DEPARTMENT OF INFORMATICS

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Master's Thesis in Informatics

Neural Network Hyperparameter Optimization with Sparse Grids

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Parameteroptimierung von neuronalen Netzen mit dünnen Gittern

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I confirm that this master's thesis in informatics is my own work and I have documented all sources and material used.

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Acknowledgments

Abstract

In recent years, machine learning has gained much importance due to the increasing amount of available data. The models that are performing very different tasks have a thing in common. They have parameters that are fixed before being trained on the data. The right choice of those hyperparameters can have a huge impact on the performance which is why they have to be optimized. Different techniques like grid search, random search, and bayesian optimization tackle this problem.

In this thesis, a new approach called adaptive sparse grid search for hyperparameter optimization is introduced. This new technique allows to adapt to the hyperparameter space and the model which leads to less training and evaluation runs compared to normal grid search while still finding the optimal model configuration for the best model results.

We compare the new approach to the other three techniques mentioned regarding execution time and resulting model performance using different machine learning tasks. The results show that adaptive sparse grid search is very efficient with a model performance similar to bayesian optimization and grid search.

Zusammenfassung

Contents

1 Introduction

2 Related Work

2.1 Hyperparameter Optimization

Most machine learning models have parameters that have to be defined before the learning phase. They are called hyperparameters and strongly influence the behavior of the model. One example is the number of epochs of the learning phase of a neural network. There are different techniques for the optimization of hyperparameters and they all define the machine learning model as a black box function f with the hyperparameters as input and the resulting performance as output. The overall goal is to find a configuration λ_{min} from $\Lambda = \Lambda_1 \times \Lambda_2 \times ... \times \Lambda_N$ that minimizes the function f with N hyperparameters with

$$\lambda_{min} = \arg\min_{\lambda \in \Lambda} f(\lambda). \tag{2.1}$$

In our case, the function f is a machine learning algorithm that is trained on a training set and evaluated on a testing set. With this, the minimization of e.g. the loss of the model optimizes the decisions it is making which leads to better prediction results. Note that one function evaluation of f is usually very expensive as the training of a machine learning model with many parameters and weights takes much time. The data set consists of $\{(x_i, y_i) | x_i \in X, y_i \in Y, 0 \leq i \leq m\}$ with m being the number of data samples. The x_i is the input data to the model and the goal is that

$$\forall i : M(x_i) = y_i. \tag{2.2}$$

where M is the model. In the context of supervised learning, the whole data set is split into a training set which is used to optimize the model and a testing set to evaluate the performance on new, unseen data [1].

All in all, the goal is get evaluation scores on the testing data set which can be achieved with Equation 2.1. [2], [3]

In the following, different techniques for the optimization are presented and discussed with their advantages and disadvantages.

2.1.1 Grid Search

The idea of the first approach for the optimization is to discretize the domains of each hyperparameter and evaluate each combination. This suffers from the curse of the dimensionality as it scales exponentially with the number of hyperparameters. For d parameters and n values per hyperparameter, n^d different configurations are possible which all have to be evaluated.

2.1.2 Random Search

2.1.3 Bayesian Optimization

2.1.4 Other Techniques

2.2 Sparse Grids

2.2.1 Numerical Approximation of Functions

2.2.2 Adaptive Sparse Grids

3 Hyperparameter optimization with sparse grids

3.1 Methodology

3.1.1 Adaptive Grid Search with Sparse Grids

3.1.2 Implementation

3.2 Results

4 Conclusion and Outlook

List of Figures

List of Tables

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