

# Physics

XI & XII

## FORMULA SHEET

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# PHYSICAL CONSTANTS

Speed of Light  $c = 3 \times 10^8 \text{ m/s}$   
 Plank constant  $h = 6.63 \times 10^{-34} \text{ Js}$   $hc = 1242 \text{ eV} \cdot \text{nm}$   
 Gravitation constant  $G = 6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2$   
 Boltzmann constant  $k = 1.38 \times 10^{-23} \text{ J/K}$   
 Molar gas constant  $R = 8.314 \text{ J/mol} \cdot \text{K}$   
 Avogadro's number  $N_A = 6.023 \times 10^{23} / \text{mol}$   
 Charge of electron  $e = 1.602 \times 10^{-19} \text{ C}$   
 Permeability of vacuum  $\mu_0 = 4\pi \times 10^{-7} \text{ N/A}^2$   
 Permittivity of vacuum  $\epsilon_0 = 8.85 \times 10^{-12} \text{ F/m}$   
 Coulomb constant  $1/4\pi\epsilon_0 = 9 \times 10^9 \text{ N m}^2/\text{C}^2$   
 Faraday constant  $F = 96485 \text{ C/mol}$   
 Mass of electron  $m_e = 9.1 \times 10^{-31} \text{ kg}$   
 Mass of proton  $m_p = 1.6726 \times 10^{-27} \text{ kg}$   
 Mass of neutron  $m_n = 1.6749 \times 10^{-27} \text{ kg}$   
 Atomic mass unit  $u = 1.66 \times 10^{-27} \text{ kg}$   
 Stefan-Boltzmann constant  $\sigma = 5.67 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4$   
 Rydberg constant  $R_\infty = 1.097 \times 10^7 / \text{m}$   
 Bohr magneton  $\mu_B = 9.27 \times 10^{-24} \text{ J/T}$   
 Bohr radius  $a_0 = 0.529 \times 10^{-10} \text{ m}$   
 Standard atmosphere  $1 \text{ atm} = 1.01325 \times 10^5 \text{ Pa}$   
 Wien displacement constant  $b = 2.9 \times 10^{-3} \text{ mK}$

# VECTORS

$\vec{a} = a_x \hat{i} + a_y \hat{j} + a_z \hat{k}$   $|\vec{a}| = \sqrt{a_x^2 + a_y^2 + a_z^2}$   
 DOT PRODUCT  $\vec{a} \cdot \vec{b} = a_x b_x + a_y b_y + a_z b_z = ab \cos \theta$

CROSS PRODUCT  $\vec{a} \times \vec{b} = ab \sin \theta$    
 $\vec{a} \times \vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix} = (a_y b_z - b_y a_z) \hat{i} + (a_z b_x - b_z a_x) \hat{j} + (a_x b_y - b_x a_y) \hat{k}$

# KINEMATICS

$\vec{v}_{avg} = \Delta \vec{s} / \Delta t$   $\vec{v}_{inst} = d\vec{s} / dt$   
 $\vec{a}_{avg} = \Delta \vec{v} / \Delta t$   $\vec{a}_{inst} = d\vec{v} / dt$

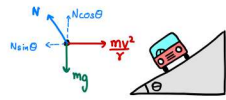
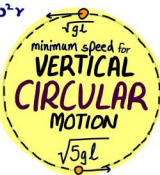
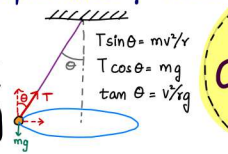
$s = ut + \frac{1}{2} at^2$   $v = u + at$   $v^2 = u^2 + 2as$   
**RELATIVE VELOCITY**  
 $v_{A/B} = v_A - v_B$

# PROJECTILE MOTION

$u_x = u \cos \theta$   $u_y = u \sin \theta$   $H = \frac{u^2 \sin^2 \theta}{2g}$   
 Time of Flight  $= 2u_y / g \Rightarrow T = 2u \sin \theta / g$   
 Range  $= u_x T \Rightarrow R = \frac{u^2 \sin 2\theta}{g}$   
 $y = \tan \theta \cdot x - \left( \frac{g}{2u^2 \cos^2 \theta} \right) x^2$

# LAWS OF MOTION

1<sup>st</sup> LAW: INERTIA 2<sup>nd</sup> LAW:  $F = d\vec{p} / dt = m\vec{a}$  3<sup>rd</sup> LAW: Action  $\Rightarrow$  Reaction  
 Friction:  $f_{static, maximum} = \mu_s N$   $f_{kinetic} = \mu_k N$   
 Centripetal force  $= \frac{mv^2}{r} = m\omega^2 r$



# WORK, POWER & ENERGY

Work  $= \vec{F} \cdot \vec{s} = F s \cos \theta = \int \vec{F} \cdot d\vec{s}$   
 $\oint \vec{F} \cdot d\vec{s} = 0$  (Work by Conservative force in a closed path)  
 KE  $= \frac{1}{2} mv^2$  (K)  
 POTENTIAL ENERGY (U)  
 $U_g = mgh$   $F = -\frac{dU}{dx}$  FOR CONSERVATIVE FORCES  
 $U_{spring} = \frac{1}{2} kx^2$   
**WORK-ENERGY THEOREM**  
 $W_{net} = \Delta K$   
 POWER  $= dW / dt = \vec{F} \cdot \vec{v}$   
 K + U = Conserved

# CENTER OF MASS

$x_{cm} = \frac{\sum x_i m_i}{\sum m_i} = \frac{\int x dm}{\int dm}$   
 $\vec{v}_{cm} = \frac{\sum m_i \vec{v}_i}{\sum m_i}$   $\vec{F} = m \vec{a}_{cm}$   

 HOLLOW CONE  $= h/3$  SOLID CONE  $= h/4$  HOLLOW SOLID

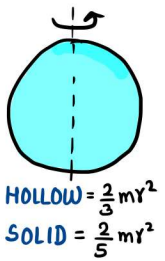
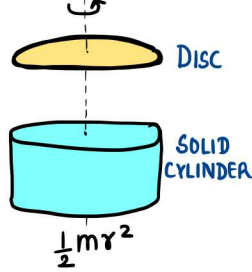
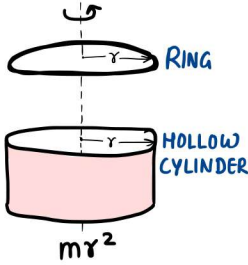
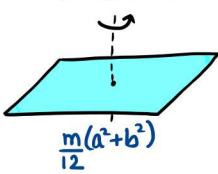
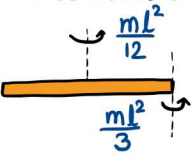
# COLLISION

$\frac{m_1}{u_1} + \frac{m_2}{u_2} = \frac{m_1}{v_1} + \frac{m_2}{v_2}$   
 MOMENTUM CONSERVATION {Always}  
 $m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$   
 $m_1 \gg m_2$   
 $m_1 \rightarrow$  undisturbed motion  $m_1 = m_2$   
 Solve using CoR in  $m_1$  frame Velocity Exchange for Elastic  
 KE  $\rightarrow$  ELASTIC INELASTIC  
 CAN BE NON ZERO  
 $CoR = e = \frac{v_{separation}}{v_{approach}} = \frac{v_2 - v_1}{u_1 - u_2}$   
 ENERGY CONSERVATION {Elastic}  
 $\frac{1}{2} m_1 u_1^2 + \frac{1}{2} m_2 u_2^2 = \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2$

# RIGID BODY DYNAMICS

$\omega = \frac{\Delta \theta}{\Delta t} = \frac{d\theta}{dt}$   $\alpha = \frac{\Delta \omega}{\Delta t} = \frac{d\omega}{dt}$   $\vec{v} = \vec{\omega} \times \vec{r}$   $\vec{a}_{tan} = \vec{\alpha} \times \vec{r}$   $\vec{a}_{centri} = \omega^2 r$   
 $\theta = \omega_0 t + \frac{1}{2} \alpha t^2$   $\vec{L} = \vec{r} \times \vec{p} = m \vec{v} \times \vec{r}$   
 $\omega = \omega_0 + \alpha t$   $\vec{z} = I \vec{\alpha} = d\vec{L} / dt$   
 $\omega^2 = \omega_0^2 + 2\alpha \theta$   $\vec{\tau} = \vec{r} \times \vec{F} = r_\perp F = r F \sin \theta$   
 EQUILIBRIUM:  $F_{net} = 0$   $\vec{z}_{net} = 0$   $\omega = 2\pi f$   $T = 1/f$   
 $\omega = v_\perp / r$

# MOMENT OF INERTIA



$$I = \sum m_i r_i^2$$

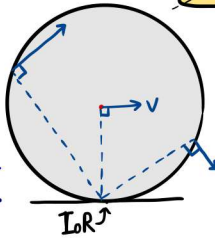
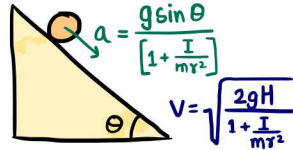
$$I = \int r^2 dm$$

$$R_{GYRATION} \quad mk^2 = I$$

## KINETIC ENERGY

$$K = \frac{1}{2} mv_c^2 + \frac{1}{2} I_c \omega^2$$

$$K = \frac{1}{2} I_H \omega^2 \quad \left\{ \begin{array}{l} \text{About Hinge} \\ \text{or } I_{OR} \end{array} \right\}$$



## ROLLING MOTION

$$v = \omega r \quad (\text{no slip condition})$$

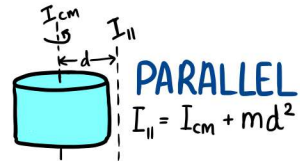
$$I_{OR} \text{ INSTANTANEOUS AXIS OF ROTATION}$$

$$\vec{v} = \vec{\omega} \times \vec{r}$$

## AXIS THEOREMS

### PERPENDICULAR

$$I_z = I_x + I_y$$



### PARALLEL

# GRAVITATION

$$F = G \frac{Mm}{R^2} \quad \text{POT ENERGY } (U) = -GMm/R$$

$$g = G \frac{M}{R^2} \quad g' = g \left[ 1 - \frac{d}{R_e} \right] \quad g' \approx g \left[ 1 - \frac{2h}{R_e} \right]$$

## HOOKE'S LAW

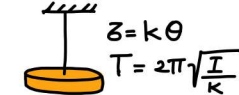
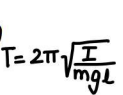
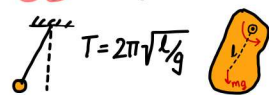
$$F = -kx$$

$$x = A \sin(\omega t + \phi)$$

$$v = A \omega \cos(\omega t + \phi)$$

$$a = -\omega^2 x = -k/m x$$

$$T = \frac{2\pi}{\omega} = 2\pi \sqrt{m/k}$$



# PROPERTIES OF MATTER

$$\text{YOUNG'S MODULUS } (Y) = \frac{F/A}{\Delta l/l}$$

$$\text{BULK MODULUS } (B) = -V \frac{\Delta P}{\Delta V}$$

$$\text{POISSON'S RATIO } (\sigma) = \frac{\text{LATERAL STRAIN}}{\text{LONGITUDINAL STRAIN}} = \frac{\Delta D/D}{\Delta l/l}$$

$$\text{ELASTIC ENERGY } (U) = \frac{1}{2} \text{STRESS} \times \text{STRAIN} \times \text{VOLUME}$$

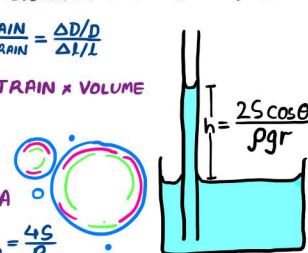
$$\text{SURFACE TENSION } (S) = F/l$$

$$\text{SURFACE ENERGY } (U) = S \cdot \text{AREA}$$

$$P_{EXCESS} = \Delta P_{AIR} = \frac{2S}{R} \quad \Delta P_{SOAP} = \frac{4S}{R}$$

$$\text{SHEAR MODULUS } (\eta) = \frac{F/A}{\tan \theta}$$

$$\text{COMPRESSIBILITY } (K) = \frac{1}{B} = -\frac{1}{V} \frac{\Delta V}{\Delta P}$$



# KEPLER'S LAWS

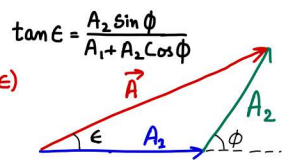
- 1<sup>st</sup> Elliptical Orbits, Sun @ foci
- 2<sup>nd</sup> Equal Area in Equal time ( $L^2$ )
- 3<sup>rd</sup>  $T^2 \propto a^3$  [semi major axis]

$$x_1 = A_1 \sin(\omega t)$$

$$x_2 = A_2 \sin(\omega t + \phi)$$

$$x = x_1 + x_2 = A \sin(\omega t + \epsilon)$$

$$A = \sqrt{A_1^2 + A_2^2 + 2A_1 A_2 \cos \phi}$$



## SERIES

$$\frac{1}{K_{eq}} = \frac{1}{K_1} + \frac{1}{K_2}$$

## PARALLEL

$$K_{eq} = K_1 + K_2$$

$$P_{HYDROSTATIC} = \rho g h \quad F_{BUOYANT} = \rho g V$$

$$\text{CONTINUITY } A_1 v_1 = A_2 v_2$$

$$\text{BERNOULLI'S } P + \rho g h + \frac{1}{2} \rho v^2 = \text{Const}$$

$$F_{VISCOUS} = -\eta A \frac{dv}{dx}$$

$$\text{TORRICELLI'S } v_{EFFLUX} = \sqrt{2gh}$$

$$\text{STOKE'S LAW } F = 6\pi \eta r v$$

$$v_{TERMINAL} = \frac{2r^2(\rho - \sigma)g}{9\eta}$$

$$\text{POISEUILLI'S EQN } \frac{\text{VOLUME FLOW}}{\Delta t} = \frac{\pi \rho r^4}{8\eta L}$$



# WAVES

$$\frac{\partial^2 y}{\partial x^2} = \frac{1}{v^2} \frac{\partial^2 y}{\partial t^2}$$

$$Y = A \sin(kx - \omega t) = A \sin\left[2\pi\left(\frac{x}{\lambda} - \frac{t}{T}\right)\right]$$

$$T = \frac{1}{\nu} = \frac{2\pi}{\omega} \quad v = \nu \lambda \quad \text{Wave Number } (k) = \frac{2\pi}{\lambda}$$

$$Y_1 = A_1 \sin(kx - \omega t) \quad Y_2 = A_2 \sin(kx - \omega t + \phi)$$

$$Y = A \sin(kx - \omega t + \epsilon) \quad A^2 = \sqrt{A_1^2 + A_2^2 \cos^2 \phi + (A_1 A_2 \sin \phi)^2}$$

$$\phi = 2n\pi \text{ (even)} : \text{Constructive}$$

$$= (2n+1)\pi \text{ (odd)} : \text{Destructive}$$

$$\tan \epsilon = \frac{A_2 \sin \phi}{A_1 + A_2 \cos \phi}$$

$$P_{avg} = 2\pi^2 \mu \nu A v^2 \quad v = \sqrt{\frac{T}{\mu}}$$

## STANDING WAVES

$$y_1 = A \sin(kx - \omega t) \quad y_2 = A \sin(kx + \omega t)$$

$$Y = 2A \cos kx \sin \omega t \quad \text{Node if } \cos kx = 0 \Rightarrow x = (n + \frac{1}{2})\lambda$$

$$L = n \cdot \frac{\lambda}{2} \quad v = \frac{n}{2L} \sqrt{\frac{T}{\mu}}$$

$$L = (2n+1) \frac{\lambda}{4} \quad v = \frac{2n+1}{4L} \sqrt{\frac{T}{\mu}}$$

## SOUND WAVES

$$S = S_m \sin[\omega(t - x/v)]$$

$$P = P_m \cos[\omega(t - x/v)]$$

$$P_m = \left(\frac{\rho \omega v}{2}\right) S_m$$

$$I = \frac{2\pi^2 B}{v} S_m^2 \nu^2 = \frac{P_m^2}{2B} = \frac{P_m}{2\rho v}$$

## STANDING LONGITUDINAL WAVES

$$P_1 = P_m \sin[\omega(t - x/v)] \quad P_2 = P_m \sin[\omega(t + x/v)]$$

$$P = P_1 + P_2 = 2P_m \cos kx \sin \omega t$$

$$\text{CLOSED ORGAN PIPE} \quad L = (2n+1) \frac{\lambda}{4} \quad v = (2n+1) \frac{v}{4L}$$

$$\text{OPEN ORGAN PIPE} \quad L = n \frac{\lambda}{2} \quad v = n \frac{v}{2L}$$

## RESONANCE COLUMN

$$L_1 + d = \frac{\lambda}{2} \quad L_2 + d = \frac{3\lambda}{2}$$

$$v = 2(L_2 - L_1)\nu$$

### BEATS

(if  $\omega_1 \approx \omega_2$ )

$$P_1 = P_m \sin \omega_1(t - x/v) \quad P_2 = P_m \sin \omega_2(t - x/v)$$

$$P = 2P_m \cos \Delta\omega(t - x/v) \sin \omega(t - x/v)$$

$$\omega = (\omega_1 + \omega_2)/2 \quad \text{Beats} \rightarrow \Delta\omega = \omega_1 - \omega_2$$

### DOPPLER

$$v = \frac{v + v_o}{v - v_s} v_o$$

## LIGHT WAVES

### PLANE WAVES

$$E = E_0 \sin \omega(t - x/v); \quad I = I_0$$

### SPHERICAL WAVES

$$E = \frac{aE_0}{r} \sin \omega(t - r/v); \quad I = \frac{I_0}{r^2}$$

### DIFFRACTION

$$\Delta x = b \sin \theta \approx b \theta$$

$$\text{Minima } b \theta = n \lambda$$

$$\text{Resolution } \sin \theta = 1.22 \frac{\lambda}{b}$$

## YOUNG'S DOUBLE SLIT EXPERIMENT

Path diff:  $\Delta x = y \frac{\lambda}{D}$  Phase diff:  $\delta = \frac{2\pi}{\lambda} \Delta x$

### CONSTRUCTIVE

$$\delta = 2n\pi; \Delta x = n\lambda$$

### DESTRUCTIVE

$$\delta = (2n+1)\pi; \Delta x = (n + \frac{1}{2})\lambda$$

$$\text{Intensity } I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \delta \quad I_{\max/\min} = (\sqrt{I_1} \pm \sqrt{I_2})^2$$

$$\text{Fringe Width } \omega = \frac{\lambda D}{d} \quad \text{Optical Path } \Delta x' = \mu \Delta x$$

### LAW OF MALUS

$$I = I_0 \cos^2 \theta$$

### INTERFERENCE THROUGH THIN FILM

$$\Delta x = 2\mu d = \frac{n\lambda}{(2n+1)\lambda_2} \rightarrow \text{Constructive}$$

$$\rightarrow \text{Destructive}$$

## OPTICS

### REFLECTION

(i)  $\angle i = \angle r$

(ii)  $i, r$  & normal in same plane

$$f = R/2$$

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{f}$$

$$\text{Magnification } m = -\frac{v}{u}$$

### REFRACTION

$$\mu = \frac{c}{v} = \frac{\text{vacuum}}{\text{medium}}$$

### SNAIL'S LAW

$$\mu_1 \sin i = \mu_2 \sin r$$

### APPARENT DEPTH

$$d' = d/\mu$$

### TIR CRITICAL ANGLE

$$\mu \sin \theta_c = \sin 90^\circ = 1$$

### PRISM

$$S = i + i' - A$$

$$\mu = \frac{\sin\left(\frac{A + \delta_{\min}}{2}\right)}{\sin\left(\frac{A}{2}\right)}$$

$$\delta_{\min} = (\mu - 1)A$$

For small 'A'

### SPHERICAL SURFACE

$$\frac{\mu_2}{v} - \frac{\mu_1}{u} = \frac{\mu_2 - \mu_1}{R}$$

$$m = \frac{\mu_1 v}{\mu_2 u}$$

### LENS MAKER'S

$$\frac{1}{f} = (\mu - 1)\left(\frac{1}{R_1} - \frac{1}{R_2}\right)$$

### LENS FORMULA

$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}; \quad m = \frac{v}{u}$$

### POWER

$$P = 1/f$$

### THIN LENSES

$$\frac{1}{F} = \frac{1}{f_1} + \frac{1}{f_2} - \frac{d}{f_1 f_2}$$

### MICROSCOPE

Simple  $m = D/f$

Compound

$$m = \frac{v}{u} \frac{D}{f_e}$$

$$\text{Resolving Pow } R = \frac{1}{\Delta\theta} = \frac{2\mu \sin \theta}{\lambda}$$

### TELESCOPE

$$m = -f_o/f_e$$

$$L = f_o + f_e$$

$$R = \frac{1}{\Delta\theta} = \frac{1}{1.22\lambda}$$

### DISPERSION

Cauchy's  $\mu = \mu_0 + A/\lambda^2 \quad A > 0$

For small  $A$  &  $i$

mean deviation  $\delta_y = (\mu_y - 1)A$

Angular dispersion  $\theta = (\mu_y - \mu_r)A$

Dispersive Power

$$\omega = \frac{\mu_r - \mu_y}{\mu_y - 1} \approx \frac{\theta}{\delta_y}$$

DISPERSION only

$$(\mu_y - 1)A + (\mu_y - 1)A' = 0$$

DEVIATION only

$$(\mu_r - \mu_y)A = (\mu_r' - \mu_y')A'$$

PHYSICS

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# HEAT AND TEMP

$$F = 32 + \frac{9}{5}C$$

$$K = C + 273.16$$

$$\text{Ideal Gas} \rightarrow PV = nRT$$

$$\text{van der Waals}$$

$$(p + \frac{a}{V^2})(V - b) = nRT$$

$$L = L_0(1 + \alpha \Delta T)$$

$$A = A_0(1 + 2\alpha \Delta T)$$

$$V = V_0(1 + 3\alpha \Delta T)$$

$$\text{THERMAL STRESS}$$

$$\frac{F}{A} = Y \frac{\Delta L}{L}$$

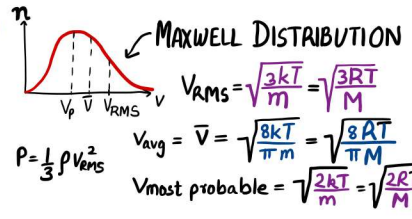
# KINETIC THEORY

$$\text{EQUIPARTITION OF ENERGY}$$

$$K = \frac{1}{2}kT \text{ for each DoF}$$

$$K = \frac{f}{2}kT \text{ for } f \text{ Degrees of Freedom}$$

$$\text{Internal Energy } U = \frac{f}{2}nRT$$



$$f = 3 (\text{monatomic}); 5 (\text{diatomic})$$

# SPECIFIC HEAT

$$\text{Specific heat } S = \frac{Q}{m\Delta T}$$

$$\text{Latent heat } L = Q/m$$

$$C_v = \frac{f}{2}R \quad C_p = C_v + R \quad r = C_p/C_v$$

$$C_v = \frac{n_1 C_{v1} + n_2 C_{v2}}{n_1 + n_2} \quad r = \frac{n_1 C_{p1} + n_2 C_{p2}}{n_1 C_{v1} + n_2 C_{v2}}$$

# THERMODYNAMICS

$$\text{1st LAW } \Delta Q = \Delta U + W \quad W = \int p dV$$

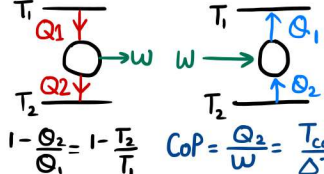
$$\text{ADIABATIC } W = \frac{p_1 V_1 - p_2 V_2}{\gamma - 1}$$

$$\text{ISOTHERMAL } W = nRT \ln \left( \frac{V_2}{V_1} \right)$$

$$\text{ISOBARIC } W = p(V_2 - V_1)$$

$$\text{ADIABATIC: } \Delta Q = 0; pV^\gamma = \text{const}$$

$$\text{2nd LAW } \text{ENTROPY } dS = \frac{dQ}{T}$$

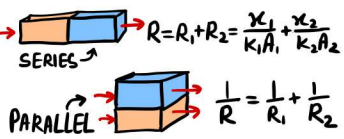


$$\eta = \frac{W}{Q_1} = 1 - \frac{Q_2}{Q_1} = 1 - \frac{T_2}{T_1} \quad \text{COP} = \frac{Q_2}{W} = \frac{T_{\text{cold}}}{\Delta T}$$

# HEAT TRANSFER

$$\text{CONDUCTION } \frac{\Delta Q}{\Delta t} = -KA \frac{\Delta T}{x}$$

$$\text{Thermal Resistance} = \frac{x}{KA}$$



$$\text{KIRCHHOFF'S LAW } \frac{\text{Emissive Power}}{\text{Absorptive Power}} = \frac{E_{\text{body}}}{a_{\text{body}}} = E_{\text{blackbody}}$$

$$\text{WIEN'S DISPLACEMENT } \lambda_m T = b \quad \text{STEFAN-BOLTZMANN } \Delta \theta / \Delta t = \sigma e A T^4$$

$$\text{NEWTON'S COOLING } \frac{dT}{dt} = -bA(T - T_0)$$

# ELECTROSTATICS

$$\text{COULOMB'S LAW } F = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

$$\vec{E} = \vec{F}/q = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

$$\text{POTENTIAL (V)} = \frac{1}{4\pi\epsilon_0} \frac{q}{r}$$

$$\text{PE (V)} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r} \quad \vec{E} = -\frac{dV}{dr}$$

$$\text{DIPOLE MOMENT}$$

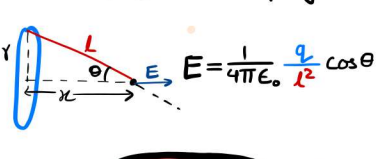
$$\vec{p} = q\vec{d} \quad \frac{1}{4\pi\epsilon_0} \frac{p \cos \theta}{r^2} = V(r)$$

$$\text{DIPOLE IN FIELD}$$

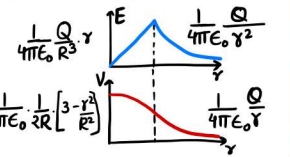
$$\vec{\tau} = \vec{p} \times \vec{E} \quad U = -\vec{p} \cdot \vec{E} \quad E_r = \frac{1}{4\pi\epsilon_0} \frac{2p \cos \theta}{r^3} \quad E_\theta = \frac{1}{4\pi\epsilon_0} \frac{p \sin \theta}{r^3}$$

$$\text{GAUSS'S LAW}$$

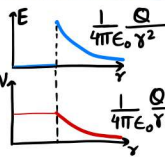
$$\phi = q_{in}/\epsilon_0 \quad \text{FLUX } \phi = \oint \vec{E} \cdot d\vec{s}$$



$$\text{UNIFORMLY CHARGED SPHERE}$$



$$\text{UNIFORM SHELL}$$



$$\text{LINE CHARGE } E = \frac{\lambda}{2\pi\epsilon_0 r}$$

$$\infty\text{-sheet } E = \frac{\sigma}{2\epsilon_0}$$

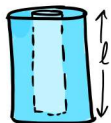
$$\vec{E} \text{ near } \text{CONDUCTING SURFACE } E = \frac{\sigma}{\epsilon_0}$$



# CAPACITORS

$$C = q/V \quad C = \epsilon_0 A/d$$

$$\text{SPHERE } C = \frac{2\pi\epsilon_0 L}{\ln(r_2/r_1)} \quad C = 4\pi\epsilon_0 \frac{r_1 r_2}{r_2 - r_1}$$



$$\text{PARALLEL } C_{eq} = C_1 + C_2$$

$$\text{SERIES } \frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$\text{WITH DIELECTRIC } C = \epsilon_0 \frac{KA}{d}$$

$$\text{Force b/w plates} = \frac{Q^2}{2A\epsilon_0} \quad U = \frac{1}{2} CV^2 = \frac{Q^2}{2C} = \frac{1}{2} QV$$

# CURRENT ELECTRICITY

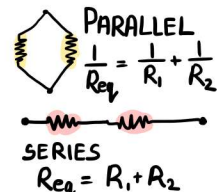
$$\text{DENSITY } j = I/A = \sigma E$$

$$v_{drift} = \frac{eE\tau}{m} = \frac{j}{neA}$$

$$R_{\text{WIRE}} = \rho L/A \quad \rho = \frac{1}{\sigma}$$

$$R = R_0(1 + \alpha \Delta T)$$

$$\text{OHM'S LAW } V = iR$$

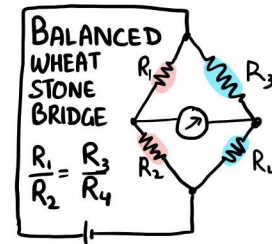


$$\text{KIRCHHOFF'S LAWS}$$

$$\text{* JUNCTION LAW } \sum I_i = 0 \quad \text{Sum of all } i \text{ towards a node} = 0$$

$$\text{* LOOP LAW } \sum \Delta V = 0 \quad \text{Sum of all } \Delta V \text{ in closed loop} = 0$$

$$\text{POWER} = i^2 R = V^2/R = iV$$





### GALVANOMETER

$i_g G = (i - i_g) S$   
 $i_g G = (i - i_g) S$   
**Volmeter**  
 $V_{AB} = i_g (R + G)$

### CAPACITOR

Charging  $q(t) = CV(G - e^{-t/RC})$   
 Discharging  $q(t) = Q_0 e^{-t/RC}$   
 Time Constant  $\tau = RC$

### MAGNETISM

$\vec{F}_{\text{LORENTZ}} = q\vec{v} \times \vec{B} + q\vec{E}$   
 $q\vec{v} \times \vec{B} = m\vec{v} \times \vec{r}$   
 $T = \frac{2\pi m}{qB}$   
 $\vec{F} = i\vec{L} \times \vec{B}$

### MAGNETIC DIPOLE

$\vec{\mu} = i \text{Area} \vec{\hat{n}}$   
 $\vec{\tau} = \vec{\mu} \times \vec{B}$   
 $U = -\vec{\mu} \cdot \vec{B}$   
**HALL EFFECT**  
 $V_w = \frac{Bi}{ned}$

### PELTIER EFFECT

$\text{emf } e = \frac{\Delta H}{\Delta \theta}$

### THOMSON EFFECT

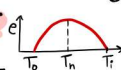
$\text{emf } e = \frac{\Delta H}{\Delta \theta} = \sigma \Delta T$

### FARADAY'S LAW OF ELECTROLYSIS

$m = Zit = \frac{1}{F} e it$   
 $E = \text{Chem equivalent}$   
 $Z = \text{Electro Chem eq}$   
 $F = 96485 \text{ C/g}$

### SEEBACK EFFECT

$e = aT + \frac{1}{2} bT^2$   
 $T_{\text{neutral}} = -a/b$   
 $T_{\text{inversion}} = -2a/b$



### Wires

$\frac{dF}{dl} = \frac{\mu_0 i_1 i_2}{2\pi d}$

### AXIS OF RING

$B_p = \frac{\mu_0 i r^2}{2(a^2 + r^2)^{3/2}}$

### CENTER OF ARC

$B = \frac{\mu_0 i \theta}{4\pi r}$   
 $B = \frac{\mu_0 i}{2r} (\text{ring})$

### SOLENOID

$B = \mu_0 n i$   
 $n = N/L$

### TOROID

$B = \mu_0 n i$   
 $n = N/2\pi r$

### AMPERE'S LAW

$\oint \vec{B} \cdot d\vec{l} = \mu_0 I_{\text{in}}$

### BAR MAGNET

$B_1 = \frac{\mu_0}{4\pi} \frac{2M}{d^3}$   
 $B_2 = \frac{\mu_0}{4\pi} \frac{M}{d^3}$

### ANGLE OF DIP

$B_h = B \cos \delta$   
 $B_v = B \sin \delta$



### TANGENT GALVANOMETER

$B_h \tan \theta = \frac{\mu_0 n i}{2r} \Rightarrow i = K \tan \theta$   
**MOVING COIL GALVANOMETER**  
 $n i A B = k \theta \Rightarrow i = \frac{k}{nAB} \theta$

### PERMEABILITY

$\vec{B} = \mu \vec{H}$   
**MAGNETOMETER**  
 $T = 2\pi \sqrt{I/M B_h}$

## ELECTROMAGNETIC INDUCTION

**MAGNETIC FLUX**  $\Phi = \oint \vec{B} \cdot d\vec{s}$  **FARADAY'S LAW**  $e = - \frac{d\Phi}{dt}$   
**LENZ'S LAW:** Induced current produces  $\vec{B}$  that opposes change in  $\Phi$

### SELF INDUCTANCE

$\Phi = Li$   $e = -L \frac{di}{dt}$   
**SOLENOID**  $L = \mu_0 n^2 \pi r^2 l$   
**MUTUAL INDUCTANCE**  
 $\Phi = M i$   $e = -M \frac{di}{dt}$

### GROWTH

$i = \frac{V}{R} [1 - e^{-t/\tau}]$   
**DECAY**  
 $i = i_0 e^{-t/\tau}$   
 Time Const  $\tau = L/R$   
 ENERGY  $U = \frac{1}{2} L i^2$   
 ENERGY DENSITY OF B-FIELD  
 $u = \frac{B^2}{2\mu_0}$   
**ROTATING COIL**  $e = NAB\omega \sin \omega t$   
**TRANSFORMER**  $\frac{N_1}{N_2} = \frac{e_1}{e_2}$   
 $C = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$

### ALTERNATING CURRENT

$i = i_0 \sin(\omega t + \phi)$   
 $i_{\text{rms}} = i_0 / \sqrt{2}$   
 POWER  $= i_{\text{rms}}^2 \cdot R$

### RC-CIRCUIT

$\frac{1}{\omega C}$   
 $\tan \phi = \frac{1}{\omega RC}$   
 $Z = \sqrt{R^2 + X_C^2}$   
 $X_C = \frac{1}{\omega R}$

### LR-CIRCUIT

$\omega L$   
 $\tan \phi = \frac{\omega L}{R}$   
 $Z = \sqrt{R^2 + X_L^2}$   
 $X_L = \omega L$

### LCR-CIRCUIT

$\tan \phi = \frac{X_C - X_L}{R}$   
 $Z = \sqrt{R^2 + (X_C - X_L)^2}$   
 $\phi_{\text{RESONANCE}} = \frac{1}{2\pi \sqrt{LC}}$   
 $(X_C = X_L)$   
 $P = e_{\text{rms}} i_{\text{rms}} \cos \phi$   
**POWER FACTOR**

### REACTANCE

CAPACITIVE  $X_C = 1/\omega C$   
 INDUCTIVE  $X_L = \omega L$   
 IMPEDANCE  $Z = e_0/i_0$

## MODERN PHYSICS

$E = h\nu = hc/\lambda$   $p = h/\lambda = E/c$   $E = mc^2$   
 Ejected photo-electron  $K_{\text{max}} = h\nu - \phi$   
**THRESHOLD**  $\nu_0 = \phi/h$   
**STOPPING**  $V_0 = \frac{hc}{e} \left( \frac{1}{\lambda} - \frac{1}{\lambda_0} \right)$   
 de Broglie  $\lambda = h/p$

### BOHR'S ATOM

QUANTIZATION OF ANGULAR MOMENTUM  
 $E_n = -\frac{m^2 Z^4 e^4}{8 \epsilon_0^2 h^2 n^2} = -\frac{13.6 Z^2}{n^2} \text{ eV}$   
 $\gamma_n = \frac{E_n - E_m}{hc} = \frac{13.6 Z^2}{hc} \left( \frac{1}{n^2} - \frac{1}{m^2} \right)$   
 $E_{\text{TRANSITION}} = 13.6 Z^2 \left( \frac{1}{n^2} - \frac{1}{m^2} \right) \text{ eV}$

**HEISENBERG**  $\Delta x \Delta p \geq h/2\pi$   $\Delta E \Delta t \geq h/2\pi$   
**MOSLEY'S LAW**  $\sqrt{\nu} = a(Z - b)$   
**X-RAY DIFFRACTION**  $2d \sin \theta = n\lambda$   
 $\lambda_{\text{min}} = \frac{hc}{eV}$

## NUCLEUS

$R = R_0 A^{1/3}$   $R_0 = 1.1 \times 10^{-15} \text{ m}$   
**RADIOACTIVE DECAY**  
 $\frac{dN}{dt} = -\lambda N$   $N = N_0 e^{-\lambda t}$   
**HALF LIFE**  $t_{1/2} = 0.693/\lambda$   
**Avg LIFE**  $t_{\text{avg}} = 1/\lambda$

### MASS DEFECT

$\Delta m = [Z m_p + (A-Z) m_n] - M$   
**BINDING E**  $= \Delta m c^2$   
**Q-VALUE**  $Q = U_i - U_f$

## SEMICONDUCTORS

### HALF WAVE RECTIFIER

### FULL WAVE RECTIFIER

### TRIODE VALVE

Cathode, Filament, Grid, Plate  
**TRIODE**  
 Plate Resistance  $r_p = \frac{\Delta V_p}{\Delta i_p} \bigg|_{\Delta V_g = 0}$   
 Trans-conductance  $g_m = \frac{\Delta i_p}{\Delta V_g} \bigg|_{\Delta V_p = 0}$   
 Amplification  $\mu = \frac{\Delta V_p}{\Delta V_g} \bigg|_{\Delta i_p = 0}$   
 $\mu = r_p \times g_m$

### TRANSISTOR

$I_e = I_b + I_c$   
 $\alpha = \frac{I_c}{I_e}$   $\beta = \frac{I_c}{I_b}$   $\beta = \frac{\alpha}{1-\alpha}$   
 Trans conductance  $g_m = \frac{\Delta I_c}{\Delta V_{be}}$

### LOGIC GATES

AND, OR, NOT, NAND, NOR, XOR  

A \ B	AB	A+B	AB	A+B	AB + AB
0 0	0	1	0	1	0
0 1	0	1	0	1	0
1 0	0	1	1	1	0
1 1	1	1	1	1	1

NOW, YOU'RE ONE STEP CLOSER TO YOUR GOAL