

## Mathematica Problems on Recurrence Relations (RR) and Cellular Automata (CA)

1. A particle moves horizontally to the right. For  $n \in \mathbf{Z}^+$ , the distance the particle travels in the  $(n + 1)$ st second is equal to twice the distance it travels during the  $n$ th second. If  $x_n, n \geq 0$ , denotes the position of the particle at the start of the  $(n + 1)$ st second, find a recurrence relation for  $x_n$ , where  $x_0 = 1$  and  $x_1 = 5$ . Solve it.
2. Plot the value of the derivative of  $g(x) = ax(1 - x)$  at the two fix points for  $0 < a < 4$ . Formulate a criteria for the stability of a fix point.
3. Consider rule 170. Run it for the seed ...WWWBWBWBWWW..... 3 times. This is an example of a reversible CA, that is, each state has a unique predecessor. Try to understand that!
4. Iterate Game of Life 3 times with the initial state below. What do you observe? Outer square is 8 times 8 and inner square is 4 times 4.

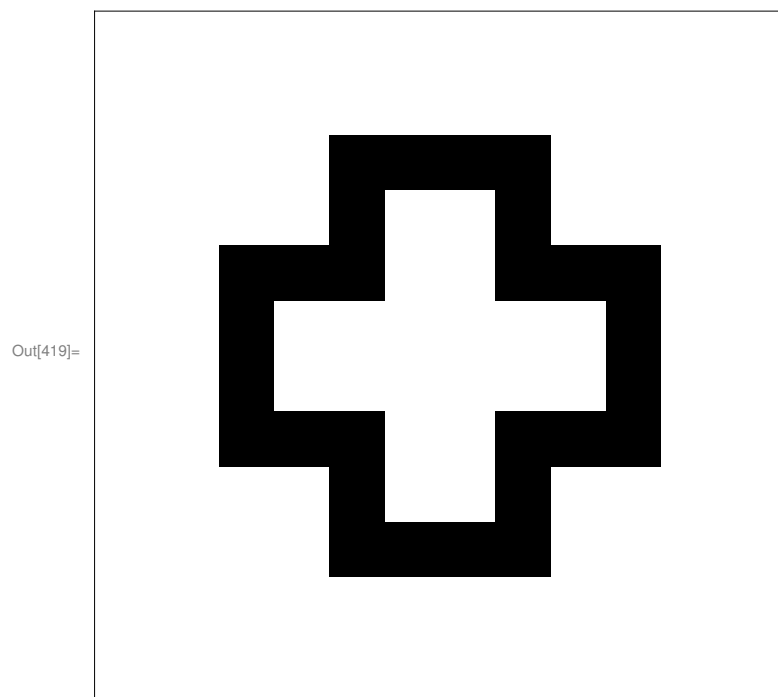


Figure 1: Your initial state to Game of Life.