

Linear Regression.

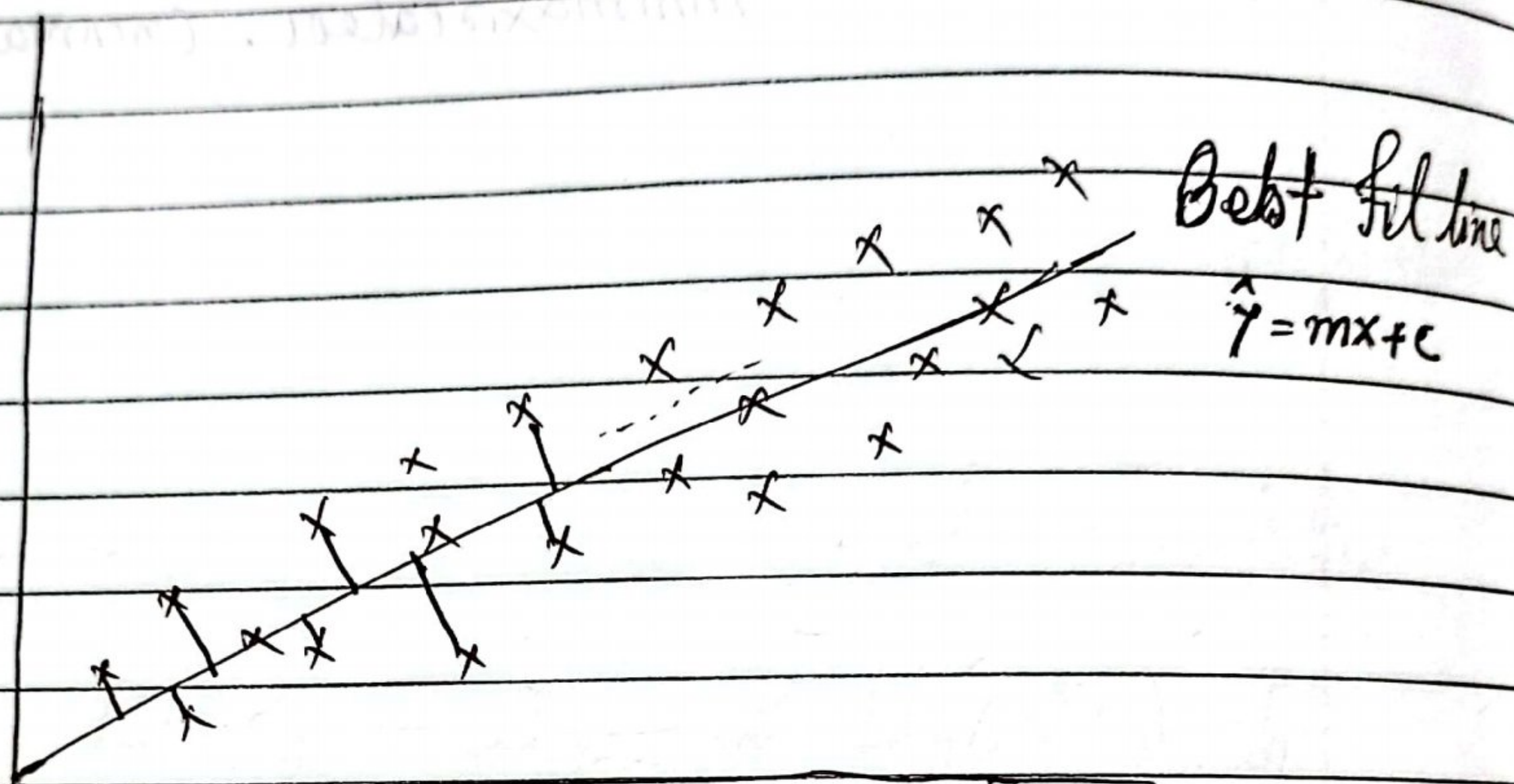
$$y = mx + c$$

when $x=0$

$m = \text{slope / Gradient / Derivative.}$

$$y = c$$

$c = \text{Intercept}$



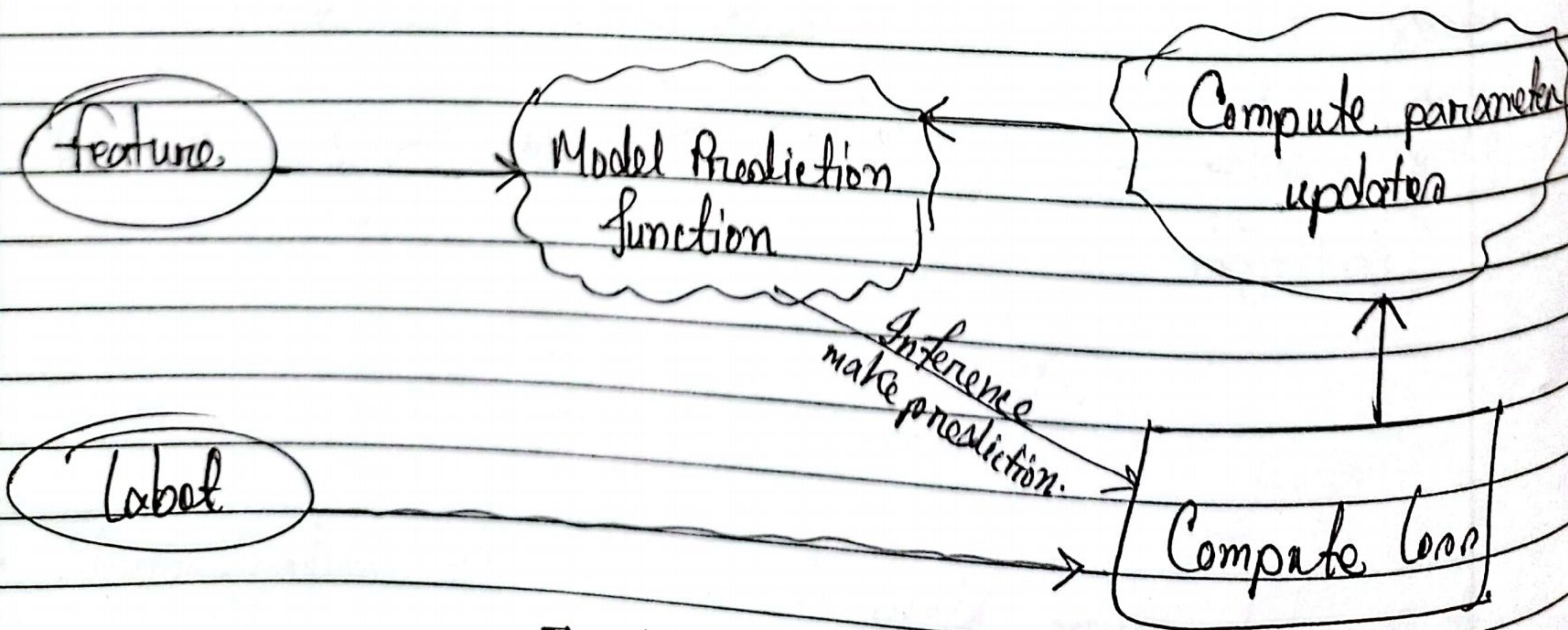
$$\frac{1}{2n} \sum_{i=1}^n (\hat{y}_i - y_i)^2$$

\hat{y}_i → Predicted Point.
 y_i → Real point.
 n → number of points.

⑤ Mean Absolute error

⑤ Mean square error.

⑤ Cost function.



Iterative approach.

$$\hat{y} = mx + c$$

$$= 1(1)$$

$$\hat{y} = 1$$

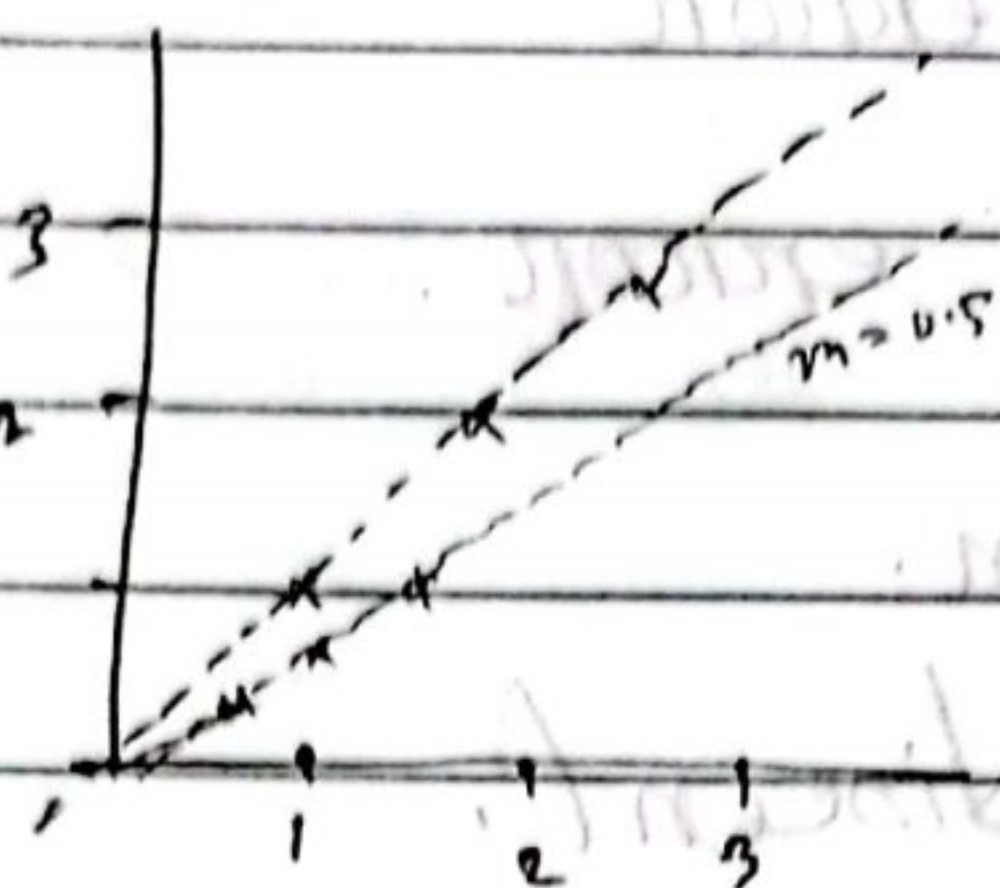
$$\hat{y} = 2$$

$$\hat{y} = 3$$

$$m = 1$$

$$n = 1, 2, 3 \dots$$

$$c = 0$$



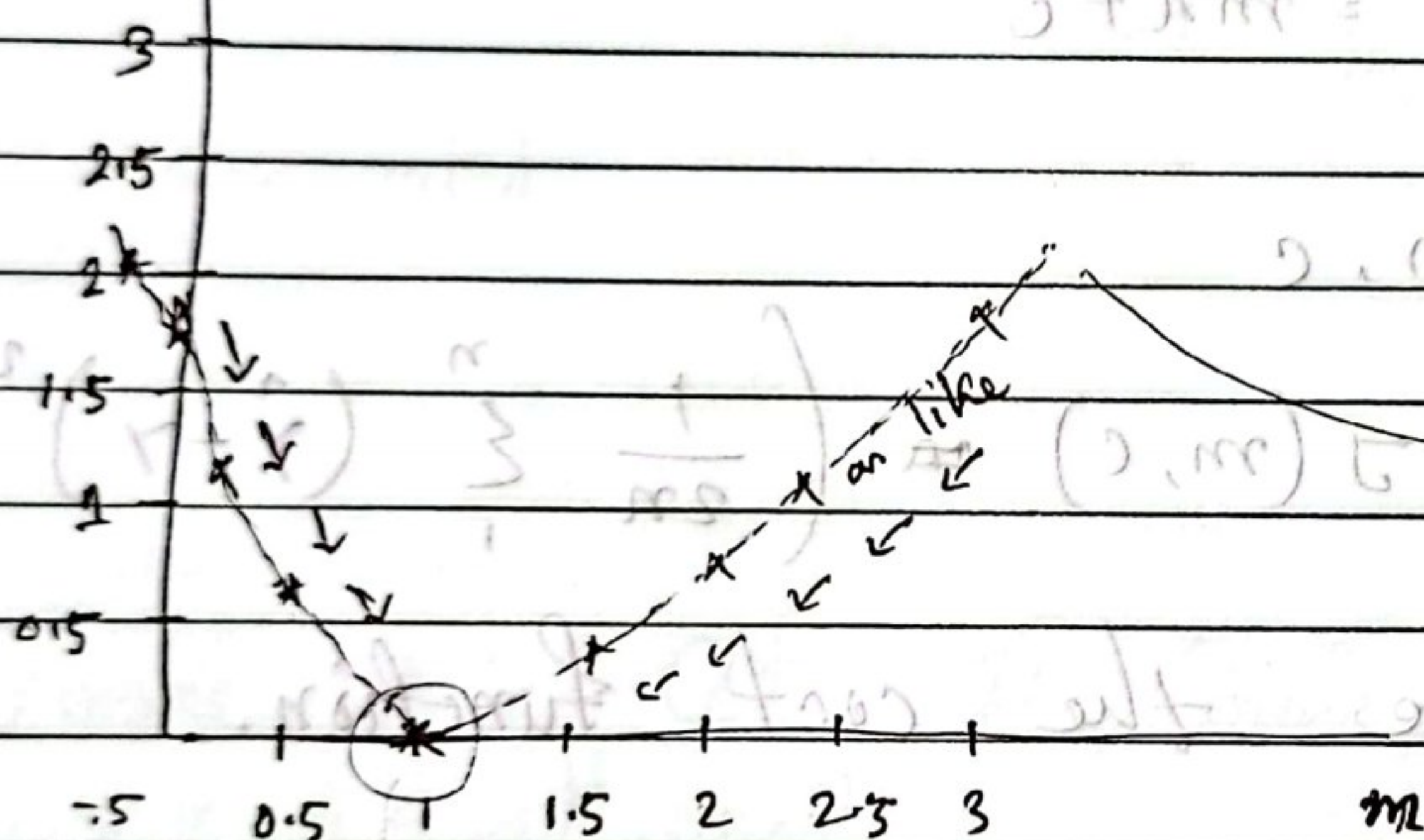
$$m = 0, 0.5, 1.0 \dots$$

$$c = 0$$

$$\text{Cost function} = \frac{1}{2 \times 3} \times [(1-1)^2 + (2-2)^2 + (3-3)^2]$$

$$= 0$$

Cost func.



Learning Rate

Gradient descent.

Step size.

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$$m = 1$$

$$\text{Cost } J = 0$$

Global minimum.

Converge theorem.

$$m = m - \frac{\partial J(m)}{\partial m} \times \alpha$$

Learning rate.

$$m = 0.5$$

$$\hat{y} = 0.5 \times 1 = 0.5$$

$$\hat{y} = 0.5 \times 2 = 1$$

$$\hat{y} = 0.5 \times 3 = 1.5$$

(Left)

$$m = m - (-ve) \times \text{small value}$$

$$= m + \text{small value}$$

(Right)

$$m = m - (+ve) \times \text{small value}$$

Learning Rate

Small value.

$$\frac{1}{2m} ((0.5-1)^2 + (1-2)^2 + (1.5-3)^2)$$

$$= \frac{1}{6} \times (0.25 + 1 + 2.25) = 0.58$$

→ not too small

→ not too large

• Mean Absolute error

$$MAE = \frac{1}{n} \sum_{i=1}^n (y - \hat{y})$$

• Mean Square error.

$$MSE = \frac{1}{2n} \sum_{i=1}^n (\hat{y} - y)^2$$

• Cost function.

• Gradient descent.

• Learning Rate (α)

Hypothesis $\hat{y} = mx + c$

Parameter m, c

$$\text{Cost function } J(m, c) = \left(\frac{1}{2n} \sum_{i=1}^n (\hat{y} - y)^2 \right)$$

Goal = minimize the cost function.

Repeat

$$H-T \quad h_0(x) = \theta_0 + \theta_1 x$$

Parameters θ_0, θ_1

$$\text{Cost function } J(\theta_0, \theta_1) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2$$

Goal : minimize $J(\theta_0, \theta_1)$

→ Start with θ_0, θ_1 and keep changing them to reduce $J(\theta_0, \theta_1)$ until we hopefully end up at a minimum.

Gradient descent algorithm.

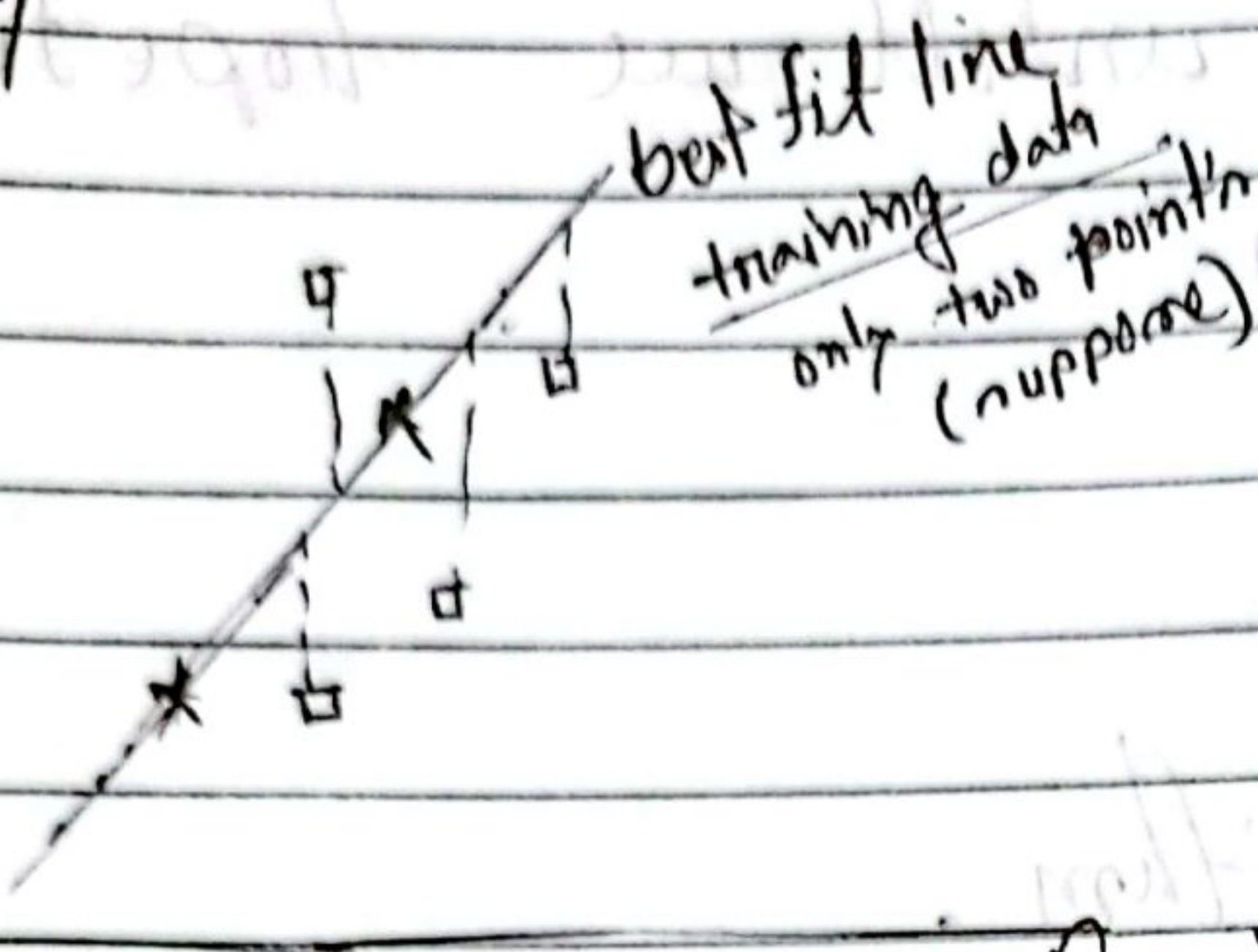
repeat until convergence

$$\theta_j := \theta_j - \frac{\partial}{\partial \theta_j} (J(\theta_0, \theta_1)) \times \alpha \quad \left. \begin{array}{l} j=0, j=1 \\ \text{learning rate} \end{array} \right\}$$

Andrew NG @ Linear Regression term and details summary in "Krish Naik" video.

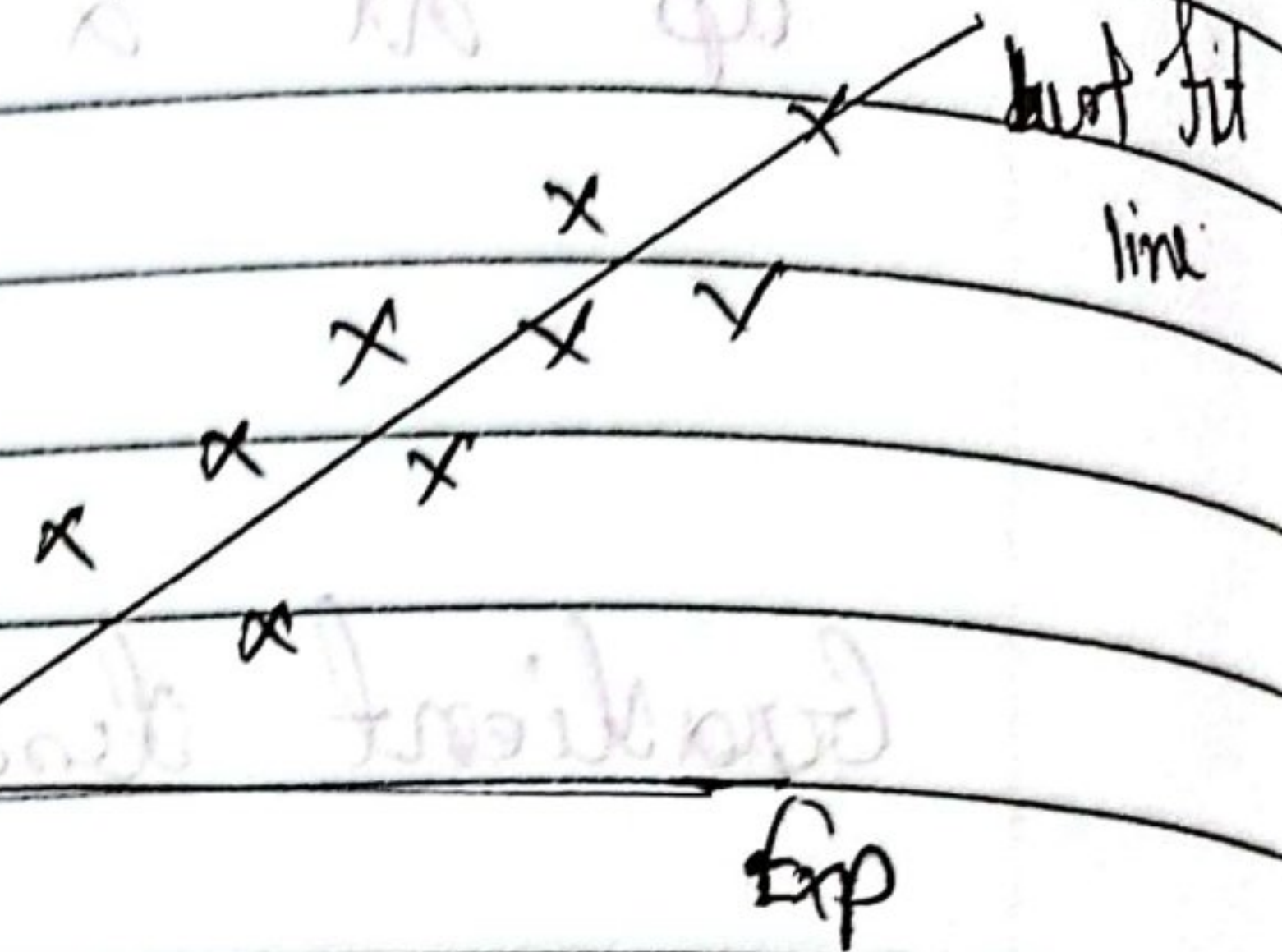
Ridge and Lasso Regression.

Salary



Experience

Salary



Exp

Cost Function

Sum of Residuals $\sum_{i=1}^n (y - \hat{y})^2 = 0$

$\hat{y} = mx + c$

In linear Regression.

but for testing data \oplus high error.

→ Overfitting → for training low error

→ " testing high "

high variance

low variance

→ Underfitting → for training data get high error and

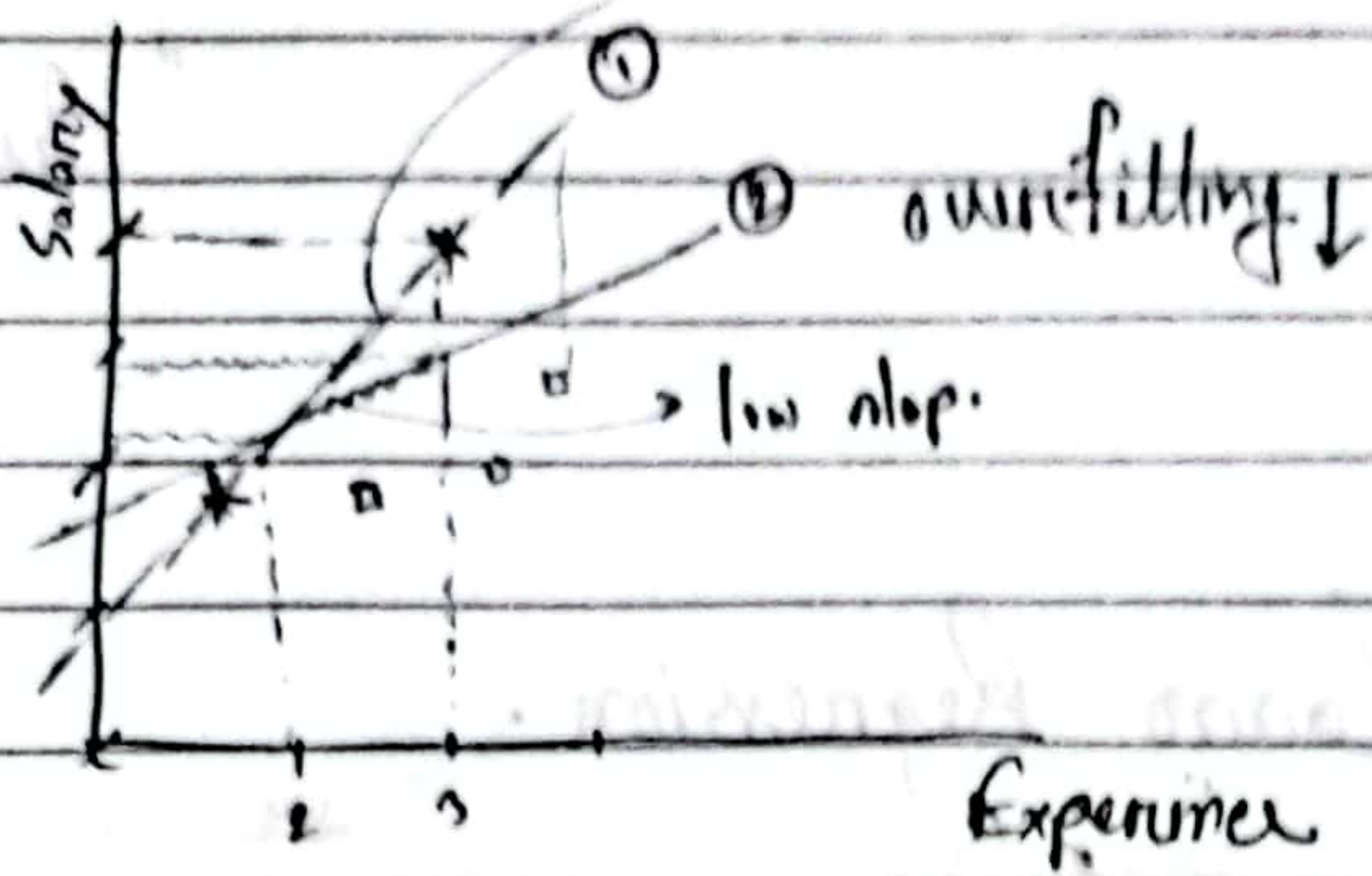
for the testing dataset getting high error.

Generalized or Good Model

Should always low bias and low variance.

By Ridge and Lasso Regression

Ridge Regression



Cost function -

$$\sum_{i=1}^n (y - \hat{y})^2 + \lambda (\text{slope})$$

Step slope
slope

① x - a single unit of change
y - a change in the value (slope)

target -> slope is low

② Small change in x-axis
small change in y-axis - (slope)

① let $\lambda = 1$ for simplicity
slope = 1.39

② slope = 1
Small value + 1 x 1²

-> 1.39 like

Cost -> 0 + 1 x 1.69

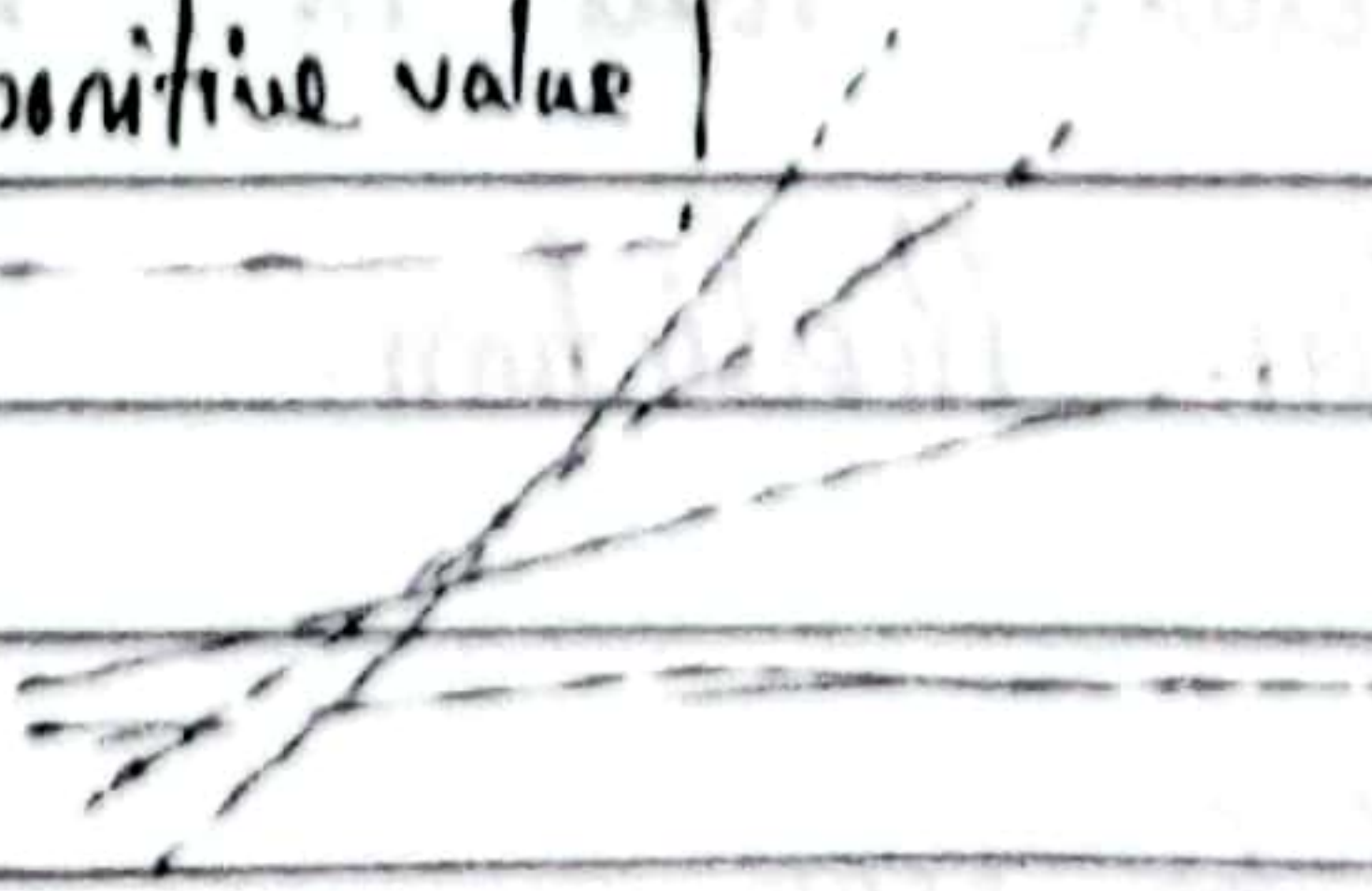
= 1.69

$\therefore 1.69 > 1.39$

② num best fit line is better than ①

-> Selected

$\lambda > 0$ to any positive value



tends to zero
not to zero

regularized

Main Aim of Ridge Regression is Reducing "Overfitting".

Lasso Regression

we

Feature Selection

Cost Function.

$$\sum_{i=1}^n (y - \hat{y})^2 + \lambda \times |\text{slope}|$$

magnitude of slope.

$$y = m_1 x_1 + m_2 x_2 + m_3 x_3 + \dots + e$$

$$\lambda |m_1 + m_2 + m_3 + m_4 + \dots|$$

slope value is very very less

those feature Remove

Moving towards zero $\rightarrow \rightarrow \rightarrow 0$

and feature will Remove.

because that is not important for Prediction.

* once a time it will be zero

"Multicollinearity"

In linear Regression.

- Keep it as usual
 - Drop the feature $[p\text{-value} > 0.05]$
- Those are highly correlated, keep only one.

"when independent variables [internally] highly Correlated" \leftarrow multicollinearity occurs.

As like Pearson Correlation

Ridge Regression also be moving towards β_1 tends to zero, but not zero.