

Laplace Transform $F(s)$	Time Function $f(t)$ , $t > 0$
1	$\delta(t)$ , unit impulse
$\frac{1}{s}$	$u_s(t)$ , unit step
$\frac{1}{s^2}$	$t$
$\frac{1}{s^{n+1}}$	$\frac{t^n}{n!}$
$\frac{1}{s+a}$	$e^{-at}$
$\frac{1}{(s+a)^2}$	$te^{-at}$
$\frac{1}{(s+a)^n}$	$\frac{1}{(n-1)!} t^{n-1} e^{-at}$
$\frac{1}{s(s+a)}$	$\frac{1}{a}(1 - e^{-at})$
$\frac{\omega}{s^2 + \omega^2}$	$\sin(\omega t)$
$\frac{s}{s^2 + \omega^2}$	$\cos(\omega t)$
$\frac{\omega}{(s+b)^2 + \omega^2}$	$e^{-bt} \sin(\omega t)$
$\frac{s+b}{(s+b)^2 + \omega^2}$	$e^{-bt} \cos(\omega t)$
$\frac{1}{s(s+a)^2}$	$\frac{1}{a^2}(1 - e^{-at} - ate^{-at})$
$\frac{s}{(s+a)(s+b)}$	$\frac{1}{b-a}(be^{-bt} - ae^{-at})$ , $a \neq b$
$\frac{1}{(s+a)(s+b)}$	$\frac{1}{b-a}(e^{-at} - e^{-bt})$ , $a \neq b$
$\frac{s+c}{(s+a)(s+b)}$	$\frac{1}{b-a}((b-c)e^{-bt} - (a-c)e^{-at})$ , $a \neq b$
$\frac{\omega}{s^2 - \omega^2}$	$\sinh(\omega t)$
$\frac{s}{s^2 - \omega^2}$	$\cosh(\omega t)$
$\frac{a^2}{s^2(s+a)}$	$at - 1 + e^{-at}$
$\frac{a^2}{s(s+a)^2}$	$1 - (at+1)e^{-at}$
$\frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2}$	$\frac{\omega_n}{\sqrt{1-\zeta^2}} e^{-\zeta\omega_n t} \sin\left(\omega_n\sqrt{1-\zeta^2} t + \cos^{-1}(\zeta)\right) u_s(t)$ , $0 < \zeta < 1$
$\frac{\omega_n^2}{s(s^2 + 2\zeta\omega_n s + \omega_n^2)}$	$\left(1 - \frac{e^{-\zeta\omega_n t}}{\sqrt{1-\zeta^2}} \sin\left(\omega_n\sqrt{1-\zeta^2} t + \cos^{-1}(\zeta)\right)\right) u_s(t)$ , $0 < \zeta < 1$

Property	$f(t)$	$F(s)$
Linearity	$k_1 f_1(t) \pm k_2 f_2(t)$	$k_1 F_1(s) \pm k_2 F_2(s)$ , $k_1, k_2 \in \mathbb{C}$
Time-delay (Shift in Time)	$f(t - T), t > 0$	$e^{-Ts} F(s)$
Differentiation	$f'(t) = \frac{df(t)}{dt}$	$sF(s) - f(0)$
	$f''(t) = \frac{d^2 f(t)}{dt^2}$	$s^2 F(s) - sf(0) - f'(0)$
	$f^{(n)}(t) = \frac{d^n f(t)}{dt^n}$	$s^n F(s) - \sum_{k=1}^n s^{n-k} f^{(k-1)}(0)$
Integration	$\int_0^t f(\tau) d\tau$	$\frac{F(s)}{s}$
Convolution	$f_1(t) * f_2(t)$	$F_1(s) \cdot F_2(s)$
Time Scaling	$f(at), a > 0$	$\frac{1}{a} F\left(\frac{s}{a}\right)$
Initial-value Theorem	$f(0^+) = \lim_{t \rightarrow 0^+} f(t)$	$\lim_{s \rightarrow \infty} sF(s)$
Final-value Theorem	$f(\infty) = \lim_{t \rightarrow \infty} f(t)$	$\lim_{s \rightarrow 0} sF(s)$