## 1

## Assignment -1 in LATEX

## Muzaan Mohammed Faizel A P EE22BTECH11036

**Question 1.4.1** Consider a triangle with vertices

$$\mathbf{A} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}, \ \mathbf{B} = \begin{pmatrix} -4 \\ 6 \end{pmatrix}, \ \mathbf{C} = \begin{pmatrix} -3 \\ -5 \end{pmatrix}$$

The equation of the perpendicular bisector of BC is

$$\left(\mathbf{x} - \frac{\mathbf{B} + \mathbf{C}}{2}\right)(\mathbf{B} - \mathbf{C}) = 0 \tag{1}$$

To find the equations of perpendicular bisectors of BC,AB,CA.

## **Solution:**

1) *BC*: Given equation for the perpendicular bisector of *BC*:

$$\left(\mathbf{x} - \frac{\mathbf{B} + \mathbf{C}}{2}\right)(\mathbf{B} - \mathbf{C}) = 0 \tag{2}$$

On substituting the values,

$$\frac{\mathbf{B} + \mathbf{C}}{2} = \begin{pmatrix} -\frac{7}{2} \\ \frac{1}{2} \end{pmatrix} \tag{3}$$

$$\mathbf{B} - \mathbf{C} = \begin{pmatrix} -1\\11 \end{pmatrix} \tag{4}$$

Solving using matrix multiplication:

$$(\mathbf{B} - \mathbf{C})^{\mathsf{T}} \left( \mathbf{x} - \frac{\mathbf{B} + \mathbf{C}}{2} \right) = 0 \tag{5}$$

$$(\mathbf{B} - \mathbf{C})^{\mathsf{T}} = \begin{pmatrix} -1 & 11 \end{pmatrix} \tag{6}$$

$$(\mathbf{B} - \mathbf{C})^{\mathsf{T}} \left( \frac{\mathbf{B} + \mathbf{C}}{2} \right) \tag{7}$$

$$= \begin{pmatrix} -1 & 11 \end{pmatrix} \begin{pmatrix} -\frac{7}{2} \\ \frac{1}{2} \end{pmatrix} \tag{8}$$

$$=9 (9)$$

Therefore, perpendicular bisector of BC is

$$\begin{pmatrix} -1 & 11 \end{pmatrix} \mathbf{x} = 9 \tag{10}$$

2) AB: Similar to the equation for the perpendicular bisector of BC,

$$\frac{\mathbf{A} + \mathbf{B}}{2} = \begin{pmatrix} -\frac{3}{2} \\ \frac{5}{2} \end{pmatrix} \tag{11}$$

$$\mathbf{A} - \mathbf{B} = \begin{pmatrix} 5 \\ -7 \end{pmatrix} \tag{12}$$

$$(\mathbf{A} - \mathbf{B})^{\mathsf{T}} = \begin{pmatrix} 5 & -7 \end{pmatrix} \tag{13}$$

Now,

$$(\mathbf{A} - \mathbf{B})^{\mathsf{T}} \left( \frac{\mathbf{A} + \mathbf{B}}{2} \right) \tag{14}$$

$$= \begin{pmatrix} 5 & -7 \end{pmatrix} \begin{pmatrix} -\frac{3}{2} \\ \frac{5}{2} \end{pmatrix} \quad (15)$$

$$= -25 \tag{16}$$

Therefore, perpendicular bisector of AB is

$$(5 \quad -7)\mathbf{x} = -25$$
 (17)

3) *CA*:

$$\frac{\mathbf{C} + \mathbf{A}}{2} = \begin{pmatrix} -1 \\ -3 \end{pmatrix} \tag{18}$$

$$\mathbf{C} - \mathbf{A} = \begin{pmatrix} -4 \\ -4 \end{pmatrix} \tag{19}$$

$$(\mathbf{C} - \mathbf{A})^{\mathsf{T}} = \begin{pmatrix} -4 & -4 \end{pmatrix} \tag{20}$$

Now,

$$(\mathbf{C} - \mathbf{A})^{\mathsf{T}} \left( \frac{\mathbf{C} + \mathbf{A}}{2} \right) \tag{21}$$

$$= \left( -4 \quad -4 \right) \begin{pmatrix} -1 \\ -3 \end{pmatrix} \tag{22}$$

$$= 16 \tag{23}$$

Therefore, perpendicular bisector of CA is

$$(-4 \quad -4)\mathbf{x} = 16 \tag{24}$$

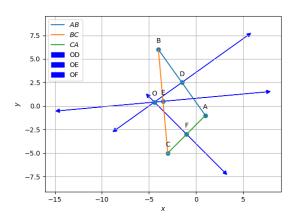


Fig. 3: Plot of the perpendicular bisectors