Two Sided Limit

Question: Find the limits.

6.
$$\lim_{x\to 0} \frac{6x-9}{x^3-12x+3}$$

Answer:

this limit is
$$(6 \cdot 0 - 9)/(0^3 - 12 \cdot 0 + 3) = -3$$
.

Question: Find the limits.

10.
$$\lim_{x \to 2} \frac{x^2 - 4x + 4}{x^2 + x - 6}$$

Answer:

After simplification,
$$\frac{x^2-4x+4}{x^2+x-6} = \frac{x-2}{x+3}$$
, and the limit is $(2-2)/(2+3) = 0$.

Question: Find the limits.

13.
$$\lim_{t \to 2} \frac{t^3 + 3t^2 - 12t + 4}{t^3 - 4t}$$

Answer:

After simplification,
$$\frac{t^3 + 3t^2 - 12t + 4}{t^3 - 4t} = \frac{t^2 + 5t - 2}{t^2 + 2t}$$
, and the limit is $(2^2 + 5 \cdot 2 - 2)/(2^2 + 2 \cdot 2) = 3/2$.

Question: Find the limits.

29.
$$\lim_{x\to 9} \frac{x-9}{\sqrt{x}-3}$$

Answer:

After simplification,
$$\frac{x-9}{\sqrt{x}-3} = \sqrt{x}+3$$
, and the limit is $\sqrt{9}+3=6$.