

1.3

August 31, 2025

$$\begin{array}{ccccc} A & B & C & D & E \\ (4 \times 5) & (4 \times 5) & (5 \times 2) & (4 \times 2) & (5 \times 4) \end{array}$$

Determine whether the given matrix expression is defined. For those that are defined give size of the resulting matrix.

1 a)

$$BA$$

c)

$$AC + D$$

$$A = \begin{bmatrix} 3 & 0 \\ -1 & 2 \\ 1 & 1 \end{bmatrix}, \quad B = \begin{bmatrix} 4 & -1 \\ 0 & 2 \end{bmatrix}, \quad C = \begin{bmatrix} 1 & 4 & 2 \\ 3 & 1 & 5 \end{bmatrix}, \quad D = \begin{bmatrix} 1 & 5 & 2 \\ -1 & 0 & 1 \\ 3 & 2 & 4 \end{bmatrix}, \quad E = \begin{bmatrix} 6 & 1 & 3 \\ -1 & 1 & 2 \\ 4 & 1 & 3 \end{bmatrix}$$

Compute Matrices if defined

3 e)

$$2B - C$$

g)

$$-3(D + 2E)$$

i)

$$\text{tr}(D)$$

4 a)

$$2A^T + C$$

g)

$$2E^T - 3D^T$$

5 c)

$$(3E)D$$

d)

$$(AB)C$$

g)

$$(DA)^T$$

i)

$$\text{tr}(DD^T)$$

In each part of Exercises 11–12, find matrices A , \mathbf{x} , and \mathbf{b} that express the given linear system as a single matrix equation $A\mathbf{x} = \mathbf{b}$, and write out this matrix equation.

11 b)

$$\begin{array}{rcl} 4x_1 - 3x_3 + x_4 & = & 1 \\ 5x_1 + x_2 - 8x_4 & = & 3 \\ 2x_1 - 5x_2 + 9x_3 - x_4 & = & 0 \\ 3x_2 - x_3 + 7x_4 & = & 2 \end{array}$$