

Vectors

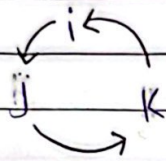
$$\vec{V} = |\vec{V}| \cdot \hat{V}$$

$$\vec{A} \cdot \vec{B} = AB \cos \theta \quad \text{or} \quad \vec{A} \cdot \vec{B}_n$$

$$\vec{A} \times \vec{B} = AB \sin \theta \quad \text{or} \quad \vec{A} B_y$$

$$\hat{i} \cdot \hat{i} = \hat{j} \cdot \hat{j} = \hat{k} \cdot \hat{k} = 1$$

$$\hat{i} \cdot \hat{j} = \hat{j} \cdot \hat{k} = \hat{k} \cdot \hat{i} = 0$$



$$\hat{i} \times \hat{j} = \hat{k} \quad \hat{j} \times \hat{k} = \hat{i} \quad \hat{k} \times \hat{i} = \hat{j}$$

$$\vec{A} \times \vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ A_x & A_y & A_z \\ B_x & B_y & B_z \end{vmatrix}$$

$$a \cdot b = b \cdot a$$

$$a \times b = -(b \times a)$$

Motion in 1-D

$$V_f = V_i + at$$

$$S = V_i t + \frac{1}{2} at^2$$

$$2aS = V_f^2 - V_i^2$$

$$V_{avg} = \frac{x_f - x_i}{\Delta t}$$

$$V_{ins} = \lim_{\Delta t \rightarrow 0} \frac{dx}{dt}$$

$$\Delta x = x_f(t_f) - x_i(t_i)$$

Motion in 2D

$$V_x = V_0 \cos \theta$$

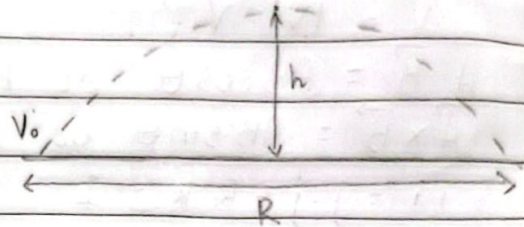
$$V_y = V_0 \sin \theta$$

$$t = \frac{V_0 \sin \theta}{g}$$

$$R = \frac{V_0^2 \sin 2\theta}{g}$$

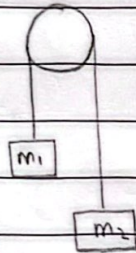
$$h = \frac{V_0^2 \sin^2 \theta}{2g}$$

$$h = \frac{1}{2} g t^2 \text{ (for free falling bodies)}$$

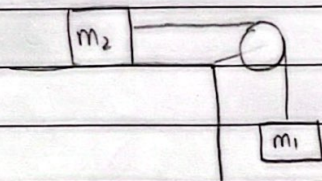


time taken = t

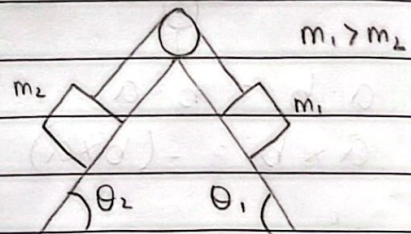
Newton Laws of motion:-



$$\bar{T} = \frac{2m_1 m_2 g}{m_1 + m_2} \quad a = \frac{(m_1 - m_2)g}{m_1 + m_2}$$



$$\bar{T} = \frac{m_1 m_2 g}{m_1 + m_2} \quad a = \frac{m_1 g}{m_1 + m_2}$$

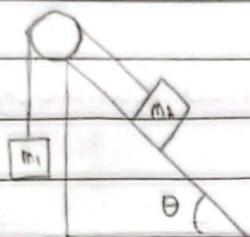


let

$$\theta_1 = \theta_2 = \theta$$

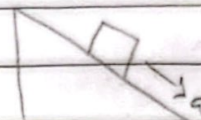
$$T = \frac{2m_1 m_2 g \sin \theta}{m_1 + m_2}$$

$$a = \frac{(m_1 - m_2)g \sin \theta}{m_1 + m_2}$$



$$F = kx$$

$$f_{\text{friction}} = \mu F$$



$$a = \frac{m_2 g \sin \theta - m_1 g}{m_1 + m_2}$$

$$T = \frac{m_1 m_2 g (\sin \theta + 1)}{m_1 + m_2}$$

$$a = g \sin \theta$$

Simple harmonic motion

$$- x = x_m \cos(\omega t + \phi)$$

$$- V = -V_m \sin(\omega t + \phi)$$

$$- V = \omega x_m$$

$$- a = \omega^2 x_m$$

$$- \omega = 2\pi f$$

$$- \omega = \sqrt{\frac{k}{m}}$$

$$- F = kx$$

$$- K.E = \frac{1}{2} m v^2$$

$$- T = 2\pi \sqrt{\frac{m}{k}}$$

$$- \omega = \sqrt{\frac{k}{m} - \left(\frac{b}{2m}\right)^2}$$

$$- \text{Damp factor} = \frac{b}{2m}$$

$$- P.E = \frac{1}{2} k x^2$$

$$- E = K.E + P.E \text{ or } \frac{1}{2} k x_m^2$$

$$x = x_m e^{-\frac{bt}{2m}} \cos(\omega t + \phi)$$

Waves

$$y(x, t) = y_m \sin(kx - \omega t)$$

$$k = \frac{2\pi}{\lambda}$$

$$\omega = \frac{2\pi}{t}$$

$$v = \sqrt{\frac{T}{\mu}} \rightarrow \begin{matrix} T \rightarrow \text{Tension} \\ \mu \rightarrow \text{linear density} \end{matrix}$$

$$\mu = \frac{m}{L}$$

$$v = f \lambda$$

$$v = A \omega \text{ or } x_m \omega$$

$$v = \frac{\omega}{k}$$

| | |
|---|---|
| Electrostatics | Cylindrical Capacitor |
| $Q = nE$ | $C = \frac{L}{2K_e \ln(b/a)}$ |
| $F = \frac{Kq_1q_2}{r^2}$ | |
| $K = \frac{1}{4\pi\epsilon_0}$ | Spherical Capacitor |
| $E = \frac{F}{q}$ | $C = \frac{ab}{K_e(b-a)}$ |
| Capacitors | Parallel capacitors |
| $q = CV$ | $C = C_1 + C_2 + \dots + C_n$ |
| $V = \frac{E_p}{q}$ | $V = \text{constant}$ |
| | Series Capacitors |
| $W = -\Delta V q$ | $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2} + \dots + \frac{1}{C_n}$ |
| $C = \frac{\epsilon_0 A}{d}$ (without dielectric) | $V = V_1 + V_2 + \dots + V_n$ |
| $C = \frac{K\epsilon_0 A}{d}$ (with dielectric) | $q = \text{constant}$ |
| $U_e = \frac{1}{2} \epsilon_0 E^2$ (Energy stored in capacitor) | $I = \frac{V}{L}$ |
| $E = \frac{V}{d}$ | $R = \frac{\rho L}{A}$ |
| $E = \frac{\sigma}{\epsilon_0}$ | $I = nAqV_d$ |
| $\sigma = \frac{q}{A}$ | $V = IR$ $P = \text{power}$ |
| $E = \frac{\sigma}{3\epsilon_0}$ | $P = IV$ |
| | $P = I^2 R$ |
| | $P = \frac{V^2}{R}$ |

Gauss's Law and electric field -

$$\Phi = \vec{E} \cdot \vec{\Delta A}$$

$$\Phi = E \Delta A \cos \theta$$

\vec{A} = surface area

Φ = flux

$$\Phi_{\text{net}} = \frac{Q}{\epsilon_0}$$

Q = charge enclosed in a surface

$$V = \frac{W}{q}$$

$$E = \frac{\sigma}{2\epsilon_0} \quad \left(\text{electric field produced by infinite charge sheet} \right)$$

$$E = \frac{\sigma}{\epsilon_0} \quad \left(\text{electric field between two oppositely charged sheets} \right)$$

$$E = 0 \quad \left(\text{inside the sphere} \right)$$

$$E = \frac{KQ}{r^2} \quad \left(\text{outside the sphere} \right)$$

$$E = \frac{\sigma}{\epsilon_0} \quad \left(\text{at surface of sphere} \right)$$

Electric current and resistance

$$I = \frac{Q}{\Delta t}$$

$$J = \frac{E}{J}$$

$\sigma = \text{conductivity}$

$$I = n A q V_d$$

$$\sigma = \frac{1}{\rho}$$

$$\frac{Q}{\Delta t} = n A q V_d$$

$$J = \sigma E$$

$$V = EL$$

$$J = \frac{I}{A} = n q V_d$$

$$J = \frac{\sigma V}{L}$$

$J = \text{current density}$

$$V = \frac{J L}{\sigma}$$

$$V = IR$$

$$\therefore J = \frac{I}{A}$$

$$R = \frac{\rho L}{A}$$

$$V = \frac{L}{A \sigma} \cdot I$$

$$\therefore V = IR$$

$$P_T = P_0 [1 + \alpha (T - T_0)]$$

$$IR = \frac{L}{A \sigma} \cdot I$$

(Relation of resistance and temperature -)

$$R = \frac{\rho L}{A}$$

$$R_T = R_0 [1 + \alpha (T - T_0)]$$

$$P = IV$$

$$P = I^2 R$$

$$P = \frac{V^2}{R}$$

Magnetic field

force on charge

$$B = \frac{\mu_0 I}{2\pi r}$$

$$F = qvB \sin \theta$$

Solenoid

$$r = \frac{mv}{qB}$$

$$\vec{B} = \mu_0 n I \quad n = \frac{N}{L}$$

$n = \text{turn density}$

$$v = r\omega$$

Toroid

$\omega = \text{angular velocity}$

$$\vec{B} = \frac{\mu_0 NI}{2\pi r}$$

$$\omega = \frac{v}{r} = \frac{v \cdot q \cdot B}{mv}$$

$$r = \frac{r_i + r_o}{2}$$

$$\omega = \frac{qB}{m}$$

$$T = \frac{2\pi r}{v} = \frac{2\pi r}{r\omega} = \frac{2\pi}{\omega} = \frac{2\pi m}{qB}$$

lorentz force

$$\vec{F}_{\text{Net}} = \vec{F}_m + \vec{F}_e$$

$$= q(\vec{v} \times \vec{B}) + q\vec{E}$$

$$\frac{q}{m} = \frac{v}{B r}$$

$$qE = qvB$$

$$E = vB$$

$$v = \frac{E}{B}$$

$$q \cancel{v} B_0 = \frac{mv \cancel{v}}{r}$$

$$\frac{q}{m} = \frac{v}{B_0 r}$$

$$\frac{m}{q} = \frac{\gamma B_0}{v} = \frac{\gamma B_0 \cdot B}{E}$$

$$\boxed{\frac{m}{q} = \frac{\gamma B_0 B}{E}}$$

Hall effect:-

$$qV_d B = qE_H$$

$$E_H = V_d B$$

$$\Delta V_H = E_H L$$

$$\Delta V_H = V_d B L$$

$$\boxed{I = n A q V_d}$$

$$\Delta V_H = \frac{I B L}{n A q}$$

$$A = \text{length} \times \text{width} = L \times w$$

$$\Delta V_H = \frac{I B}{n w q}$$

$$R_H = \frac{1}{n q} = \text{Hall coefficient}$$

$$\boxed{\Delta V_H = \frac{R_H I B}{w}}$$

Force on wire carrying current-

$$F = B I L \sin \theta$$