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Class: CSc 335

Date: Mar 9, 2023

Pascal Triangle

The (r,c) entry should be $\binom{r}{c}$, which would require $c \le r$ and both r,c are non-negative integers.

From the table

$$\binom{5}{3} = \binom{4}{2} + \binom{4}{3}$$

and similarly across the table,

$$\binom{r}{c} = \binom{r-1}{c-1} + \binom{r-1}{c}$$

Suggesting for the recursion.

```
(pas r c) = (+ (pas (- r 1) (- c 1)) (pas (- r 1) c))
```

where the induction is on r.

Does Zero-based indexing deliver this?

Yes, by checking a few entries.

Divide & Conquer alone of course is not enough - we need the stopping condition(s) as well.

Observe:

$$c = 0 \Rightarrow {r \choose c} = 1$$

$$c = r \Rightarrow {r \choose c} = 1$$

Pre-conditions:

• $c \le r$ & both are non-negative integers

- still need to check the termination, and that the pre-condition holds ahead of each recursive call
- A termination condition is an argument where the stopping condition has been reached.

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Higher-Order Procedures

- 1. Passing functions as a parameters
- 2. Return functions as values from procedure calls

Supposed instead of $\sum_{i=a}^b i$, we want to compute $\sum_{i=a}^b i^2 or \sum_{i=a}^b i^3$, or generally $\sum_{i=a}^b (term\ i)$, where $term=N^{\geq 0}=>R$

• $N^{\geq 0} => R$ needs to be added in the pre-condition.

To avoid rewriting what is essentially the same code, we **ABSTRACT** the sigma function by introducing a new parameter - call it term.

- term is a function as it is a parameter, we need to mention it in the pre-condition.
- Termination argument
 - and also term(a) returns a value for the N → R

We can abstract again

• Everytime we abstract the code, we have to worry about the termination argument.

 And again - perphaps we're not always interested in the plus. So we can introduce the parameter combiner