

Assignment -2 in L^AT_EX

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Question 10.13.1.26: A school has five houses A, B, C, D and E. A class has 23 students, 4 from house A, 8 from house B, 5 from house C, 2 from house D and rest from house E. A single student is selected at random to be the class monitor. The probability that the selected student is not from A, B and C is

Solution:

A	B	C	D	E
4	8	5	2	4

TABLE 0: Student distribution in each house

W = student selected is not from A,B and C

(1)

$$\implies W = (\overline{A})(\overline{B})(\overline{C})$$

(2)

Total no of students = $n(T) = 23$

(3)

By DeMorgan's Law and Axiom 3 of probability

$$\Pr((\overline{A})(\overline{B})(\overline{C})) = \Pr(\overline{(A + B + C)})$$

(4)

$$\Pr(\overline{(A + B + C)}) = 1 - \Pr((A + B + C))$$

(5)

$$\Pr((A + B + C)) = \Pr(A) + \Pr(B) + \Pr(C)$$

(6)

$$\Pr(\text{selecting a student from house A}) = \frac{n(A)}{n(T)}$$

(7)

$$\Pr(A) = \frac{4}{23} \quad (8)$$

$$\Pr(B) = \frac{8}{23} \quad (9)$$

$$\Pr(C) = \frac{5}{23} \quad (10)$$

$$\Pr((A + B + C)) = \frac{4}{23} + \frac{8}{23} + \frac{5}{23} \quad (11)$$

$$= \frac{17}{23} \quad (12)$$

$$\Pr(\overline{ABC}) = 1 - \frac{17}{23} = \frac{6}{23} \quad (13)$$

Therefore, probability of not selecting a student from A,B and C is,

$$\Pr(W) = \frac{6}{23} \quad (14)$$