# Final project: "Stacking for improving neural optimal transport based style-transfer models"

Team:
Nikita Bogdanov
Daniil Panov
Anastasia Gavrish
Nikita Vasilev
Nikolay Kashin
TA: Nikita Gushchin



#### Unpaired image to image translation:

First image sample













Second image sample [1]

As input: two unpaired data sets
As output: some mapping function

How to find a mapping between input and output set of images?

#### **Generative models**

First image sample



Mapping









Approaches such as:

**GAN** 

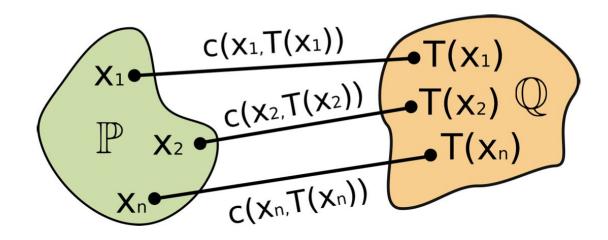
Diffusional models

VAE

**Neural Optimal Transport** 

Second image sample [1]

### **Optimal transport Monge's formulation**



Visualisation of Monge's OT formulation [1]

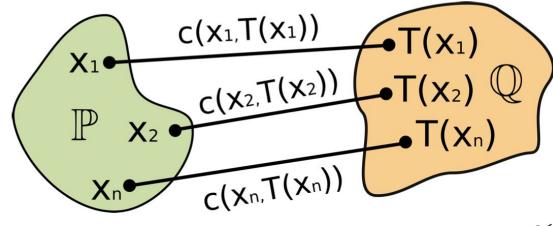
P $\in$ P(X), Q $\in$ P(Y) and a cost function c:X × Y $\rightarrow$ R, Monge's primal formulation of OT cost is

$$\operatorname{Cost}(\mathbb{P},\mathbb{Q}) \stackrel{\mathrm{def}}{=} \inf_{T_{\#}\mathbb{P} = \mathbb{Q}} \int_{\mathcal{X}} c\big(x,T(x)\big) d\mathbb{P}(x),$$

where the minimum is taken over measurable functions (transport maps)  $T: X \rightarrow Y$  that map P to Q.

The optimal T\* is called OT map

#### Max min reformulation of OT problem



Max min reformulation was applied for the problem

$$\operatorname{Cost}(\mathbb{P}, \mathbb{Q}) = \sup_{f} \inf_{T} \mathcal{L}(f, T),$$

where

$$\mathcal{L}(f,T) = \int \frac{||x-T|(x)||_2^2}{2} d\mathbb{P}(x) + \int f(y)d\mathbb{Y} - \int f(T|(x))d\mathbb{P}(x)$$

Visualisation of Monge's OT formulation [1]

f is an upper-bounded continuous function

### Max min reformulation of OT problem on practice

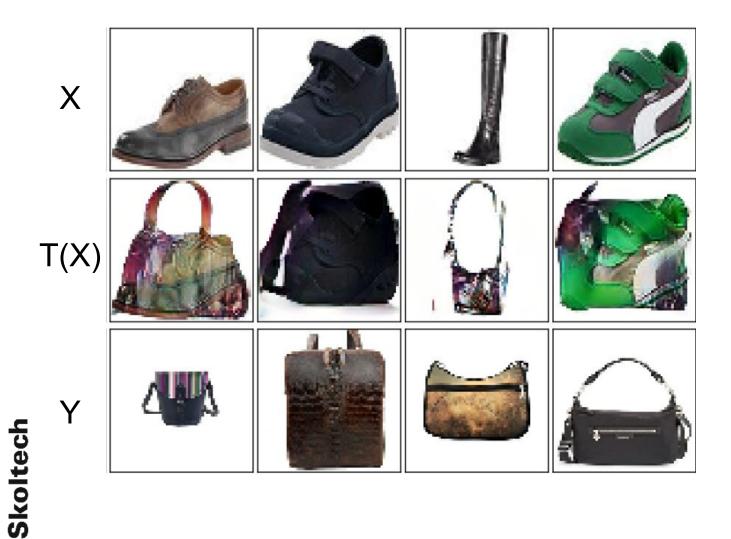
$$\sup \inf \mathcal{L}(\omega, \theta) = \int \frac{||x - T_{\theta}(x)||_{2}^{2}}{2} d\mathbb{P}(x) + \int f_{\omega}(y) d\mathbb{Y} - \int f_{\omega}(T_{\theta}(x)) d\mathbb{P}(x)$$

ResNet for kind of discrimination  $f_{\omega}: \mathbb{R}^{3 \times H \times W} \to \mathbb{R}$ 

UNet for kind of generation  $T_{\theta} : \mathbb{R}^{3 \times H \times W} \to \mathbb{R}^{3 \times H \times W}$ 

Shoes (3x64x64) dataset mapping to Bags(3x64x64) dataset

#### **Problem statement**



It is possible to find mapping function but the it is not ideal (high FID).

How to improve?

#### **Problem statement and motivation**

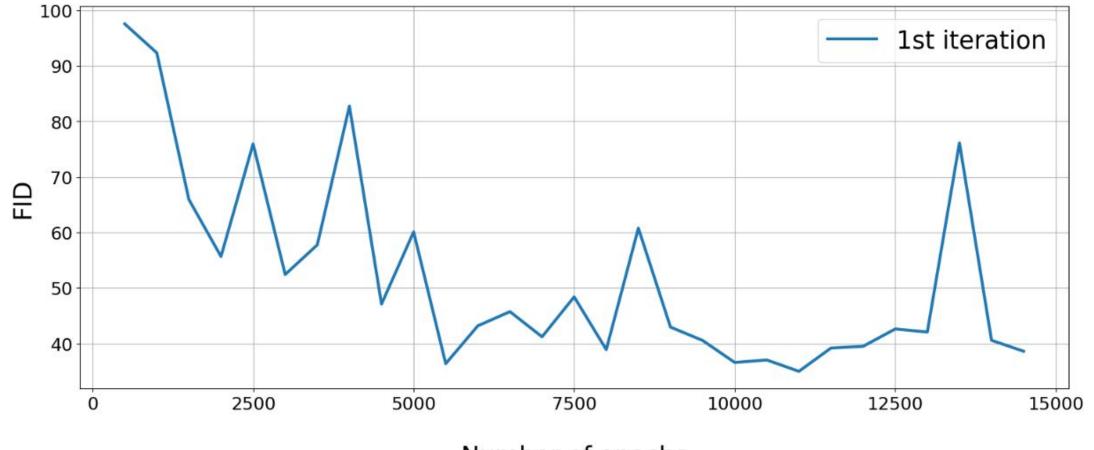


Try to stack more models.

The hypothesis that next generation of models will improve on defects of the previous generation.

Estimated parameter: FID

#### Results zero levels of stacking



Number of epochs

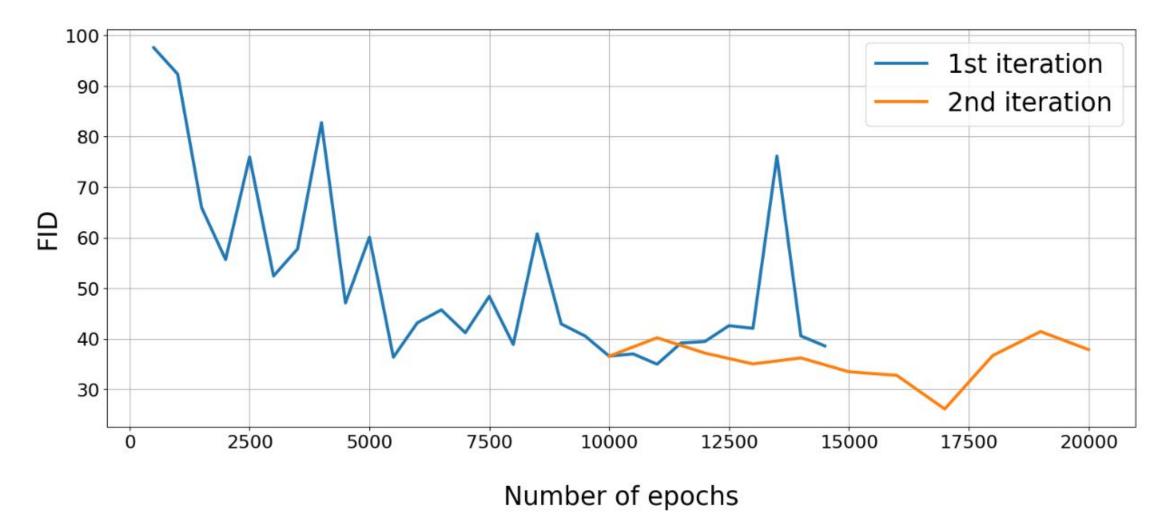
Shoes to Bags minimal FID is 34.9.

## Results zero levels of stacking



Shoes to Bags min FID is 34.9

#### Results one level of stacking



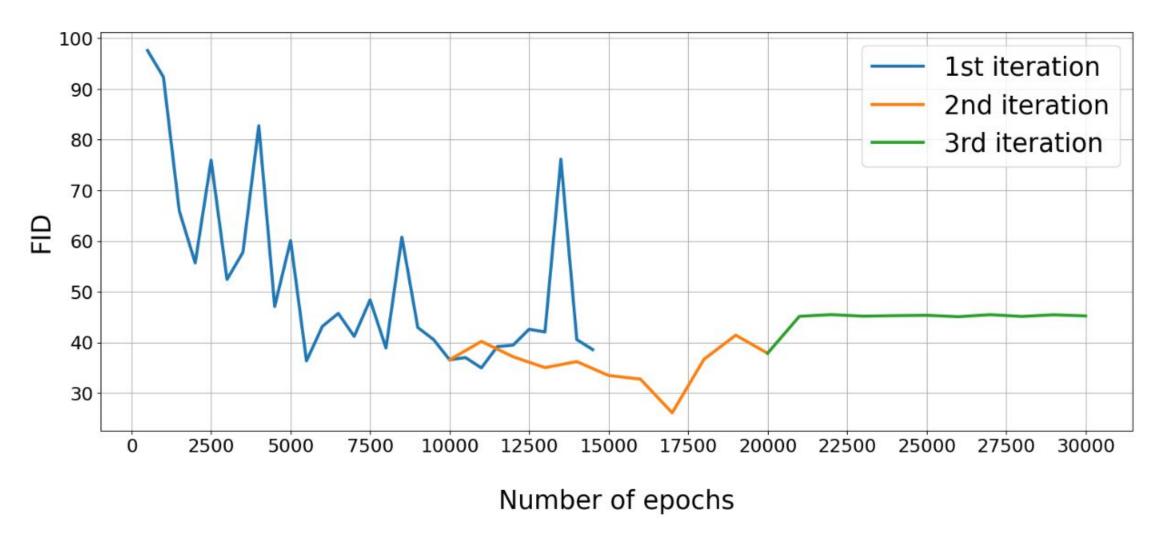
Bags from shoes to Bags min FID is 26.2 (orange line)

#### Results one level of stacking



Bags from shoes to Bags min FID is 26.2

#### Results two levels of stacking



Bags from shoes to Bags min FID is 38.9 (green line)

#### Results two levels of stacking



Bags from the first stack to Bags min FID is 38.9

### Results of stacking 3 models



#### **Conclusions**

- Model stacking was applied to Neural Optimal Transport realisation from Korotin et al.
   [1] for shoes to handbag image to image translation problem
- One level of stacking helps to obtain minimal FID compare to initial model. However, the second level provides no improvement compare to both initial model and the first level of stacking.

NOT Stacks number	Min FID
0 (no stacking)	34.9
1	26.2
2	38.9

#### Our team



Our TA Nikita Gushchin



Daniil Panov



Nikita Vasilev



Anastasia Gavrish

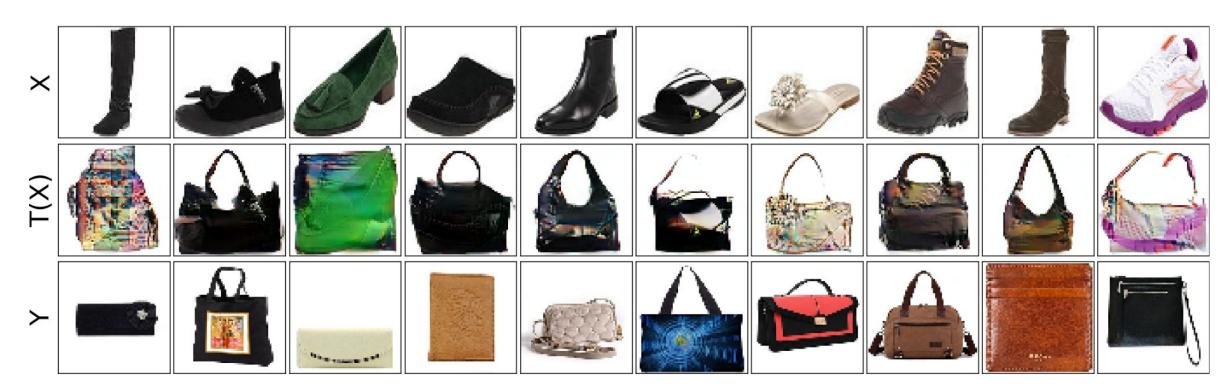


Nikolay Kashin



Nikita Bogdanov

### Results zero levels of stacking



Shoes to Bags min FID is 36.

### Results one level of stacking



MAKE SIMMILAR
PICTURES THAT SHOW
IMPROVMENT

T(T(X))

Mapping T(x) on Y







