes in average sensitivity from the default model conditions are in Table 7.

Table S1: Sensitivity of ammonium to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where L1 summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect ammonium are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
Optics		
Chla specific absorption at 490 nm	astar490	0.03
OMA specific absorption at 490 nm	astarOMA	$1.63 \times 10^{-3}$
OMZ specific absorption at 490 nm	astarOMZ	$1.5 \times 10^{-3}$
Temperature		
Optimum temperature for growth(C)	$Tref(nospA + nospZ)_{p1}$	0.79
Phytoplankton		
mortality coefficient	mA	8.49
edibility vector for Z1	edible vector(Z1)	1.32
maximum growth rate	umax	0.65
initial slope of the photosynthesis-irradiance relationship	alpha	0.6
N-uptake rate measured at umax	vmaxN	0.46
Phytoplankton threshold for grazing, is multiplied by VOLcell	Athresh	0.29
coefficient for non-limiting nutrient	aN	0.17
phytoplankton growth respiration coefficient	respg	0.16
phytoplankton basal respiration coefficient	respb	0.15
half-saturation constant for P	Кр	0.14
phytoplankton volume/cell	volcell	0.14
minimum N cell-quota	QminN	0.1
P-uptake rate measured at umax	vmaxP	0.1
phytoplankton carbon/cell	Qc	0.03
half-saturation constant for N	Kn	0.01
minimum P cell-quota	QminP	$2.24 \times 10^{-6}$
Zooplankton		
maximum growth rate of zooplankton	Zumax	1.42
assimilation efficiency as a fraction of ingestion	Zeffic	0.76
half saturation coefficient for grazing	ZKa	0.74
zooplankton nitrogen/individual	ZQn	0.62
Zooplankton mortality constant for quadratic mortality	Zm	0.5
proportion of grazed phytoplankton lost to sloppy feeding	Zslop	0.3
Zooplankton growth-dependent respiration factor	Zrespg	0.22
Zooplankton biomass-dependent respiration factor	Zrespb	0.16
zooplankton phosphorus/individual	ZQp	$1.07\times10^{-3}$
zooplankton carbon/individual	ZQc	$1.44\times10^{-4}$
Organic Matter		
maximum rate of nitrification per day	nitmax	1.54
NH4 rate constant for nitrification	KNH4	0.66
turnover rate for OM1A and OM1Z	KG1	0.07
decay rate of CDOM, 1/day	KGcdom	0.07
half-saturation concentration for O2 utilization	KO2	0.06
O2 concentration that inhibits denitrification	KstarO2	0.05
turnover rate for OM2A and OM2Z	KG2	0.03
half-saturation concentration for NO3 used in denitrification	KNO3	$7.55\times10^{-3}$

Table S2: Sensitivity of chl-a to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where L1 summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect chl-a are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
Optics		
Chla specific absorption at 490 nm	astar490	0.02
OMA specific absorption at 490 nm	astarOMA	$1.45 \times 10^{-3}$
OMZ specific absorption at 490 nm	astarOMZ	$1.13\times10^{-3}$
Temperature		
Optimum temperature for growth(C)	$Tref(nospA+nospZ)_{p1}$	0.6
Phytoplankton	^	
mortality coefficient	mA	13.94
edibility vector for Z1	ediblevector(Z1)	0.95
maximum growth rate	umax	0.85
initial slope of the photosynthesis-irradiance relationship	alpha	0.62
N-uptake rate measured at umax	vmaxN	0.53
phytoplankton growth respiration coefficient	respg	0.26
Phytoplankton threshold for grazing, is multiplied by VOLcell	Athresh	0.25
phytoplankton basal respiration coefficient	respb	0.24
coefficient for non-limiting nutrient	aN	0.17
half-saturation constant for P	Кр	0.14
P-uptake rate measured at umax	vmaxP	0.12
phytoplankton volume/cell	volcell	0.1
minimum N cell-quota	QminN	0.07
phytoplankton carbon/cell	Qc	0.02
half-saturation constant for N	Kn	0.01
minimum P cell-quota	QminP	$1.38\times10^{-6}$
Zooplankton		
maximum growth rate of zooplankton	Zumax	1.02
half saturation coefficient for grazing	ZKa	0.85
assimilation efficiency as a fraction of ingestion	Zeffic	0.57
zooplankton nitrogen/individual	ZQn	0.52
Zooplankton mortality constant for quadratic mortality	Zm	0.41
proportion of grazed phytoplankton lost to sloppy feeding	Zslop	0.23
Zooplankton growth-dependent respiration factor	Zrespg	0.17
Zooplankton biomass-dependent respiration factor	Zrespb	0.14
zooplankton phosphorus/individual	ZQp	$1.29 \times 10^{-3}$
zooplankton carbon/individual	ZQc	$7.55 \times 10^{-5}$
Organic Matter		
decay rate of CDOM, 1/day	KGcdom	0.07
turnover rate for OM1A and OM1Z	KG1	0.03
turnover rate for OM2A and OM2Z	KG2	0.01
O2 concentration that inhibits denitrification	KstarO2	0.01
half-saturation concentration for O2 utilization	KO2	$3.35\times10^{-3}$
half-saturation concentration for NO3 used in denitrification	KNO3	$1.19\times10^{-3}$
maximum rate of nitrification per day	nitmax	$3.4 \times 10^{-5}$
NH4 rate constant for nitrification	KNH4	$2.97 \times 10^{-5}$

Table S3: Sensitivity of irradiance to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where L1 summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect irradiance are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
Optics		
Chla specific absorption at 490 nm	astar490	0.02
OMA specific absorption at 490 nm	astarOMA	$1.47\times10^{-3}$
OMZ specific absorption at 490 nm	astarOMZ	$1.34 \times 10^{-3}$
Temperature		
Optimum temperature for growth(C)	$Tref(nospA + nospZ)_{p1}$	0.03
Phytoplankton		
maximum growth rate	umax	0.09
mortality coefficient	mA	0.05
initial slope of the photosynthesis-irradiance relationship	alpha	0.04
edibility vector for Z1	ediblevector(Z1)	0.04
N-uptake rate measured at umax	vmaxN	0.03
Phytoplankton threshold for grazing, is multiplied by VOLcell	Athresh	0.02
coefficient for non-limiting nutrient	aN	0.01
phytoplankton growth respiration coefficient	respg	0.01
half-saturation constant for P	Кp	0.01
P-uptake rate measured at umax	vmaxP	$9.48 \times 10^{-3}$
phytoplankton basal respiration coefficient	respb	$9.38 \times 10^{-3}$
phytoplankton volume/cell	volcell	$8.1 \times 10^{-3}$
minimum N cell-quota	QminN	$5.75\times10^{-3}$
phytoplankton carbon/cell	$\widetilde{Q}c$	$3.78 \times 10^{-3}$
half-saturation constant for N	Kn	$9.81 \times 10^{-4}$
minimum P cell-quota	QminP	$1.92 \times 10^{-7}$
Zooplankton		
half saturation coefficient for grazing	ZKa	0.13
zooplankton nitrogen/individual	ZQn	0.06
maximum growth rate of zooplankton	Zumax	0.04
Zooplankton mortality constant for quadratic mortality	Zm	0.04
assimilation efficiency as a fraction of ingestion	Zeffic	0.03
proportion of grazed phytoplankton lost to sloppy feeding	Zslop	0.02
Zooplankton growth-dependent respiration factor	Zrespg	0.01
Zooplankton biomass-dependent respiration factor	Zrespb	$9.67\times10^{-3}$
zooplankton phosphorus/individual	ZQp	$9.34 \times 10^{-5}$
zooplankton carbon/individual	ZQc	$1.99 \times 10^{-5}$
Organic Matter		
decay rate of CDOM, 1/day	KGcdom	0.05
turnover rate for OM1A and OM1Z	KG1	$3.96\times10^{-3}$
turnover rate for OM2A and OM2Z	KG2	$9.88 \times 10^{-4}$
O2 concentration that inhibits denitrification	KstarO2	$7.2 \times 10^{-4}$
half-saturation concentration for O2 utilization	KO2	$3.54 \times 10^{-4}$
half-saturation concentration for NO3 used in denitrification	KNO3	$6.18\times10^{-5}$
maximum rate of nitrification per day	nitmax	$1.72 \times 10^{-6}$
NH4 rate constant for nitrification	KNH4	$1.48\times10^{-6}$

Table S4: Sensitivity of nitrate to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where L1 summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect nitrate are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
Optics		
Chla specific absorption at 490 nm	astar490	0.02
OMZ specific absorption at 490 nm	astarOMZ	$1.27\times10^{-3}$
OMA specific absorption at 490 nm	astarOMA	$1.19\times10^{-3}$
Temperature		
Optimum temperature for growth(C)	$Tref(nospA+nospZ)_{p1}$	0.3
Phytoplankton		
maximum growth rate	umax	8.49
phytoplankton carbon/cell	Qc	0.89
initial slope of the photosynthesis-irradiance relationship	alpha	0.7
edibility vector for Z1	ediblevector(Z1)	0.33
mortality coefficient	mA	0.27
Phytoplankton threshold for grazing, is multiplied by VOLcell	Athresh	0.2
N-uptake rate measured at umax	vmaxN	0.19
coefficient for non-limiting nutrient	aN	0.13
phytoplankton growth respiration coefficient	respg	0.11
phytoplankton volume/cell	volcell	0.1
P-uptake rate measured at umax	vmaxP	0.1
half-saturation constant for P	Кр	0.09
minimum N cell-quota	QminN	0.09
phytoplankton basal respiration coefficient	respb	0.07
half-saturation constant for N	Kn	$7.06 \times 10^{-3}$
minimum P cell-quota	QminP	$6.67 \times 10^{-7}$
Zooplankton		
half saturation coefficient for grazing	ZKa	7.59
zooplankton nitrogen/individual	ZQn	1.17
Zooplankton mortality constant for quadratic mortality	Zm	0.7
maximum growth rate of zooplankton	Zumax	0.34
proportion of grazed phytoplankton lost to sloppy feeding	Zslop	0.26
assimilation efficiency as a fraction of ingestion	Zeffic	0.25
Zooplankton growth-dependent respiration factor	Zrespg	0.17
Zooplankton biomass-dependent respiration factor	Zrespb	0.1
zooplankton carbon/individual	ZQc	$3.8 \times 10^{-3}$
zooplankton phosphorus/individual	$\widetilde{ZQp}$	$8.59 \times 10^{-4}$
Organic Matter	~1	
O2 concentration that inhibits denitrification	KstarO2	0.78
half-saturation concentration for NO3 used in denitrification	KNO3	0.07
decay rate of CDOM, 1/day	KGcdom	0.04
half-saturation concentration for O2 utilization	KO2	0.03
turnover rate for OM1A and OM1Z	KG1	0.02
turnover rate for OM2A and OM2Z	KG2	0.01
maximum rate of nitrification per day	nitmax	$9.96 \times 10^{-3}$
NH4 rate constant for nitrification	KNH4	$9.87 \times 10^{-3}$

Table S5: Sensitivity of POM to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where L1 summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect POM are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
Optics		
Chla specific absorption at 490 nm	astar490	0.03
OMA specific absorption at 490 nm	astarOMA	$1.73 \times 10^{-3}$
OMZ specific absorption at 490 nm	astarOMZ	$1.49 \times 10^{-3}$
Temperature		
Optimum temperature for growth(C)	$Tref(nospA+nospZ)_{p1}$	0.86
Phytoplankton		
mortality coefficient	mA	7.22
edibility vector for Z1	ediblevector(Z1)	0.9
maximum growth rate	umax	0.89
phytoplankton carbon/cell	Qc	0.67
initial slope of the photosynthesis-irradiance relationship	alpha	0.67
N-uptake rate measured at umax	vmaxN	0.45
phytoplankton growth respiration coefficient	respg	0.29
phytoplankton basal respiration coefficient	respb	0.24
Phytoplankton threshold for grazing, is multiplied by VOLcell	Athresh	0.22
minimum N cell-quota	QminN	0.21
coefficient for non-limiting nutrient	aN	0.14
half-saturation constant for P	Кр	0.11
phytoplankton volume/cell	volcell	0.1
P-uptake rate measured at umax	vmaxP	0.09
half-saturation constant for N	Kn	0.01
minimum P cell-quota	QminP	$7.35\times10^{-4}$
Zooplankton		
maximum growth rate of zooplankton	Zumax	0.96
half saturation coefficient for grazing	ZKa	0.79
assimilation efficiency as a fraction of ingestion	Zeffic	0.54
zooplankton nitrogen/individual	ZQn	0.49
Zooplankton mortality constant for quadratic mortality	Zm	0.39
proportion of grazed phytoplankton lost to sloppy feeding	Zslop	0.27
Zooplankton growth-dependent respiration factor	Zrespg	0.16
Zooplankton biomass-dependent respiration factor	Zrespb	0.12
zooplankton carbon/individual	ZQc	$9.64 \times 10^{-3}$
zooplankton phosphorus/individual	ZQp	$1.06 \times 10^{-3}$
Organic Matter	-z <sub>r</sub>	
turnover rate for OM1A and OM1Z	KG1	0.92
decay rate of CDOM, 1/day	KGcdom	0.07
half-saturation concentration for O2 utilization	KO2	0.04
O2 concentration that inhibits denitrification	KstarO2	0.02
turnover rate for OM2A and OM2Z	KG2	0.02
half-saturation concentration for NO3 used in denitrification	KNO3	$3.72 \times 10^{-3}$
maximum rate of nitrification per day	nitmax	$6.98 \times 10^{-5}$
NH4 rate constant for nitrification	KNH4	$6.41 \times 10^{-5}$

Table S6: Sensitivity of dissolved organic matter to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where L1 summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect dissolved organic matter are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
Optics		
Chla specific absorption at 490 nm	astar490	0.04
OMA specific absorption at 490 nm	astarOMA	$2.48 \times 10^{-3}$
OMZ specific absorption at 490 nm	astarOMZ	$2.04 \times 10^{-3}$
Temperature		
Optimum temperature for growth(C)	$Tref(nospA + nospZ)_{p1}$	1.48
Phytoplankton		
mortality coefficient	mA	14.25
maximum growth rate	umax	1.11
edibility vector for Z1	ediblevector(Z1)	0.94
N-uptake rate measured at umax	vmaxN	0.86
initial slope of the photosynthesis-irradiance relationship	alpha	0.85
phytoplankton carbon/cell	Qc	0.67
phytoplankton growth respiration coefficient	respg	0.36
phytoplankton basal respiration coefficient	respb	0.29
coefficient for non-limiting nutrient	aN	0.25
minimum N cell-quota	QminN	0.24
Phytoplankton threshold for grazing, is multiplied by VOLcell	Athresh	0.22
half-saturation constant for P	Кр	0.2
P-uptake rate measured at umax	vmaxP	0.14
phytoplankton volume/cell	volcell	0.1
half-saturation constant for N	Kn	0.02
minimum P cell-quota	QminP	$4.37 \times 10^{-3}$
Zooplankton		
maximum growth rate of zooplankton	Zumax	1.01
half saturation coefficient for grazing	ZKa	0.88
assimilation efficiency as a fraction of ingestion	Zeffic	0.58
zooplankton nitrogen/individual	ZQn	0.54
Zooplankton mortality constant for quadratic mortality	Zm	0.41
Zooplankton growth-dependent respiration factor	Zrespg	0.17
Zooplankton biomass-dependent respiration factor	Zrespb	0.13
proportion of grazed phytoplankton lost to sloppy feeding	Zslop	0.12
zooplankton carbon/individual	ZQc	0.04
zooplankton phosphorus/individual	ZQp	$1.69\times10^{-3}$
Organic Matter		
turnover rate for OM2A and OM2Z	KG2	0.94
decay rate of CDOM, 1/day	KGcdom	0.1
half-saturation concentration for O2 utilization	KO2	0.04
turnover rate for OM1A and OM1Z	KG1	0.04
O2 concentration that inhibits denitrification	KstarO2	0.03
half-saturation concentration for NO3 used in denitrification	KNO3	$3.16\times10^{-3}$
maximum rate of nitrification per day	nitmax	$8.44\times10^{-5}$
NH4 rate constant for nitrification	KNH4	$7.41\times10^{-5}$

Table S7: Sensitivity of phosphate to perturbations of individual parameters. Sensitivities are based on a 50% increase from the initial parameter value, where L1 summarizes differences in model output from the default (see eq. (2)). Parameters that did not affect phosphate are not shown. Parameters are grouped by categories as optics, temperature, phytoplankton, zooplankton, and organic matter.

Description	Parameter	L1
Optics		
Chla specific absorption at 490 nm	astar490	$9.01 \times 10^{-3}$
OMZ specific absorption at 490 nm	astarOMZ	$5.21 \times 10^{-4}$
OMA specific absorption at 490 nm	astarOMA	$5.13 \times 10^{-4}$
Temperature		
Optimum temperature for growth(C)	$Tref(nospA + nospZ)_{p1}$	0.16
Phytoplankton		
maximum growth rate	umax	0.78
P-uptake rate measured at umax	vmaxP	0.59
edibility vector for Z1	ediblevector(Z1)	0.25
initial slope of the photosynthesis-irradiance relationship	alpha	0.23
mortality coefficient	mA	0.2
N-uptake rate measured at umax	vmaxN	0.18
Phytoplankton threshold for grazing, is multiplied by VOLcell	Athresh	0.13
coefficient for non-limiting nutrient	aN	0.11
phytoplankton growth respiration coefficient	respg	0.09
phytoplankton volume/cell	volcell	0.06
phytoplankton basal respiration coefficient	respb	0.06
minimum N cell-quota	QminN	0.04
half-saturation constant for P	Кp	0.03
half-saturation constant for N	Kn	$6.97 \times 10^{-3}$
phytoplankton carbon/cell	Qc	$6.68 \times 10^{-3}$
minimum P cell-quota	~ QminP	$8.21 \times 10^{-7}$
Zooplankton		
half saturation coefficient for grazing	ZKa	1.47
zooplankton nitrogen/individual	ZQn	0.5
Zooplankton mortality constant for quadratic mortality	Zm	0.35
maximum growth rate of zooplankton	Zumax	0.26
assimilation efficiency as a fraction of ingestion	Zeffic	0.19
proportion of grazed phytoplankton lost to sloppy feeding	Zslop	0.15
Zooplankton growth-dependent respiration factor	Zrespg	0.1
Zooplankton biomass-dependent respiration factor	Zrespb	0.06
zooplankton phosphorus/individual	ZQp	$6.43 \times 10^{-3}$
zooplankton carbon/individual	ZQc	$3.38 \times 10^{-5}$
Organic Matter		
turnover rate for OM1A and OM1Z	KG1	0.14
turnover rate for OM2A and OM2Z	KG2	0.06
decay rate of CDOM, 1/day	KGcdom	0.02
half-saturation concentration for O2 utilization	KO2	0.01
O2 concentration that inhibits denitrification	KstarO2	$7.29 \times 10^{-3}$
half-saturation concentration for NO3 used in denitrification	KNO3	$1.19 \times 10^{-3}$
maximum rate of nitrification per day	nitmax	$2.7\times10^{-5}$
NH4 rate constant for nitrification	KNH4	$2.64\times10^{-5}$
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