**Data Structures Lab 9**

**Course:** Data Structures (CL2001) **Semester:** Fall 2024

**Instructor:** Shafique Rehman

**Note:**

* + - * Lab manual covers following below topics:

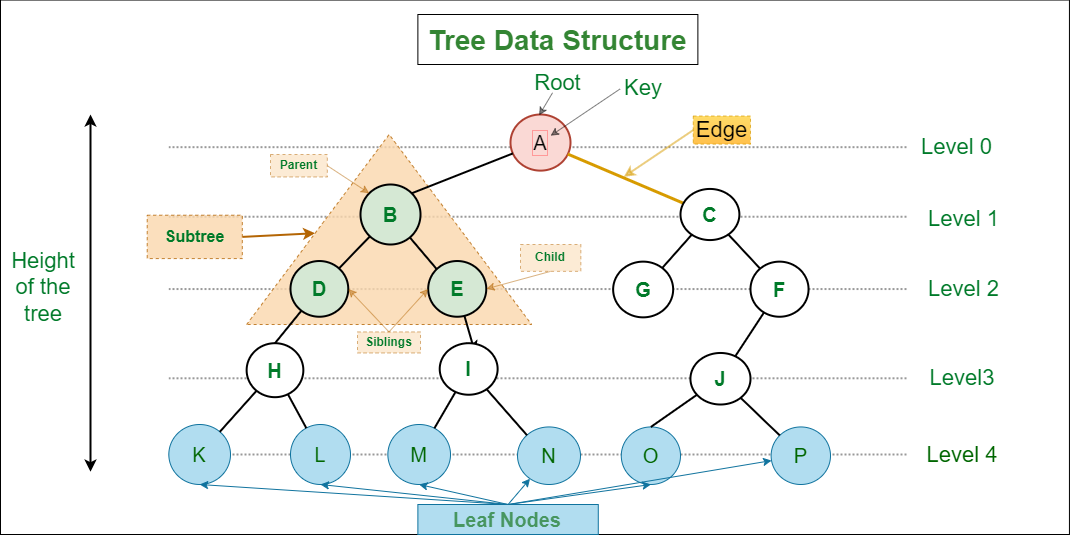
**{Tree, BST, Design and implement classes for binary tree nodes and nodes for general tree, Traverse the tree with the three common orders, Operation such as searches, insertions, and removals on a binary search tree and its applications}**

* Maintain discipline during the lab.
* Just raise your hand if you have any problem.
* Completing all tasks of each lab is compulsory.
* Get your lab checked at the end of the session.

**Tree**

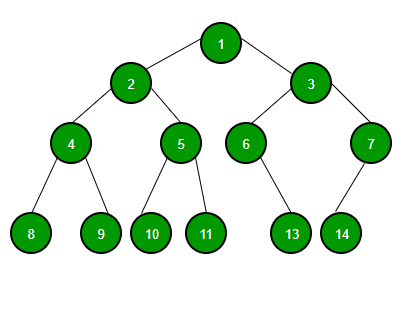
A tree data structure (**non-linear**) is a **hierarchical structure** that is used to **represent and organize data** in a way that is **easy to navigate and search**. It is a collection of nodes that are connected by **edges** and has a hierarchical relationship between the **nodes**.

**BST Visualization:** https://www.cs.usfca.edu/~galles/visualization/BST.html



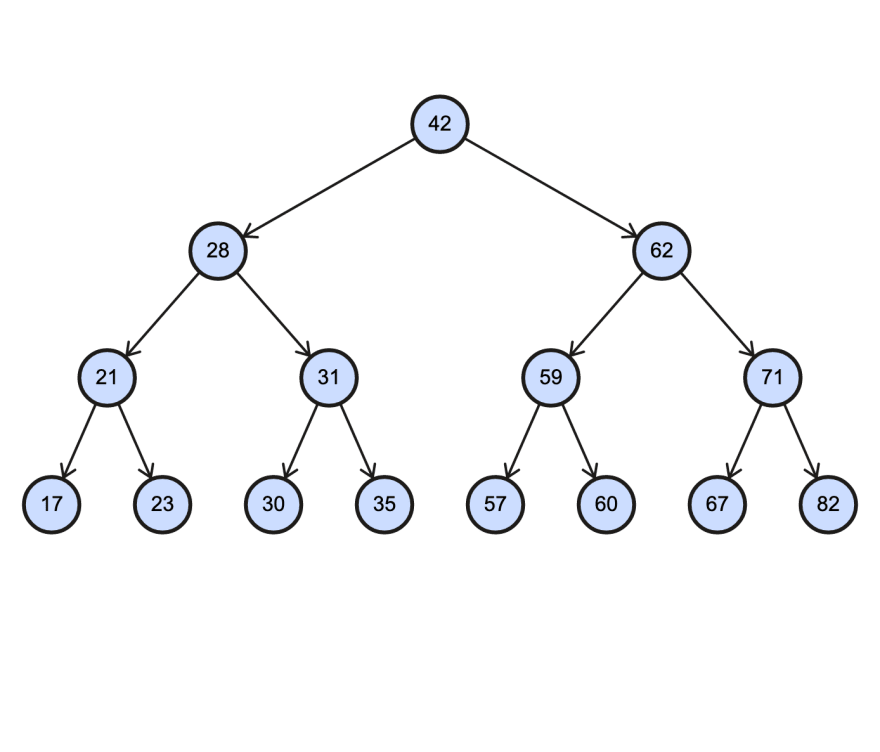
**Binary Tree**

Binary Tree is defined as a tree data structure where each node has **at most 2 children**. Since each element in a binary tree can have only 2 children, we typically name them the left and right child.



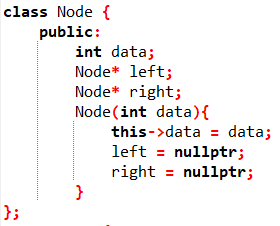
**BINARY SEARCH TREE**

Binary Search Tree is a node-based binary tree data structure which has the **left subtree of a node** that contains only nodes with **keys less than the node’s key**. Similarly, the **right subtree of a node** contains only nodes with **keys greater than the node’s key**. The left and right **subtree** each must also be a **binary search tree**.



**BST Insertion**

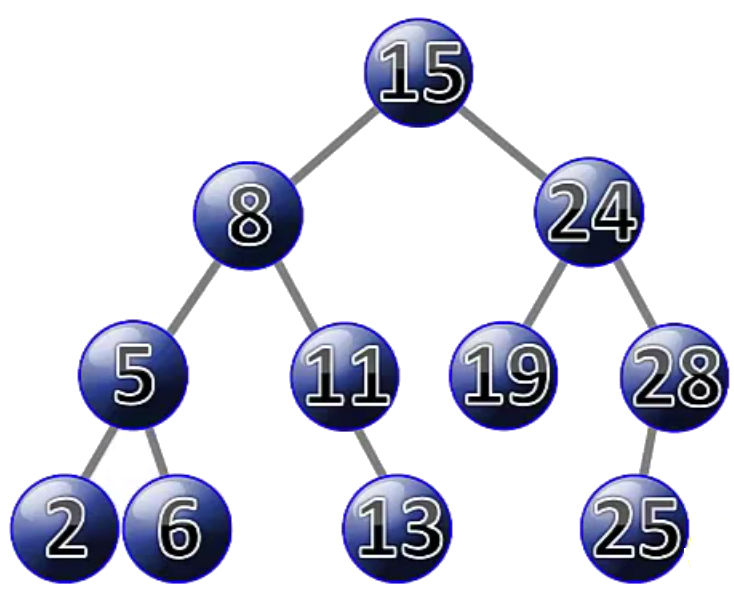
**Sample Code of class Nodes**



|  |  |
| --- | --- |
| **Insertion with without recursion** | **Insertion with recursion** |
|  | |
|  |  |

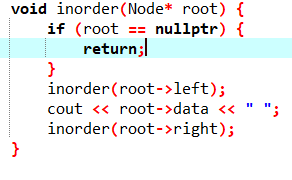
**Example:**

Add New Node with Key’s value is 12.



**Tree Traversals: Inorder, PreOrder, PostOrder**

**Tree Traversals:**



**Pseudo code for Inorder Traversal (iteration)**

1) Create an empty stack S.

2) Initialize current node as root

3) Push the current node to S and set current = current->left until current is NULL

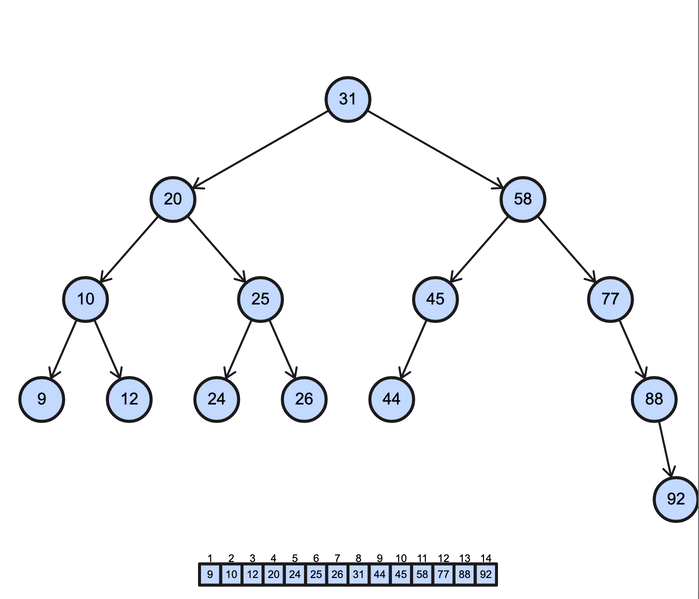
4) If current is NULL and stack is not empty then

a) Pop the top item from stack.

b) Print the popped item, set current = popped\_item->right

c) Go to step 3.

5) If current is NULL and stack is empty then we are done.



**Pre-Order Traversal**

Step 1: Repeat Steps 2 to 4 while TREE != NULL

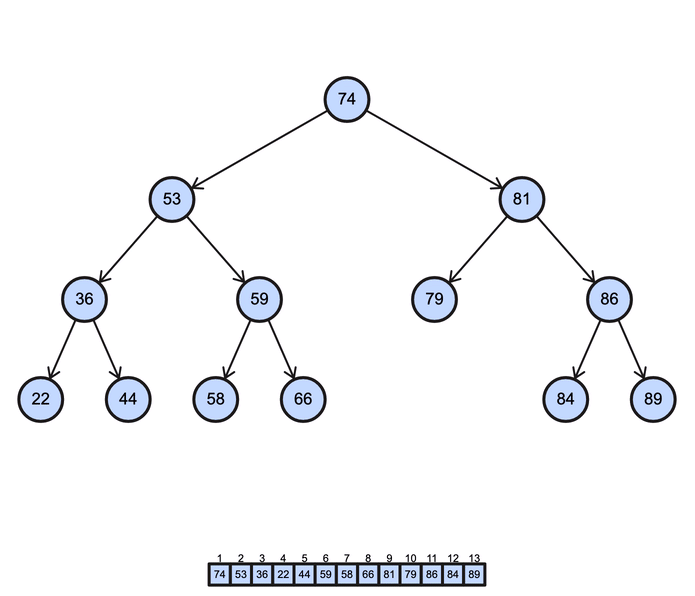
Step 2: Write TREE -> DATA

Step 3: PREORDER(TREE -> LEFT)

Step 4: PREORDER(TREE -> RIGHT)

[END OF LOOP]

Step 5: END



**Post-Order Traversal**

Step 1: Repeat Steps 2 to 4 while TREE != NULL

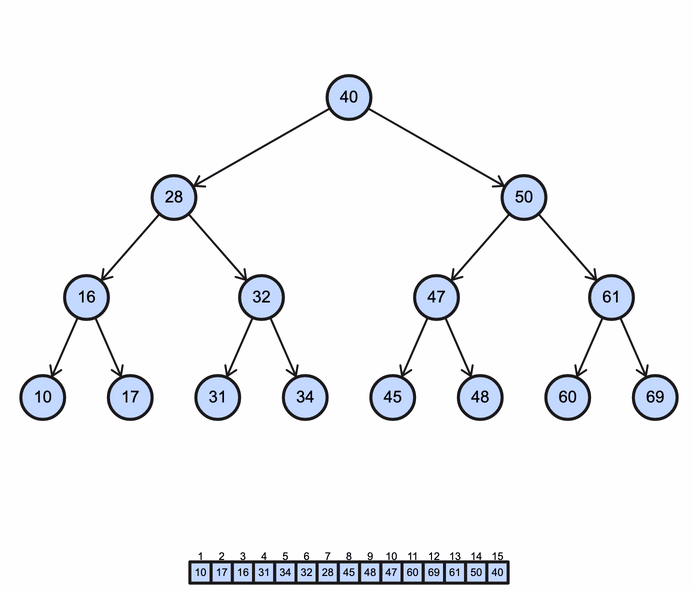
Step 2: POSTORDER(TREE -> LEFT)

Step 3: POSTORDER(TREE -> RIGHT)

Step 4: Write TREE -> DATA

[END OF LOOP]

Step 5: END



**BST Deletion**

**BST Deletion**

**1) *Node to be deleted is the*** ***leaf:*** Simply remove from the tree.

50 50

/ \ delete(20) / \

30 70 ---------> 30 70

/ \ / \ \ / \

20 40 60 80 40 60 80

**2) *Node to be deleted has only one child:*** Copy the child to the node and delete the child

50 50

/ \ delete(30) / \

30 70 ---------> 40 70

\ / \ / \

40 60 80 60 80

**3) *Node to be deleted has two children:*** Find inorder successor of the node. Copy contents of the inorder successor to the node and delete the inorder successor. Note that inorder predecessor can also be used.

50 60

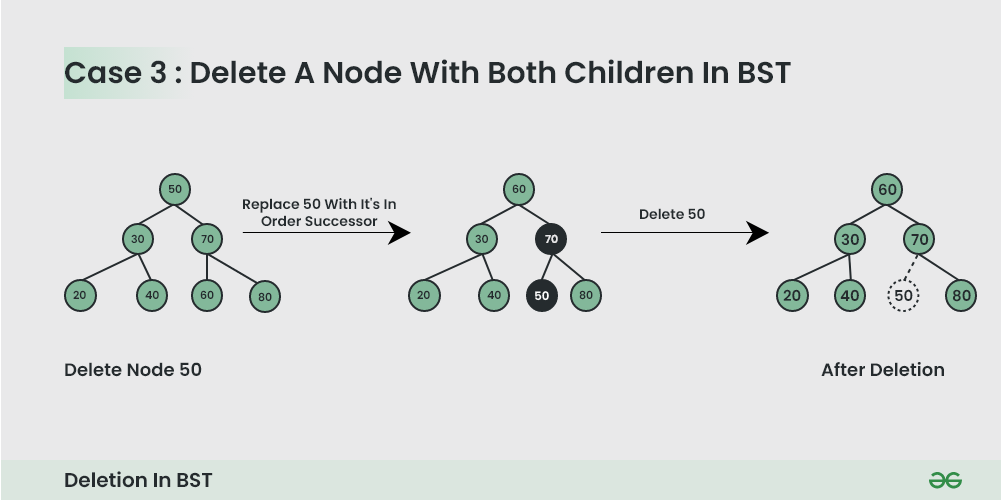
/ \ delete(50) / \

40 70 ---------> 40 70

/ \ \

60 80 80

The important thing to note is, inorder successor is needed only when the right child is not empty. In this particular case, inorder successor can be obtained by finding the **minimum value in the right child of the node**.

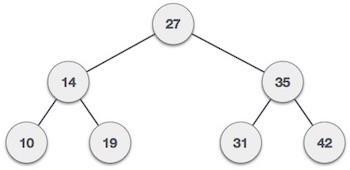


### Some points to Note:

### Binary search tree (BST)

Binary search tree (BST) or a lexicographic tree is a binary tree data structure which has the following binary search tree properties:

* Each node has a value.
* The key value of the left child of a node is less than to the parent's key value.
* The key value of the right child of a node is greater than (or equal) to the parent's key value.
* And these properties hold true for every node in the tree.



* **Subtree**: any node in a tree and its descendants.
* **Depth of a node**: the number of steps to hop from the current node to the root node of the tree.
* **Depth of a tree**: the maximum depth of any of its leaves.
* **Height of a node**: the length of the longest downward path to a leaf from that node.
* **Full binary tree:** A full Binary tree is a special type of binary tree in which every parent node/internal node has either two or no children.
* **Complete binary tree:** A complete binary tree is a binary tree in which all the levels are completely filled except possibly the lowest one, which is filled from the left. A complete binary tree is just like a full binary tree, but with two major differences:

**1.** All the leaf elements must lean towards the left.

**2.** The last leaf element might not have a right sibling i.e. a complete binary tree doesn't have to be a full binary tree.

* **Traversal**: an organized way to visit every member in the structure.

### Traversals:

The binary search tree property allows us to obtain all the keys in a binary search tree in a sorted order by a simple traversing algorithm, called an inorder tree walk, that traverses the left subtree of the root in in order traverse, then accessing the root node itself, then traversing in in-order the right sub tree of the root node.

The tree may also be traversed in preorder or post order traversals. By first accessing the root, and then the left and the right sub-tree or the right and then the left sub-tree to be traversed in preorder. And the opposite for the post order.   
The algorithms are described below, with Node initialized to the tree’s root.

• **Preorder Traversal**

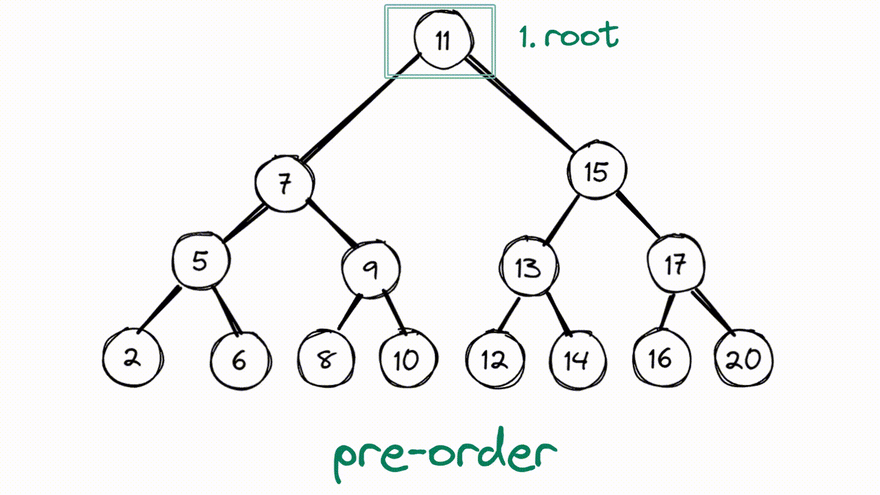
1. Visit Node.
2. Traverse Node’s left sub-tree.
3. Traverse Node’s right sub-tree.

**• In-order Traversal**

1. Traverse Node’s left sub-tree.
2. Visit Node.
3. Traverse Node’s right sub-tree

**• Post-order Traversal**

1. Traverse Node’s left sub-tree.
2. Traverse Node’s right sub-tree.
3. Visit Node

****

### Searching:

We use the following procedure to search for a node with a given key in a binary search tree. Given a pointer to the root of the tree and a key *k,* TREE-SEARCH returns a pointer to a node with key *k* if one exists; otherwise, it returns NIL.

TREE-SEARCH (*x, k*)

1 **if** *x* = NIL or *k = key*[*x*]

2 **then return** *x*

3 **if** *k < key*[*x*]

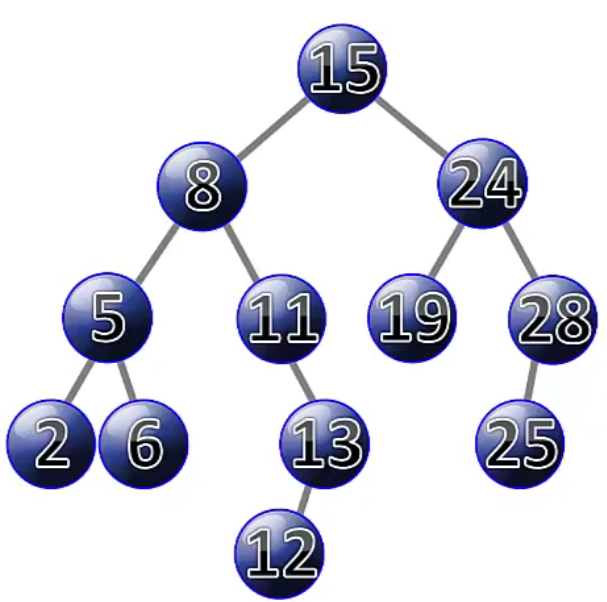
4 **then return** TREE-SEARCH *(left*[*x*], *k)*

5 **else return** TREE-SEARCH *(right*[*x*], *k)*

The procedure begins its search at the root and traces a path downward in the tree, as shown in Figure 13.2. For each node *x* it encounters, it compares the key *k* with *key*[*x*]*.* If the two keys are equal, the search terminates. If *k* is smaller than *key*[*x*]*,* the search continues in the left subtree of *x,* since the binary-search-tree property implies that *k* could not be stored in the right subtree. Symmetrically, if *k* is larger than *key*[*k*]*,* the search continues in the right subtree. The nodes encountered during the recursion form a path downward from the root of the tree, and thus the running time of TREE-SEARCH is *O*(*h*)*,* where *h* is the height of the tree.

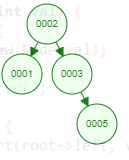
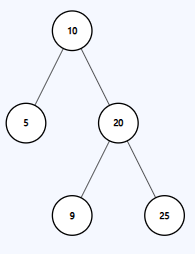
**Example:**

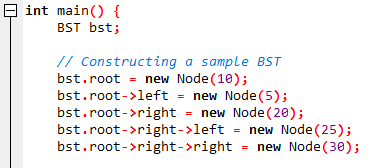
Search the node having key value is 19.



**Tasks**

Q1: Implement a binary search tree and perform all operations you learned above like: Inserting, Deleting, Searching, and Traversing  
  
Q2: Search for the value defined by the user in the tree. If the value does not exist insert it and print the new tree.

Q3: Given the root of a binary tree. Check whether these are Binary Search Tree or not.



Q4

Suppose you are working on a project for a small online retailer that needs to keep track of their inventory using a binary search tree. The retailer's inventory consists of a unique product ID and its corresponding quantity in stock. Write a C++ class for the binary search tree and add the required functionalities to insert new products into the tree, update the quantity of existing products, and search for products by their ID.

Additionally, the retailer would like to keep track of the product with the highest quantity in stock. Implement a function that returns the ID of this product, along with its quantity.

Q5: Given a Binary Search Tree, find the median of it.

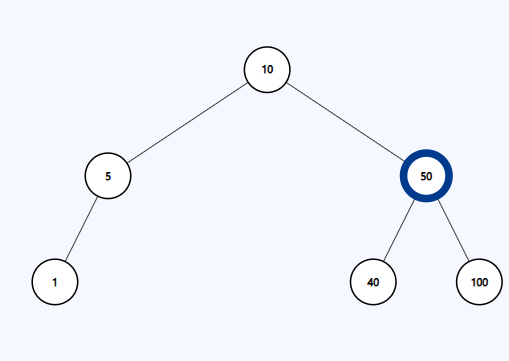
* If number of nodes are even: then median = ((n/2 + ((n)/2+1) ) /2
* If number of nodes are odd: then median = (n+1)/2

Q6:

Given a Binary Search Tree (BST) and a range [a, b], the task is to count the number of nodes in the BST that lie in the given range.

Examples:

Input: a= 5, b = 45



Output: 3

Explanation: There are three nodes in range [5, 45] = 5, 10 and 40.