# Parameter sensitivity and identifiability for a biogeochemical model of hypoxia in the northern Gulf of Mexico

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Abstract

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Bio-geo-chemical models are useful tools in environmental sciences that can guide management and policy-making. Consequently, significant time and resources are spent developing these models in system-specific contexts. The optimization of model parameters to maximize precision, including transferability of these models to different systems, are fundamental concerns in the development and application of these tools. This study describes quantitative limitations of coupled hydrodynamic-ecological modelling by contrasting numeric and ecological certainty with a systematic framework for characterizing parameter sensitivity and identifability. We evaluate a simple bio-geo-chemical model that is the zero-dimensional (0-D) unit of a larger spatio-temporal model of hypoxia on the Louisiana continental shelf of Gulf of Mexico as an example. Results from analysis of the 0-D model are used to infer larger trends in dissolved oxygen dynamics over time, having implications for understanding factors that contribute to environmental conditions that are detrimental to aquatic resources. In particular, we focus on issues of parameter identifiability using local sensitivity analyses to provide quantitative descriptions of numerical constraints on model precision. We argue that quantitative and ecological certainty in model calibration are often at odds and the practitioner must explicitly choose model components to optimize given tradeoffs between the two. We further conclude that numerically optimal parameter sets for models of hypoxia are often small subsets of the complete parameter set because of redundancies in the unique effects of paramater perturbations on model output. As a result, we demonstrate that use of a model for inference into ecological mechanisms of observed or predicted changes in hypoxic condition can be potentially misguided in the absence of quantitative descriptions of identifiability. Although these concerns have been expressed in the literature, they are rarely explicitly addressed or included in model evaluations. In addition to immediate implications for regional models, we provide a framework for describing the effects of parameter uncertainty and identifiability that can be applied to similar models to better inform environmental management.

#### 1 Introduction

Hypoxia formation in bottom waters of coastal oceans occurs primarily from excess nutrient inputs from land-based sources (Justíc et al. 1987, Diaz and Rosenberg 1995, Howarth et al. 1996). These events are detrimental to aquatic organisms and have significant negative

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effects on economic resources derived from coastal ecosystems (Lipton and Hicks 2003, Diaz and
   Rosenberg 2011). An understanding of the biological, physical, and chemical processes that
   contribute to the growth of hypoxic areas is a critical concern for mitigating and preventing these
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   negative impacts. Numerical ecosystem models have been important tools for describing current
   knowledge of ecosystem processes that contribute to hypoxia formation and for predicting the
   effects of proposed management activities or future scenarios (Scavia et al. 2004, Hagy and
   Murrell 2007, Pauer et al. 2016). Unlike statistical models that have more generic structures,
   simulation and process-based models include explicit descriptions of relevant processes that are
   constrained by empirical or observational data relevant to the system of interest (e.g. Omlin et al.
   2001b, Eldridge and Roelke 2010). These models are often coupled with hydrodynamic grids to
   provide spatially-explicit representations of patterns in three dimensions (Warner et al. 2005,
   Zhao et al. 2010, Ganju et al. 2016). Combined hydrodynamic and bio-geo-chemical models have
   been developed specifically to describe hypoxic conditions on the Louisiana continental
   shelf (LCS) in the northern Gulf of Mexico (GOM) (Fennel et al. 2013, Obenour et al. 2015,
   Pauer et al. 2016, Lehrter et al. in review). This area drains a significant portion of the continental
   United States through the Mississippi-Atchafalaya River Basin (MARB) and is the second largest
   hypoxic area in the world (Rabalais et al. 2002). Understanding processes that contribute to the
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   frequency and duration of hypoxic events remains a critical research goal for the region, including
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   the application of process-based models to characterize the current knowledge domain.
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          The development and application of a model represents a tradeoff between characteristics
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   expected from the output or provided by the structural components. An idealized model is
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   sufficiently generalizable across systems, provides results that are precise given the inputs, and
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   includes components that are realistic descriptions of actual processes (Levins 1966). Given that
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   these characteristics cannot be simultaneously achieved, models are developed in partial
   dependence of reality and theoretical constructs, completely separate from both, or dependent on
   one or the other (Morrison and Morgan 1999, Ganju et al. 2016). These challenges are analogous
   to the well-known bias-variance tradeoff in statistical models that balances the competing
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   objectives of over- and under-fitting to an observed dataset. Process-based models are more
   commonly imbalanced between reality and theory, such that most are over-parameterized in an
   attempt to completely describe reality (Denman 2003, Nossent and Bauwens 2012, Petrucci and
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Bonhomme 2014). Such over-parameterization, including use of excessive structural equations, can have serious implications for practical applications. Quantitative limitations of over-parameterization are analagous to degrees of freedom in standard statistical models as free 67 parameters cannot be numerically estimated when constrained to an observed dataset (Kirchner 2006). More importantly, over-parameterization can limit use across systems outside of the data domain and impose uncertainty in model predictions as realistic values for every variable may not be known or inaccurately applied from existing studies (Durand et al. 2002, Refsgaard et al. 2007, Wade et al. 2008). The application of process-based models to describe hypoxia dynamics has not been immune to these challenges and more comprehensive approaches are needed to develop models that more carefully balance theory with reality (e.g., Snowling and Kramer 2001). Standard approaches for uncertainty analysis can be used to begin addressing model 75 complexity issues. In the most general sense, uncertainty is evaluated relative to the effects of input conditions or the observed data used to calibrate a model, changes in parameter values, or 77 variation in the structural components (Beck 1987). Evaluating parameter uncertainty is by far the most common and simplest means of evaluating model behavior. Although uncertainty analyses should be integrated throughout model development and application, parameters are more often evaluated post-hoc as a form of 'damage control' for further calibration. This approach is 81 sometimes called inverse modelling where results from sensitivity analyses are used to guide calibration or fit of the developed model to observations (Soetaert and Petzoldt 2010, or 83 confronting models with data, sensu Hilborn and Mangel 1997). Parameter sensitivity analysis combined with inverse modelling necessarily involves questions of parameter 'identifiability', where only a subset of parameters can be numerically constrained to the data as compared to the 86 entire parameter set. Redundancies in parameter effects lead to unidentifiable models where 87 optimal solutions may be empirically impossible (i.e., standard algorithms will not converge) or parameter values may be non-unique leading to the right answer for the wrong reason (Kirchner 2006). The concept of identifiable parameter subsets is not foreign to hypoxia or eutrophication models (Omlin et al. 2001a, Estrada and Diaz 2010, Mateus and Franz 2015), although there is a 91 clear need for greater integration of these concepts in model development (Fasham et al. 2006). Moreover, the inclusion of sensitivity and identifiability analyses in model tuning will require the adoption of selection rules that are context-dependent given the subsets that are possible with

large parameter sets (e.g., Wagener et al. 2001a,b).

This study describes a parameter sensitivity analysis to evaluate identifiability for a 96 bio-geo-chemical model of hypoxia for the northern GOM. We evaluate a simple 97 zero-dimensional (0-D) unit of a larger spatial-temporal model to explore relationships between multiple parameter sets and hypoxia dynamics on the LCS. Specifically, we provide empirical results to support the assumption that models are generally over-parameterized and only a finite 100 and smaller subset of the larger parameter set can be optimized for a given research question or 101 dataset. We provide explicit guidance for choosing such subsets of the parameter space given 102 constraints on identifiability as directly related to sensitivity analyses. The objectives are to 103 1) identify the parameters that have the greatest influence on dissolved oxygen  $(O_2)$  using local 104 sensitivity analysis, 2) quantify the identifiability of subsets of the total parameter space based on 105 sensitivity, 3) and provide a set of heuristics for choosing parameters based on sensitivity, 106 identifiability, and parameter categories, including extension to other state variables provided by 107 the model. A final analysis evaluates identifiability relative to structural uncertainty to provide an 108 example of extending these methods to more complex uncertainty assessments. The optimum parameter space is defined as the chosen subset that represents the maximum number of 110 identifiable parameters. Here, 'optimum' is both a qualitative description based on a research 111 question or management goal and a quantitative objective based on numerical optimization 112 criteria for fitting model output to a calibration dataset. These results can be used to refine 113 existing models or guide application of models to novel contexts, such as downscaling or application to new environments. We conclude with a discussion of the implications for hypoxia 115 formation in coastal regions, including management strategies for nutrient reduction and use of 116 mechanistic models to inform decision-making. 117

#### 2 Methods

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### 2.1 Model description

Hypoxic events, defined as <2 mg L<sup>-1</sup> of O<sub>2</sub> (<64 mmol m<sup>-</sup>3), occur seasonally in bottom waters in the northern GOM. The LCS receives high nutrient loads from the MARB that drains a significant portion of the continental United States. Nutrient-stimulated primary production in surface waters increases biological oxygen demand in bottom waters as sinking

organic matter is decomposed (Bierman et al. 1994, Murrell et al. 2013). The hypoxic area averages 15,540 km<sup>2</sup> annually (1993-2015) with minimum concentrations observed from late 125 spring to early fall. Seasonal variation is strongly related to carbon and nutrient export from the 126 MARB (Lohrenz et al. 2008, Bianchi et al. 2010), whereas hydrologic variation, currents, and 127 wind patterns can affect vertical salinity gradients that contribute to the formation of hypoxia 128 (Wiseman et al. 1997, Paerl et al. 1998, Obenour et al. 2015).

This study evaluates a recently developed hydrodynamic and ecological model that 130 describes horizontal and vertical transport and mixing of state variables relevant for hypoxia in 131 the northern GOM. The Coastal General Ecosystem Model (CGEM) includes elements from the 132 Navy Coastal Ocean Model (Martin 2000) that describe hydrodynamics on the LCS and a biogeochemical model with multiple plankton groups, water-column metabolism, and sediment diagenesis (Eldridge and Roelke 2010). The hydrodynamic component of CGEM provides a 135 spatially-explicit description of hypoxia using an orthogonal grid with an approximate horizontal 136 resolution of 1.9 km $^2$  and twenty equally-spaced vertical sigma layers on the shelf (depth  $\leq 100$ 137 m, with additional hybrid layers at deeper depths). The biogeochemical component includes equations for 36 state variables including six phytoplankton groups (with nitrogen and 139 phosophorus quotas for each), two zooplankton groups, nitrate, ammonium, phosphate, dissolved 140 inorganic carbon, oxygen, silica, and multiple variables for dissolved and particulate organic 141 matter from different sources. Atmospheric and hydrological boundary conditions described in 142 Hodur (1997) and Lehrter et al. (2013) are also included in CGEM.

The core unit of CGEM is FishTank, a 0-D model that implements the biogeochemical 144 equations in Eldridge and Roelke (2010) and does not include any form of physical transport (i.e., 145 advection, mixing, or surface flux). Although FishTank was developed for specific application in 146 CGEM, it can easily be applied to other hydrodynamic grids. Accordingly, the sensitivity and 147 identifiability analysis described below are informative for both the LCS gridded model as well as potential applications to different systems. The FishTank model provides estimates for the 36 149 state variables described above using a 0-D parcel that is uniformly mixed as a closed system. A 150 set of initial conditions is provided as input to the model that was based on observations of relevant variables obtained from research cruises in April, June, and September 2006 Murrell et al. (Table 1 in 2014).

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Results from FishTank are based on time-dependent differential equations that describe 154 energy flow between phytoplankton and zooplankton groups as affected by nutrient uptake rates, 155 organic matter inputs and losses, inherent optical properties, sediment diagenesis, and 156 temperature (Penta et al. 2008, Eldridge and Roelke 2010, see appendix in Lehrter et al. in 157 review). A total of 108 equations are estimated at each time step to return a value for each of the 158 36 state variables described by the model. In addition to the initial conditions, 250 parameter 159 values for each of the equations is also supplied at model execution. These parameters define 160 relationships among fixed effects in the equations and represent ecological properties described 161 by the model that influence hypoxia formation. Values for each of the parameters were based on 162 estimates from the literature, field or laboratory-based measurements, or expert knowledge in absence of the former. As such, a sensitivity analysis of parameter values is warranted given that, 164 for example, literature or field-based estimates may not apply under all scenarios or expert 165 knowledge is not completely certain (Refsgaard et al. 2007). The sensitivity of O2 to 166 perturbations of all parameters for the 108 equations was estimated from January 1st to December 167 31st, 2006 by running FishTank at a timestep of five minutes. For simplicity, the parameters were grouped into one of six categories based on their respective equations: optics (n = 11169 parameters), organic matter (29), phytoplankton (156), temperature (32), and zooplankton (22). A 170 full description is available as an appendix in (Lehrter et al. in review). 171

#### 2.2 Local sensitivity analysis

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The analysis focused on sensitivity of  $O_2$  in the 0-D FishTank model to identify parameters that may affect spatial and temporal variation of hypoxia in the larger model. A local sensitivity analysis was performed for each of the 250 parameters using a simple perturbation approach to evaluate the change in  $O_2$  from the original parameter values. The analyses relied exlusively on concepts used in the FME package developed for the R statistical programming language (Soetaert and Petzoldt 2010). Each parameter was perturbed by 50% of its original value and the model was executed to obtain an estimate of the effect on  $O_2$ . For each perturbation, a sensitivity value S was estimated for each time step i given a set value for parameter j as:

$$S_{ij} = \frac{\partial y_i}{\partial \Theta_j} \cdot \frac{w_{\Theta_j}}{w_{y_i}} \tag{1}$$

where the estimate depended on the change in the predicted value for response variable y divided by the change in the parameter  $\Theta_j$  multiplied by the quotient of scaling factors w for each. The scaling factors,  $w_{\Theta_j}$  for the parameter  $\Theta_j$  and  $w_{y_i}$  for response variable  $y_i$ , were set as the default value of the unperturbed parameter and the predicted value of  $y_i$  after perturbation (Soetaert and Petzoldt 2010). The scaling ensures the estimates are unitless such that the relative magnitudes provide a comparison for model sensitivity to parameter changes that may vary in scale. Estimates for  $S_{ij}$  were summarized as L1 and L2 across the time series to obtain individual sensitivity values of  $O_2$  in response to a change in parameter j:

$$L1 = \sum |S_{ij}|/n \tag{2}$$

$$L2 = \sqrt{\sum \left(S_{ij}^2\right)/n} \tag{3}$$

In general, positive sensitivity estimates suggested a parameter had a positive effect on  $O_2$  for a given increase in the parameter, whereas the converse was true for negative sensitivity estimates. However, the effect of a parameter change may not be uniform over time such that  $S_{ij}$  can change in magnitude and sign depending on the temporal location. Time series of  $O_2$  estimates before and after perturbation were also evaluated to identify patterns not captured by the summary statistics. All parameters for each of the six equation categories (optics, organic matter, phytoplankton, temperature, and zooplankton) that had non-zero L1 or L2 were retained for identifiability analysis.

### 2.3 Identifiability and selecting parameter subsets

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Identifiability of parameter subsets was estimated from the minimum eigenvector of the cross-product of a selected sensitivity matrix (Brun et al. 2001, Omlin et al. 2001a):

$$\gamma = \frac{1}{\sqrt{\min\left(\text{EV}[\hat{S}^{\top}\hat{S}]\right)}} \tag{4}$$

where  $\gamma$  ranges from one to infinity for perfectly identifiable (orthogonal) or unidentifiable (perfectly collinear) results for parameters in a sensitivity matrix S. The sensitivity functions were supplied as a matrix  $\hat{S}$  with rows i and columns j (eq. (1)) that described deviations of predicted  $O_2$  from the default parameter values. The matrix  $\hat{S}$  was first normalized by dividing by

the square root of the summed residuals (Omlin et al. 2001a, Soetaert and Petzoldt 2010).

The collinearity index  $\gamma$  provides a measure of the linear dependence between sensitivity functions described above for subsets of parameters. Estimates of  $\gamma$  greater than 10-15 suggest parameter sets are poorly identifiable (Brun et al. 2001, Omlin et al. 2001a), meaning optimal values are inestimable given similar effects of the selected parameters on  $O_2$ . Greater sensitivity of a state variable to a subset of parameters does not always imply better identifiability if the individual effects are similar. An intuitive interpretation of  $\gamma$  is provided by Brun et al. (2001) such that a change in a state variable caused by a change in one parameter can be offset by the fraction  $1-1/\gamma$  by the remaining parameters. That is,  $\gamma=10$  suggests the relative change in  $O_2$  for a selected parameter can be compensated for by 90% with changes in the other parameters.

Initial analyses suggested that considerably limited subsets of parameters were identifiable of the 250 in the FishTank model. Given this limitation, parameter selection must consider the competing objectives of increased precision with parameter inclusion and reduced identifability as it relates to optimization. An additional challenge is the excessively high number of combinations of parameter sets, which complicates selection given sensitivity differences and desired ecological categories of each parameter. For example, Fig. 1 provides a simple graphic of the unique number of combinations that are possible for different subsets of 'complete' parameter sets of different sizes (i.e., based on n choose k combinations equal to n!/(k!(n-k)!)). The number of unique combinations increases with the total parameters in the set and is also maximized for moderate selections (e.g., selecting half the total). For example, over  $10^{14}$  combinations are possible by selecting 25 parameters from a set of 50. Accordingly, parameter selection is complicated by differing sensitivity, identifiability, and the difficulty of choosing from many combinations.

A set of heuristics was developed to balance the tradeoff in model complexity and identifiability given the challenges described above (see also Wagener et al. 2001a). These rulesets were developed with the assumption that parameters will be selected with preference for those with high sensitivity and identifability based on  $\gamma < 15$  as an acceptable threshold for subsets (e.g., 93% accountability). Selection heurestics also recognized that parameter categories (i.e., optics, organic matter, phytoplankton, temperature, zooplankton) may have unequal preferences given questions of interest. In all selection scenarios, parameters were selected by decreasing sensitivity starting with the most sensitive until identifiability did not exceed  $\gamma = 15$ 

where selections were 1) blocked within parameter category, 2) independent of parameter category, 3) or considering all categories equally. The selection rules produced seven subsets of parameters that could further be used to optimize model calibration for  $O_2$ .

The above analyses were repeated for additional state variables estimated by FishTank to provide further descriptions of ecological dynamics that are relevant for hypoxia. In addition to O<sub>2</sub>, other state variables included chlorophyll *a* (chl-*a*), photosynthetically active radiation (PAR), nitrate, ammonium, particulate organic matter, dissolved organic matter, and phosphorus.

Particulate and dissolved organic matter were estimated as the summation of the respective outputs for organic matter from phytoplankon (*OM1\_A*, *OM2\_A*), fecal pellets (*OM1\_fp*, *OM2\_fp*), river sources *OM1\_rp*, *OM2\_rp*), and boundary conditions (*OM1\_bc*, *OM2\_bc*, see Lehrter et al. in review).

#### 2.4 Identifiability and structural uncertainty

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As a final analysis, the effects of model structure on parameter identifiability were 247 evaluated for O<sub>2</sub> predictions. The FishTank model includes several processes that can be included or excluded from the equations based on expected conditions or available data. These 'switches' 249 are conceptually different from model parameters as they define the use of explicit equations or 250 processes that affect the model structure. As such, a comparison of sensitivity and identifiability 251 given different equations uses parameter uncertainty as a means to begin addressing 252 componenents of structural uncertainty. Switches in FishTank include different structural 253 equations for the vertical attenuation of light through the water column (inherent or apparent 254 optical properties, Penta et al. 2009, Eldridge and Roelke 2010) and chlorophyll to carbon ratio 255 models (fixed or dynamic given light and nutrients, Cloern et al. 1995). Several switches also 256 affect phytoplankton growth including different models for specific growth and effects of 257 temperature, light dependence, nutrient uptake, and internal cell quotas (Lehrter et al. in review, references therein). Parameter identifiability was evaluated using three scenarios of simple, 259 intermediate, and complex combinations of model switches. 260

#### 3 Results

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#### 3.1 Local sensitivity analysis

Local sensitivity analyses showed that O<sub>2</sub> was sensitive to perturbations in 140 of 250 263 parameters (56% of total) in FishTank (see Fig. S1 for other state variables). Within each 264 parameter category, O<sub>2</sub> was sensitive to four parameters for optics (36% of all optic parameters, 265 Table 1), seven for organic matter (24%, Table 2), 103 for phytoplankton (66%, Table 3), seven 266 for temperature (22%, Table 4), and 19 for zooplankton (86%, Table 5). Although O<sub>2</sub> had the 267 greatest sensitivity to parameters in the zooplankton category (as percentage of total), the relative 268 effects varied. Among all parameters, sensitivity values ranged from  $L1=3.18\times 10^{-6}$  for 269 Kcdom (optics) to 328.35 for  $Qc_{p1}$  (phytoplankton), whereas average sensitivity among all 270 parameters was L1 = 4.52. Within categories, sensitivity ranged from  $3.18 \times 10^{-6}$  (Kcdom) to 271 1.64 (astar490) for optics, 0.01 (KGcdom) to 2.11 (k11) for organic matter,  $1 \times 10^{-5}$  (Ksi<sub>p1</sub>) to 272  $328.35 (Qc_{p1})$  for phytopankton,  $0.12 (Tref(nospA + nospZ)_{p1})$  to  $2.9 (Tref(nospA + nospZ)_{p4})$  for 273 temperature, and 0 ( $ZQp_{z1}$ ) to 0.82 ( $ZKa_{z1}$ ) for zooplankton (Fig. 2, bottom). Average sensitivity 274 values in each category were L1 = 0.42 for optics, 1.24 for organic matter, 5.96 for 275 phytoplankton, 0.55 for temperature, and 0.27 for zooplankton. Within the six phytoplankton 276 groups, O<sub>2</sub> was sensitive to the same parameters within each group although the sensitivity 277 magnitudes varied. Average sensitivity across parameters in each phytoplankton groups showed 278 that  $O_2$  was most sensitive to the first and third phytoplankton groups (average L1 = 19.71, 279 14.56), whereas sensitivity to parameters in the remaining groups was much lower (all with 280 average L1 < 1). Sensitivity of  $O_2$  did not vary considerably between parameters in the two 281 zooplankton groups (average L1 = 0.31, 0.23 for groups one and two). 282 Response of O<sub>2</sub> to parameter perturbations was not uniform across the time series. Fig. 2 283 shows variation for the top parameters within each category. Because FishTank does not include a 284 spatial component, the estimated  $O_2$  trend describes a closed, heterotrophic system where 285 respiration processes eventually remove all O<sub>2</sub> from the model space. The initial decrease in the 286 time series reflects change from the initial conditions outside of the growing seasons (i.e., January, February), the spring/summer increase represents production associated with expected 288 seasonal growth, and the remaining time series from August to the end of year shows complete 289

removal of O<sub>2</sub> as respiration processes dominate metabolic activity. Although this time series is not a realistic depiction of an actual system, the biogeochemical model behaves as expected in the 291 absence of the hydrodynamic model. Accordingly, the interpretation of sensitivity results from 292 the simple model has relevance in an ecological context. As expected, parameter perturbations 293 had the largest effect during the summer months, although the effects varied. An inrease in 50% 294 from the parameter default values generally caused a reduction in O2 during the summer, with the exception of the zooplankton parameter,  $ZKa_{z1}$ , which caused an increase in  $O_2$ . The 296 phytoplankton parameter,  $Qc_{p1}$ , had the largest effect such that the  $O_2$  time series was similar to 297 the default output in April/May, whereas a dramatic decrease was observed in the remaining 298 months. The effects of perturbations early in the time series (January, February) showed similar 299 patterns such that a reduction in O2 was most common, particularly for the optics (astar490) and 300 phytoplankton ( $Qc_{p1}$ ) parameters. 301

#### 3.2 Subset identifiability

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The identifiability analyses suggested that most parameter subsets exceeded the thresholds 303 of  $\gamma = 10, 15$ , providing further justification for using selection heuristics for parameter 304 optimization. Parameter identifiability (as  $\gamma$ ) increased at different rates depending on the 305 parameter category or the number of top parameters that were selected (Fig. 3). By category, 306 identifiability was lowest for parameter subsets in the phytoplankton (7% less than  $\gamma = 15, 5.9\%$ 307 less than  $\gamma = 10$ ) and zooplankton categories (28.9%, less than  $\gamma = 15, 24.2\%$ , less than  $\gamma = 10$ ), whereas a majority of combinations for temperature were identifiable (83.3% less than  $\gamma = 15$ , 309 73.3%, less than  $\gamma = 10$ ). All subset combinations for optics and organic matter parameters had 310  $\gamma$  < 10. All parameter subsets for choosing the top, top two, and top three parameters in each 311 category were identifiable (Fig. 3), whereas a majority were identifiable for choosing the top four 312  $(77\% \text{ less than } \gamma = 15, 70.8\% \text{ less than } \gamma = 10)$  and top five  $(77\% \text{ less than } \gamma = 15, 70.8\%, \text{ less than } \gamma = 10)$ than  $\gamma = 10$ ) parameters. 314 A comparison of average and median identifiability by parameter category and top 315 parameters in each category suggested that individual parameters had large effects on  $\gamma$  (Fig. 3). 316 For example, a consistent increase in average  $\gamma$  from 2 to 7 parameters in a combination for 317 temperature was observed, whereas median identiability remained low until 6 parameter 318

combinations were evaluated. Further evaluation showed that identifiability was greatly affected

by the inclusion of one or two specific parameters in a subset combination. Fig. 4 shows the temperature collinearity  $(\gamma)$  ranges in detail for the parameter subsets in Fig. 3 before and after 321 excluding individual parameters. Collinearity increases with more parameters included in a 322 subset, although the increase varies depending on the specific parameter. Exclusion of the 323 parameters  $Tref(nospA + nospZ)_{p2}$  and  $Tref(nospA + nospZ)_{p5}$  showed that  $\gamma$  remained well below 324 the 10, 15 threshold for all parameter combinations. Morever, inclusion of  $Tref(nospA + nospZ)_{p1}$ ,  $Tref(nospA + nospZ)_{p4}$ ,  $Tref(nospA + nospZ)_{z1}$ , and  $Tref(nospA + nospZ)_{z2}$  generally reduced 326 collinearity relative to when the parameters were excluded. Similar analyses identified parameters 327 in other categories that had disproportionate effects on identifiability if included in a subset (see 328 supplementary information). 329

Comparison of identifiability between categories showed that phytoplankton and 330 zooplankton had the least identifiable parameter subsets. As noted above, FishTank includes six 331 phytoplankton and two zooplankton groups to characterize community structure and foodweb 332 dynamics that likely have an important role in hypoxia development. However, structural 333 equations for each group do not vary considerably such that variation in parameter values primarily control differences between the groups, e.g., large-bodied vs small-bodied plankton, 335 slow-growing vs. fast-growing plankton. To obtain identifiability estimates of the plankton 336 categories that were independent of groups, the identifiability analyses were re-evaluated using 337 only one phytoplankton and one zooplankton group (Fig. 5). Compared to all groups, evaluating a 338 single group improved identifiability such that a majority of parameter combinations were below 339 the threshold (56.3% less than  $\gamma = 15, 47.1\%$  less than  $\gamma = 10$  for Phytoplankton; 83.4%, less 340 than  $\gamma=15,72.6\%$ , less than  $\gamma=10$  for zooplankton). Analysis of identifiability for top 341 parameters in all categories did not show similar changes in identifiability. Although all 342 combinations for the top one, two, and three parameters in each category were still well below the threshold, selecting the top four and five parameters showed an increase (84.2% less than  $\gamma = 15$ , 78.7% less than  $\gamma = 10$ ) and a decrease (54.4% less than  $\gamma = 15$ , 51% less than  $\gamma = 10$ ) in identifiability, respectively (Fig. 5), compared to results that included all phytoplankton and 346 zooplankton groups (Fig. 3).

#### 3.3 Parameter selection

Each of the three selection heuristics (blocked by parameter category, independent of 349 category, all categories equally) for O2 differed in the number of selected parameters and 350 distribution of parameters within each category (if applicable, Fig. 6 and Table 6). For the first 35 selection heuristic, all sensitive parameters from the optics ( $n=4,\,\gamma=3.7$ ) and organic matter 352  $(n=7,\gamma=1.7)$  categories were selected, whereas 23 were selected for phytoplankton ( $\gamma=$ 353 13.7), five for temperature (  $\gamma=11.4$  ), and five for zooplankton (  $\gamma=3.1$  ). For the second 354 selection heuristic, 20 parameters were selected ( $\gamma=4.6$ , with a majority from the phytoplankton 355 category, Table 6). For the third heuristic, 18 parameters were selected ( $\gamma=9.2$ ) with equal 356 representation between categories. For the second and third selection heuristics, an individual 357 parameter caused a disproportianate increase in  $\gamma$  that forced the selection to stop. Selection 358 independent of category showed that including KNO3 caused in increase in  $\gamma$  from 4.6 to 15.6 and 359 equal selection within cateogies showed that including  $Tref(nospA + nospZ)_{p2}$  caused in increase in 360  $\gamma$  from 9.2 to 66.2. Finally, parameter selection for other state variables (chl-a, PAR, nitrate, ammonium, particulate organic matter, dissolved organic matter, phosphorus) also showed that a 362 limited number of parameters were identifiable (for brevity, only results using the second set of 363 selection heuristics are shown, Fig. 7 and Table 7). Less than ten parameters were selected for 364 each of the remaining state variables with most selected from the phytoplankton category. 365 Interestingly, no parameters from the temperature category were selected.

#### 4 Discussion

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We showed only small subsets are identifiable, similar conclusions have been described by citations in (Wagener et al. 2001a), p. 14 for models that follow traditional calibration schemes (e.g., objective function minimization).

Emphasize that parameters that have the greatest effect on collinearity are not those that have the highest sensitivity (contrast the identifiability by category vs identifiability by top parameters), also note that groups of parameters together can have large effects on collinearity, maybe some kind of bootstrap analysis could be done looking at doubletons, etc. The example in teh results highlights how redundant variables can be identified as a necessary part of the model calibration process.

Why did identifiability decrease for top five parameters in each category after removing redundant phyto/zoop groups?

(Denman 2003) describes over-parameterization for multiple phyto groups, use this to emphasize collinearity issues with the phyto groups despite differing sensitivity values between groups

Identifiability by category - varies with number of parameters in the category but some were more redundant than others (phytoplankton).

Questions specific to GOM - what initial conditions are important? How many phytoplankton groups do we need (e.g., related to structural uncertainty)?

How does the assimilation of additional parameters (e.g., other state variables) during calibration influence the conclusions? Wagener et al. (2001a) describes this as a potential approach to improving model performance by improving the availability of information for model calibration (p. 14).

How does uncertainty translate to what a model should provide (generality v precision)? The first step - find out what can be optimized but then do not overfit....

What about structural uncertainty - does sensitivity of a model to variation in a parameter imply parameter uncertainty and/or structural uncertainty?

A final point about optimization with identifiable parameter sets - optimization to fit the data still does not ensure a correct model. Failing in one way can be over-compensated by another feature, e.g., the parameter set that is optimized (see Flynn (2005), p. 1207, third paragraph), also (Durand et al. 2002, Arhonditsis et al. 2008), also note that over-parameterized models are not necessarily bad, see (Omlin et al. 2001a), models must be validated for the uses which they were intended where a comparison of observed and predicted is the simplest approach and other methods should be used depending on analysis needs (Jr. 1996)

Omlin et al. (2001a) state that the sensitivity, identifiability, estimation process is iterative (p. 113), need to rinse and repeat for proper calibration.

How to improve identifiability - get more/better observed data, include obs from other state variables in RSS minimization (eqn q in Omlin et al. (2001a))

Alternative methods for uncertainty analysis - bayesian, MCMC, nonlinear calibration-constrained optimization (Gallagher and Doherty 2007), (Arhonditsis et al. 2008)

Our heuristic products are partially analogous to the Rainfall-Runoff Modelling Toolbox (RRMT) presented by (Wagener et al. 2001b)2001 (cited on page 15, in Wagener et al. 2001a), although ours is simple in comparison

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Table 1: Sensitivities of  $O_2$  to perturbation of optics parameters. Sensitivities are based on a 50% increase from the default parameter value, where L1 and L2 summarize differences in model output from the default (see eqs. (2) and (3)). Parameters that did not affect  $O_2$  are not shown.

Description	Parameter	Value	L1	L2
Chla specific absorption at 490 nm	astar490	0.04	1.64	8.64
OMA specific absorption at 490 nm	astarOMA	0.1	0.02	0.1
OMZ specific absorption at 490 nm	astarOMZ	0.1	0.01	0.01
AOP, light attenuation due to CDOM	Kcdom	0	$3.18\times10^{-6}$	$1.09 \times 10^{-5}$

Table 2: Sensitivities of  $O_2$  to perturbation of organic matter parameters. Sensitivities are based on a 50% increase from the default parameter value, where L1 and L2 summarize differences in model output from the default (see eqs. (2) and (3)). Parameters that did not affect  $O_2$  are not shown.

Description	Parameter	Value	L1	L2
rate constant for nitrification	k11	5	2.11	16.1
O2 concentration that inhibits denitrification	KstarO2	10	1.91	11.76
turnover rate for OM1A and OM1G	KG1	50	1.49	6.83
turnover rate for OM2A and OM2G	KG2	50	1.37	3.46
half-saturation concentration for NO3 used in denitrification	KNO3	10	1.24	7.98
half-saturation concentration for O2 utilization	KO2	10	0.56	1.92
decay rate of CDOM, 1/day	KGcdom	0.01	0.01	0.03

Table 3: Sensitivities of  $O_2$  to perturbation of phytoplankton parameters. Sensitivities are based on a 50% increase from the default parameter value, where L1 and L2 summarize differences in model output from the default (see eqs. (2) and (3)). Parameters that did not affect  $O_2$  are not shown. Subscripts show the phytoplankton or zooplankton group that applies for the parameter. Parameters less than the 75<sup>th</sup> percentile (0.59) for L1 were removed for brevity.

Description, Parameter	Value	L1	L2
coefficient for non-limiting nutrient			
$aN_{p1}$	1	2.7	47.26
$aN_{p3}$	1	0.66	3.16
half-saturation constant for n			
$Kn_{p3}$	5.93	1.15	9.22
$Kn_{p4}$	1.13	0.62	2.5
initial slope of the photosynthesis-irradiance relationship			
$alpha_{p4}$	$3.96 \times 10^{-16}$	1.61	7.46
$alpha_{p3}$	$6.19 \times 10^{-17}$	1.06	3.74
$alpha_{p5}$	$3.87 \times 10^{-16}$	0.81	5.54
minimum n cell-quota			
$QminN_{p3}$	$1.27 \times 10^{-8}$	1.53	6.4
$QminN_{p4}$	$1.53 \times 10^{-10}$	0.91	2.76
$QminN_{p1}$	$6.08 \times 10^{-9}$	0.62	4.55
mortality coefficient			
$mA_{p3}$	0.03	2.98	14.34
$mA_{p4}$	0.11	1.35	7.04
n-uptake rate measured at umax			
$vmaxN_{p5}$	$1.4 \times 10^{-9}$	7.57	43.9
$vmaxN_{p4}$	$1.33 \times 10^{-9}$	2.88	16.56
$vmaxN_{p3}$	$8.11 \times 10^{-8}$	1.99	15.23
$vmaxN_{p1}$	$4.1 \times 10^{-8}$	0.84	2.92
p-uptake rate measured at umax			
$vmaxP_{p3}$	$6.15 \times 10^{-8}$	2.23	9.89
$\underline{\hspace{1cm}}$ $vmaxP_{p1}$	$2.68 \times 10^{-8}$	0.74	11.41
phytoplankton basal respiration coefficient			
$\mathit{respb}_{p4}$	0.02	3.1	26.48
$\mathit{respb}_{p3}$	0.02	2.15	6.35
$\_\mathit{respb}_{p5}$	0.02	0.81	8.61
phytoplankton carbon/cell			
$\mathcal{Q}c_{p1}$	$1.35 \times 10^{-6}$	328.35	2181.05
$\mathcal{Q}c_{p3}$	$2.65 \times 10^{-6}$	232.8	1574.72
$\mathcal{Q}c_{p2}$	$1.68 \times 10^{-7}$	4.08	61.25
$Qc_{p4}$	$4.54 \times 10^{-8}$	1.03	3.75
phytoplankton growth respiration coefficient			
$respg_{p4}$	0.1	0.98	7.37

Table 4: Sensitivities of  $O_2$  to perturbation of temperature parameters. Sensitivities are based on a 50% increase from the default parameter value, where L1 and L2 summarize differences in model output from the default (see eqs. (2) and (3)). Parameters that did not affect  $O_2$  are not shown. Subscripts show the phytoplankton or zooplankton group that applies for the parameter.

Description, Parameter	Value	L1	L2
optimum temperature for growth(c)			
$Tref(nospA+nospZ)_{p4}$	17	2.9	22.95
$Tref(nospA + nospZ)_{z2}$	26	0.18	2.59
$Tref(nospA+nospZ)_{p5}$	26	0.17	0.72
$Tref(nospA + nospZ)_{p2}$	22	0.16	0.82
$Tref(nospA + nospZ)_{z1}$	22	0.16	0.33
$Tref(nospA+nospZ)_{p3}$	17	0.14	0.78
$Tref(nospA + nospZ)_{p1}$	22	0.12	0.29

Table 5: Sensitivities of  $O_2$  to perturbation of zooplankton parameters. Sensitivities are based on a 50% increase from the default parameter value, where L1 and L2 summarize differences in model output from the default (see eqs. (2) and (3)). Parameters that did not affect  $O_2$  are not shown. Subscripts show the phytoplankton or zooplankton group that applies for the parameter.

Description, Parameter	Value	L1	L2
assimilation efficiency as a fraction of ingestion			
$Zeffic_{z1}$	0.4	0.23	0.55
$Zeffic_{z2}$	0.4	0.21	0.75
half saturation coefficient for grazing			
$Z K a_{z1}$	$1.12\times10^{12}$	0.82	6.29
$Z K a_{z2}$	$1.12 \times 10^{12}$	0.46	3.24
maximum growth rate of zooplankton			
$Zumax_{z2}$	$2.98 \times 10^{7}$	0.48	1.84
$Zumax_{z1}$	$9.45 \times 10^{8}$	0.46	0.91
proportion of grazed phytoplankton lost to sloppy feeding			
$Zslop_{z1}$	0.25	0.12	0.33
zooplankton biomass-dependent respiration factor			
$Zrespb_{z1}$	0.1	0.45	3.02
$Zrespb_{z2}$	0.42	0.09	1.05
zooplankton carbon/individual			
$ZQc_{z2}$	$7.08 \times 10^{-7}$	0.1	0.36
$ZQc_{z1}$	$3.13 \times 10^{-4}$	0.06	0.62
zooplankton growth-dependent respiration factor			
$Zrespg_{z1}$	0.2	0.24	3.19
$Zrespg_{z2}$	0.3	0.12	0.31
zooplankton mortality constant for quadratic mortality			
$Zm_{z2}$	$7.2 \times 10^{-4}$	0.33	2.85
$Zm_{z1}$	$7.2 \times 10^{-4}$	0.26	0.8
zooplankton nitrogen/individual			
$ZQn_{z1}$	$6.95 \times 10^{-5}$	0.47	1.64
$ZQn_{z2}$	$1.57 \times 10^{-7}$	0.24	1.35
zooplankton phosphorus/individual			
$ZQp_{z2}$	$8.53 \times 10^{-9}$	0.01	0.01
$ZQp_{z1}$	$3.77 \times 10^{-6}$	0	0

Table 6: Parameter identifiability for dissolved oxygen. Selection followed the second heuristic where parameters were selected by decreasing sensitivity up to maximum  $\gamma < 15$ . Rank describes the parameter sensitivity in each category (O: optics, OM: organic matter, P: phytoplankton, T: temperature, Z: zooplankton).

Parameter description	Parameter	Rank	L1	$\gamma$
phytoplankton carbon/cell	$Qc_{p1}$	1 <sup>P</sup>	328.35	1
phytoplankton carbon/cell	$Qc_{p3}$	$2^{\mathbf{P}}$	232.8	1
N-uptake rate measured at umax	$vmaxN_{p5}$	$3^{P}$	7.57	1
phytoplankton carbon/cell	$Qc_{p2}$	$4^{P}$	4.08	1
phytoplankton basal respiration coefficient	$respb_{p4}$	$5^{P}$	3.1	1
mortality coefficient	$mA_{p3}$	$6^{P}$	2.98	1.01
Tref(nospA+nospZ): Optimum temperature for growth(C)	$Tref(nospA + nospZ)_{p4}$	$1^{\mathrm{T}}$	2.9	1.02
N-uptake rate measured at umax	$vmaxN_{p4}$	$7^{\mathrm{P}}$	2.88	1.04
coefficient for non-limiting nutrient	$aN_{p1}$	$8^{P}$	2.7	1.05
P-uptake rate measured at umax	$vmaxP_{p3}$	$9^{P}$	2.23	1.07
phytoplankton basal respiration coefficient	$respb_{p3}$	$10^{P}$	2.15	1.73
rate constant for nitrification	k11	$1^{\text{OM}}$	2.11	1.73
N-uptake rate measured at umax	$vmaxN_{p3}$	11 <sup>P</sup>	1.99	1.73
O2 concentration that inhibits denitrification	KstarO2	$2^{\text{OM}}$	1.91	1.73
Chla specific absorption at 490 nm	astar490	$1^{\rm O}$	1.64	1.77
initial slope of the photosynthesis-irradiance relationship	$alpha_{p4}$	$12^{P}$	1.61	4.1
minimum N cell-quota	$QminN_{p3}$	$13^{P}$	1.53	4.1
turnover rate for OM1A and OM1G	KG1	$3^{\text{OM}}$	1.49	4.2
turnover rate for OM2A and OM2G	KG2	$4^{\text{OM}}$	1.37	4.62
mortality coefficient	$mA_{p4}$	$14^{\mathbf{P}}$	1.35	4.62

Table 7: Parameter identifiability for ammonium, chlorophyll, irradiance, nitrate, OM1, OM2, and phosphate. Selection followed the second heuristic where parameters were selected by decreasing sensitivity up to maximum  $\gamma < 15$ . Rank describes the parameter sensitivity in each category (O: optics, OM: organic matter, P: phytoplankton, T: temperature, Z: zooplankton).

State variable, parameter description	Parameter	Rank	L1	$\gamma$
Ammonium				
phytoplankton carbon/cell	$Qc_{p3}$	$1^{P}$	2.38	1
phytoplankton carbon/cell	$Qc_{p1}$	$2^{P}$	2.23	3.1
rate constant for nitrification	k11	$1^{\text{OM}}$	0.68	3.1
O2 concentration that inhibits denitrification	KstarO2	$2^{OM}$	0.46	3.12
turnover rate for OM2A and OM2G	KG2	$3^{\text{OM}}$	0.39	6.53
initial slope of the photosynthesis-irradiance relationship	$alpha_{p4}$	$3^{P}$	0.35	7.18
N-uptake rate measured at umax	$vmaxN_{p4}$	$4^{P}$	0.35	7.26
N-uptake rate measured at umax	$vmaxN_{p3}$	$5^{P}$	0.34	13.14
Chlorophyll				
phytoplankton carbon/cell	$Qc_{p3}$	$1^{\mathbf{P}}$	104.26	1
phytoplankton carbon/cell	$Qc_{p1}$	$2^{P}$	47.86	3.65
mortality coefficient	$mA_{p3}$	$3^{P}$	1.71	4.07
O2 concentration that inhibits denitrification	KstarO2	$1^{\text{OM}}$	1.29	5.58
Irradiance				
phytoplankton carbon/cell	$Qc_{p3}$	$1^{P}$	0.32	1
phytoplankton carbon/cell	$Qc_{p1}$	$2^{P}$	0.25	4.87
initial slope of the photosynthesis-irradiance relationship	$alpha_{p3}$	$3^{P}$	0.19	5.38
mortality coefficient	$mA_{p3}$	$4^{P}$	0.17	7.61
Chla specific absorption at 490 nm	astar490	1 <sup>O</sup>	0.15	13.34
phytoplankton basal respiration coefficient	$respb_{p3}$	$5^{P}$	0.11	13.5
O2 concentration that inhibits denitrification	KstarO2	1 <sup>OM</sup>	0.08	14.64
Nitrate	115141 02	-	0.00	11.01
phytoplankton carbon/cell	$Qc_{p3}$	1 <sup>P</sup>	$1.07\times10^{38}$	1
phytoplankton carbon/cell	$Qc_{p3}$ $Qc_{p1}$	$2^{P}$	$1.44 \times 10^{23}$	1
turnover rate for OM1A and OM1G	KG1	1 <sup>OM</sup>	$2 \times 10^5$	10.55
OM1	KOI		2 / 10	10.00
phytoplankton carbon/cell	$Qc_{p3}$	$1.5^{P}$	1.13	1
mortality coefficient	$mA_{p4}$	$1.5^{P}$	0.78	1.68
phytoplankton carbon/cell	-	$3^{P}$	0.76	8.66
turnover rate for OM1A and OM1G	$Qc_{p1}$ $KGI$	1 <sup>OM</sup>	0.71	8.98
initial slope of the photosynthesis-irradiance relationship	$alpha_{p4}$	$4^{P}$	0.48	9.22
Chla specific absorption at 490 nm	astar490	1 <sup>O</sup>	0.43	9.22
OM2	usia1490	1	0.40	3.22
turnover rate for OM2A and OM2G	KG2	1 <sup>OM</sup>	1.3	1
		1 <sup>P</sup>	0.94	$\frac{1}{2.01}$
phytoplankton carbon/cell	$Qc_{p3}$	$2^{P}$		
phytoplankton carbon/cell	$Qc_{p1}$	$3^{P}$	0.74	7.65
initial slope of the photosynthesis-irradiance relationship	alpha <sub>p4</sub>	3° 2 <sup>OM</sup>	0.35	11 20
O2 concentration that inhibits denitrification	KstarO2	4 <sup>P</sup>	0.34	11.29
initial slope of the photosynthesis-irradiance relationship	$alpha_{p3}$	1 <sup>O</sup>	0.31	11.44
Chla specific absorption at 490 nm	astar490	1 <sup>Z</sup>	0.29	11.54
maximum growth rate of zooplankton	$Zumax_{z1}$	1~	0.29	11.66
Phosphate		4 D	2.02	
Phosphate initial slope of the photosynthesis-irradiance relationship	$alpha_{p3}$	1 <sup>P</sup>	2.92	1
Phosphate initial slope of the photosynthesis-irradiance relationship P-uptake rate measured at umax	$alpha_{p3}$ $vmaxP_{p3}$	$2^{P}$	1.57	2.23
Phosphate initial slope of the photosynthesis-irradiance relationship	$alpha_{p3}$			



Fig. 1: Examples of unique parameter combinations from different parameter sets and number of selected parameters. The number of combinations are shown for increasing numbers of selected parameters from the total in the set, where 50 parameter sets are shown each with one through 50 total parameters. Note that the number of unique combinations is shown as the natural-log.

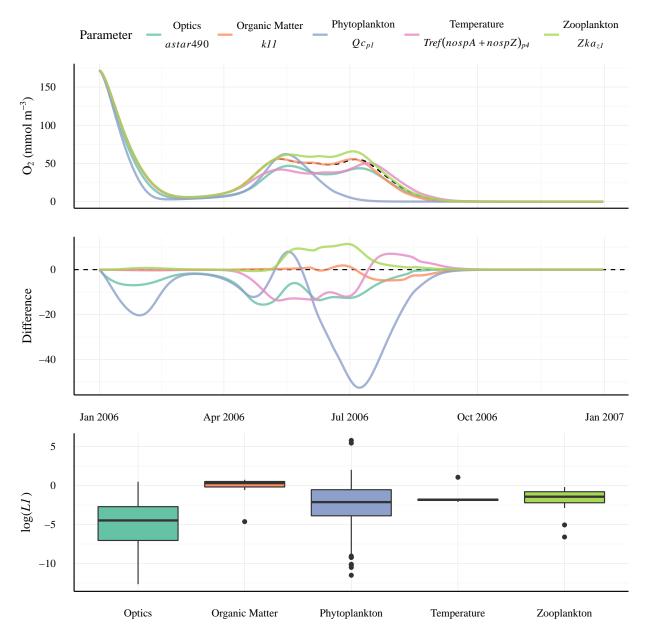


Fig. 2: Sensitivity of  $O_2$  to parameter changes. The solid lines show the change in  $O_2$  based on a 50% change from the default parameter values (dashed line) for each parameter. Individual parameters with the largest effect are shown for each category. The top plot shows the model output and the middle plot shows the estimated  $O_2$  as a difference from the default. The bottom plot shows the distribution of error values (as log(L1)) for all parameters in each category.

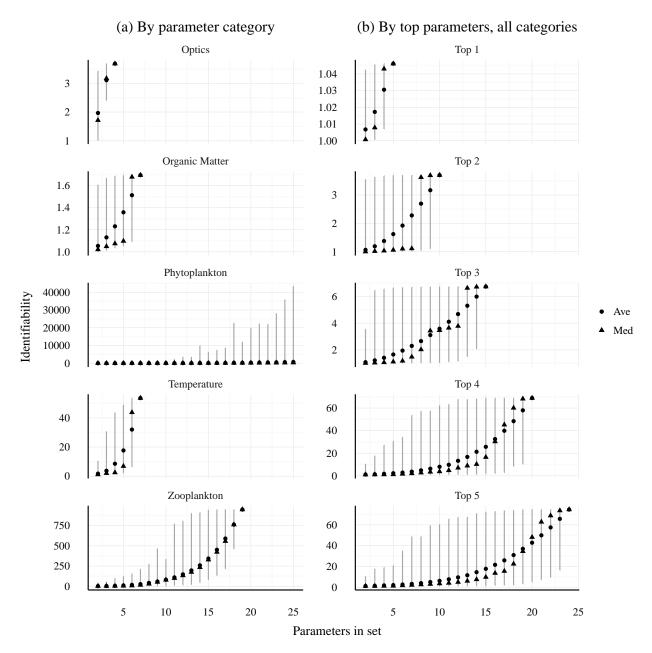


Fig. 3: Identifiability (as  $\gamma$ , eq. (4)) of parameter subsets for  $O_2$ . Plots in (a) show identifiability by parameter categories and (b) shows identifiability by selecting the top 1 through 5 parameters regardless of category. Lines represent identifiability ranges for the possible combinations given the number of parameters in the set. The phytoplankton category is limited to 25 total parameters.

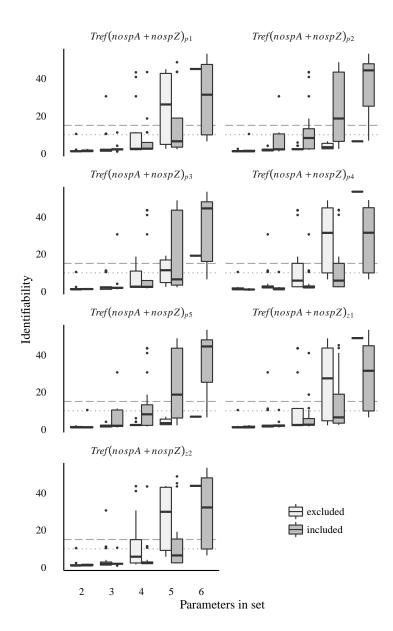


Fig. 4: Identifiability (as  $\gamma$ , eq. (4)) of temperature parameters for subset combinations in Fig. 3. Identifiability is evaluated for subsets that excluded and included the parameters at the top of each plot. Identifiability of including all seven parameters is in Fig. 3. Grey lines indicate potential thresholds at  $\gamma=10,15$  for maximum acceptable identifiability.

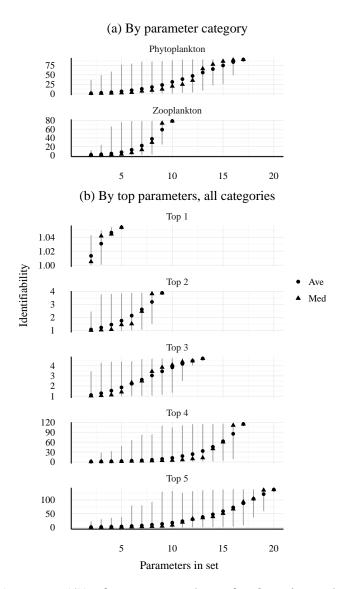


Fig. 5: Identifiability (as  $\gamma$ , eq. (4)) of parameter subsets for  $O_2$  using only subsets from the first phytoplankon group and first zooplankton group. Plots in (a) show identifiability for only the phytoplankton and zooplankton categories and (b) shows identifiability by selecting the top 1 through 5 parameters regardless of category. Lines represent identifiability ranges for the possible combinations given the number of parameters in the set.

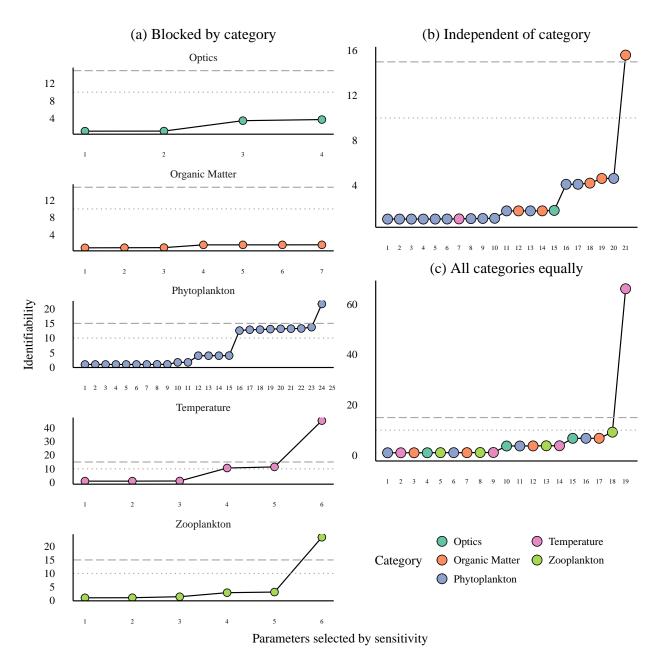


Fig. 6: Identifiability (as  $\gamma$ , eq. (4)) of selecting parameters with three different heuristics. Parameters are selected by decreasing sensitivity for all examples (Tables 1 to 5). The parameter selections are blocked within each category (a), independent of category (b), or considering all categories equally (c). Grey lines indicate potential thresholds at  $\gamma=10,15$  for maximum acceptable identifiability. Selection stops after  $\gamma>15$  or if the maximum number of possible parameters is selected. See Table 6 for values in (b).

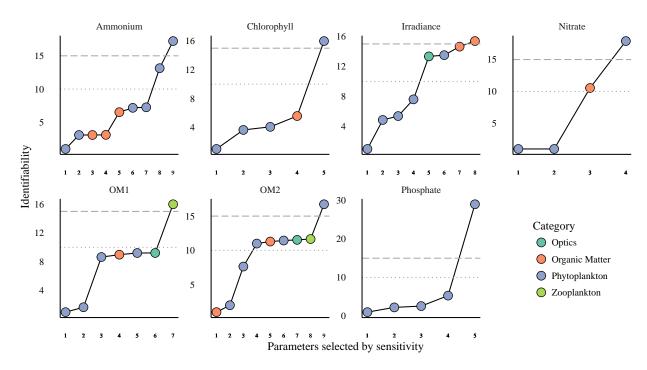


Fig. 7: Identifiability (as  $\gamma$ , eq. (4)) of selecting parameters for selected state variables. Parameters are selected by decreasing sensitivity indepent of parameter categories. Grey lines indicate potential thresholds at  $\gamma=10,15$  for maximum acceptable identifiability. Selection stops after  $\gamma>15$ . See Table 7 for values.

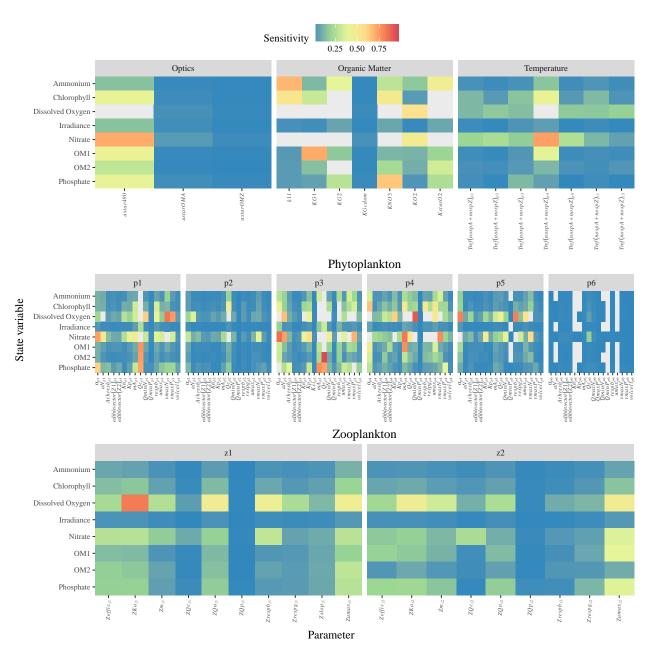


Fig. S1: Sensitivity values (L1, eq. (2)) for local analyses of all state variables. Values are truncated by the 5<sup>th</sup> and 95<sup>th</sup> sensitivity values between all parameters for visual appearance. Parameters are grouped by category (plot strips). Phytoplankton and zooplankton categories are further separated into one through six, and one and two groups (p1-p6, z1, z2), respectively.