

# Support Vector Machine.

Solve  $\rightarrow$  Classification or Regression.

Term should know.

1. Support vectors.

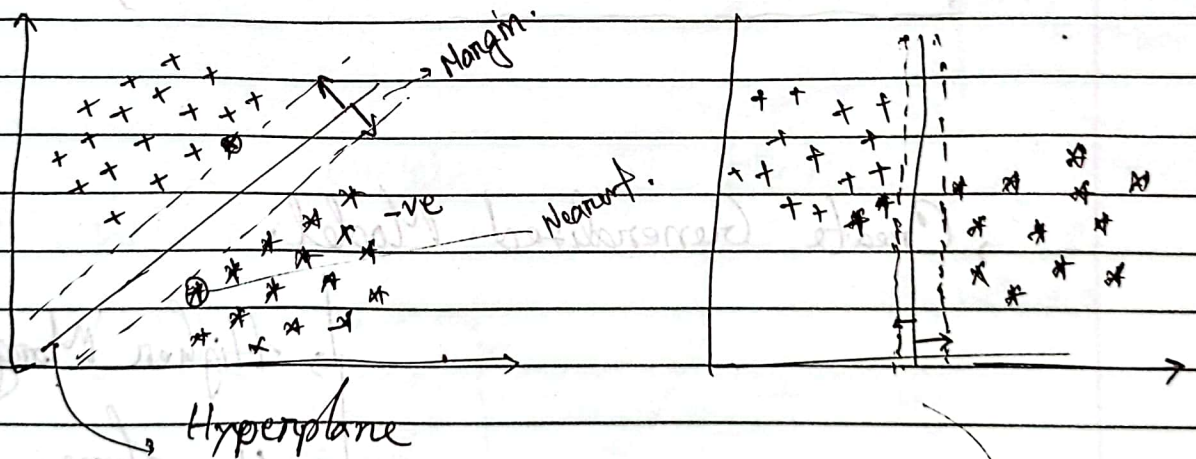
2. Hyperplanes.

3. Marginal Distance

4. Linear Separable Points.

5. Non-linear Separable Points.

Let's Consider a Classification Problem:



Aim  $\rightarrow$  Maximize the "marginal Distance"

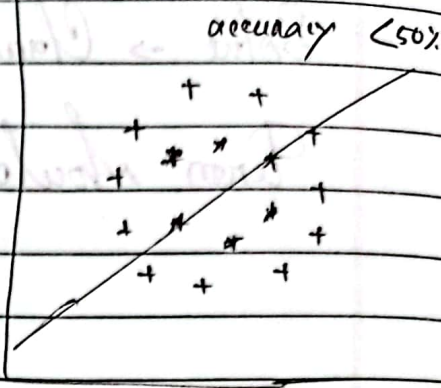
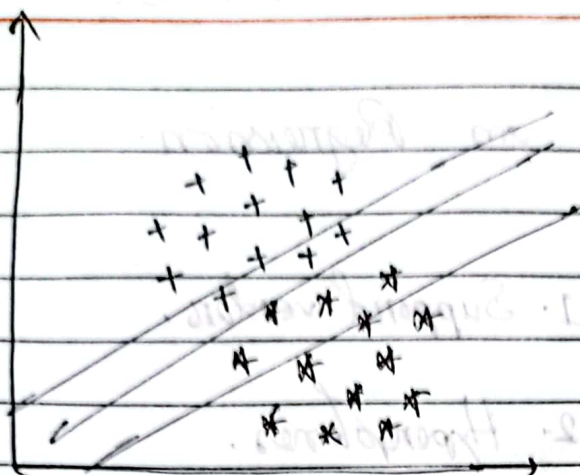
[Selected]

it may be

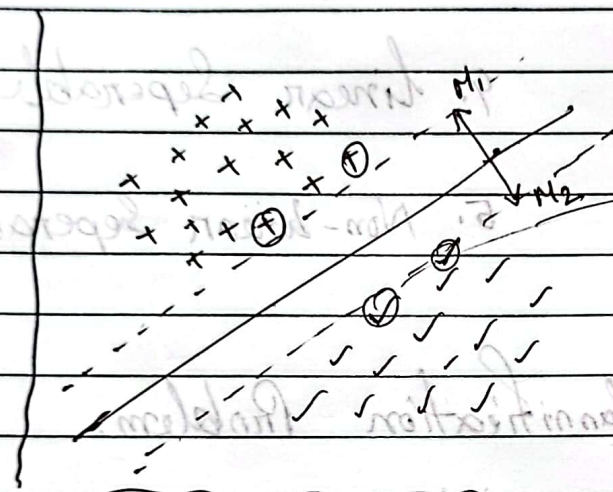
many way, many  
ways of hyperplane.

linearly Separable.  $\swarrow$  draw straight line.

2D



No linear



→ Nearest Point  
↓  
Support Vector  
↓  
Any Num of Points.

, Create Generalized Model.

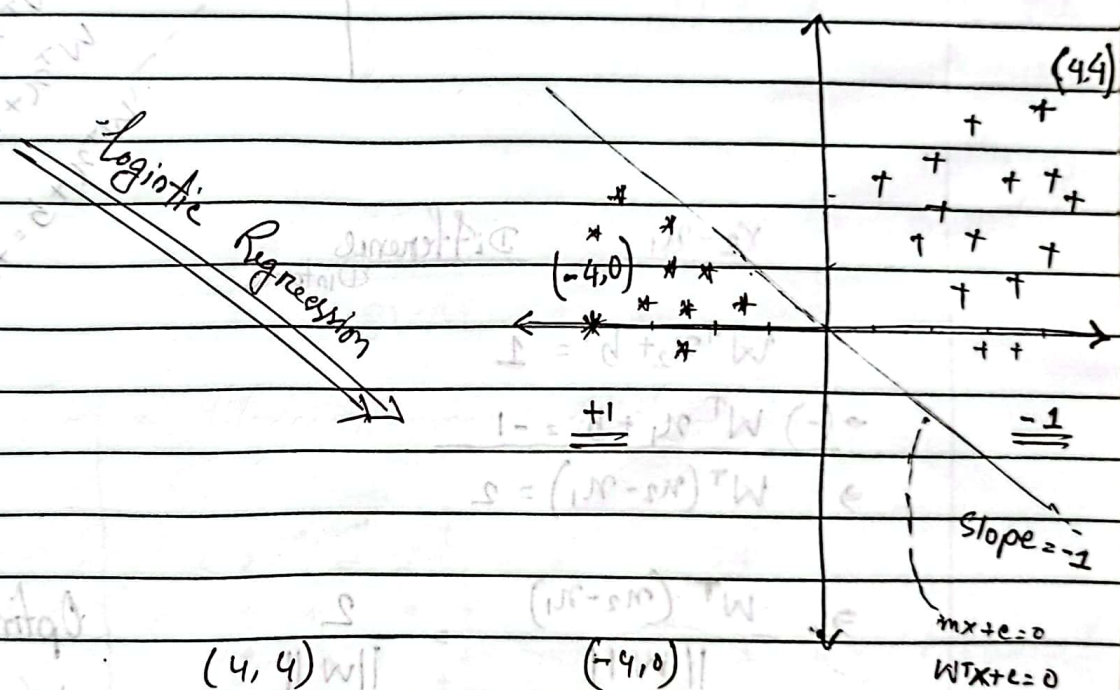
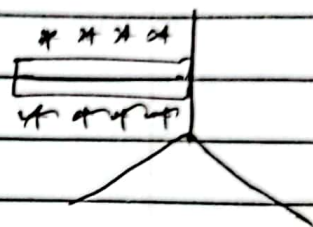
→ Higher Marginal Distance  
→ the plane

Support Vector Machine Vs Logistic Regression.

↗  
Marginal Distance  
↘



Kernel.  
SVM  $\rightarrow$  Convert's 2 Dimension (low dimension) into a  
 $\hookrightarrow$  High Dimension. if 3



$$y = W^T x + c$$

$$= \begin{bmatrix} -1 \\ 0 \end{bmatrix} \begin{bmatrix} 4 & 4 \end{bmatrix}$$

$$= -4 \quad \text{-ve value}$$

Going to be always  
 -ve.

$$y = mx + c$$

$$= W^T x + c$$

$$m = -1$$

$$c = 0$$

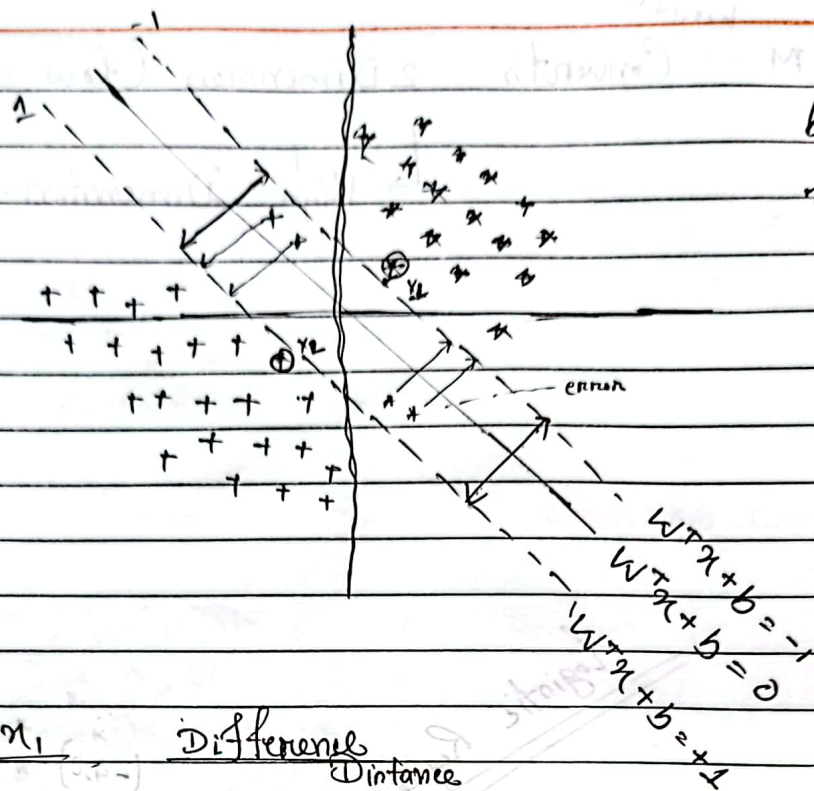
$$y = W^T x + c$$

$$= W^T x + 0$$

$$= \begin{bmatrix} 0 & -1 \\ 0 \end{bmatrix} \begin{bmatrix} -4 & 0 \end{bmatrix}$$

$$= 4 \quad \text{+ve value}$$

$\rightarrow$  Going to be always  
 +ve.



based on  
logistic Regression

$x_2 - x_1$  Difference  
Distance

$$W^T x_2 + b = 1$$

$$\Rightarrow (-) W^T x_1 + b = -1$$

$$\Rightarrow W^T (x_2 - x_1) = 2$$

$$\Rightarrow \frac{W^T (x_2 - x_1)}{\|W\|} = \frac{2}{\|W\|}$$

Optimization function.  
We need to  
maximize this

$$\gamma_i \begin{cases} 1 & \text{if } W^T x_i + b \geq 1 \\ -1 & \text{if } W^T x_i + b \leq -1 \end{cases}$$

$$(w, b) \rightarrow \max \left( \frac{2}{\|W\|} \right)$$

↓  
update

$$\gamma_i * W^T x_i + b_i \geq 1$$

true → true  
false → false



Real world Scenario's data is not distributed in a proper way.

$$(w, b) \rightarrow \min \left\{ \frac{\|w\|^2}{2} + c \sum_{i=1}^n \xi_i \right\}$$

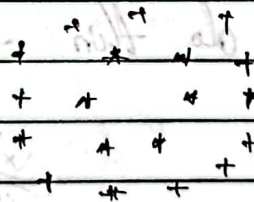
Regularization

how many errors my model considers

value of the error.

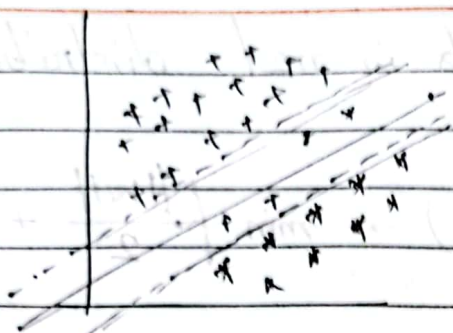
(4 \* 4 point distance sum) this means.

SVM



SVM Kernel trick.

# SVM Kernels.



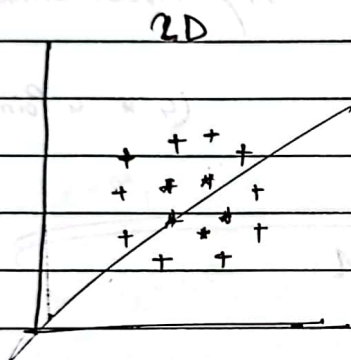
① Polynomial Kernel.

② RBF Kernel.

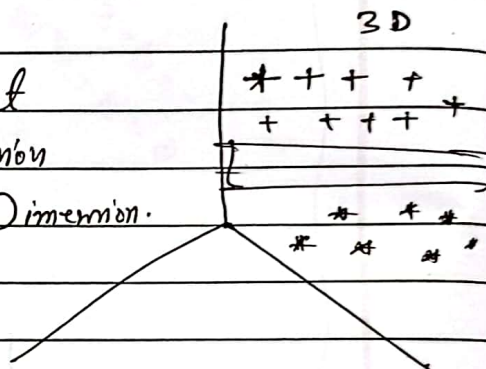
③ Sigmoid Kernel.

Soft margin  $\rightarrow$  small % of error

Hard margin  $\rightarrow$  Properly classify

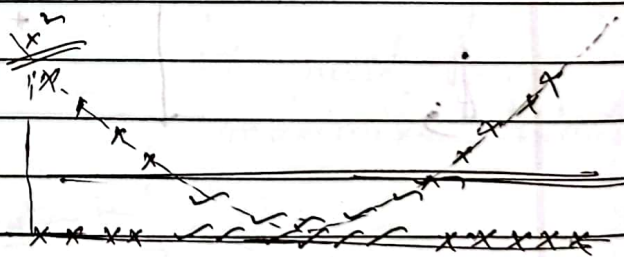
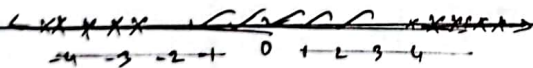


SVM Convert  
lower Dimension  
to higher Dimension.



How the do the do this  $\rightarrow$  Mathematical Formula.

1 Dimension.



2 Dimension.

$$\gamma = \frac{1}{2} (x) \cdot x^2$$

Int apply SVM NORMALLY  $\rightarrow$  50%  $\rightarrow$  that means SVC = linear.

Apply SVM Kernels.



Polynomial Kernels  $\rightarrow (X_1^T \cdot X_2 + 1)$  dimension.

2 Dimension

$x_1$	$x_2$	$y$
1	1	1
1	0	0
0	1	0
0	0	1

2

$x_1$	$x_1$	$x_2$
$x_2$		

$$\gamma = f(x_1, x_2)$$

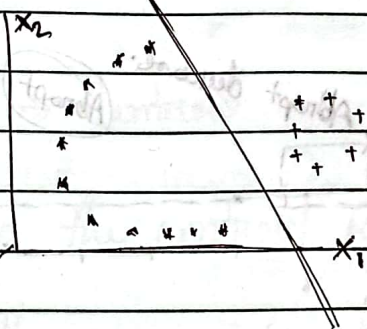
2

$x_1^2$	$x_1 x_2$
$x_1 x_2$	$x_2^2$

unique

$x_1$	$x_2$	$1$	$x_1^2$	$x_1 x_2$	$x_2^2$

3 Dimension



SVM Kernel = "Poly" or "rbf"

Consider like this.

$$z = x_1 x_2$$

How do we decide that whether we should use Polynomial or RBF or Sigmoid.

Determine by Hyperparameter tuning.

$K = 2$ , mean.

2 Centroid /

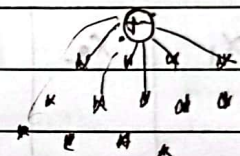
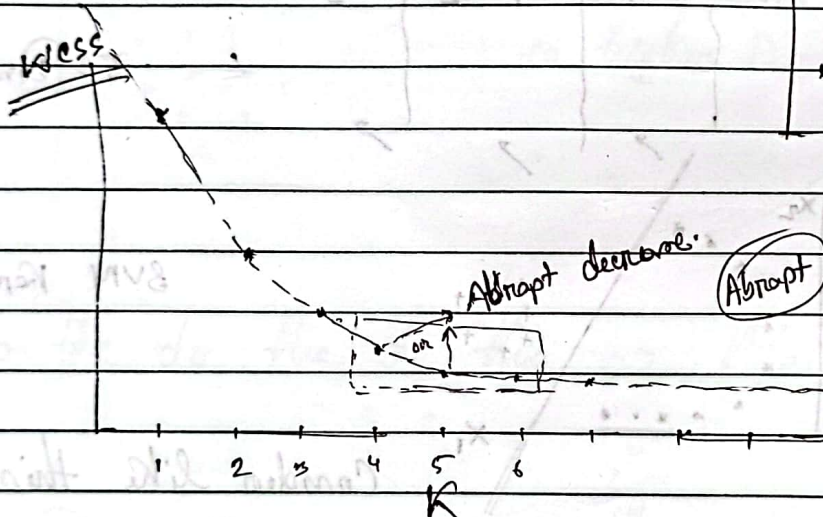
"Krish Naik."

2 cluster /

2 Group.

WESS = Within cluster Sum of Square.

$$= \sum_{i=1}^n (C_i + X_i)^2$$



Shape of  
Elbow

Elbow method.

$K = 4$

$K = 5$

[Analytically detailed explanation.]

$K$  = highest possibility  
= num. of observation.