Assignment -3 in LATEX

1

Muzaan Mohammed Faizel A P EE22BTECH11036

Question 11.16.3.12: Check whether the following probabilities Pr(A) and Pr(B) are consistently defined

1)
$$Pr(A) = 0.5, Pr(B) = 0.7, Pr(AB) = 0.6$$

2)
$$Pr(A) = 0.5, Pr(B) = 0.4, Pr(A + B) = 0.8$$

Solution: The given probabilities are consistently defined if it satisfies the following properties:

$$Pr(AB) \le Pr(A), Pr(B)$$
 (1)

$$0 \le \Pr(A), \Pr(B), \Pr(AB), \Pr(A+B) \le 1$$
 (2)

$$Pr(A + B) = Pr(A) + Pr(B) - Pr(AB)$$
 (3)

Proof of (1):

$$Pr(A) = Pr(A(B + B'))$$
 (4)

$$\implies \Pr(A) = \Pr(AB) + \Pr(AB')$$
 (5)

Therefore,
$$Pr(AB) \le Pr(A)$$
 (6)

$$Pr(AB) \le Pr(B)$$
 (8)

1) Given:

$$Pr(A) = 0.5,$$
 (9)

$$Pr(B) = 0.7,$$
 (10)

$$Pr(AB) = 0.6 \tag{11}$$

Since

$$\Pr(AB) \ge \Pr(A)$$
 (12)

Pr(A) and Pr(B) are not consistently defined.

2) Given:

$$Pr(A) = 0.5,$$
 (13)

$$Pr(B) = 0.4,$$
 (14)

$$\Pr(A + B) = 0.8$$
 (15)

From (3),

$$Pr(AB) = 0.5 + 0.4 - 0.8 \tag{16}$$

$$=0.1\tag{17}$$

This also satisfies (2) and (1)

Therefore Pr(A) and Pr(B) are consistently defined.