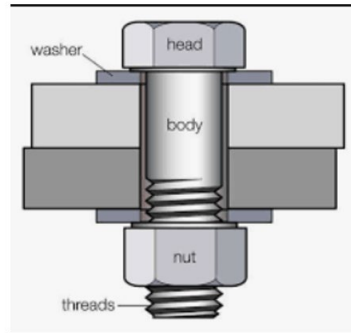
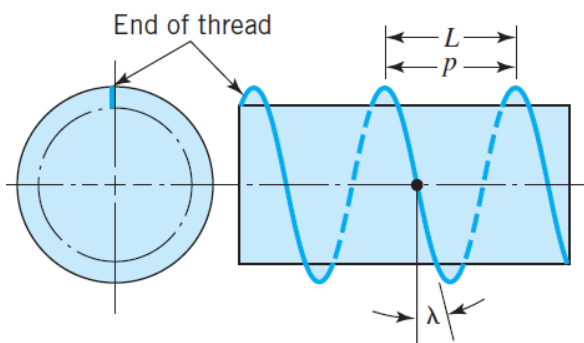




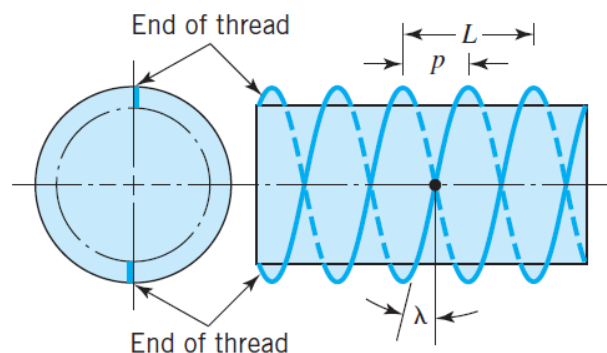
## Lesson 03- Fasteners



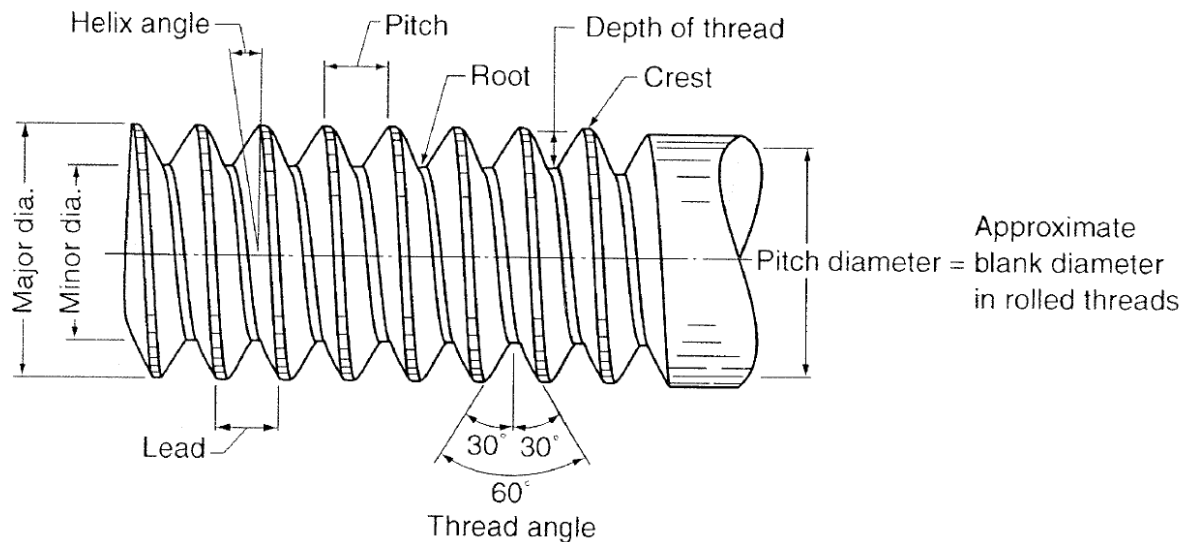
- Threads are the basic arrangement of a helical thread wound around a cylinder,
- Threads could be defined by : Pitch, lead, lead angle, and hand-of-thread
- In general all bolts and screws have a single thread, however power screws sometimes have double, triple, and even quadruple threads.
- Unless otherwise noted, all threads are assumed to be right-hand.



(a)  
Single thread-right hand



(b)  
Double thread-left hand



**Major (nominal) diameter:** This is the largest diameter of a screw thread, touching the crests on an external thread or the roots of an internal thread.

**Minor (core) diameter:** This is the smallest diameter of a screw thread, touching the roots or core of an external thread (root or core diameter) or the crests of an internal thread.

**Pitch diameter:** This is the diameter of an imaginary cylinder, passing through the threads at the points where the thread width is equal to the space between the threads.

**Pitch:** It is the distance measured parallel to the axis, between corresponding points on adjacent screw threads.

**Lead:** It is the distance a screw advances axially in one turn.

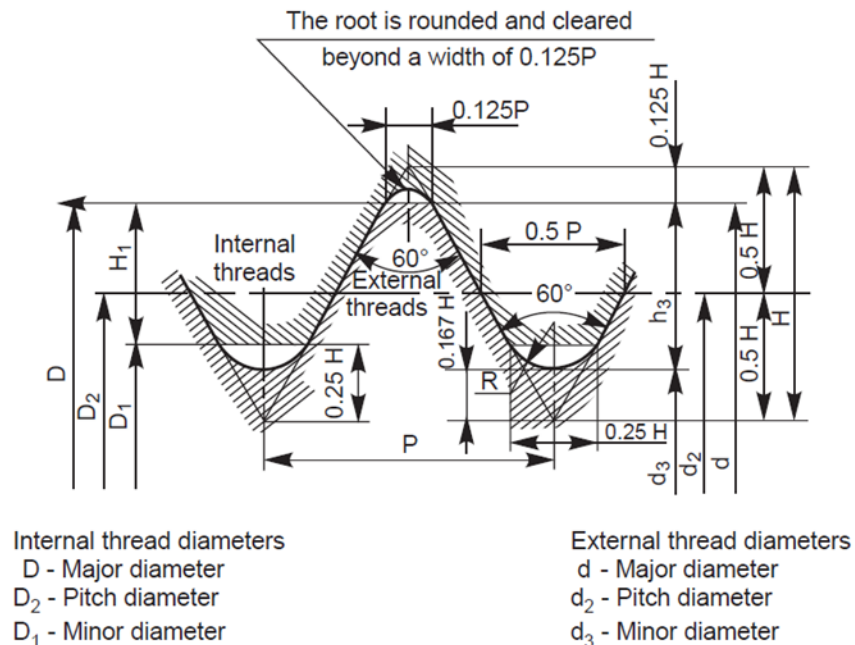
**Crest:** It is the peak edge of a screw thread, that connects the adjacent flanks at the top.

**Root:** It is the bottom edge of the thread that connects the adjacent flanks at the bottom.

**Thread angle:** This is the angle included between the flanks of the thread, measured in an axial plane.

Forms of thread:

The ISO (International Organization for Standards) threads adapted the metric threads.



Where:

$$\begin{aligned}
 P &= \text{Pitch} \\
 H &= 0.86 P \\
 D &= d = \text{Major diameter} \\
 D_2 &= d_2 = d - 0.75H \\
 D_1 &= d_3 = d - 2(H/2 - H/4) = d - 2H_1 \\
 d_3 &= d_2 - 2(H/2 - H/6) = d - 1.22P \\
 H_1 &= (D - D_1)/2 = 5H/8 = 0.54P \\
 h_3 &= (d - d_3)/2 = 17/24H = 0.61P \\
 R &= H/6 = 0.14P
 \end{aligned}$$

### Other types of threads:

The V thread (sharp):

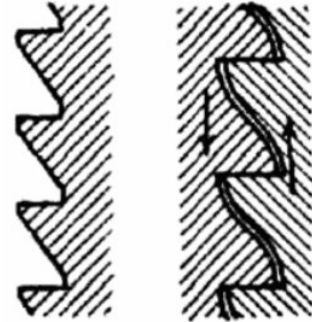
- This thread profile has a larger contact area, providing more frictional resistance to motion
- Hence, it is used where effective positioning is required. It is also used in brass pipe work.

The British Standard Thread:

- This thread form is adopted in Britain in inch units.
- The profile has rounded ends, making it less liable to damage than sharp V-thread.

The Buttress thread:

- This thread is a combination of V-and square threads.
- It exhibits the advantages of square thread, the ability to transmit power and low frictional resistance,
- It is used where power transmission takes place in one direction only such as screw press,
- Quick acting carpenter's vice, etc



The square thread:

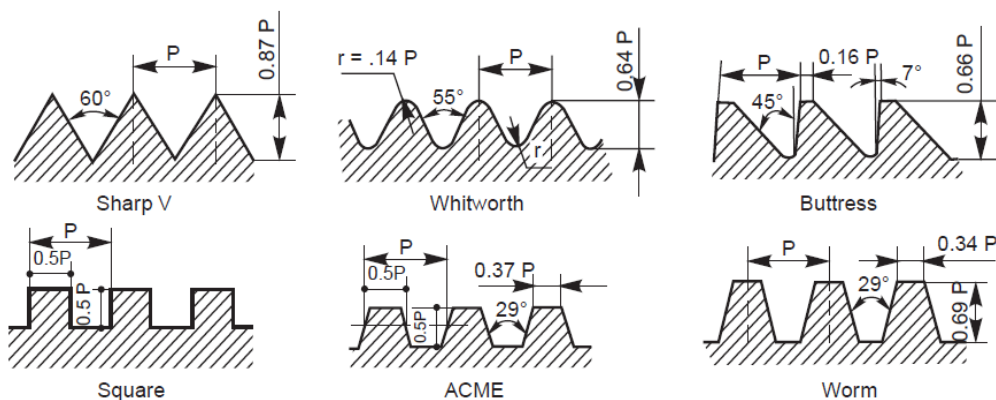
- Square thread is an ideal thread form for power transmission.
- As the thread flank is at right angle to the axis, the normal force between the threads acts parallel to the axis, with zero radial component.
- This enables the nut to transmit very high pressures, as in the case of a screw jack and other similar applications.

Acme thread:

- It is a modified form of square thread. It is much stronger than square thread because of the wider base and it is easy to cut.
- The inclined sides of the thread facilitate quick and easy engagement and disengagement as for example, the split nut with the lead screw of a lathe.

Worm thread:

- Worm thread is like the ACME thread but is deeper. It is used on shafts to carry power to worm wheels.



### Thread series:

The Table below gives the nominal diameter and pitch combinations for coarse and fine series of ISO metric screw threads

| <i>Nominal diameter</i> |                      | <i>Pitch</i>  |             |          |          |
|-------------------------|----------------------|---------------|-------------|----------|----------|
| <i>First choice</i>     | <i>Second choice</i> | <i>Coarse</i> | <i>Fine</i> |          |          |
|                         |                      |               | <i>1</i>    | <i>2</i> | <i>3</i> |
| 2                       | —                    | 0.4           | 0.25        | —        | —        |
| —                       | 2.2                  | 0.45          | 0.25        | —        | —        |
| 2.5                     | —                    | 0.45          | 0.35        | —        | —        |
| 3                       | —                    | 0.5           | 0.35        | —        | —        |
| —                       | 3.5                  | 0.6           | 0.35        | —        | —        |
| 4                       | —                    | 0.7           | 0.5         | —        | —        |
| —                       | 4.5                  | 0.75          | 0.5         | —        | —        |
| 5                       | —                    | 0.8           | 0.5         | —        | —        |
| 6                       | —                    | 1             | 0.75        | 0.5      | —        |
| 8                       | —                    | 1.25          | 1           | 0.75     | —        |
| 10                      | —                    | 1.5           | 1.25        | 1        | 0.75     |
| 12                      | —                    | 1.75          | 1.5         | 1.25     | —        |
| 16                      | 14                   | 2             | 1.5         | 1        | —        |
| 20                      | 18,22                | 2.5           | 2           | 1.5      | 1        |
| 24                      | 27                   | 3             | 2           | 1.5      | 1        |
| 30                      | 33                   | 3.5           | 2           | 1.5      | 1        |
| 36                      | 39                   | 4             | 3           | 2        | 1.5      |
| 42                      | 45                   | 4.5           | 4           | 3        | 2        |
| 48                      | 52                   | 5             | 4           | 3        | 2        |
| 56                      | 60                   | 5.5           | 4           | 3        | 2        |
| 64                      | 68                   | 6             | 4           | 3        | 2        |
| 72                      | 76                   | 6             | 4           | 3        | 2        |
| 80                      | 85                   | 6             | 4           | 3        | 2        |
| 90                      | 95                   | 6             | 4           | 3        | 2        |
| 100                     | —                    | 6             | 4           | 3        | 2        |
| 105 to 300              | —                    | —             | 6           | 4        | 3        |

The diameter-pitch combination of an ISO metric screw thread is designated by the letter ‘M’ followed by the value of the nominal diameter and pitch, the two values being separated by the sign ‘×’.

Example: a diameter pitch combination of nominal diameter 10 mm and pitch 1.25 mm is designated as M10 × 1.25



## MENG 3050-Power Transmission Components

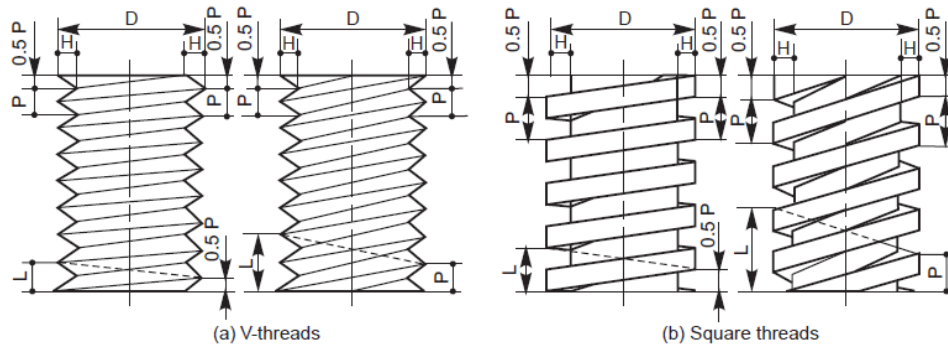
| Size           | Major Diameter<br>$d$ (in.) | Coarse Threads—UNC  |   |  | Fine Threads—UNF    |   |  |
|----------------|-----------------------------|---------------------|---|--|---------------------|---|--|
|                |                             | Threads<br>per Inch | Minor<br>Diameter<br>of External<br>Thread<br>$d_r$ (in.) | Tensile<br>Stress<br>Area<br>$A_t$ (in. <sup>2</sup> ) | Threads<br>per Inch | Minor<br>Diameter<br>of External<br>Thread<br>$d_r$ (in.) | Tensile<br>Stress<br>Area<br>$A_t$ (in. <sup>2</sup> ) |
| 0(.060)        | 0.0600                      | —                   | —   | —  | 80                  | 0.0447  | 0.00180  |
| 1(.073)        | 0.0730                      | 64                  | 0.0538  | 0.00263  | 72                  | 0.0560  | 0.00278  |
| 2(.086)        | 0.0860                      | 56                  | 0.0641  | 0.00370  | 64                  | 0.0668  | 0.00394  |
| 3(.099)        | 0.0990                      | 48                  | 0.0734  | 0.00487  | 56                  | 0.0771  | 0.00523  |
| 4(.112)        | 0.1120                      | 40                  | 0.0813  | 0.00604  | 48                  | 0.0864  | 0.00661  |
| 5(.125)        | 0.1250                      | 40                  | 0.0943  | 0.00796  | 44                  | 0.0971  | 0.00830  |
| 6(.138)        | 0.1380                      | 32                  | 0.0997  | 0.00909  | 40                  | 0.1073  | 0.01015  |
| 8(.164)        | 0.1640                      | 32                  | 0.1257  | 0.0140   | 36                  | 0.1299  | 0.01474  |
| 10(.190)       | 0.1900                      | 24                  | 0.1389  | 0.0175   | 32                  | 0.1517  | 0.0200   |
| 12(.216)       | 0.2160                      | 24                  | 0.1649  | 0.0242   | 28                  | 0.1722  | 0.0258   |
| $\frac{1}{4}$  | 0.2500                      | 20                  | 0.1887  | 0.0318   | 28                  | 0.2062  | 0.0364   |
| $\frac{5}{16}$ | 0.3125                      | 18                  | 0.2443  | 0.0524   | 24                  | 0.2614  | 0.0580   |
| $\frac{3}{8}$  | 0.3750                      | 16                  | 0.2983  | 0.0775   | 24                  | 0.3239  | 0.0878   |
| $\frac{7}{16}$ | 0.4375                      | 14                  | 0.3499  | 0.1063   | 20                  | 0.3762  | 0.1187   |
| $\frac{1}{2}$  | 0.5000                      | 13                  | 0.4056  | 0.1419   | 20                  | 0.4387  | 0.1599   |
| $\frac{9}{16}$ | 0.5625                      | 12                  | 0.4603  | 0.182  | 18                  | 0.4943  | 0.203  |
| $\frac{5}{8}$  | 0.6250                      | 11                  | 0.5135  | 0.226  | 18                  | 0.5568  | 0.256  |
| $\frac{3}{4}$  | 0.7500                      | 10                  | 0.6273  | 0.334  | 16                  | 0.6733  | 0.373  |
| $\frac{7}{8}$  | 0.8750                      | 9                   | 0.7387  | 0.462  | 14                  | 0.7874  | 0.509  |
| 1              | 1.0000                      | 8                   | 0.8466  | 0.606  | 12                  | 0.8978  | 0.663  |
| $1\frac{1}{8}$ | 1.1250                      | 7                   | 0.9497  | 0.763  | 12                  | 1.0228  | 0.856  |
| $1\frac{1}{4}$ | 1.2500                      | 7                   | 1.0747  | 0.969  | 12                  | 1.1478  | 1.073  |
| $1\frac{3}{8}$ | 1.3750                      | 6                   | 1.1705  | 1.155  | 12                  | 1.2728  | 1.315  |
| $1\frac{1}{2}$ | 1.5000                      | 6                   | 1.2955  | 1.405  | 12                  | 1.3978  | 1.581  |
| $1\frac{3}{4}$ | 1.7500                      | 5                   | 1.5046  | 1.90   |                     |   |  |
| 2              | 2.0000                      | $4\frac{1}{2}$      | 1.7274  | 2.50   |                     |   |  |
| $2\frac{1}{4}$ | 2.2500                      | $4\frac{1}{2}$      | 1.9774  | 3.25   |                     |   |  |
| $2\frac{1}{2}$ | 2.5000                      | 4                   | 2.1933  | 4.00   |                     |   |  |
| $2\frac{3}{4}$ | 2.7500                      | 4                   | 2.4433  | 4.93   |                     |   |  |
| 3              | 3.0000                      | 4                   | 2.6933  | 5.97   |                     |   |  |
| $3\frac{1}{4}$ | 3.2500                      | 4                   | 2.9433  | 7.10   |                     |   |  |
| $3\frac{1}{2}$ | 3.5000                      | 4                   | 3.1933  | 8.33   |                     |   |  |
| $3\frac{3}{4}$ | 3.7500                      | 4                   | 3.4433  | 9.66   |                     |   |  |
| 4              | 4.0000                      | 4                   | 3.6933  | 11.08  |                     |   |  |

We specify standard bolting as follows:

$\frac{1}{4}$ -20UNC-2A

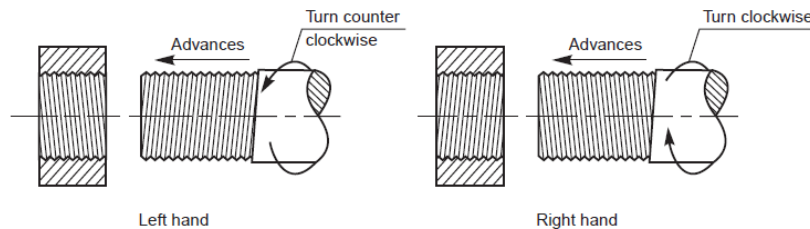
### Multi Start thread:

- A single-start thread consists of a single, continuous helical groove for which the lead is equal to the pitch
- As the depth of the thread depends on the pitch, greater the lead desired, greater will be the pitch and hence smaller will be the core diameter, reducing the strength of the fastener. To overcome this drawback, multi-start threads are recommended
- Multi-start threads are used wherever quick action is desired



### Right hand or left-hand threads:

- Screw threads may be right hand or left hand, depending on the direction of the helix.
- A right-hand thread is one which advances into the nut, when turned in a clockwise direction and a left is the opposite.
- Unless otherwise stated, a thread should be considered as a right hand one.





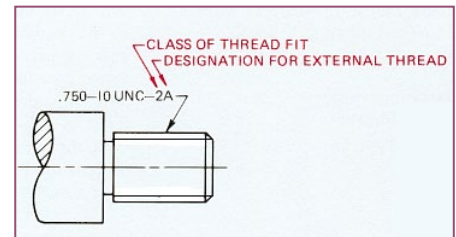
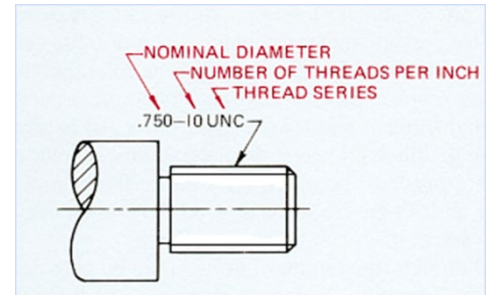
### Inch Threads

- Nominal size = screw or bolt diameter = major diameter
- Number of thread per inch
- Thread series: coarse, fine, extra fine

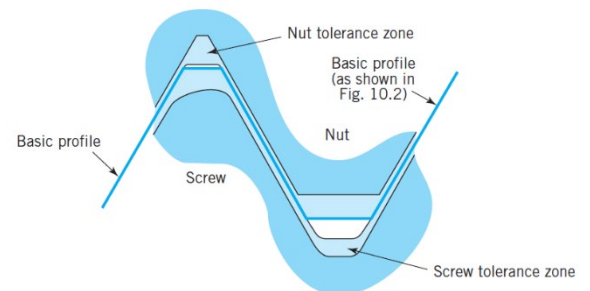
### Thread Class:

Class of thread fit:

- 1 – Loose fit
- 2 – General commercial grade
- 3 – Close fit, for high grade commercial products



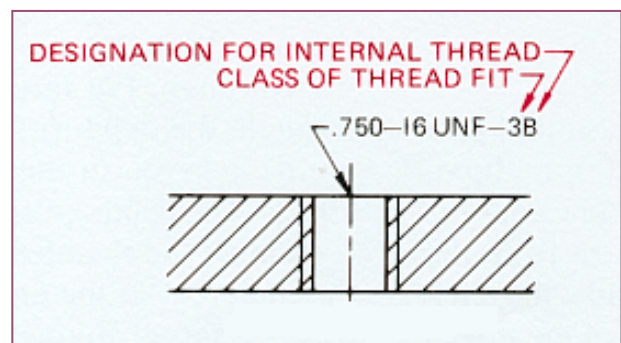
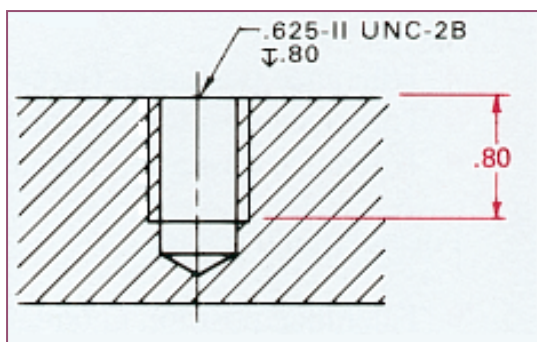
Tolerance zones for various classes of unified threads.  
Note: Each class—1, 2, and 3—uses a portion of the zones shown



Designation for thread:

- A – External thread
- B – Internal thread

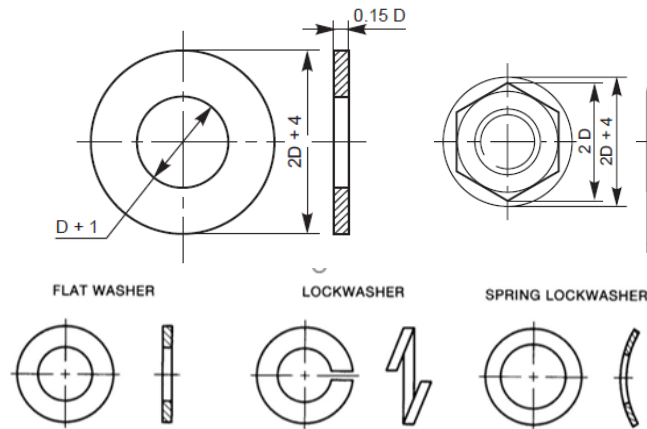
### Internal thread examples.





### Washers:

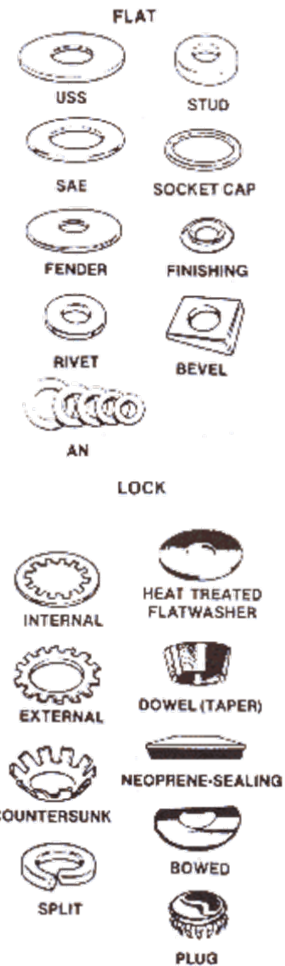
- A washer is a cylindrical piece of metal with a hole to receive the bolt.
- It is used to give a perfect seating for the nut
- and to distribute the tightening force uniformly to the parts under the joint.
- It also prevents the nut from damaging the metal surface under the joint.
- Common washer metric sizes shown in the figure below.



| Bolt Size | Flat Washer |    |           | Lockwasher |      |           | Spring Lockwasher |      |             |
|-----------|-------------|----|-----------|------------|------|-----------|-------------------|------|-------------|
|           | ID          | OD | Thickness | ID         | OD   | Thickness | ID                | OD   | Thickness   |
| 2         | 2.2         | 5  | 0.5       | 2.1        | 3.3  | 0.5       |                   |      |             |
| 3         | 3.2         | 7  | 0.5       | 3.1        | 5.7  | 0.8       |                   |      |             |
| 4         | 4.3         | 9  | 0.8       | 4.1        | 7.1  | 0.9       | 4.2               | 8    | 0.3<br>0.4  |
| 5         | 5.3         | 11 | 1         | 5.1        | 8.7  | 1.2       | 5.2               | 10   | 0.4<br>0.5  |
| 6         | 6.4         | 12 | 1.5       | 6.1        | 11.1 | 1.6       | 6.2               | 12.5 | 0.5<br>0.7  |
| 7         | 7.4         | 14 | 1.5       | 7.1        | 12.1 | 1.6       | 7.2               | 14   | 0.5<br>0.8  |
| 8         | 8.4         | 17 | 2         | 8.2        | 14.2 | 2         | 8.2               | 16   | 0.6<br>0.9  |
| 10        | 10.5        | 21 | 2.5       | 10.2       | 17.2 | 2.2       | 10.2              | 20   | 0.8<br>1.1  |
| 12        | 13          | 24 | 2.5       | 12.3       | 20.2 | 2.5       | 12.2              | 25   | 0.9<br>1.5  |
| 14        | 15          | 28 | 2.5       | 14.2       | 23.2 | 3         | 14.2              | 28   | 1<br>1.5    |
| 16        | 17          | 30 | 3         | 16.2       | 26.2 | 3.5       | 16.3              | 31.5 | 1.2<br>1.7  |
| 18        | 19          | 34 | 3         | 18.2       | 28.2 | 3.5       | 18.3              | 35.5 | 1.2<br>2    |
| 20        | 21          | 36 | 3         | 20.2       | 32.2 | 4         | 20.4              | 40   | 1.5<br>2.25 |
| 22        | 23          | 39 | 4         | 22.5       | 34.5 | 4         | 22.4              | 45   | 1.75<br>2.5 |
| 24        | 25          | 44 | 4         | 24.5       | 38.5 | 5         |                   |      |             |
| 27        | 28          | 50 | 4         | 27.5       | 41.5 | 5         |                   |      |             |
| 30        | 31          | 56 | 4         | 30.5       | 46.5 | 6         |                   |      |             |

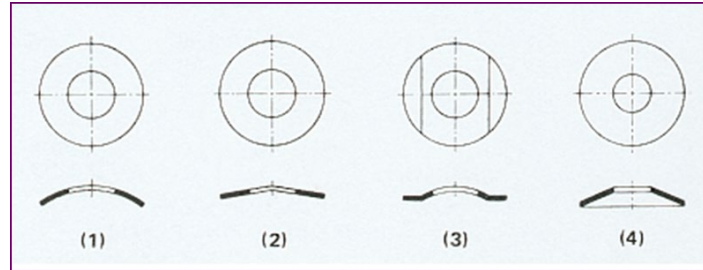
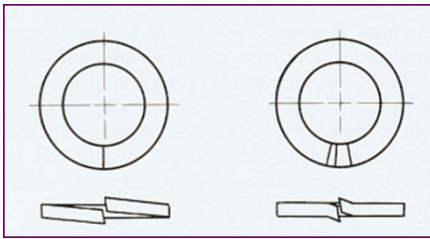
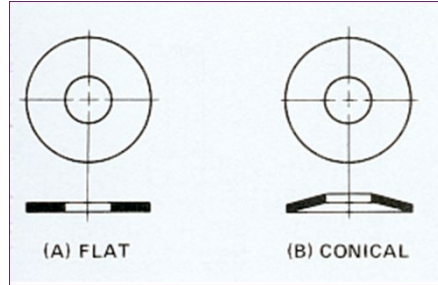
MILLIMETRE SIZES

### WASHERS

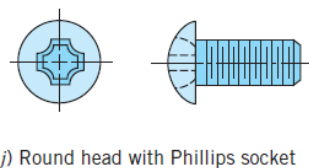
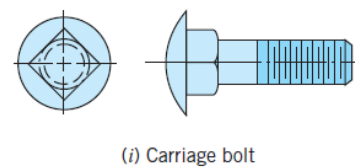
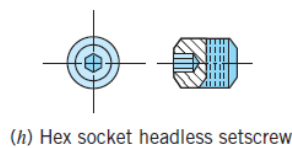
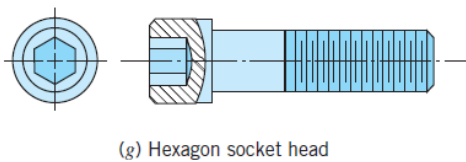
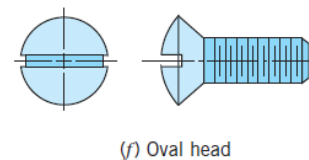
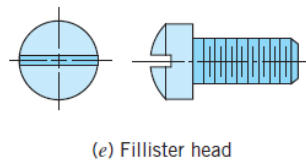
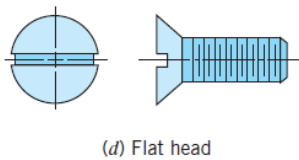
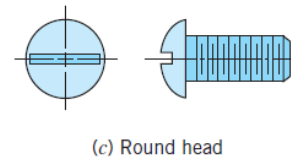
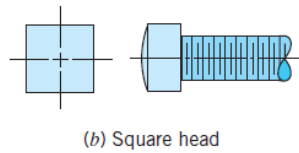
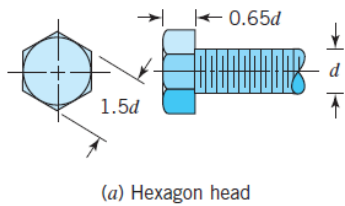


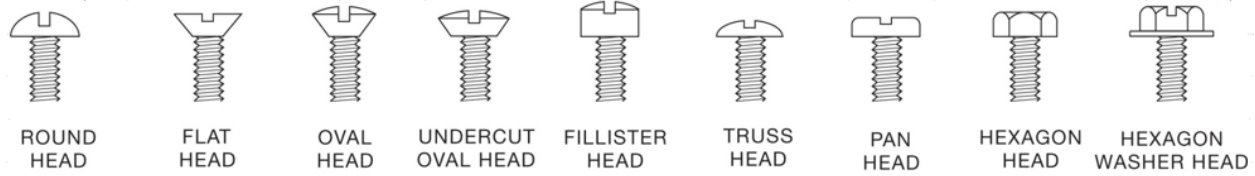
### Classification of Washers:

- Flat washer
- Conical washer
- Helical Spring washer
- Spring washer
- Tooth Lock washer



### Threaded Fasteners



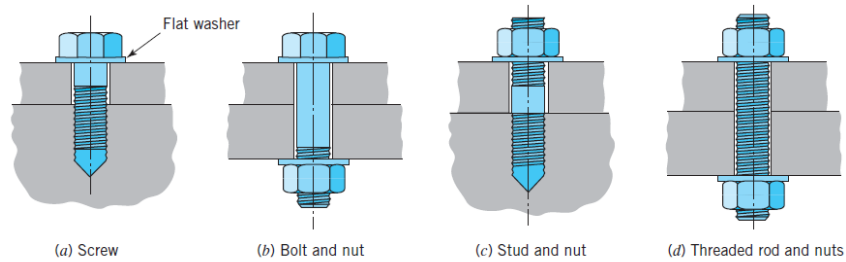


(A) SCREWS



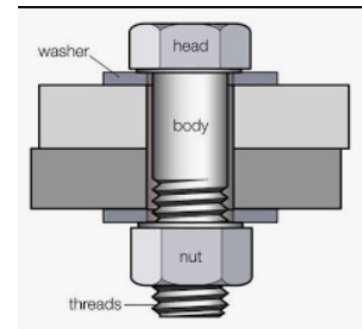
(B) BOLTS

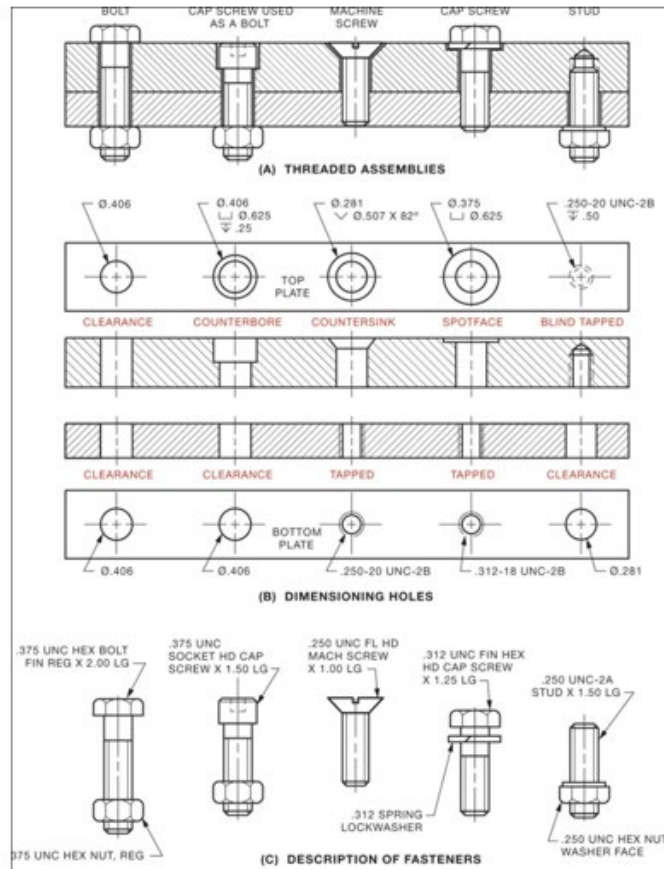
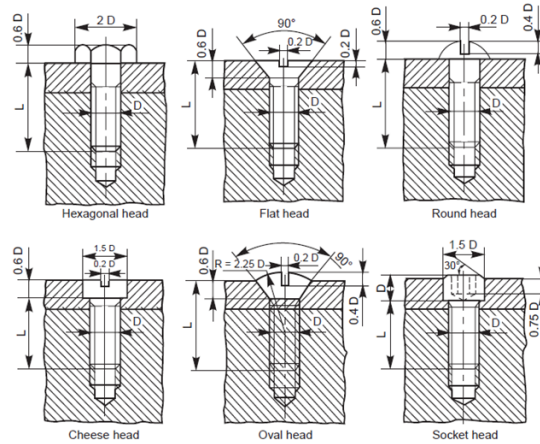
(C) STUDS



### Cap screws

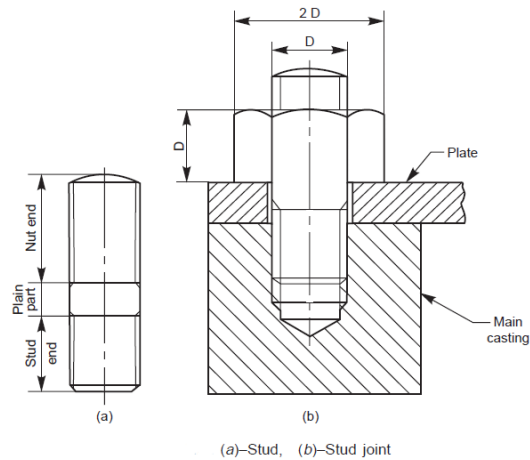
- Used for fastening two parts,
- The clearance of the unthreaded hole need not be shown on the drawing as its presence is obvious.
- Cap screws are:
  - Produced in finish form and are used on machines where accuracy and appearance are important.
  - They are used only on machines requiring few adjustments and are not suitable where frequent removal is necessary.
  - These are produced in different diameters, up to a maximum of 100 mm and lengths 250 mm.





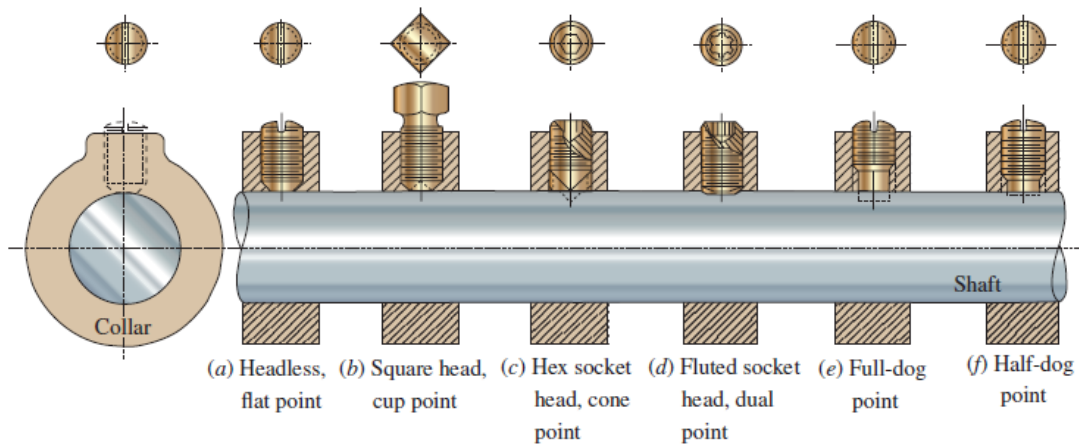
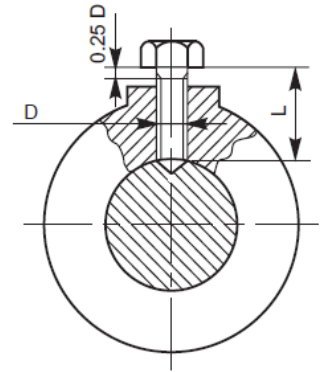
### Stud screw:

- It consists of cylindrical shank with threads cut on both the ends.
- It is used where there is no place for accommodating the bolt head
- or when one of the parts to be joined is too thick to use an ordinary bolt.








### Set Screws:

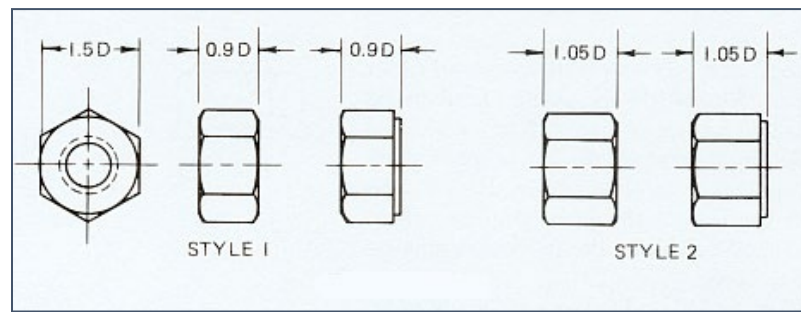
- These are used to prevent relative motion between two rotating parts, such as the movement of pulley on shaft.
- a set screw is screwed into the pulley hub so that its end-point bears firmly against the shaft.
- Set screws are not efficient and so are used only for transmitting very light loads.
- For longer life, set screws are made of steel and case hardened.
- for better results, the shaft surface is suitably machined for providing more grip, eliminating any slipping tendency.



Set screws with different head and point styles applied to hold a collar on a shaft

|   |   |
|---|---|
|  | <b>CUP</b><br>Most generally used. Suitable for quick and semi-permanent location of parts on soft shafts, where cutting in of edges of cup shape on shaft is not objectionable.  |
|  | <b>FLAT</b><br>Used where frequent resetting is required, on hard steel shafts, and where minimum damage to shafts is necessary. Flat is usually ground on shaft for better contact.  |
|  | <b>CONICAL</b><br>For setting machine parts permanently on shaft, which should be spotted to receive cone point. Also used as a pivot or hanger.  |
|  | <b>SPHERICAL</b><br>Should be used against shafts spotted, splined, or grooved to receive it. Sometimes substituted for cup point.  |
|  | <b>HALF DOG</b><br>For permanent location of machine parts, although cone point is usually preferred for this purpose. Point should fit closely to diameter of drilled hole in shaft. Sometimes used in place of a dowel pin. |

### Hex Nut:





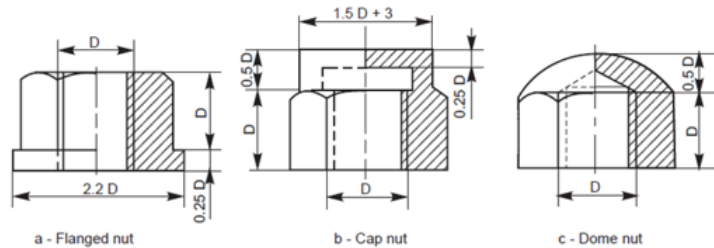
### Other types of nuts:

#### *Flanged nut:*

This is a hexagonal nut with a collar or flange, provided integral with it. This permits the use of a bolt in a comparatively large size hole

#### *Cap Nut:*

It is a hexagonal nut with a cylindrical cap at the top. This design protects the end of the bolt from corrosion and also prevents leakage through the threads. Cap nuts are used in smoke boxes or locomotive and steam pipe connections.

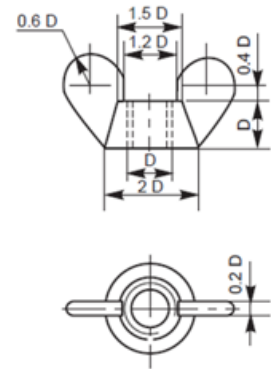


#### *Dom Nut:*

It is another form of a cap nut, having a spherical dome at the top.

#### *Wing Nut:*

This nut is used when frequent removal is required, such as inspection covers, lids, etc. It is operated by the thumb,



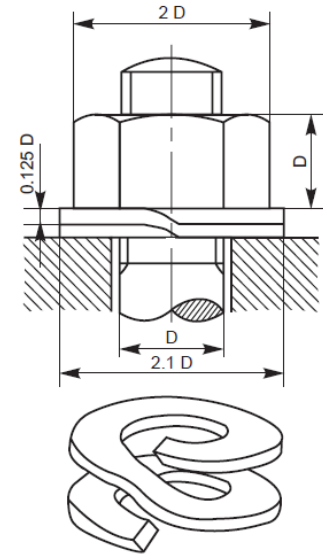
### Locking arrangements for nuts:

- The bolted joints are required to stay firm without becoming loose, of their own accord.
- However, the joints used in the moving parts of a machinery may be subjected to vibrations. This may slacken the joint, leading to serious breakdown.
- To eliminate the slackening tendency, different arrangements are used to lock the nuts



In this arrangement, a spring washer of either single or double coil is placed under the nut and tightened.

The spring force of the washer will be acting upwards on the nut. This force makes the threads in the nut jammed on the bolt threads; thus, preventing the nut from loosening

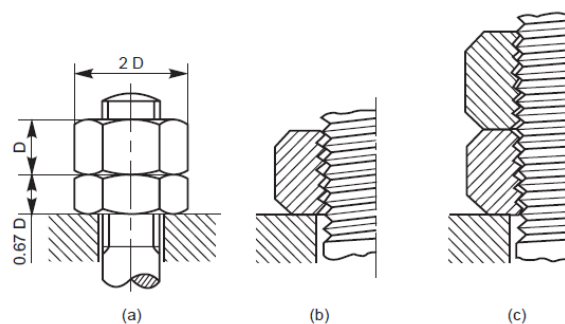


### *Locking Nut:*

- It is the most commonly used locking device.
- In this arrangement, a second nut, known as lock nut, is used in combination with a standard nut.
- The thickness of a lock nut is usually two-thirds  $D$ , where  $D$  is the major diameter of the bolt.
- The lock nut is usually placed below the standard nut. To make the joint, the lock nut is first screwed.
- tightly and then the standard nut is tightened till it touches the lock nut.

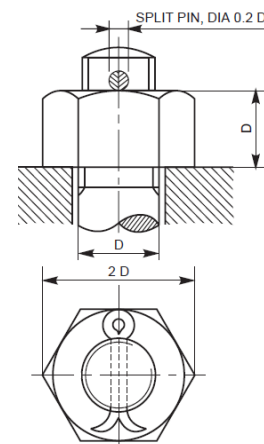
Afterwards, the locknut is then screwed back on the standard nut, which is held by a spanner.

- The threads of the two nuts become wedged between the threads of the bolt.
- When the lock nut is first screwed into its position, the top flanks of it press against the bottom flanks of the bolt (Fig. b).
- Fig c shows the condition between the flanks of the nuts and the bolt, when the second nut is locked in position. It may be observed that in this position, the top flanks of the top nut, press against the bottom flanks of the bolt, whereas, the bottom flanks of the lock nut press against the top flanks of the bolt



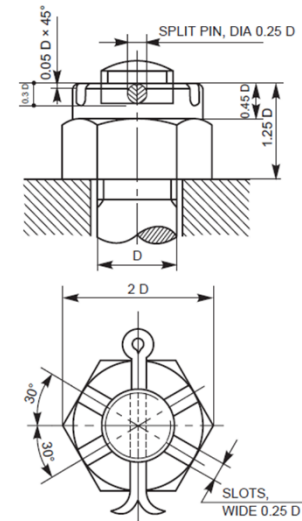
### *Locking by a split pin*

- A split pin, made of steel wire of semi-circular cross-section is used for locking the nut.
- In this arrangement, the split pin is inserted through a hole in the bolt body and touching just the top surface of the nut. Then, the ends of the pin are split open to prevent it from coming out while in use



### *Locking by a castell nut:*

- A castle nut is a hexagonal nut with a cylindrical collar turned on one end.
- Threads are cut in the nut portion only and six rectangular slots are cut through the collar.
- A split pin is inserted through a hole in the bolt body after adjusting the nut such that the hole in the bolt body comes in-line with slots.
- This arrangement is used in automobile works



### *Nylon lock nut:*



### *Spin Lock Nuts:*

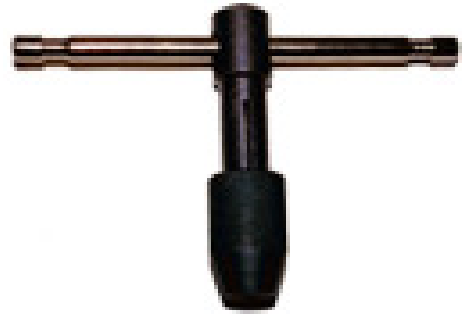
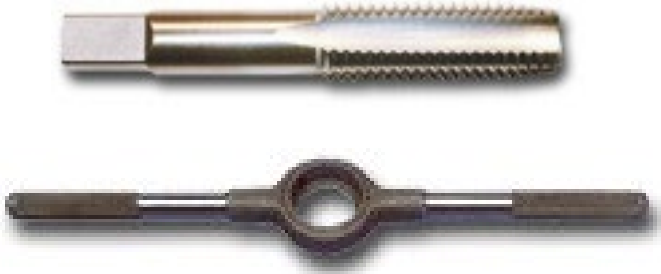
- A flange provides a large bearing surface and also acts as a washer for these nuts. Locking action is provided by serrations on the flange bottom.



### Tap and Dies:

- Taps for internal threading
- Die for external threading





SAE: Society of automotive engineering

ASTM: American society for testing of material









Proof strength: around %85-95 of the yields strength

Grades applies on STEEL made bolts only, not for other material

#### Fastener Materials and Methods of Manufacture:










- Materials for screws, nuts, and bolts are normally selected on the basis of strength (at the operating temperatures involved), weight, corrosion resistance, magnetic properties, life expectancy, and cost.
- Most fasteners are made from steel of specifications standardized by the Society of Automotive Engineers and summarized in Tables below:

**Specifications for Steel Used in Inch Series Screws and Bolts**
**SAE Specifications for Steel Bolts**

| SAE Grade No. | Size Range Inclusive, in  | Minimum Proof Strength,* kpsi | Minimum Tensile Strength,* kpsi | Minimum Yield Strength,* kpsi | Material                   | Head Marking  |
|---------------|---|-------------------------------|---------------------------------|-------------------------------|----------------------------|---|
| 1             | $\frac{1}{4}$ – $1\frac{1}{2}$                                  | 33                            | 60                              | 36                            | Low or medium carbon       |    |
| 2             | $\frac{1}{4}$ – $\frac{3}{4}$<br>$\frac{7}{8}$ – $1\frac{1}{2}$ | 55<br>33                      | 74<br>60                        | 57<br>36                      | Low or medium carbon       |    |
| 4             | $\frac{1}{4}$ – $1\frac{1}{2}$                                  | 65                            | 115                             | 100                           | Medium carbon, cold-drawn  |    |
| 5             | $\frac{1}{4}$ –1<br>$1\frac{1}{8}$ – $1\frac{1}{2}$             | 85<br>74                      | 120<br>105                      | 92<br>81                      | Medium carbon, Q&T         |    |
| 5.2           | $\frac{1}{4}$ –1  | 85                            | 120                             | 92                            | Low-carbon martensite, Q&T |   |
| 7             | $\frac{1}{4}$ – $1\frac{1}{2}$                                  | 105                           | 133                             | 115                           | Medium-carbon alloy, Q&T   |  |
| 8             | $\frac{1}{4}$ – $1\frac{1}{2}$                                  | 120                           | 150                             | 130                           | Medium-carbon alloy, Q&T   |  |
| 8.2           | $\frac{1}{4}$ –1  | 120                           | 150                             | 130                           | Low-carbon martensite, Q&T |  |

Note: Q & T : Quenched and Tempered  
SAE stand for Society of Automobile Engineers.








**ASTM Specifications for Steel Bolts**

| ASTM Designation No. | Size Range, Inclusive, in       | Minimum Proof Strength,* kpsi | Minimum Tensile Strength,* kpsi | Minimum Yield Strength,* kpsi | Material                    | Head Marking  |
|----------------------|---------------------------------|-------------------------------|---------------------------------|-------------------------------|-----------------------------|---|
| A307                 | $\frac{1}{4}$ – $1\frac{1}{2}$  | 33                            | 60                              | 36                            | Low carbon                  |    |
| A325, type 1         | $\frac{1}{2}$ –1                | 85                            | 120                             | 92                            | Medium carbon, Q&T          |    |
|                      | $1\frac{1}{8}$ – $1\frac{1}{2}$ | 74                            | 105                             | 81                            |                             |   |
| A325, type 2         | $\frac{1}{2}$ –1                | 85                            | 120                             | 92                            | Low-carbon, martensite, Q&T |    |
|                      | $1\frac{1}{8}$ – $1\frac{1}{2}$ | 74                            | 105                             | 81                            |                             |   |
| A325, type 3         | $\frac{1}{2}$ –1                | 85                            | 120                             | 92                            | Weathering steel, Q&T       |    |
|                      | $1\frac{1}{8}$ – $1\frac{1}{2}$ | 74                            | 105                             | 81                            |                             |   |
| A354, grade BC       | $\frac{1}{4}$ – $2\frac{1}{2}$  | 105                           | 125                             | 109                           | Alloy steel, Q&T            |  |
|                      | $2\frac{3}{4}$ –4               | 95                            | 115                             | 99                            |                             |   |
| A354, grade BD       | $\frac{1}{4}$ –4                | 120                           | 150                             | 130                           | Alloy steel, Q&T            |  |
| A449                 | $\frac{1}{4}$ –1                | 85                            | 120                             | 92                            | Medium-carbon, Q&T          |  |
|                      | $1\frac{1}{8}$ – $1\frac{1}{2}$ | 74                            | 105                             | 81                            |                             |   |
|                      | $1\frac{3}{4}$ –3               | 55                            | 90                              | 58                            |                             |   |
| A490, type 1         | $\frac{1}{2}$ – $1\frac{1}{2}$  | 120                           | 150                             | 130                           | Alloy steel, Q&T            |  |
| A490, type 3         | $\frac{1}{2}$ – $1\frac{1}{2}$  | 120                           | 150                             | 130                           | Weathering steel, Q&T       |  |

ASTM: stand for American Society for Testing and Materials

**Specifications for Steel Used in Millimeter Series Screws and Bolts**

Metric Mechanical-Property Classes for Steel Bolts, Screws, and Studs

| Property Class | Size Range, Inclusive | Minimum Proof Strength,* MPa | Minimum Tensile Strength,* MPa | Minimum Yield Strength,* MPa | Material                   | Head Marking  |
|----------------|-----------------------|------------------------------|--------------------------------|------------------------------|----------------------------|---|
| 4.6            | M5–M36                | 225                          | 400                            | 240                          | Low or medium carbon       |    |
| 4.8            | M1.6–M16              | 310                          | 420                            | 340                          | Low or medium carbon       |    |
| 5.8            | M5–M24                | 380                          | 520                            | 420                          | Low or medium carbon       |    |
| 8.8            | M16–M36               | 600                          | 830                            | 660                          | Medium carbon, Q&T         |    |
| 9.8            | M1.6–M16              | 650                          | 900                            | 720                          | Medium carbon, Q&T         |   |
| 10.9           | M5–M36                | 830                          | 1040                           | 940                          | Low-carbon martensite, Q&T |  |
| 12.9           | M1.6–M36              | 970                          | 1220                           | 1100                         | Alloy, Q&T                 |  |

**Bolted joint analyses:**

$P$ , Bolted joint tensile force.

$d_c$ : the weakest cross section

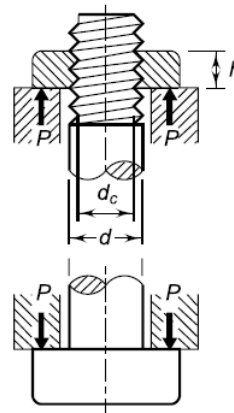
$d$ : bolt nominal diameter

$h$ : nut height

$f_s$ : factor of safety

Maximum tensile stress is given by:

$$\sigma_t = \frac{P}{\left(\frac{\pi}{4} d_c^2\right)}$$



To find the shear in the nut thread: need to make the following assumptions:

- Equal loads are distributing on nut threads,
- There is no stress concentration,
- Failure occurs in bolt thread not in the nut.
- Yield strength in shear is equal to  $\frac{1}{2}$  the yield strength in tension.

$$(S_{sy} = 0.5S_{yt})$$

Hence:

$$\sigma_t = \frac{S_{yt}}{(fs)}$$

Lead to:

$$P = \frac{\pi}{4} d_c^2 \left( \frac{S_{yt}}{fs} \right) \quad (a)$$

Shear stress will be subjected to the nut thread area equal to:

$$(\pi d_c h),$$

Applying shear stress formula:

$$\begin{aligned} P &= (\pi d_c h) \left( \frac{S_{sy}}{fs} \right) \\ &= (\pi d_c h) \left( \frac{S_{yt}}{2fs} \right) \end{aligned} \quad (b)$$

Equating (a) and (b),

$$h = 0.5d_c$$

Assuming ( $d_c = 0.8d$ ),

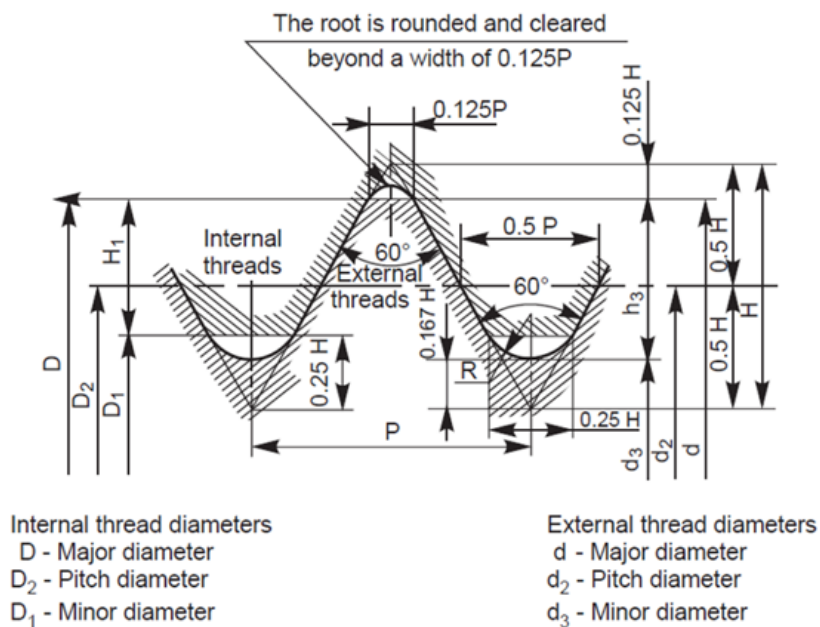
$$h = 0.4d$$



Therefore:

- For standard coarse threads, when the height of nut is approximately 0.4 times the nominal diameter of the bolt, the threads are equally strong in failure by shear and failure by tension,
- The height of standard hexagonal nut is  $0.8d$ , hence threads will not fail by shear.

Or use the geometry of an ISO thread:



Where:

$$\begin{aligned}
 P &= \text{Pitch} \\
 H &= 0.86 P \\
 D &= d = \text{Major diameter} \\
 D_2 &= d_2 = d - 0.75H \\
 D_1 &= d_2 - 2(H/2 - H/4) = d - 2H_1 \\
 d_3 &= d_2 - 2(H/2 - H/6) \\
 &= d - 1.22P \\
 H_1 &= (D - D_1)/2 = 5H/8 = 0.54P \\
 h_3 &= (d - d_3)/2 = 17/24H = 0.61P \\
 R &= H/6 = 0.14P
 \end{aligned}$$

Basic dimension for ISO metric coarse threads:

| <i>Designation</i> | <i>Nominal or major<br/>dia d/D<br/>(mm)</i> | <i>Pitch (p)<br/>(mm)</i> | <i>Pitch diameter<br/><math>d_p/D_p</math><br/>(mm)</i> | <i>Minor diameter</i> |        | <i>Tensile stress area<br/>(mm<sup>2</sup>)</i> |
|--------------------|--|---------------------------|---|-----------------------|--------|---|
|                    |  |                           |   | $d_c$                 | $D_c$  |   |
|                    |  |                           |   | <i>(mm)</i>           |        |   |
| M 4                | 4  | 0.70                      | 3.545   | 3.141                 | 3.242  | 8.78  |
| M 5                | 5  | 0.80                      | 4.480   | 4.019                 | 4.134  | 14.20   |
| M 6                | 6  | 1.00                      | 5.350   | 4.773                 | 4.917  | 20.10   |
| M 8                | 8  | 1.25                      | 7.188   | 6.466                 | 6.647  | 36.60   |
| M 10               | 10   | 1.50                      | 9.026   | 8.160                 | 8.376  | 58.00   |
| M 12               | 12   | 1.75                      | 10.863  | 9.853                 | 10.106 | 84.30   |
| M 16               | 16   | 2.00                      | 14.701  | 13.546                | 13.835 | 157   |
| M 20               | 20   | 2.50                      | 18.376  | 16.933                | 17.294 | 245   |
| M 24               | 24   | 3.00                      | 22.051  | 20.319                | 20.752 | 353   |
| M 30               | 30   | 3.50                      | 27.727  | 25.706                | 26.211 | 561   |
| M 36               | 36   | 4.00                      | 33.402  | 31.093                | 31.670 | 817   |
| M 42               | 42   | 4.50                      | 39.077  | 36.479                | 37.129 | 1120  |
| M 48               | 48   | 5.00                      | 44.752  | 41.866                | 42.587 | 1470  |
| M 56               | 56   | 5.50                      | 52.428  | 49.252                | 50.046 | 2030  |
| M 64               | 64   | 6.00                      | 60.103  | 56.639                | 57.505 | 2680  |
| M 72               | 72   | 6.00                      | 68.103  | 64.639                | 65.505 | 3460  |
| M 80               | 80   | 6.00                      | 76.103  | 72.639                | 73.505 | 4340  |
| M 90               | 90   | 6.00                      | 86.103  | 82.639                | 83.505 | 5590  |
| M 100              | 100  | 6.00                      | 96.103  | 92.639                | 93.505 | 7000  |



## MENG 3050-Power Transmission Components

Basic dimension for ISO metric Fine threads:

| Designation | Nominal or major<br>dia $d/D$<br>(mm) | Pitch ( $p$ )<br>(mm) | Pitch diameter<br>$d_p/D_p$<br>(mm) | Minor diameter |        | Tensile stress<br>area<br>(mm <sup>2</sup> ) |
|-------------|---------------------------------------|-----------------------|-------------------------------------|----------------|--------|--|
|             |                                       |                       |                                     | $d_c$          | $D_c$  |  |
| M 6 × 1     | 6                                     | 1.00                  | 5.350                               | 4.773          | 4.917  | 20.1   |
| M 6 × 0.75  | 6                                     | 0.75                  | 5.513                               | 5.080          | 5.188  | 22.0   |
| M 8 × 1.25  | 8                                     | 1.25                  | 7.188                               | 6.466          | 6.647  | 36.6   |
| M 8 × 1     | 8                                     | 1.00                  | 7.350                               | 6.773          | 6.917  | 39.2   |
| M 10 × 1.25 | 10                                    | 1.25                  | 9.188                               | 8.466          | 8.647  | 61.2   |
| M 10 × 1    | 10                                    | 1.00                  | 9.350                               | 8.773          | 8.917  | 64.5   |
| M 12 × 1.5  | 12                                    | 1.50                  | 11.026                              | 10.160         | 10.376 | 88.1   |
| M 12 × 1.25 | 12                                    | 1.25                  | 11.188                              | 10.466         | 10.647 | 92.1   |
| M 16 × 1.5  | 16                                    | 1.50                  | 15.026                              | 14.160         | 14.376 | 167  |
| M 16 × 1    | 16                                    | 1.00                  | 15.350                              | 14.773         | 14.917 | 178  |
| M 20 × 2    | 20                                    | 2.00                  | 18.701                              | 17.546         | 17.835 | 258  |
| M 20 × 1.5  | 20                                    | 1.50                  | 19.026                              | 18.160         | 18.376 | 272  |
| M 24 × 2    | 24                                    | 2.00                  | 22.701                              | 21.546         | 21.835 | 384  |
| M 24 × 1.5  | 24                                    | 1.50                  | 23.026                              | 22.160         | 22.376 | 401  |
| M 30 × 3    | 30                                    | 3.00                  | 28.051                              | 26.319         | 26.752 | 581  |
| M 30 × 2    | 30                                    | 2.00                  | 28.701                              | 27.546         | 27.835 | 621  |
| M 36 × 3    | 36                                    | 3.00                  | 34.051                              | 32.319         | 32.752 | 865  |
| M 36 × 2    | 36                                    | 2.00                  | 34.701                              | 33.546         | 33.835 | 915  |
| M 42 × 4    | 42                                    | 4.00                  | 39.402                              | 37.093         | 37.670 | 1150   |
| M 42 × 3    | 42                                    | 3.00                  | 40.051                              | 38.319         | 38.752 | 1210   |
| M 48 × 4    | 48                                    | 4.00                  | 45.402                              | 43.093         | 43.670 | 1540   |
| M 48 × 3    | 48                                    | 3.00                  | 46.051                              | 44.319         | 44.752 | 1600   |



## MENG 3050-Power Transmission Components

### Basic Dimensions of Unified Screw Threads (imperial threads)

| Size           | Major Diameter<br>$d$ (in.) | Coarse Threads—UNC |  |  | Fine Threads—UNF |  |  |
|----------------|-----------------------------|--------------------|--|--|------------------|--|--|
|                |                             | Threads per Inch   | Minor Diameter of External Thread<br>$d_r$ (in.) | Tensile Stress Area<br>$A_t$ (in. <sup>2</sup> ) | Threads per Inch | Minor Diameter of External Thread<br>$d_r$ (in.) | Tensile Stress Area<br>$A_t$ (in. <sup>2</sup> ) |
| 0(.060)        | 0.0600                      | —                  | —  | —  | 80               | 0.0447   | 0.00180  |
| 1(.073)        | 0.0730                      | 64                 | 0.0538   | 0.00263  | 72               | 0.0560   | 0.00278  |
| 2(.086)        | 0.0860                      | 56                 | 0.0641   | 0.00370  | 64               | 0.0668   | 0.00394  |
| 3(.099)        | 0.0990                      | 48                 | 0.0734   | 0.00487  | 56               | 0.0771   | 0.00523  |
| 4(.112)        | 0.1120                      | 40                 | 0.0813   | 0.00604  | 48               | 0.0864   | 0.00661  |
| 5(.125)        | 0.1250                      | 40                 | 0.0943   | 0.00796  | 44               | 0.0971   | 0.00830  |
| 6(.138)        | 0.1380                      | 32                 | 0.0997   | 0.00909  | 40               | 0.1073   | 0.01015  |
| 8(.164)        | 0.1640                      | 32                 | 0.1257   | 0.0140   | 36               | 0.1299   | 0.01474  |
| 10(.190)       | 0.1900                      | 24                 | 0.1389   | 0.0175   | 32               | 0.1517   | 0.0200   |
| 12(.216)       | 0.2160                      | 24                 | 0.1649   | 0.0242   | 28               | 0.1722   | 0.0258   |
| $\frac{1}{4}$  | 0.2500                      | 20                 | 0.1887   | 0.0318   | 28               | 0.2062   | 0.0364   |
| $\frac{5}{16}$ | 0.3125                      | 18                 | 0.2443   | 0.0524   | 24               | 0.2614   | 0.0580   |
| $\frac{3}{8}$  | 0.3750                      | 16                 | 0.2983   | 0.0775   | 24               | 0.3239   | 0.0878   |
| $\frac{7}{16}$ | 0.4375                      | 14                 | 0.3499   | 0.1063   | 20               | 0.3762   | 0.1187   |
| $\frac{1}{2}$  | 0.5000                      | 13                 | 0.4056   | 0.1419   | 20               | 0.4387   | 0.1599   |
| $\frac{9}{16}$ | 0.5625                      | 12                 | 0.4603   | 0.182  | 18               | 0.4943   | 0.203  |
| $\frac{5}{8}$  | 0.6250                      | 11                 | 0.5135   | 0.226  | 18               | 0.5568   | 0.256  |
| $\frac{3}{4}$  | 0.7500                      | 10                 | 0.6273   | 0.334  | 16               | 0.6733   | 0.373  |
| $\frac{7}{8}$  | 0.8750                      | 9                  | 0.7387   | 0.462  | 14               | 0.7874   | 0.509  |
| 1              | 1.0000                      | 8                  | 0.8466   | 0.606  | 12               | 0.8978   | 0.663  |
| $1\frac{1}{8}$ | 1.1250                      | 7                  | 0.9497   | 0.763  | 12               | 1.0228   | 0.856  |
| $1\frac{1}{4}$ | 1.2500                      | 7                  | 1.0747   | 0.969  | 12               | 1.1478   | 1.073  |
| $1\frac{3}{8}$ | 1.3750                      | 6                  | 1.1705   | 1.155  | 12               | 1.2728   | 1.315  |
| $1\frac{1}{2}$ | 1.5000                      | 6                  | 1.2955   | 1.405  | 12               | 1.3978   | 1.581  |
| $1\frac{3}{4}$ | 1.7500                      | 5                  | 1.5046   | 1.90   |                  |  |  |
| 2              | 2.0000                      | $4\frac{1}{2}$     | 1.7274   | 2.50   |                  |  |  |
| $2\frac{1}{4}$ | 2.2500                      | $4\frac{1}{2}$     | 1.9774   | 3.25   |                  |  |  |
| $2\frac{1}{2}$ | 2.5000                      | 4                  | 2.1933   | 4.00   |                  |  |  |
| $2\frac{3}{4}$ | 2.7500                      | 4                  | 2.4433   | 4.93   |                  |  |  |
| 3              | 3.0000                      | 4                  | 2.6933   | 5.97   |                  |  |  |
| $3\frac{1}{4}$ | 3.2500                      | 4                  | 2.9433   | 7.10   |                  |  |  |
| $3\frac{1}{2}$ | 3.5000                      | 4                  | 3.1933   | 8.33   |                  |  |  |
| $3\frac{3}{4}$ | 3.7500                      | 4                  | 3.4433   | 9.66   |                  |  |  |
| 4              | 4.0000                      | 4                  | 3.6933   | 11.08  |                  |  |  |

Example:

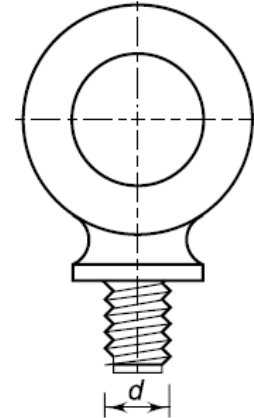
A metal block weighing 10kN, lifted by an eye bolt to be screws to the center of gravity line of action of the block. If the eye bolt has coarse thread, made of carbon steel 30C8 ( $S_{yt}=400\text{N/mm}^2$ ) with factor of safety equal to 6. What would be the bolt size?

$$\sigma_t = \frac{S_{yt}}{(fs)} = \frac{400}{6} = 66.67 \text{ N/mm}^2$$

$$\sigma_t = \frac{P}{\frac{\pi}{4} d_c^2} \quad \therefore 66.67 = \frac{(10 \times 10^3)}{\frac{\pi}{4} d_c^2}$$

$$d_c = 13.82 \text{ mm}$$

$$d = \frac{d_c}{0.8} = \frac{13.82}{0.8} = 17.27 \text{ or } 18 \text{ mm}$$



From the table we go with M20...

Example:

Two plates are fastened as shown, the bolt made of carbon steel 30C8 ( $S_{yt}=400\text{N/mm}^2$ ), and safety factor of 5. Determine the bolt size.

$$S_{sy} = 0.5 S_{yt} = 0.5 (400) = 200 \text{ N/mm}^2$$

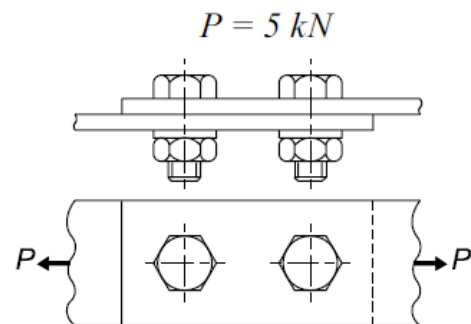
$$\tau = \frac{S_{sy}}{(fs)} = \frac{200}{5} = 40 \text{ N/mm}^2$$

$$\text{Shear area of 2 bolts} = 2 \left( \frac{\pi}{4} d^2 \right) \text{ mm}^2$$

$$\text{Therefore, } P = 2 \left( \frac{\pi}{4} d^2 \right) \tau$$

$$5 \times 10^3 = 2 \left( \frac{\pi}{4} d^2 \right) (40)$$

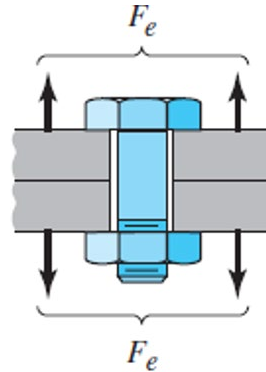
$$\text{or } d = 8.92 \text{ or } 9 \text{ mm}$$



Hence, we will use M10,

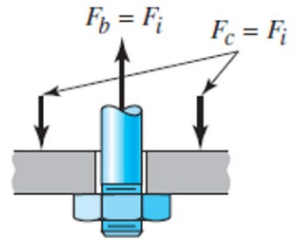
### BOLT TENSION WITH EXTERNAL JOINT-SEPARATING FORCE:

Bolts are typically used to hold parts together in opposition to forces tending to pull, or slide, them apart. The general case of two parts connected with a bolt and subjected to an external force  $F_e$  tending to separate them shown below:



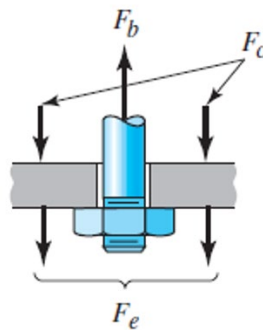
(a)  
Complete joint

Apportion of the above assembly as a free body diagram shown, the nut has been tightened, but the external force has not yet been applied. The bolt axial load  $F_b$  and the clamping force between the two plates  $F_c$  are both equal to the initial tightening force  $F_i$ .



(b)  
Free body without  
external load

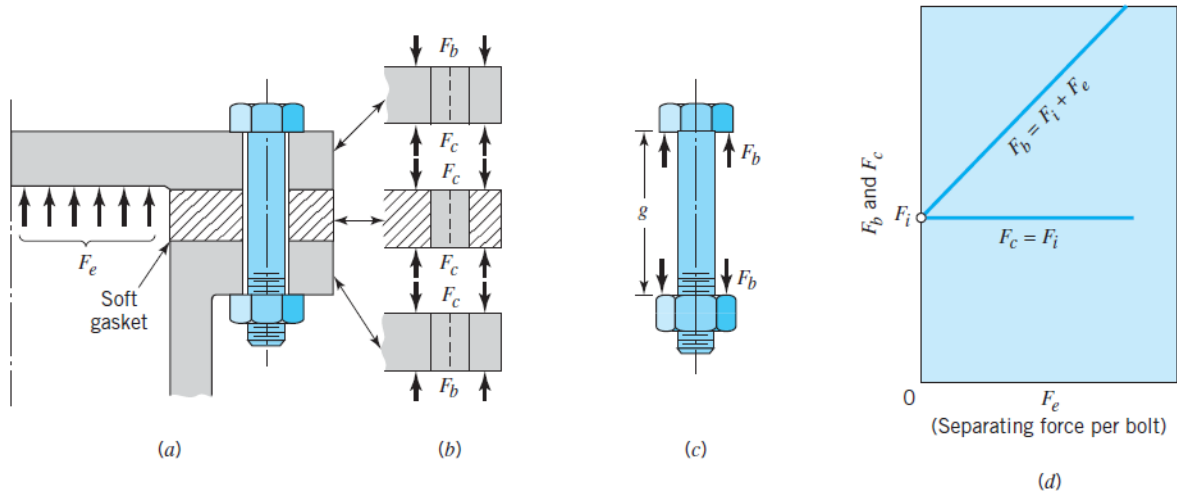
The figure below shows the same members as a free body after external force  $F_e$  has been applied.



(c)  
Free body with  
external load

Example:

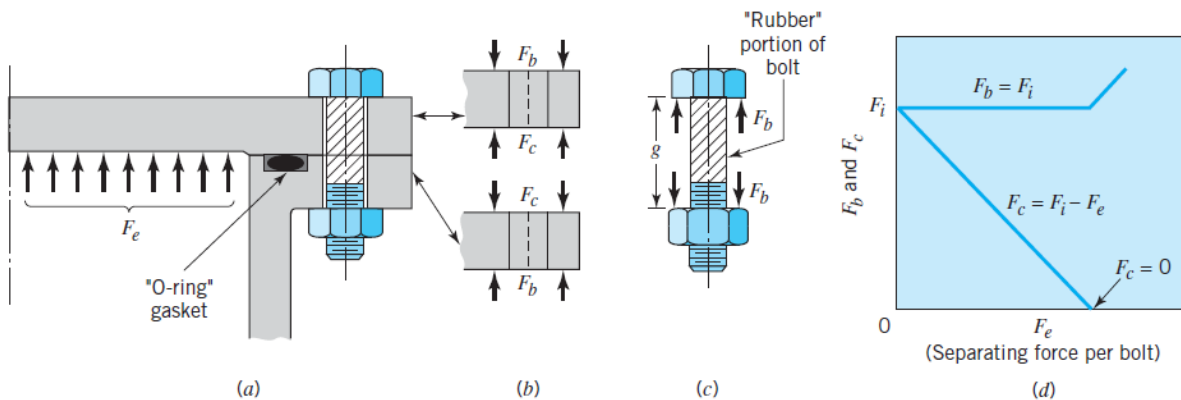
$F_b$  and  $F_c$  versus  $F_e$  per bolt for soft clamped members - rigid bolt



The change in  $F_b$  and  $F_c$  as separating load  $F_e$  is applied. The elastic stretch of the bolt caused by  $F_e$  is so small that the thick rubber gasket cannot expand significantly. Thus, the clamping force  $F_c$  does not diminish, and the *entire* load  $F_e$  goes to increasing bolt tension.

Example:

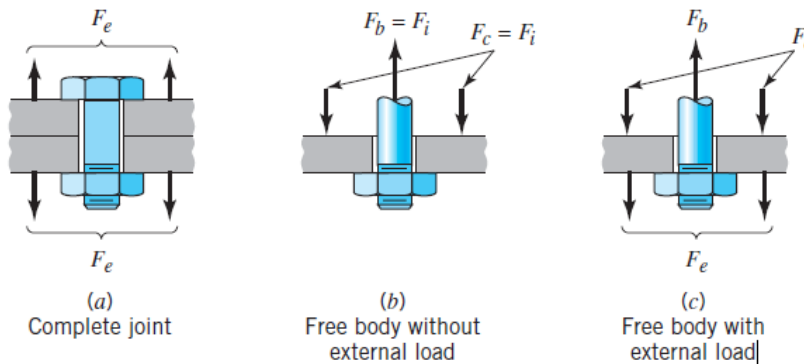
$F_b$  and  $F_c$  versus  $F_e$  per bolt for rigid clamped members—soft bolt.



The clamped members are “rigid” metal parts with precision-ground mating surfaces and no gasket between them. The bolt has a center portion made of rubber. In this case the initial tightening stretches the bolt; it does not significantly compress the clamped members. (Sealing of the fluid is accomplished by a “confined gasket” in the form of a rubber O-ring. Before being compressed by the cover plate, the cross section of the O-ring was circular).



The separating force must be equal to the sum of the increased bolt force plus the decreased clamping force, or



$$F_e = \Delta F_b + \Delta F_c$$

By definition,

$$\Delta F_b = k_b \delta \quad \text{and} \quad \Delta F_c = k_c \delta$$

$$F_e = (k_b + k_c) \delta \quad \text{or} \quad \delta = \frac{F_e}{k_b + k_c}$$

Combining the equations:

$$\Delta F_b = \frac{k_b}{k_b + k_c} F_e \quad \text{and} \quad \Delta F_c = \frac{k_c}{k_b + k_c} F_e$$

Substitute:

$$F_b = F_i + \frac{k_b}{k_b + k_c} F_e \quad \text{and} \quad F_c = F_i - \frac{k_c}{k_b + k_c} F_e$$

The basic equations for axial deflection ( $\delta = PL/AE$ ) and for spring rate ( $k = P/\delta$ ),

$$k_b = \frac{A_b E_b}{g} \quad \text{and} \quad k_c = \frac{A_c E_c}{g}$$

where the grip  $g$  represents the approximate effective length for both



## MENG 3050-Power Transmission Components

### THE TORQUE METHOD:

To impart a preloaded part:

$$T = C \cdot D \cdot F_i$$

where  $T$  = torque

$C$  = torque coefficient

$D$  = nominal diameter of thread

$F_i$  = desired initial preload

Torque coefficient equal to:

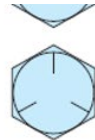
- 0.15 for intensely lubricated fasteners
- 0.2 for partially lubricated, and if cutting oil not washed out yet,
- 0.34 for dry assembly.

### Example:

A  $\frac{3}{4}$ -UNC-grade 5 bolt is to be preloaded to 85 percent of its proof strength.

- The length of the engagement is 5 inches.
- The bolt is new and non-lubricated but likely has traces of cutting oil present.
- Determine the required torque.

|   |                                 |    |     |    |                    |
|---|---------------------------------|----|-----|----|--------------------|
| 5 | $\frac{1}{4}$ -1                | 85 | 120 | 92 | Medium carbon, Q&T |
|   | $1\frac{1}{8}$ - $1\frac{1}{2}$ | 74 | 105 | 81 |                    |



$$A_s = .334 \text{ in}^2$$

$$S_p = 85 \text{ ksi}$$

$$F_i = .85 S_p A_s$$

$$F_i = .85 (85,000 \text{ lb/in}^2) (.334 \text{ in}^2)$$

$$F_i = 24,130 \text{ lb}$$

Using  $C = .2$  non-lubricated with traces of oil:

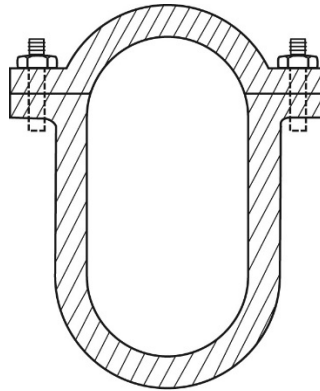
$$T = C D F_i$$

$$T = 0.2 \left(\frac{3}{4} \text{ in}\right) 24,130 \text{ lb}$$

$$T = 3620 \text{ in-lb or } 302 \text{ ft-lb}$$

Example Problem:

- As shown below, a pressure vessel has a sealed head diameter of 20 inches. Using a gasket in between.
- It uses ten 1¼ UNF studs that are fully threaded and have an effective clamping length of 6 inches.
- The clamped area of the flange is 50 in<sup>2</sup>.
- The studs are made of class 8 material.
- $E=30 \times 10^6$  psi (both bolts and flange).



Section view

- Find the torque, assuming new lubricated threads necessary to tighten to 90 percent of the proof strength:
- If the pressure vessel is now pressurized to 500 psi, determine the total load on the bolts. Find the stiffness of both studs and flanges, would the bolts bear such load?

Solution: Find the torque

$$A) \quad T = C \cdot D \cdot F_i$$

$$F_i = S \cdot A$$

$$F_i = 0.90 (120,000 \text{ lb/in}^2) (1.073 \text{ in}^2)$$

$$F_i = 115,884 \text{ lb}$$

$$T = C \cdot D \cdot F_i$$

$$C = 0.15 \text{ lubricating threads}$$

$$T = 0.15 (1.25 \text{ in}) (115,884 \text{ lb})$$

$$T = 21,728 \text{ in-lb or } 1810 \text{ ft-lb}$$

b) total load on the bolts

$$k_b = \frac{AE}{L} = \frac{1.073 \text{ in}^2}{6 \text{ in}} \frac{30 \times 10^6 \text{ lb/in}^2}{}$$

$$k_b = 5.365 \times 10^6 \text{ lb/in per stud}$$

$$k_c = \frac{AE}{L} = \frac{50 \text{ in}^2}{6 \text{ in}} \frac{30 \times 10^6 \text{ lb/in}^2}{}$$

$$k_c = 2.5 \times 10^8 \text{ lb/in}$$

$$F_e = P A \quad (\text{pressure} \times \text{projected area})$$

$$A = \frac{\pi D^2}{4} = \pi (20 \text{ in})^2 / 4 = 314 \text{ in}^2$$

$$F_e = 500 \text{ lb/in}^2 (314 \text{ in}^2)$$

$$F_e = 157,000 \text{ lb}$$

$$F_B = F_i + \left( \frac{k_b}{k_b + k_c} \right) F_e$$

$$F_B = 10 (115,884 \text{ lb}) + \left( \frac{10 \times 5.365 \times 10^6 \text{ lb/in}}{10 \times 5.365 \times 10^6 \text{ lb/in} + 2.5 \times 10^8 \text{ lb/in}} \right) 157,000 \text{ lb}$$

$$F_B = 1.19 \times 10^6 \text{ lb} \quad \text{or} \quad 119,000 \text{ lb/stud}$$