

## Association Rule

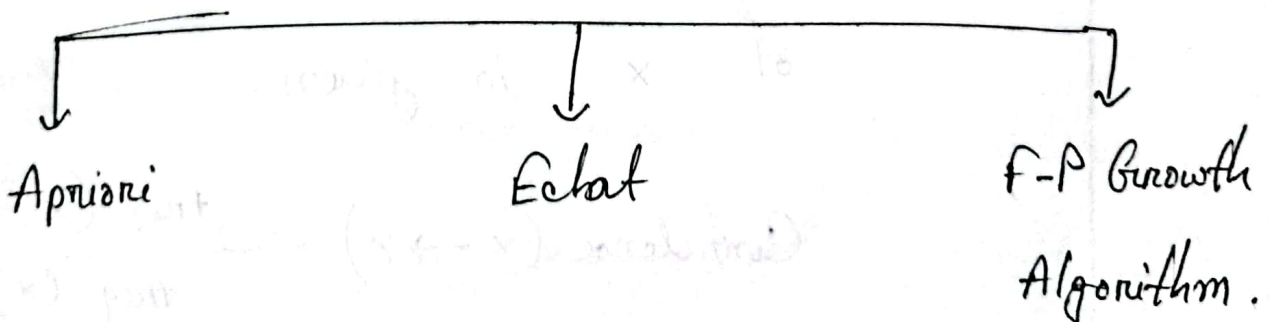
It is a type of learning technique that checks for dependency of one data item on another data item and maps accordingly, so that it can be more profitable.

### Representation

→ If items "coffee" are purchased, then the possibility of buying "sugar" is ... which can be represented by:

→  $\{ \text{Coffee} \} \rightarrow \{ \text{Sugar} \}$

### ARL (Unsupervised)



Working : Support. "People who bought  
Confidence also bought."  
lift.

Support  $\rightarrow$  frequency of item (x)

$$\text{Support} = \frac{\text{frequency (x)}}{\text{Total transaction}} \%$$

\*\*\* Support count = frequency of x.

Confidence = it indicates how often the items  
x and y both occur together in  
dataset, when the occurrence  
of x is given.

$$\text{Confidence (x} \rightarrow \text{y)} = \frac{\text{freq (x, y)}}{\text{freq (x)}}$$

lift  $\Rightarrow$  it is the strength of any value rule.

$$= \frac{\text{Support}(x, y)}{\text{Support}(x) \cdot \text{Support}(y)}$$

or,

$$= \frac{\text{Confidence}(x \rightarrow y)}{\text{Support}(y)}$$

if, lift = 1, items independent to each other.

if, lift > 1, items dependent to each other.

if lift < 1, one item is substitute for other items.

Application

$\rightarrow$  Market Basket analysis

$\rightarrow$  Medical Diagnosis.

$\rightarrow$  Protein Sequence.

### Example

Step 1: Set a minimum support and confidence.

Step 2: Take all the subsets in transactions having higher support than minimum support.

Step 3: Take all the Rules of those subsets having higher confidence than minimum confidence.

Step 4: Sort the rules by decreasing lift.

<u>Transaction id</u>	<u>Item Sets</u>
T <sub>1</sub>	A, B
T <sub>2</sub>	B, D
T <sub>3</sub>	B, C
T <sub>4</sub>	A, B, D
T <sub>5</sub>	A, C
T <sub>6</sub>	B, C
T <sub>7</sub>	A, C
T <sub>8</sub>	A, B, C, E
T <sub>9</sub>	A, B, C



Given, minimum Support = 2

minimum confidence = 50%

Apply Apriori algorithm

1) Calculate  $C_1 \in$  Candidate set.

$L_1 \in$  frequent item set.

$C_1 =$	Item set	Support count
	A	6
	B	2
	C	6
	D	2
	E	1

$L_1 =$	Item set	Support count
	A	6
	B	2
	C	6
	D	2

all the itemset  
have greater  
or equal than  
minimum support

$C_2$	<u>Item set</u>	<u>Support count</u>
	{A, B}	4
	{A, C}	4
	{A, D}	1
	{B, C}	4
	{B, D}	2
	{C, D}	0

$L_2$	<u>Item Set</u>	<u>Support count</u>
	{A, B}	4
	{A, C}	4
	{B, C}	4
	{B, D}	2

$C_3$	<u>Item Set</u>	<u>Support Count</u>
	{A, B, C}	2
	{A, B, D}	1
	{B, C, D}	0
	{A, C, D}	0

$$L_3 = \frac{\text{Item Set}}{\{A, B, C\}} \quad \frac{\text{Support Count}}{2}$$

finding Association Rules for subsets:

→ we will calculate the confidence  $\frac{\text{Sup}(A, B)}{\text{Sup}(A)}$

↓

→ we will exclude rules that have less confidence than min threshold (50%)

<u>Rules</u>	<u>Support</u>	<u>Confidence</u>
$\{A, B\} \rightarrow C$	2	$\frac{\text{Sup}(\{A, B\}, C)}{\text{Sup}(A, B)}$ $= \frac{2}{4}$ $= 50\%$
$\{B, C\} \rightarrow A$	2	$= \frac{2}{4} = 50\%$
$\{A, C\} \rightarrow B$	2	$= \frac{2}{4} = 50\%$

$$C \rightarrow (A, B) \quad 2 \quad \frac{2}{6} = 33.33\%$$

$$A \rightarrow (B, C) \quad 2 \quad \frac{2}{6} = 33.33\%$$

$$B \rightarrow (A, C) \quad 2 \quad \frac{2}{7} = 28\%$$

So the first 3 Rules  $(A, B) \rightarrow C$

$$(B, C) \rightarrow A$$

$$(A, C) \rightarrow B$$

Can be considered as the strong association Rules for given problem.

→ Related algorithm questions → check MC A-2 Course Pdf.



Institute of Information Technology  
Noakhali Science and Technology University

Course Code: CSE-4213  
Duration: 30 Minutes

[Class Test-2]

Course Title: Applied Data Science  
Full Marks: 15

*Answer all the following questions*

1. Consider the transaction dataset given as follows.

TID	Items
T1	11, 12, 15
T2	12, 14
T3	12, 13
T4	11, 12, 14
T5	11, 13
T6	12, 13
T7	11, 12, 13, 15
T8	11, 13
T9	11, 12, 13

- (a) Generate association rules for the items where minimum support count is 2 and minimum confidence is 60%. 3
- (b) Calculate the value of *confidence* ( $\{12, 13\} \Rightarrow \{11\}$ ) and *confidence* ( $\{11\} \Rightarrow \{12, 13\}$ ). 2
2. Dr. Strange have applied hierarchical clustering and got two clusters,  $C1 = \{(1,1), (2,2), (3,1)\}$  and  $C2 = \{(5,3), (6,4)\}$ . Now he wants to approximate the distance between these two clusters. [Note: Dr. Strange will apply Euclidean distance as it is his favorite distance metric.]
- (a) Calculate the distance between  $C1$  and  $C2$  applying single link distance measure. 1
- (b) Calculate the distance between  $C1$  and  $C2$  applying average link distance measure. 1
- (c) Calculate the distance between  $C1$  and  $C2$  applying complete link distance measure. 1
- (d) Calculate the distance between  $C1$  and  $C2$  applying centroid based distance measure. 1
3. A perceptron can learn the operation *OR* but not Exclusive-OR (*XOR*).
- (a) Why do you think a perceptron cannot learn the *XOR* operation whether it learns the *OR* operation? 3
- (b) How can you cope with the problem and propose a way so that *XOR* operation can be learnt? 3

Good Luck!

## Exam Question Solution

<u><math>C_1</math></u>	<u>Item</u>	<u>Support count</u>
	$T_1$	6
	$T_2$	2
	$T_3$	6
	$T_4$	2
	$T_5$	2

<u><math>L_1</math></u>	<u>Item</u>	<u>Support Count</u>
	$T_1$	6
	$T_2$	2
	$T_3$	6
	$T_4$	2
	$T_5$	2

$C_2$        $\Pi_{\text{term}}$       Support count

$(T_1, T_2)$       4

$(T_1, T_3)$       4

$(T_1, T_4)$       1

$(T_1, T_5)$       2

$(T_2, T_3)$       4

$(T_2, T_4)$       2

$(T_2, T_5)$       2

$(T_3, T_4)$       0

$(T_3, T_5)$       1

$(T_4, T_5)$       0

$L_2$

$(T_1, T_2)$       4

$(T_1, T_3)$       4

$(T_1, T_5)$       2

$(T_2, T_3)$       4

$(T_2, T_4)$       2

$(T_2, T_5)$       2

c<sub>3</sub>

$$(\mathbb{I}_1, \mathbb{I}_2, \mathbb{I}_3) \longrightarrow 2$$

$$(\mathbb{I}_1, \mathbb{I}_2, \mathbb{I}_4) \longrightarrow 1$$

$$(\mathbb{I}_1, \mathbb{I}_2, \mathbb{I}_5) \longrightarrow 2$$

$$(\mathbb{I}_2, \mathbb{I}_3, \mathbb{I}_4) \longrightarrow 0$$

$$(\mathbb{I}_2, \mathbb{I}_3, \mathbb{I}_5) \longrightarrow 1$$

$$(\mathbb{I}_2, \mathbb{I}_4, \mathbb{I}_5) \longrightarrow 0$$

(

c<sub>3</sub>

$$(\mathbb{I}_1, \mathbb{I}_2, \mathbb{I}_3) \longrightarrow 2$$

$$(\mathbb{I}_1, \mathbb{I}_2, \mathbb{I}_5) \longrightarrow 2$$

c<sub>4</sub>

$$(\mathbb{I}_1, \mathbb{I}_2, \mathbb{I}_3, \mathbb{I}_4) \longrightarrow 0$$

$$(\mathbb{I}_1, \mathbb{I}_2, \mathbb{I}_3, \mathbb{I}_5) \longrightarrow 1$$

$$(\mathbb{I}_1, \mathbb{I}_2, \mathbb{I}_4, \mathbb{I}_5) \longrightarrow 0$$

<u>Rules</u>	<u>Support</u>	<u>Confidence</u>
$(I_2, I_3) \rightarrow I_1$	2	$\Rightarrow \frac{2}{4}$ $= 50\%$

$(I_1) \rightarrow (I_2, I_3)$	2	$= \frac{2}{6}$ $= 33.33\%$
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