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Clear["`*"]
(* After 1D CA we turn to two dimensional
   CA. Still each cell can have two states. BUT
   there are now 8 neighbours. 3 above and below and one
   to the right and one to the left. So including the
   middle cell there are  $2^9=512$  states for these
   cells. Can you tell how many CA rules we then have?
   The most famous of these is called Game of Life,
http://en.wikipedia.org/wiki/Conway%27s\_Game\_of\_Life
   and http://mathworld.wolfram.com/GameofLife.html *)
(* This example is for rule 746. I call it circular growth. The
   birth rule (white->black) is exactly 3 living neighbours.
   Survival (black->black) if no more than 4 neighbours are
   alive. Death (black->white) if there are 5-8 living neighbours
   in the previous generation. Game of Life is rule 224. Same birth
   condition as for Circular Growth but death happens due to loneliness
   (0 or 1 living cell next to the cell) or over population
   (4-8 living cells around the middle cell). As in our world!
   If you write 746 and 224 in base 2 I hope you can
   figure out how this rule numbers are obtained.*)
CircularGrowth = {746, {2, {{2, 2, 2}, {2, 1, 2}, {2, 2, 2}}}, {1, 1}};
(* This list above specifies the 2D CA*)
seed = Table[0, {200}, {200}];
seed[[98, 100]] = 1;
seed[[99, 100]] = 1;
seed[[100, 100]] = 1;
seed[[102, 100]] = 1;
(* seed is the input matrix. Here we start with a "worm", or better seed,
   with 5 cells but the next lowest is dead (ill) to begin with.
   200 iterations. In fact something shocking happens after 3000
   iterations for this seed. To see it you have to have a big matrix and
   it takes around 25 minutes on my machine. For five healthy
   cells in a row this effect has not been seen. It seems like
   radius of ball is  $=C * (\text{number of iterations})$ . Can you estimate C?*)
ArrayPlot[CellularAutomaton[CircularGrowth, seed, {{{200}}}],
(* If you want to see Circular Growth - The Movie you use instead:
   Animate[ArrayPlot[CellularAutomaton[CircularGrowth, seed, {{{n}}}],
     Mesh->False], {n, 0, 200, 1}, AnimationRate -> 10, AnimationRunning->False]*)

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