

So Far...

- ▶ It's time for
 - Unsupervised learning
 - We are only given inputs
 - Goal: find "interesting patterns"
 - Discovering clusters
 - Clustering
 - Discovering latent factors
 - Dimensionality reduction
 - Topic modeling
 - Matrix factorization

Topic Modeling

Deng Cai (蔡登)



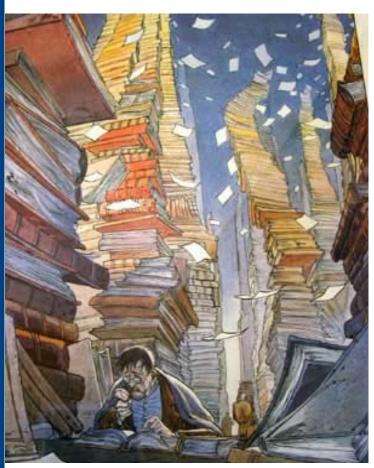
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Text Analysis



www.betaversion.org/~stefano/linotype/news/26/

- Text data
 - Web page
 - Emails
 - Documents
 - •



Bag-of-Words (BOW)

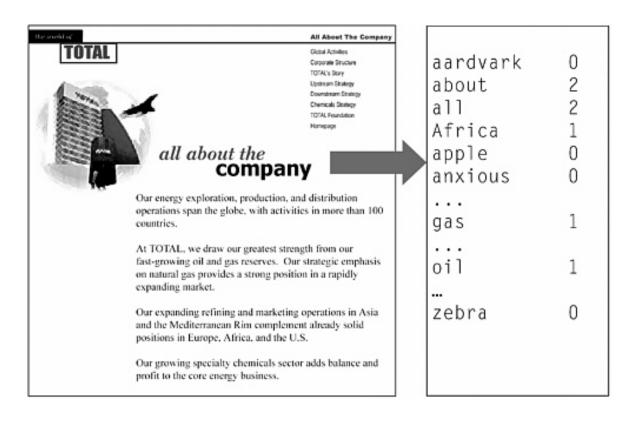
Assumes order of words has no significance
 e.g., the term "home made" has the same probability as "made home"

▶ It is a simplifying assumption used in natural language processing and information retrieval



Salton's Vector Space Model (Prior to 1988)

Represent each document by a high-dimensional vector in the space of words







Document-Term Matrix

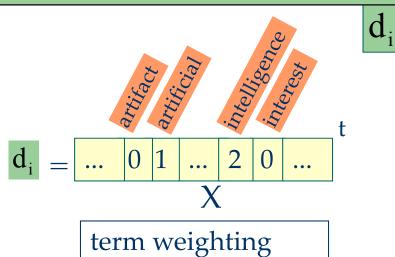
D = Document collection

W = Lexicon/Vocabulary

intelligence

 \mathbf{W}_{j}

Texas Instruments said it has developed the first 32-bit computer chip designed specifically for artificial intelligence applications [...]

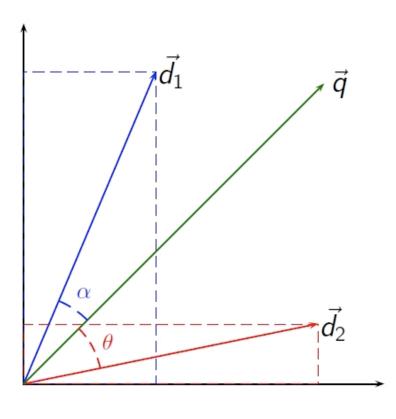


 $Document-Term\ Matrix \\ \hline W \\ \hline W_1 & \cdots & W_j & \cdots & W_J \\ \hline d_1 & & & & & \\ \hline \cdots & & & \cdots & & \\ \hline d_i & & \cdots & & & \\ \hline \vdots & & & & \ddots & \\ \hline d_I & & & & & \\ \hline \end{bmatrix}$



Query

Compute the similarity between queries(q) and documents(d)



$$\cos(\boldsymbol{q}, \boldsymbol{d}) = \frac{\boldsymbol{q}^T \boldsymbol{d}}{\|\boldsymbol{q}\| \|\boldsymbol{d}\|}$$

Simple, intuitive
Fast to compute, because both
they are sparse

Retrieval Methods

- Rank documents according to similarity with query
- Term weighting schemes, for example, TF-IDF

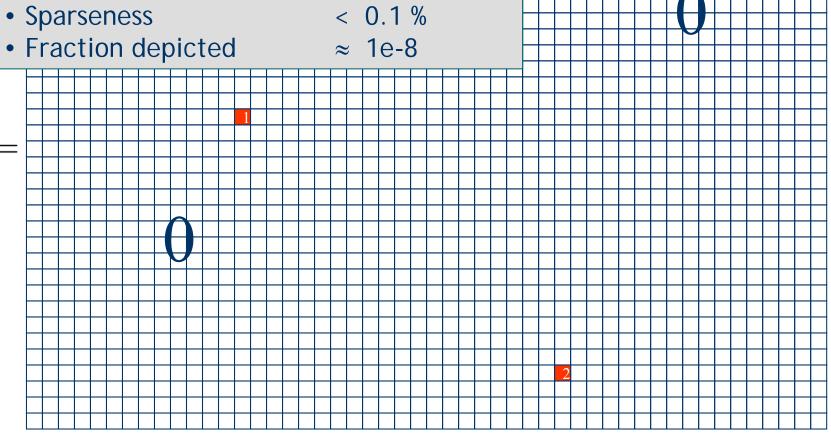


A 100 Million^{ths} of a Typical **Document-Term Matrix**

Typical:

- Number of documents ≈ 1.000.000
- Vocabulary

≈ 100.000



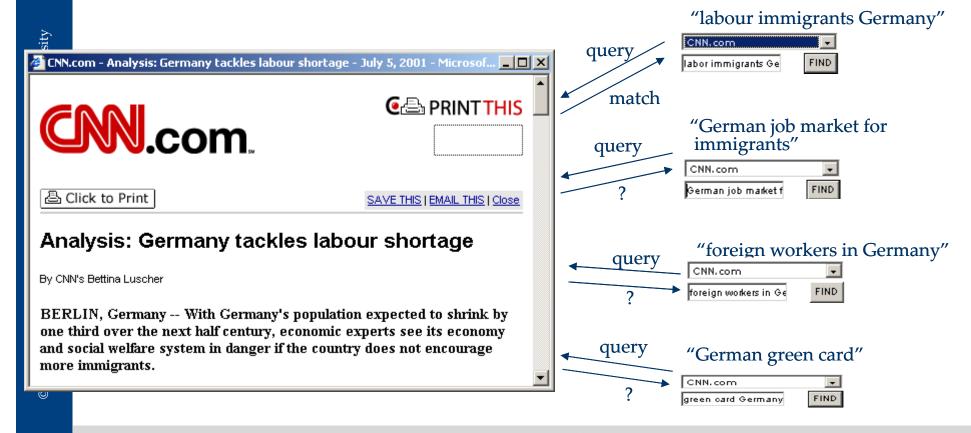
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Robust Information Retrieval — Beyond Keyword-based Search

Vocabulary Mismatch Problem

- different people using different vocabulary to describe the same concept
- matching queries and documents based on keywords is insufficient





The lost meaning of words

- Polysemy: words with multiple meanings
 - The vector space model is unable to discriminate between different meaning of the same word.

$$sim(d, q) < cos(\angle(\overrightarrow{d}, \overrightarrow{q}))$$

- Synonymy: separate words that have the same meaning.
 - No associations between words are made in the vector space representation

$$sim(d, q) > cos(\angle(\overrightarrow{d}, \overrightarrow{q}))$$

There is a disconnect between topics and words



Language Model Paradigm in IR

- Probabilistic relevance model
 - Random variables

 $R_d \in \{0,1\}$: relevance of document d

 $q \subseteq \Sigma$: query, set of words

Bayes' rule

query q to ask for relevant d

probability of generating a prior probability of relevance for document d (e.g. quality, popularity)

$$P(R_d = 1|q) = \frac{P(q|R_d = 1) \cdot P(R_d = 1)}{P(q)}$$

probability that document d is relevant for query q



Language Model Paradigm

$$P(R_d = 1|q) \propto P(q|R_d = 1) P(R_d = 1)$$
(1)

- 1 First contribution: **prior probability of relevance**
 - simplest case: uniform (drops out for ranking)
 - **popularity**: document usage statistics (e.g. library circulation records, download or access statistics, hyperlink structure)

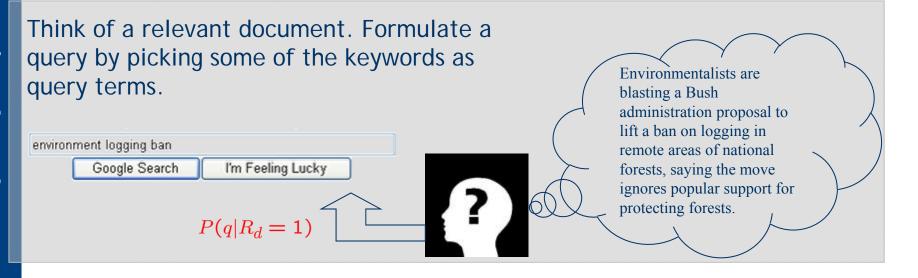
- Second contribution: query likelihood
 - query terms q are treated as a sample drawn from an (unknown) relevant document



Language Model Paradigm

Query generation model: how might a query look like that would ask for a specific document?

- Maron & Kuhns: Indexer manually assigns probabilities for pre-specified set of tags/terms
- Ponte & Croft: Statistical estimation problem





Query Likelihood

$$P(q|R_d = 1) \equiv P(q|d)$$

▶ Independent Assumption

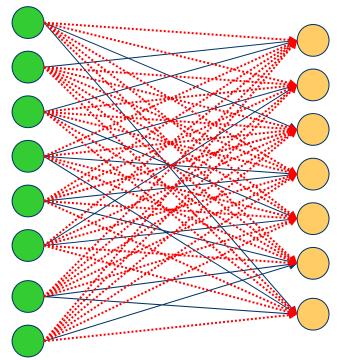
$$P(q|d) = \Pi_{w \in q} P(w|d)$$

P(w|d)?



Naive Approach





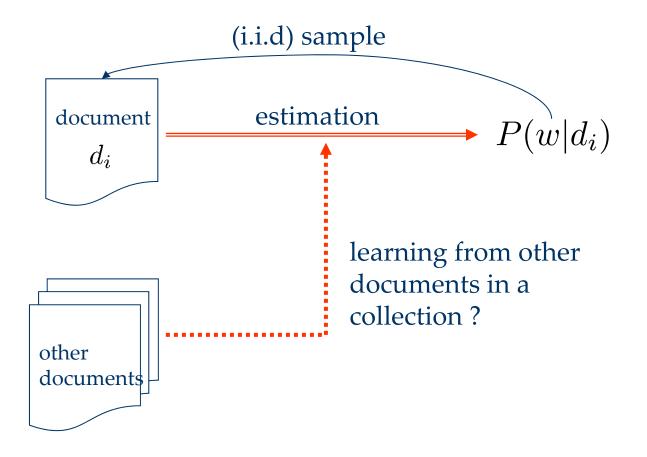
Maximum Likelihood Estimation

number of occurrences of term w in document d $\widehat{P}(w|d) = \frac{n(d,w)}{\sum_{w'} n(d,w')}$

Zero frequency problem: terms not occurring in a document get zero probability



Estimation Problem

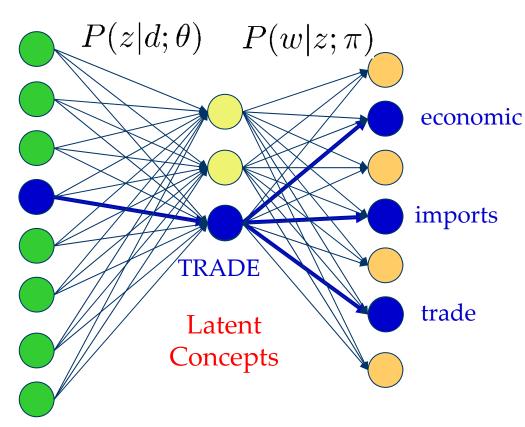


► Crucial question: In which way can the document collection be utilized to improve probability estimates?



Probabilistic Latent Semantic Analysis

Documents Terms



$$\widehat{P}(w|d) = \sum_{z} P(w|z)P(z|d)$$

Concept expression probabilities are estimated based on all documents that are dealing with a concept.

"Unmixing" of superimposed concepts is achieved by statistical learning algorithm.



Probabilistic Latent Semantic Analysis

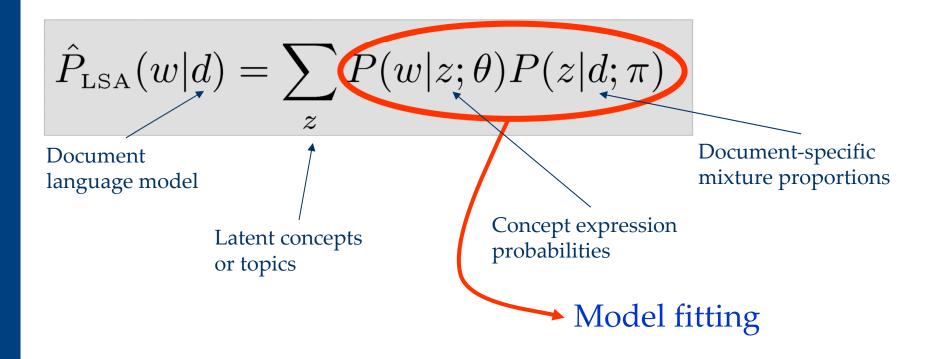
- ▶ PLSA evolved from Latent semantic analysis, adding a sounder probabilistic model
- ▶ It was introduced in 1999 by Thomas Hofmann (UAI'99)
- It is related to non-negative matrix factorization (NMF)





pLSA – Latent Variable Model

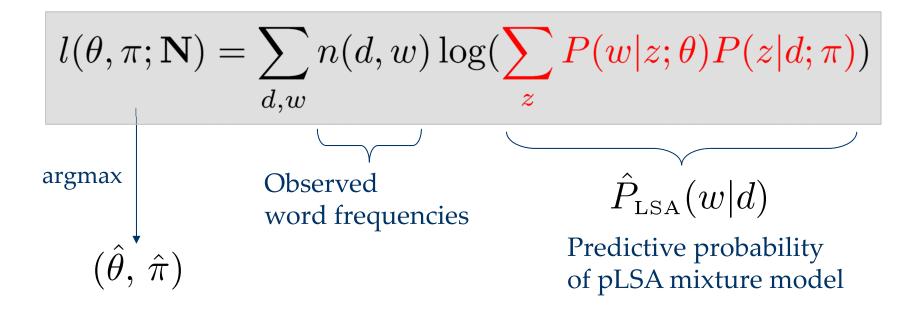
Structural modeling assumption (mixture model)





pLSA via Likelihood Maximization

Log-Likelihood



▶ Goal: Find model parameters that maximize the log-likelihood, i.e. maximize the average predictive probability for observed word occurrences (non-convex optimization problem)



EM Algorithm: Derivation

Q-parameterized lower bound on log-likelihood

$$l(\theta, \pi; Q) = \sum_{\langle d, w, r \rangle} \sum_{z} Q_{r}(z) \log \frac{P(w|z; \theta) P(z|d; \pi)}{Q_{r}(z)}$$
observed pairs with index r

Follows from Jensen's inequality

$$l(\theta, \pi) = \sum_{\langle d, w, r \rangle} \log \sum_{z} Q_r(z) \frac{P(w|z; \theta) P(z|d; \pi)}{Q_r(z)}$$
$$\geq \sum_{\langle d, w, r \rangle} \sum_{z} Q_r(z) \log \frac{P(w|z; \theta) P(z|d; \pi)}{Q_r(z)} = l(\theta, \pi; Q)$$



Expectation Maximization Algorithm

E step: posterior probability of latent variables ("concepts")

$$P(z|d,w) = \frac{P(z|d;\pi)P(w|z;\theta)}{\sum_{z'} P(z'|d;\pi)P(w|z';\theta)}$$

Probability that the occurence of term w in document d can be "explained" by concept z

M step: parameter estimation based on "completed" statistics

$$P(w|z;\theta) \propto \sum_{d} n(d,w) P(z|d,w), \quad P(z|d;\pi) \propto \sum_{w} n(d,w) P(z|d,w)$$

$$P(z|d;\pi) \propto \sum_{w} n(d,w) P(z|d,w)$$

how often is term w associated with concept z?

how often is document d associated with concept z?

A.P. Dempster, N.M. Laird, and D.B. Rubin, Maximum Likelihood from Incomplete Data via the EM Algorithm, Journal of Royal Statistical Society B, vol. 39, no. 1, pp. 1-38, 1977

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"Arts"	"Budgets"	"Children"	"Education"
NEW	MILLION	CHILDREN	SCHOOL
FILM	TAX	WOMEN	STUDENTS
SHOW	PROGRAM	PEOPLE	SCHOOLS
MUSIC	BUDGET	CHILD	EDUCATION
MOVIE	BILLION	YEARS	TEACHERS
PLAY	FEDERAL	FAMILIES	HIGH
MUSICAL	YEAR	WORK	PUBLIC
BEST	SPENDING	PARENTS	TEACHER
ACTOR	NEW	SAYS	BENNETT
FIRST	STATE	FAMILY	MANIGAT
YORK	PLAN	WELFARE	NAMPHY
OPERA	MONEY	MEN	STATE
THEATER	PROGRAMS	PERCENT	PRESIDENT
ACTRESS	GOVERNMENT	CARE	ELEMENTARY
LOVE	CONGRESS	LIFE	HAITI

The William Randolph Hearst Foundation will give \$1.25 million to Lincoln Center, Metropolitan Opera Co., New York Philharmonic and Juilliard School. "Our board felt that we had a real opportunity to make a mark on the future of the performing arts with these grants an act every bit as important as our traditional areas of support in health, medical research, education and the social services," Hearst Foundation President Randolph A. Hearst said Monday in announcing the grants. Lincoln Center's share will be \$200,000 for its new building, which will house young artists and provide new public facilities. The Metropolitan Opera Co. and New York Philharmonic will receive \$400,000 each. The Juilliard School, where music and the performing arts are taught, will get \$250,000. The Hearst Foundation, a leading supporter of the Lincoln Center Consolidated Corporate Fund, will make its usual annual \$100,000 donation, too.



Variations of pLSA

- Hierarchical extensions:
 - Asymmetric: MASHA ("Multinomial Asymmetric Hierarchical Analysis")
 - Symmetric: HPLSA ("Hierarchical Probabilistic Latent Semantic Analysis")
- Manifold regularizer:
 - Probabilistic Dyadic Data Analysis with Local and Global Consistency
- Generative models:
 - Latent Dirichlet allocation adds a Dirichlet prior on the perdocument topic distribution, trying to address an often-criticized shortcoming of PLSA, namely that it is not a proper generative model for new documents and at the same time avoid the overfitting problem.