Neural Networks: Representation

5 questions

1 point

1.

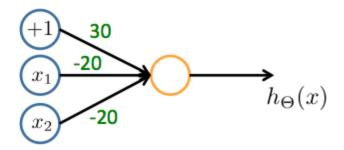
Which of the following statements are true? Check all that apply.

- A two layer (one input layer, one output layer; no hidden layer) neural network can represent the XOR function.
- The activation values of the hidden units in a neural network, with the sigmoid activation function applied at every layer, are always in the range (0, 1).
- Any logical function over binary-valued (0 or 1) inputs x_1 and x_2 can be (approximately) represented using some neural network.
- Suppose you have a multi-class classification problem with three classes, trained with a 3 layer network. Let $a_1^{(3)}=(h_\Theta(x))_1$ be the activation of the first output unit, and similarly $a_2^{(3)}=(h_\Theta(x))_2$ and $a_3^{(3)}=(h_\Theta(x))_3$. Then for any input x, it must be the case that $a_1^{(3)}+a_2^{(3)}+a_3^{(3)}=1$.

1 point

2.

Consider the following neural network which takes two binary-valued inputs $x_1,x_2\in\{0,1\}$ and outputs $h_\Theta(x)$. Which of the following logical functions does it (approximately) compute?

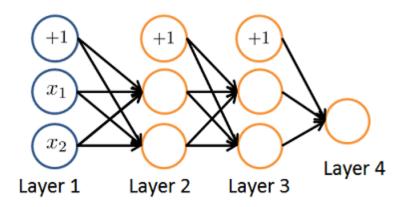


- NAND (meaning "NOT AND")
- O AND
- O OR
- O XOR (exclusive OR)

1 point

3.

Consider the neural network given below. Which of the following equations correctly computes the activation $a_1^{(3)}$? Note: g(z) is the sigmoid activation function.



$$oldsymbol{O} \quad a_1^{(3)} = g(\Theta_{1,0}^{(2)} a_0^{(2)} + \Theta_{1,1}^{(2)} a_1^{(2)} + \Theta_{1,2}^{(2)} a_2^{(2)})$$

$$oldsymbol{O} \quad a_1^{(3)} = g(\Theta_{1,0}^{(2)}a_0^{(1)} + \Theta_{1,1}^{(2)}a_1^{(1)} + \Theta_{1,2}^{(2)}a_2^{(1)})$$

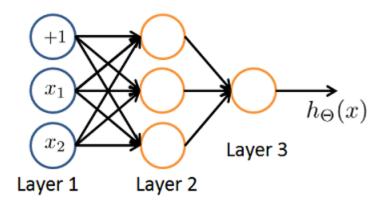
$$oldsymbol{O} \quad a_1^{(3)} = g(\Theta_{1,0}^{(1)}a_0^{(2)} + \Theta_{1,1}^{(1)}a_1^{(2)} + \Theta_{1,2}^{(1)}a_2^{(2)})$$

$$oldsymbol{O} \quad a_1^{(3)} = g(\Theta_{2,0}^{(2)} a_0^{(2)} + \Theta_{2,1}^{(2)} a_1^{(2)} + \Theta_{2,2}^{(2)} a_2^{(2)})$$

1 point

4.

You have the following neural network:



You'd like to compute the activations of the hidden layer $a^{(2)} \in \mathbb{R}^3$. One way to do so is the following Octave code:

```
% Theta1 is Theta with superscript "(1)" from lecture
% ie, the matrix of parameters for the mapping from layer 1 (input) to layer 2
% Theta1 has size 3x3
% Assume 'sigmoid' is a built-in function to compute 1 / (1 + exp(-z))

a2 = zeros (3, 1);
for i = 1:3
    for j = 1:3
        a2(i) = a2(i) + x(j) * Theta1(i, j);
    end
        a2(i) = sigmoid (a2(i));
end
```

You want to have a vectorized implementation of this (i.e., one that does not use for loops). Which of the following implementations correctly compute $a^{(2)}$? Check all that apply.

```
z = Theta1 * x; a2 = sigmoid (z);

a2 = sigmoid (x * Theta1);

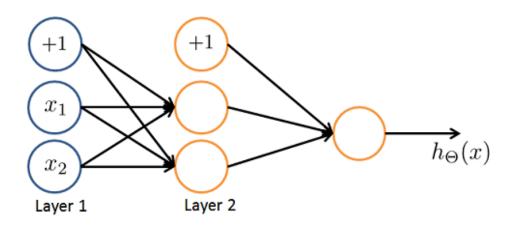
a2 = sigmoid (Theta2 * x);
```

 \Box z = sigmoid(x); a2 = sigmoid (Theta1 * z);

1 point

5.

You are using the neural network pictured below and have learned the parameters $\Theta^{(1)}=\begin{bmatrix}1&0.5&1.9\\1&1.2&2.7\end{bmatrix}$ (used to compute $a^{(2)}$) and $\Theta^{(2)}=[1&-0.2&-1.7]$ (used to compute $a^{(3)}$) as a function of $a^{(2)}$). Suppose you swap the parameters for the first hidden layer between its two units so $\Theta^{(1)}=\begin{bmatrix}1&1.2&2.7\\1&0.5&1.9\end{bmatrix}$ and also swap the output layer so $\Theta^{(2)}=[1&-1.7&-0.2]$. How will this change the value of the output $h_{\Theta}(x)$?



- O It will stay the same.
- O It will increase.
- O It will decrease
- O Insufficient information to tell: it may increase or decrease.