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Class: CSc 335

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## Strong induction

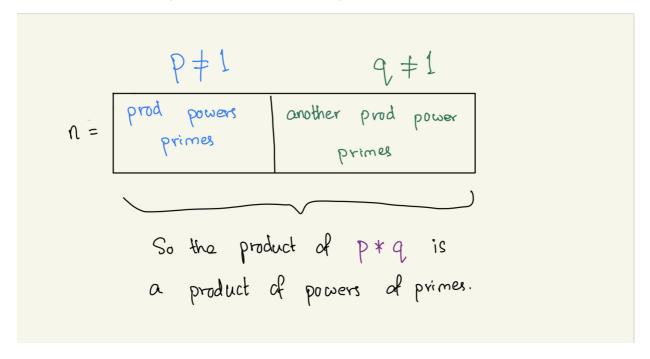
Motivation: We will need strong induction when we begin discussing data structures.

Prove: every integer  $n \ge 2$  can be written as a product of powers of primes (proof by strong induction)

Try inducting on n, with divide & conquer: if n = p \* q, with neither p nor q equal to 1. Then assume p is a product of powers of primes and also that q is a product of powers of primes.

Now that we have the divide & conquer strategy, here is the full argument

- Consider  $n \ge 2$ 
  - If n = 2, there's nothing to show, since 2 = 2' is a product of powers of primes.
- Consider n > 2
  - $\circ$  Either n is prime or not n i.e. composite
  - o If n is prime, we're done.
  - Otherwise, n = p \* q for some integers p, q > 1 [def. of composite number]
  - Now the argument is the one we just gave.



This is a strong induction because

- 1. We know neither p nor q is\$n-1\$
- 2. We don't know in advance the values of the factors p and q So we actually need all of the hypotheses.

## Tree Recusion

;; Fib-sequence

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- ullet a cool technique is memoization ullet to transform the results of a function into something to remember
  - example: creating a dictionary to remember the value of fib 2 or fib 3 in computing fib 5

## What about an iterative solution?

A design idea flows from the def of fib(n+1) as fib(n) + fib(n-1) when  $n \ge 2$ . where

If we introduce curr and prev as variables with design roles:

```
curr = (fib n)
prev = (fib (- n 1))
```

with the idea of maintaining these with as count increases from 0 up to n.

i.e.: Take the GI as the logical AND of the design roles:

• GI:

```
next = curr + prev
where next = fib(count)
```