

Class 10

March 27, 2023 11:27 PM

ENGI-1500 Physics -2

Faruk Erkmen, Professor

Faculty of Applied Sciences & Technology
Humber Institute of Technology and Advanced Learning
Winter 2023



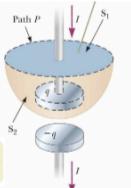
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Reminder of the previous week

Displacement Current

$$\oint \vec{B} \cdot d\vec{s} = \mu_0 I$$

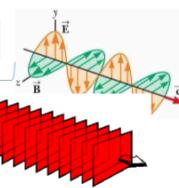
Ampere's law expanded / generalized

$$\oint \vec{B} \cdot d\vec{s} = \mu_0(I + I_d) = \mu_0 I + \mu_0 \epsilon_0 \frac{d\Phi_E}{dt}$$


Plane EM Waves

$$\frac{\partial^2 E}{\partial x^2} = \mu_0 \epsilon_0 \frac{\partial^2 E}{\partial t^2}$$
$$\frac{\partial^2 B}{\partial x^2} = \mu_0 \epsilon_0 \frac{\partial^2 B}{\partial t^2}$$

Solutions to the wave equation

$$E = E_{\max} \cos(kx - \omega t)$$
$$B = B_{\max} \cos(kx - \omega t)$$
$$\frac{\omega}{k} = \frac{2\pi f}{2\pi/\lambda} = \lambda f = c$$
$$c = \frac{1}{\sqrt{(4\pi \times 10^{-7} T \cdot m/A)(8.854 19 \times 10^{-12} C^2/N \cdot m^2)}} = 2.997 92 \times 10^8 \text{ m/s}$$


Momentum & Radiation Pressure

EM waves transport energy as well as momentum. Absorption or reflection of EM waves results in momentum.

$$p = \frac{2T_{ER}}{c} \quad (\text{complete reflection})$$

$$P = \frac{2S}{c} \quad (\text{complete reflection})$$

Solar sailing

Maxwell's Equations

$$\int \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$$

◀ Gauss's law

$$\int \vec{B} \cdot d\vec{A} = 0$$

◀ Gauss's law in magnetism

$$\int \vec{E} \cdot d\vec{s} = -\frac{d\Phi_E}{dt}$$

◀ Faraday's law

$$\int \vec{B} \cdot d\vec{s} = \mu_0 I + \epsilon_0 \mu_0 \frac{d\Phi_B}{dt}$$

◀ Ampère-Maxwell law

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Energy Carried by EM Waves

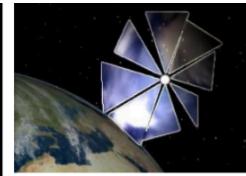
$$\vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B}$$

Poynting vector

$$I = S_{avg} = \frac{E_{max} B_{max}}{2\mu_0} = \frac{E_{max}^2}{2\mu_0 c} = \frac{c B_{max}^2}{2\mu_0}$$

Time average of S: wave intensity

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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.
https://commons.wikimedia.org/wiki/File%3ACosmot_1_solar_sail.jpg
 Source: https://en.wikipedia.org/wiki/Plane_wave

Week 12 / Class 10

Nature of Light and Ray Optics (Ch. 34)

Outline of Week 12 / Class 10

- Reminder of the previous week
- Nature of Light and Ray Optics (Ch. 34)
 - The Nature of Light
 - The Ray Approximation in Ray Optics
 - Analysis Model: Wave Under Reflection
 - Analysis Model: Wave Under Refraction
 - Huygen's Principle [Optional – Reading from Textbook]
 - Dispersion
 - Total Internal Reflection
- Examples
- Next week's topic

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Nature of Light and Ray Optics (Ch. 34)

→ The Nature of Light

The Ray Approximation in Ray Optics
 Analysis Model: Wave Under Reflection
 Analysis Model: Wave Under Refraction
 Huygen's Principle [Optional – Reading from Textbook]
 Dispersion
 Total Internal Reflection

Nature of Light and Ray Optics (Ch. 34)

The Nature of Light

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The Nature of Light

History

- Before the beginning of 19th century:
 - Light was considered to be a stream of particles either emitted by an object being viewed or emanated from the eyes of the viewer
- **Newton:** chief architect of particle model of light
 - Believed that **the particles were emitted from the light source**
 - These particles stimulated a sense of sight upon entering the eye
- Using this idea: able to explain reflection and refraction
- Most scientists accepted Newton's particle model
- During Newton's lifetime another model was proposed:
 - Light might be **some sort of a wave motion**
- In 1678 **Christian Huygens** showed that wave model of light could also explain reflection and refraction

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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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The Nature of Light

History

- In 1801, **Thomas Young** provided the first clear experimental demonstration of wave nature of light
 - Light rays **interfere with one another** according to waves in interference model
 - Such behavior could not be explained by particle model
 - Not conceivable for particles to combine or cancel one another
- In 1873, **Maxwell** asserted that light was a form of high-frequency electromagnetic waves
- **Hertz** provided experimental confirmation of Maxwell's theory in 1887 by producing and detecting electromagnetic waves
- Results represented were convincing information that light has wave nature
→ Scientists accepted **wave nature of light**

The Nature of Light

History

- Light travels at a high speed ($c \approx 3.00 \times 10^8 \text{ m/s}$)
- Early attempts to measure speed were unsuccessful
 - Galileo attempted to measure speed of light by positioning two observers in towers separated by $\approx 10 \text{ km}$
 - Each observer carried a shuttered lantern
 - One observer would open his shutter first, then the other would open his shutter at the moment he saw light from the first lantern
 - Reasoning: calculating the light speed with the distance divided by the transit time of the light beams from one lantern to the other
- Measurement was not successful
 - Transit time: $10000 \text{ m}/(3 \times 10^8 \text{ m/s}) = 33 \mu\text{s}$
 - << reaction time of observers in opening the shutters



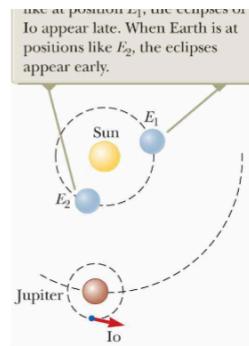
The Nature of Light

Measuring Speed of Light: Roemer's Method

- In 1675: **Ole Roemer** made observations that led to the first successful estimate of the speed of light
- After collecting data for more than a year, Roemer observed a systematic variation in **Io**'s period (Io: one of the moons of Jupiter)

When Earth is far from Jupiter
The orbital period of Io is longer

- Longer than average - when Earth was at the opposite side of the Sun and far from Jupiter (E_1 in figure)
- Earlier than average - when Earth was on the same side of the Sun and close to Jupiter (E_2 in figure)
- Roemer attributed the variation in observed period to the extra time interval required for light for earth at different distances from Jupiter
- Using Roemer's data, **Huygens** estimated lower limit for speed of light $\approx 2.3 \times 10^8$ m/s



Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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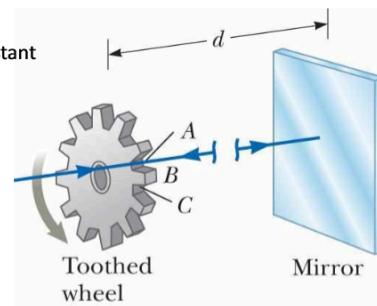
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The Nature of Light

Measuring Speed of Light: Fizeau's Method

- First successful method for measuring the speed of light by purely terrestrial techniques was developed in 1849 by **Armand H. L. Fizeau**
- Fizeau measured the total time interval during which light travels from some point to a distant mirror and back (*approximately 8km/s away*)
 - d = distance between the light source and the mirror
 - Time interval for one round trip = Δt
 - Speed of light is $c = 2d/\Delta t$
- To measure the transit time: Fizeau used rotating toothed wheel
 - Converts continuous beam of light into series of light pulses
 - Wheel acts as light source and defines one end of distance d
 - Observer looks through the teeth and determines whether or not the reflected light is observable
- At a great enough rate of rotation →
 - Opening at point C could move into position to allow reflected pulse to reach the observer
- Knowing distance d , number of teeth in wheel, and angular speed of wheel:
 - Fizeau arrived at a value of 3.1×10^8 m/s



More accurate $c = 2.99792458 \times 10^8$ m/s.

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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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Nature of Light and Ray Optics (Ch. 34)

The Ray Approximation in Ray Optics

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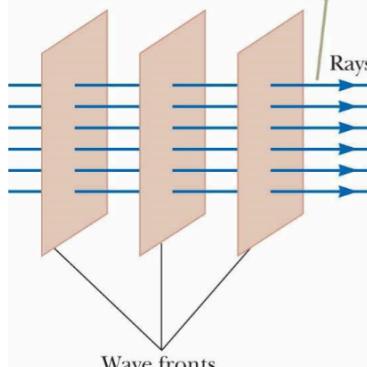
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The Ray Approximation in Ray Optics

- **Ray optics (geometric optics):** involves the study of propagation of light
 - Assumes light travels in a fixed direction in a straight line as it passes through a uniform medium
 - Changes direction when it meets a surface of a different medium or if the optical properties of a medium is nonuniform in either space or time
- **Ray approximation:** recall that the rays of a given wave are straight lines that are perpendicular to the wave fronts for plane waves (figure)
 - Wave moving through a uniform medium travels in a straight line in the direction of its rays

The rays, which always point in the direction of the wave propagation, are straight lines perpendicular to the wave fronts.



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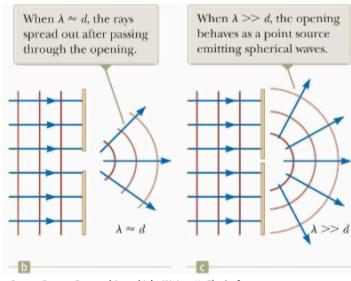
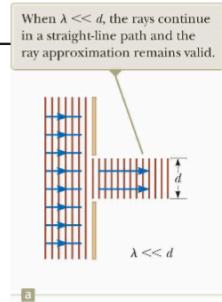
Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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The Ray Approximation in Ray Optics

If the wave meets a barrier in which there is a circular opening;

- **Figure (a):** diameter of the opening \gg (much larger than) wavelength
 - Wave emerging from the opening continues to move in a straight line (apart from some small edge effects)
 - Ray approximation is valid
- **Figure (b):** diameter of the opening \sim (comparable to) wavelength
 - Waves spread out from the opening in all directions: **diffraction**
- **Figure (c):** opening \ll (much smaller than) wavelength
 - Waves to the right of the barrier can be approximated as if there is a point source at the opening
- Similar effects can be seen when the waves encounter an opaque object of dimension d
- Ray approximation and the assumption $\lambda \ll d$ is used in this chapter.
 - Appropriate for study of mirrors, lenses, prisms, and associated optical instruments such as telescopes, cameras, and eyeglasses



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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Nature of Light and Ray Optics (Ch. 34)

The Nature of Light

The Ray Approximation in Ray Optics

→ **Analysis Model: Wave Under Reflection**

Analysis Model: Wave Under Refraction

Huygen's Principle [Optional – Reading from Textbook]

Dispersion

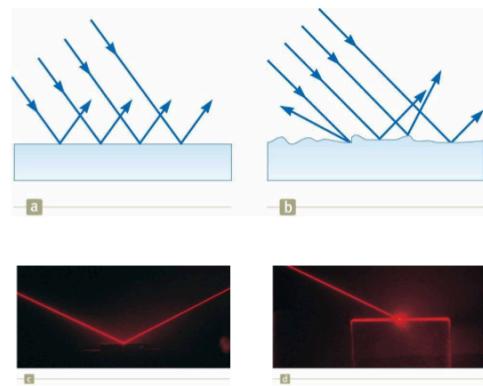
Total Internal Reflection

Nature of Light and Ray Optics (Ch. 34)

Analysis Model: Wave Under Reflection

Analysis Model: Wave Under Reflection

- When a light ray traveling in one medium encounters a boundary with another medium:
 - Part of the incident light gets reflected from the smooth, mirror-like, reflecting surface (figures (a) & (c))
 - Reflected rays are parallel to one another
 - Direction of reflected rays are in a plane perpendicular to the reflecting surface
- Reflection of light from smooth surfaces: ***specular reflection***
- If the reflecting surface is rough (figures (b) & (d)):
 - Surface reflects rays in various directions
- Reflection from any rough surface: ***diffuse reflection***
- A surface behaves as a smooth surface as long as the surface variations are << wavelength of the incident light
- For the scope of this course, we restrict our study to specular reflection and use the term **reflection** to mean ***specular reflection***



Analysis Model: Wave Under Reflection

- Consider a light ray traveling in the air and it's incident at an angle on a flat, smooth surface as shown in the figure

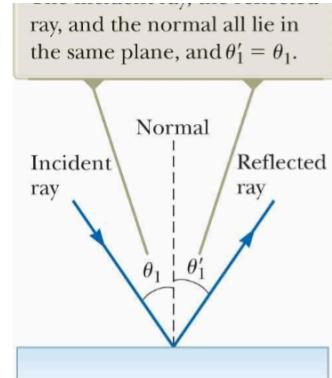
The incident ray, the reflected

surface as shown in the figure.

- Incident and reflected rays make angles θ_1 and θ'_1 , respectively
 - The angles are measured between the normal and the rays
 - **Normal** = a line drawn perpendicular to the surface at the point where the incident ray strikes the surface
- Experiments and theory show that the angle of reflection = the angle of incidence

$$\theta'_1 = \theta_1$$

Law of Reflection



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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Quick Quiz

Quick Quiz

In the movies, you sometimes see an actor looking in a mirror and you can see his face in the mirror. It can be said with certainty that during the filming of such a scene, the actor sees in the mirror:

- (a) his face
- (b) your face
- (c) the director's face
- (d) the movie camera
- (e) impossible to determine

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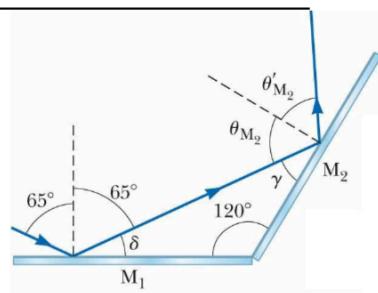
Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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The Double-Reflected Light Ray

Example 34.2

Two mirrors make an angle of 120° with each other as illustrated in the figure. A ray is incident on mirror M_1 at an angle of 65° to the normal. Find the direction of the ray after it is reflected from mirror M_2 .



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The Double-Reflected Light Ray

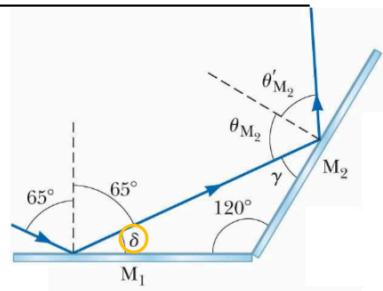
Example 34.2

Two mirrors make an angle of 120° with each other as illustrated in the figure. A ray is incident on mirror M_1 at an angle of 65° to the normal. Find the direction of the ray after it is reflected from mirror M_2 .

Solution

From the law of reflection, the first reflected ray makes an angle of 65° with the normal.

Find the angle the first reflected ray makes with the horizontal: $\delta = 90^\circ - 65^\circ = 25^\circ$



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

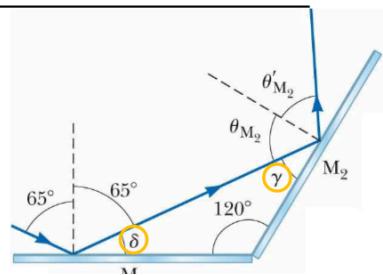
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The Double-Reflected Light Ray

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Solution



From the law of reflection, the first reflected ray makes an angle of 65° with the normal.

Find the angle the first reflected ray makes with the horizontal:

$$\delta = 90^\circ - 65^\circ = 25^\circ$$

From the triangle made by the first reflected ray and the two mirrors, find the angle the reflected ray makes with M_2 :

$$\gamma = 180^\circ - 25^\circ - 120^\circ = 35^\circ$$

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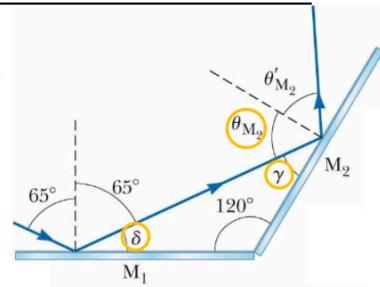
$$\delta = 90^\circ - 65^\circ = 25^\circ$$

From the triangle made by the first reflected ray and the two mirrors, find the angle the reflected ray makes with M_2 :

$$\gamma = 180^\circ - 25^\circ - 120^\circ = 35^\circ$$

Find the angle the first reflected ray makes with the normal to M_2 :

$$\theta_{M_2} = 90^\circ - 35^\circ = 55^\circ$$



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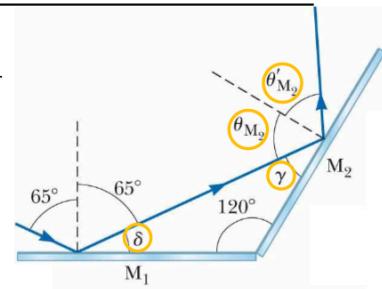
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The Double-Reflected Light Ray

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Solution

From the law of reflection, the first reflected ray makes an angle of 65° with the normal.

Find the angle the first reflected ray makes with the horizontal:

$$\delta = 90^\circ - 65^\circ = 25^\circ$$

From the triangle made by the first reflected ray and the two mirrors, find the angle the reflected ray makes with M_2 :

$$\gamma = 180^\circ - 25^\circ - 120^\circ = 35^\circ$$

Find the angle the first reflected ray makes with the normal to M_2 :

$$\theta_{M_2} = 90^\circ - 35^\circ = 55^\circ$$

From the law of reflection, find the angle the second reflected ray makes with the normal to M_2 :

$$\theta'_{M_2} = \theta_{M_2} = 55^\circ$$

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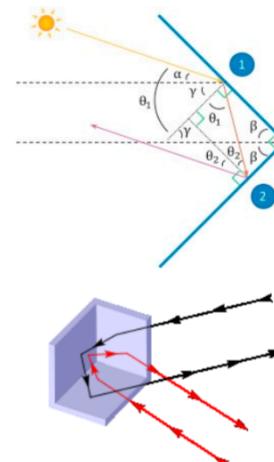
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Analysis Model: Wave Under Reflection

Retroreflection

- If the angle between two mirrors is 90° , the reflected beam returns to the source parallel to its original path.
- This phenomenon, called **retroreflection**, has many practical applications:
 - If a third mirror is placed perpendicular to first two:
 - A cube corner for 3D retroreflection



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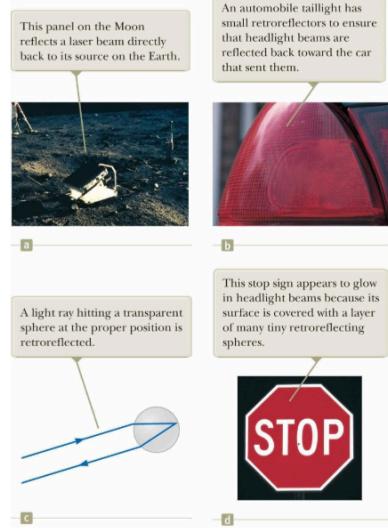
Source:
<https://www.sciencedirect.com/science/article/pii/S0977024819304465>
<https://en.wikipedia.org/wiki/Retroreflector>

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Analysis Model: Wave Under Reflection

Retroreflection

- Applications:
 - In 1969: retroreflectors were placed on the Moon (figure (a)) to reflect a laser beam from Earth in order to determine the distance to the Moon within certainty of 15 cm
 - Automobile taillights consist of many tiny cube corners (figure (b)) or small spherical bumps (figure (c)) to reflect headlight beams from cars approaching in the back
 - Road signs coated with tiny clear spheres appear much brighter due to retroreflection
 - Retroreflectors are used for reflective panels on running shoes and running clothing for joggers to be seen at night



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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Nature of Light and Ray Optics (Ch. 34)

The Nature of Light

The Ray Approximation in Ray Optics

Analysis Model: Wave Under Reflection

→ Analysis Model: Wave Under Refraction

Huygen's Principle [Optional – Reading from Textbook]

Dispersion

Total Internal Reflection

Nature of Light and Ray Optics (Ch. 34)

Analysis Model: Wave Under Refraction

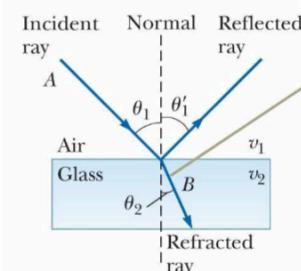
Analysis Model: Wave Under Refraction

- When a ray of light travels through one transparent medium to another transparent medium (figure), at the boundary;
 - Part of the light energy is reflected;
 - Part of the energy enters (is refracted into) the second medium;
- The ray that enters the second medium (transmitted) changes its direction of propagation at the boundary and is said to be **refracted**.
- The incident ray, the reflected ray, and the refracted ray all lie in the same plane.
- The angle of refraction θ_2 depends on the properties of the two media and on the angle of incidence θ_1 through the relationship
 - θ_2 : angle of refraction
 - v_1 : speed of light in the first medium
 - v_2 : speed of light in the second medium

$$\theta'_1 = \theta_1$$

$$\frac{\sin \theta_2}{\sin \theta_1} = \frac{v_2}{v_1}$$

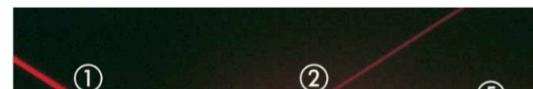
All rays and the normal lie in the same plane, and the refracted ray is bent toward the normal because $v_2 < v_1$.



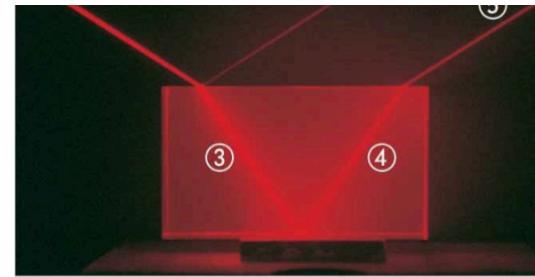
Quick Quiz

Quick Quiz

If beam 1 is the incoming beam in the figure, which of the other four red lines are reflected beams and which are refracted beams?



- 1) Incident
- 2)
- 3)
- 4)
- 5)



b

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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

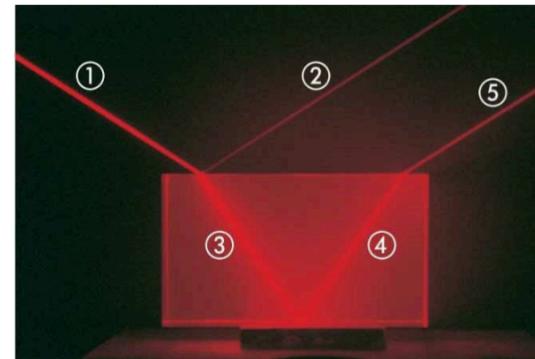
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Quick Quiz

Quick Quiz

If beam 1 is the incoming beam in the figure, which of the other four red lines are reflected beams and which are refracted beams?

- 1) Incident
- 2) Reflected
- 3) Refracted
- 4) Reflected
- 5) Refracted



b

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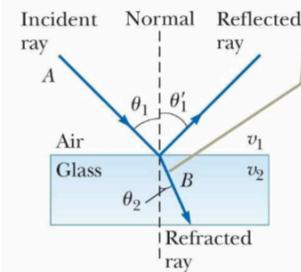
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Analysis Model: Wave Under Refraction

Reversible path

- The path of a light ray through a refracting surface is **reversible**
- For example: the ray shown in the figure travels from point A to point B
 - If the ray originated at B →
 - It would travel upward to the point of incidence at the surface
 - Then bends away from the normal
 - Then reaches point A

All rays and the normal lie in the same plane, and the refracted ray is bent toward the normal because $v_2 < v_1$.



a

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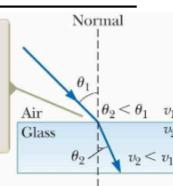
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Analysis Model: Wave Under Refraction

- When light moves from the 1st material with a higher speed to the 2nd material with a slower speed (figure (a)):
 - Angle of refraction $\theta_2 <$ angle of incidence θ_1
 - Ray bent *toward* surface normal
- If light moves from the 1st material with a lower speed to the 2nd material with a higher speed (figure (b)):
 - $\theta_2 > \theta_1$
 - Ray is bent *away* from the surface normal

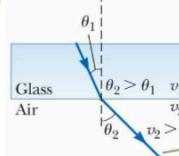
When the light beam moves from air into glass, the light slows down upon entering the glass and its path is bent toward the normal.



a

$$\frac{\sin \theta_2}{\sin \theta_1} = \frac{v_2}{v_1}$$

When the beam moves from glass into air, the light speeds up upon entering the air and its path is bent away from the normal.



b

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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

31

Analysis Model: Wave Under Refraction

Index of refraction

- In general: speed of light in any material is *less* than its speed in vacuum
 - Light travels at its maximum speed c in vacuum.*
- Index of refraction n of a medium is:**

$$n \equiv \frac{\text{speed of light in vacuum}}{\text{speed of light in a medium}} \equiv \frac{c}{v}$$

TABLE 34.1 Indices of Refraction

Substance	Index of Refraction	Substance	Index of Refraction
<i>Solids at 20°C</i>			
Cubic zirconia	2.20	Benzene	1.501
Diamond (C)	2.419	Carbon disulfide	1.628
Fluorite (CaF_2)	1.434	Carbon tetrachloride	1.461
Fused quartz (SiO_2)	1.458	Ethyl alcohol	1.361
Gallium phosphide	3.50	Glycerin	1.473
Glass, crown	1.52	Water	1.333
Glass, flint	1.66		
Ice (H_2O)	1.309	<i>Gases at 0°C, 1 atm</i>	
Polystyrene	1.49	Air	1.000 293
Sodium chloride (NaCl)	1.514	Carbon dioxide	1.000 45

Note: All values are for light having a wavelength of 589 nm in vacuum.

- Index of refraction: dimensionless number > 1 (because v always $< c$)
- $n = 1$ for vacuum

- Table: indices of refraction for various substances
 - Use $n = 1$ for air

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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

32

Analysis Model: Wave Under Refraction

Index of refraction

- As light travels from one medium to another, its frequency does not change but its wavelength does.

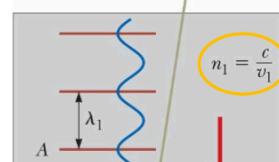
$$v = \lambda f$$

$$f_1 = f_2 = f$$

$$v_1 = \lambda_1 f \quad \text{and} \quad v_2 = \lambda_2 f$$

$$\lambda_1 = \frac{v_1}{n_1} = \frac{c/n_1}{n_1} = \frac{n_2}{n_1}$$

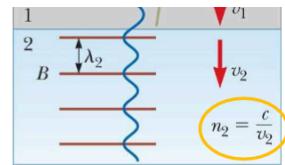
As a wave moves between the media, its wavelength changes but its frequency remains constant.



$$\lambda_2 = v_2 = c/n_2 = n_1 \quad n = \frac{\lambda}{\lambda_n}$$

λ = wavelength of light in vacuum
 λ_n = wavelength of light in medium with index of refraction n

Because $n > 1$, $\lambda_n < \lambda$



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Source: Serway, Raymond A., and John W. Jewett. Physics for scientists and engineers. 10th Edition. Cengage learning, 2018.

33

Analysis Model: Wave Under Refraction

Snell's Law

- With the definition of '**index of refraction**', we can have an alternative formula:

$$\frac{\sin \theta_2}{\sin \theta_1} = \frac{v_2}{v_1}$$

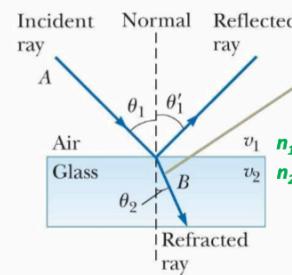
$$\downarrow$$

$$\begin{aligned} n &= c/v \\ v_2/v_1 &= n_1/n_2 \end{aligned}$$

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

Snell's Law of Refraction

All rays and the normal lie in the same plane, and the refracted ray is bent toward the normal because $v_2 < v_1$.



- Experimental discovery of this relationship was credited to **Willebrord Snell**
- Other waves (e.g., seismic waves and sound waves) also exhibit refraction according to this model.

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Source: Serway, Raymond A., and John W. Jewett. Physics for scientists and engineers. 10th Edition. Cengage learning, 2018.

34

Angle of Refraction for Glass

TABLE 34.1 Indices of Refraction

Example 34.3

A light ray of wavelength $\lambda=589\text{nm}$ traveling through air is incident on a smooth, flat slab of crown glass at an angle of $\theta_1=30.0^\circ$ to the normal.

(A) Find the angle of refraction.

(B) Find the speed of this light once it enters the glass.

(C) What is the wavelength of this light in the glass?

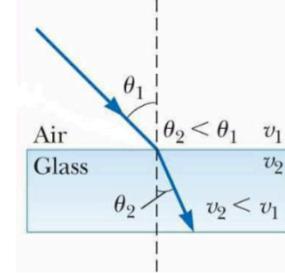
$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2} = \frac{c/n_1}{c/n_2} = \frac{n_2}{n_1}$$

Substance	Index of Refraction	Substance	Index of Refraction
Solids at 20°C		Liquids at 20°C	
Cubic zirconia	2.20	Benzene	1.501
Diamond (C)	2.419	Carbon disulfide	1.628
Fluorite (CaF ₂)	1.434	Carbon tetrachloride	1.461
Fused quartz (SiO ₂)	1.458	Ethyl alcohol	1.361
Gallium phosphide	3.50	Glycerin	1.473
Glass, crown	1.52	Water	1.333
Glass, flint	1.66		
Ice (H ₂ O)	1.309	Gases at 0°C, 1 atm	
Polystyrene	1.49	Air	1.000 293
Sodium chloride (NaCl)	1.544	Carbon dioxide	1.000 45

Note: All values are for light having a wavelength of 589 nm in vacuum.

Normal



Source: Serway, Raymond A., and John W. Jewett. Physics for scientists and engineers. 10th Edition. Cengage learning, 2018. 35

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Angle of Refraction for Glass

Example 34.3

A light ray of wavelength $\lambda=589\text{nm}$ traveling through air is incident on a smooth, flat slab of crown glass at an angle of $\theta_1=30.0^\circ$ to the normal.

(A) Find the angle of refraction.

(B) Find the speed of this light once it enters the glass.

(C) What is the wavelength of this light in the glass?

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2} = \frac{c/n_1}{c/n_2} = \frac{n_2}{n_1}$$

Solution

Solution for (A)

Rearrange Snell's law:

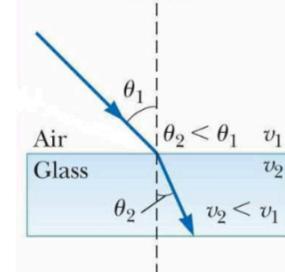
$$\sin \theta_2 = \frac{n_1}{n_2} \sin \theta_1$$

TABLE 34.1 Indices of Refraction

Substance	Index of Refraction	Substance	Index of Refraction
Solids at 20°C		Liquids at 20°C	
Cubic zirconia	2.20	Benzene	1.501
Diamond (C)	2.419	Carbon disulfide	1.628
Fluorite (CaF ₂)	1.434	Carbon tetrachloride	1.461
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Glass, crown	1.52	Water	1.333
Glass, flint	1.66		
Ice (H ₂ O)	1.309	Gases at 0°C, 1 atm	
Polystyrene	1.49	Air	1.000 293
Sodium chloride (NaCl)	1.544	Carbon dioxide	1.000 45

Note: All values are for light having a wavelength of 589 nm in vacuum.

Normal



Source: Serway, Raymond A., and John W. Jewett. Physics for scientists and engineers. 10th Edition. Cengage learning, 2018. 36

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Angle of Refraction for Glass

Example 34.3

A light ray of wavelength $\lambda=589\text{nm}$ traveling through air is incident on a smooth, flat slab of crown glass at an angle of $\theta_1=30.0^\circ$ to the normal.

(A) Find the angle of refraction.

- (B) Find the speed of this light once it enters the glass.
 (C) What is the wavelength of this light in the glass?

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2} = \frac{c/n_1}{c/n_2} = \frac{n_2}{n_1}$$

Solution

Solution for (A)

Rearrange Snell's law:

$$\sin \theta_2 = \frac{n_1}{n_2} \sin \theta_1$$

Solve for θ_2 :

$$\theta_2 = \sin^{-1} \left(\frac{n_1}{n_2} \sin \theta_1 \right)$$

Substitute values:

$$\theta_2 = \sin^{-1} \left(\frac{1.00}{1.52} \sin 30.0^\circ \right) = ?$$

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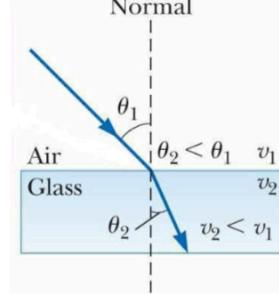
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TABLE 34.1 Indices of Refraction

Substance	Index of Refraction	Substance	Index of Refraction
Solids at 20°C		Liquids at 20°C	
Cubic zirconia	2.20	Benzene	1.501
Diamond (C)	2.419	Carbon disulfide	1.628
Fluorite (CaF ₂)	1.434	Carbon tetrachloride	1.461
Fused quartz (SiO ₂)	1.458	Ethyl alcohol	1.361
Gallium phosphide	3.50	Glycerin	1.473
Glass, crown	1.52	Water	1.333
Glass, flint	1.66		
Ice (H ₂ O)	1.309	Gases at 0°C, 1 atm	
Polystyrene	1.49	Air	1.000 293
Sodium chloride (NaCl)	1.544	Carbon dioxide	1.000 45

Note: All values are for light having a wavelength of 589 nm in vacuum.

Normal



Source: Serway, Raymond A., and John W. Jewett. Physics for scientists and engineers. 10th Edition. Cengage learning, 2018. 37

Angle of Refraction for Glass

Example 34.3

A light ray of wavelength $\lambda=589\text{nm}$ traveling through air is incident on a smooth, flat slab of crown glass at an angle of $\theta_1=30.0^\circ$ to the normal.

(A) Find the angle of refraction.

- (B) Find the speed of this light once it enters the glass.
 (C) What is the wavelength of this light in the glass?

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2} = \frac{c/n_1}{c/n_2} = \frac{n_2}{n_1}$$

Solution

Solution for (A)

Rearrange Snell's law:

$$\sin \theta_2 = \frac{n_1}{n_2} \sin \theta_1$$

Solve for θ_2 :

$$\theta_2 = \sin^{-1} \left(\frac{n_1}{n_2} \sin \theta_1 \right)$$

Substitute values:

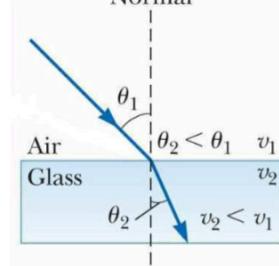
$$\theta_2 = \sin^{-1} \left(\frac{1.00}{1.52} \sin 30.0^\circ \right) = 19.2^\circ$$

TABLE 34.1 Indices of Refraction

Substance	Index of Refraction	Substance	Index of Refraction
Solids at 20°C		Liquids at 20°C	
Cubic zirconia	2.20	Benzene	1.501
Diamond (C)	2.419	Carbon disulfide	1.628
Fluorite (CaF ₂)	1.434	Carbon tetrachloride	1.461
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Gallium phosphide	3.50	Glycerin	1.473
Glass, crown	1.52	Water	1.333
Glass, flint	1.66		
Ice (H ₂ O)	1.309	Gases at 0°C, 1 atm	
Polystyrene	1.49	Air	1.000 293
Sodium chloride (NaCl)	1.544	Carbon dioxide	1.000 45

Note: All values are for light having a wavelength of 589 nm in vacuum.

Normal



Angle of Refraction for Glass

Example 34.3

A light ray of wavelength $\lambda=589\text{nm}$ traveling through air is incident on a smooth, flat slab of crown glass at an angle of $\theta_1=30.0^\circ$ to the normal.

(A) Find the angle of refraction.

(B) Find the speed of this light once it enters the glass.

(C) What is the wavelength of this light in the glass?

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2} = \frac{c/n_1}{c/n_2} = \frac{n_2}{n_1}$$

Solution

Solution for (B)

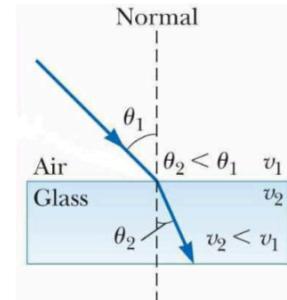
$$v = \frac{c}{n}$$

$$v = \frac{3.00 \times 10^8 \text{ m/s}}{1.52} = 1.97 \times 10^8 \text{ m/s}$$

TABLE 34.1 Indices of Refraction

Substance	Index of Refraction	Substance	Index of Refraction
Solids at 20°C		Liquids at 20°C	
Cubic zirconia	2.20	Benzene	1.501
Diamond (C)	2.419	Carbon disulfide	1.628
Fluorite (CaF ₂)	1.434	Carbon tetrachloride	1.461
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Ice (H ₂ O)	1.309	Gases at 0°C, 1 atm	
Polystyrene	1.49	Air	1.000 293
Sodium chloride (NaCl)	1.544	Carbon dioxide	1.000 45

Note: All values are for light having a wavelength of 589 nm in vacuum.



Angle of Refraction for Glass

Example 34.3

A light ray of wavelength $\lambda=589\text{nm}$ traveling through air is incident on a smooth, flat slab of crown glass at an angle of $\theta_1=30.0^\circ$ to the normal.

(A) Find the angle of refraction.

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(C) What is the wavelength of this light in the glass?

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2} = \frac{c/n_1}{c/n_2} = \frac{n_2}{n_1}$$

TABLE 34.1 Indices of Refraction

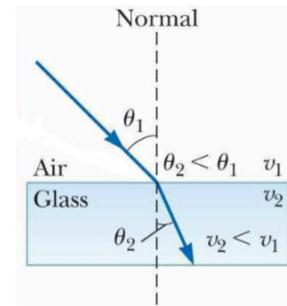
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Glass, crown	1.52	Water	1.333
Glass, flint	1.66		
Ice (H ₂ O)	1.309	Gases at 0°C, 1 atm	
Polystyrene	1.49	Air	1.000 293
Sodium chloride (NaCl)	1.544	Carbon dioxide	1.000 45

Solution

Solution for (C)

$$\lambda_n = \frac{\lambda}{n} = \frac{589 \text{ nm}}{1.52} = 388 \text{ nm}$$

Note: All values are for light having a wavelength of 589 nm in vacuum.



Source: Serway, Raymond A., and John W. Jewett. Physics for scientists and engineers. 10th Edition. Cengage learning, 2018. 40

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Angle of Refraction for Glass

Example 34.3

A light ray of wavelength $\lambda=589\text{nm}$ traveling through air is incident on a smooth, flat slab of crown glass at an angle of $\theta_1=30.0^\circ$ to the normal.

- (A) Find the angle of refraction.
- (B) Find the speed of this light once it enters the glass.
- (C) What is the wavelength of this light in the glass?

$$n_1 \sin \theta_1 = n_2 \sin \theta_2$$

$$\frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2} = \frac{c/n_1}{c/n_2} = \frac{n_2}{n_1}$$

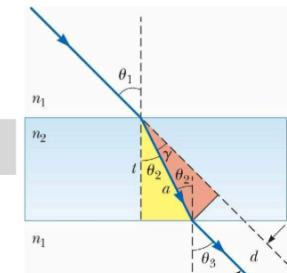
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Gallium phosphide	3.50	Glycerin	1.473
Glass, crown	1.52	Water	1.333
Glass, flint	1.60		
Ice (H_2O)	1.309	<i>Liquids at 20°C</i>	
Polystyrene	1.49	Benzene	1.501
Sodium chloride (NaCl)	1.544	Carbon disulfide	1.628
<i>Gases at 0°C, 1 atm</i>			
Air	1.000 293		
Carbon dioxide	1.000 45		

Note: All values are for light having a wavelength of 589 nm in vacuum.

Example 34.4

What would happen if the light beam was passing through a thick slab of material whose index of refraction is n_2 ? Show that the beam emerging into medium 1 from the other side is parallel to the incident beam.



Source: Serway, Raymond A., and John W. Jewett. Physics for scientists and engineers. 10th Edition. Cengage learning, 2018. 41

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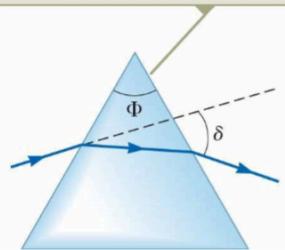
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Analysis Model: Wave Under Refraction

Prisms

- We talked about a slab of material with parallel sides.
- What happens when light strikes a prism with nonparallel sides as shown in the figure?
- In this case, the outgoing ray does not propagate in the same direction as the incoming ray. A ray of single-wavelength light incident on the prism from the left emerges at angle δ from its original direction of travel.
- This angle δ is called the angle of deviation.
- The apex angle Φ of the prism, shown in the figure, is defined as the angle between the surface at which the light enters the prism and the second surface that the light encounters.

The apex angle Φ is the angle between the sides of the prism through which the light enters and leaves.



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

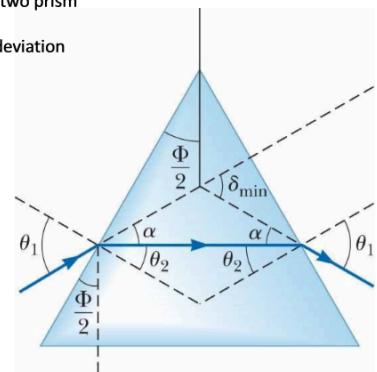
42

Angle of Refraction for Glass

Example 34.5

Although we do not prove it here, the minimum angle of deviation δ_{\min} for a prism occurs when the angle of incidence θ_1 is such that the refracted ray inside the prism makes the same angle with the normal to the two prism faces as shown in the figure.

Obtain an expression for the index of refraction of the prism material in terms of the minimum angle of deviation (δ_{\min}) and the apex angle (Φ).



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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Angle of Refraction for Glass

Example 34.5

Although we do not prove it here, the minimum angle of deviation δ_{\min} for a prism occurs when the angle of incidence θ_1 is such that the refracted ray inside the prism makes the same angle with the normal to the two prism faces as shown in the figure.

Obtain an expression for the index of refraction of the prism material in terms of the minimum angle of deviation (δ_{\min}) and the apex angle (Φ).

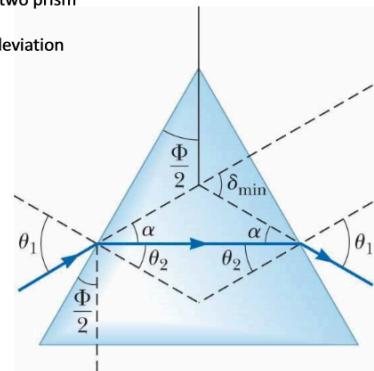
Solution

First, can we observe:

$$\theta_1 = \theta_2 + \alpha$$

$$\theta_2 = \frac{\Phi}{2}$$

$$\delta_{\min} = 2\alpha$$



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018. 44

Angle of Refraction for Glass

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Obtain an expression for the index of refraction of the prism material in terms of the minimum angle of deviation (δ_{\min}) and the apex angle (Φ).

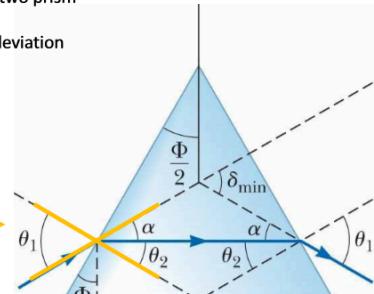
Solution

First, can we observe:

$$\theta_1 = \theta_2 + \alpha$$

$$\theta_2 = \frac{\Phi}{2}$$

$$\alpha = 9\alpha$$





Angle of Refraction for Glass

Example 34.5

Although we do not prove it here, the minimum angle of deviation δ_{\min} for a prism occurs when the angle of incidence θ_1 is such that the refracted ray inside the prism makes the same angle with the normal to the two prism faces as shown in the figure.

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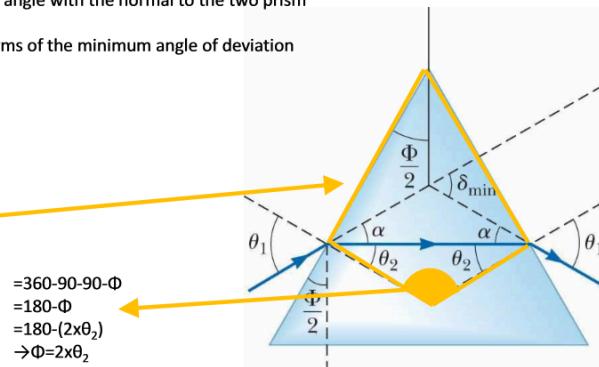
Solution

First, can we observe:

$$\theta_1 = \theta_2 + \alpha$$

$$\theta_2 = \Phi/2$$

$$\delta_{\min} = 2\alpha$$



Angle of Refraction for Glass

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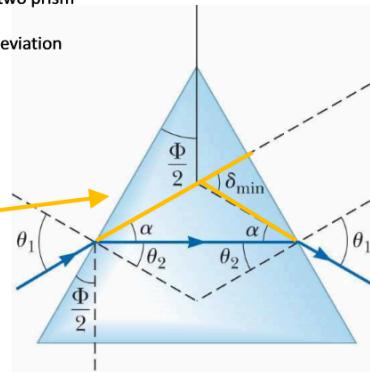
Solution

First, can we observe:

$$\theta_1 = \theta_2 + \alpha$$

$$\theta_2 = \Phi/2$$

$$\delta_{\min} = 2\alpha$$



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018. 47

Angle of Refraction for Glass

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Obtain an expression for the index of refraction of the prism material in terms of the minimum angle of deviation (δ_{\min}) and the apex angle (Φ).

Solution

First, can we observe:

$$\theta_1 = \theta_2 + \alpha$$

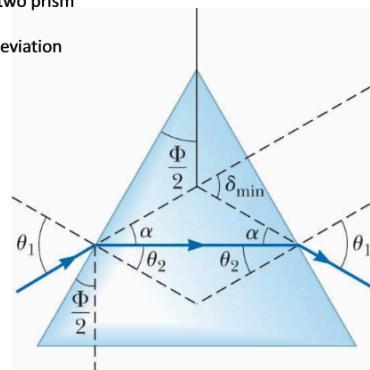
$$\theta_1 = \frac{\Phi}{2} + \frac{\delta_{\min}}{2} = \frac{\Phi + \delta_{\min}}{2}$$

$$\theta_2 = \Phi/2$$

$$(1.00) \sin \theta_1 = n \sin \theta_2 \rightarrow n = \frac{\sin \theta_1}{\sin \theta_2}$$

$$\delta_{\min} = 2\alpha$$

$$n = \frac{\sin \left(\frac{\Phi + \delta_{\min}}{2} \right)}{\sin (\Phi/2)}$$



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018. 48

Nature of Light and Ray Optics (Ch. 34)

The Nature of Light
The Ray Approximation in Ray Optics
Analysis Model: Wave Under Reflection
Analysis Model: Wave Under Refraction
→ Huygen's Principle [Optional – Reading from Textbook]
Dispersion
Total Internal Reflection

Nature of Light and Ray Optics (Ch. 34)

Huygen's Principle [Optional – Reading from text book]

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Nature of Light and Ray Optics (Ch. 34)

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Nature of Light and Ray Optics (Ch. 34)

Dispersion

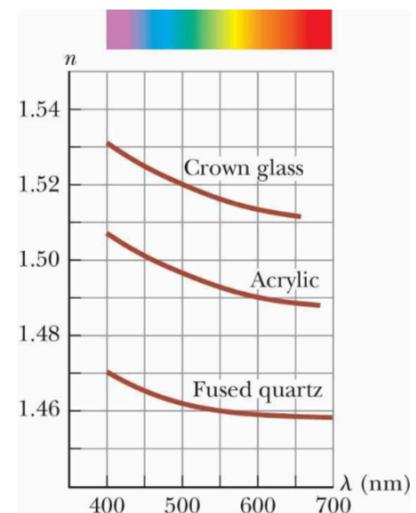
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Dispersion

- **Dispersion:** For a given material, index of refraction varies with wavelength of light passing through the material (figure):
 - n is a function of wavelength →
 - Snell's law of refraction indicates that light of different wavelengths refracts at different angles
- Figure: shows that index of refraction generally decreases with increasing wavelength
- Example:
 - Violet light refracts more than red light does when passing into a material



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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Dispersion

- Figure: a beam of **white light** (combination of all visible wavelengths) is incident onto a prism from the left
- Angle of deviation depends on the index of refraction →
 - Angle depends on the wavelength
- Rays that emerge spread out in series of colors (**visible**

The colors in the refracted beam are separated because dispersion in the prism causes different wavelengths of light to be refracted through different angles.

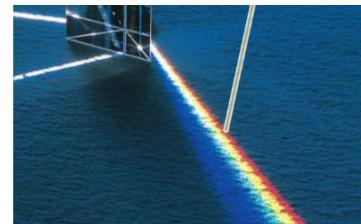


spectrum)

- In order of decreasing wavelength: red, orange, yellow, green, blue, and violet

• Newton showed:

- Each color has a particular angle of deviation
- Colors can be recombined to form original white light



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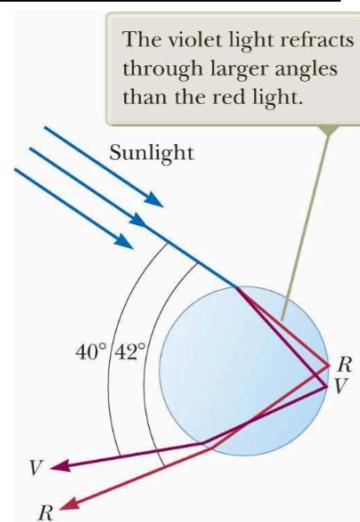
Source: Serway, Raymond A., and John W. Jewett. Physics for scientists and engineers. 10th Edition. Cengage learning, 2018.

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Dispersion

Rainbows

- **Rainbow:** dispersion of light into spectrum
 - Often seen by an observer positioned between the Sun and a rain shower
- Apply both '*wave under reflection*' and '*wave under refraction*' models
- Rays of sunlight (white light) strike a drop of water in atmosphere (figure)
- Light **refracted** and **reflected** as shown:
 - First refracted at the front surface of the drop
 - Violet light deviating most and red light least.
 - At the back surface of the drop:
 - Light is reflected and returns to front surface
 - Again undergoes refraction as it moves from water into air
- Small angular difference between returning rays: causes us to see a colored bow



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Source: Serway, Raymond A., and John W. Jewett. Physics for scientists and engineers. 10th Edition. Cengage learning, 2018.

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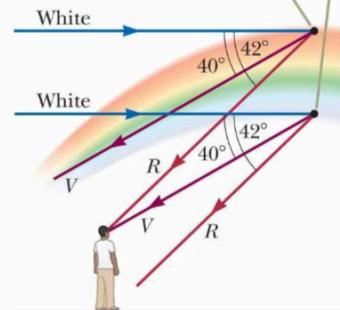
Dispersion

DISPERSION

Rainbows

- Figure: observer viewing a rainbow
- If raindrop high in the sky is being observed:
 - Most intense red light returning from drop reaches the observer →
 - Because it deviated the least
 - Most intense violet light from this drop passes over observer →
 - Because it deviated the most
 - Observer sees red light coming from drop
- Drop lower in sky directs most intense violet light toward observer
 - Appears violet
 - Most intense red light from this drop passes below observer's eye
- Most intense light from other colors of spectrum reaches observer from raindrops lying between these two extreme positions

The highest-intensity light traveling from higher raindrops toward the eyes of the observer is red, whereas the most intense light from lower drops is violet.



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

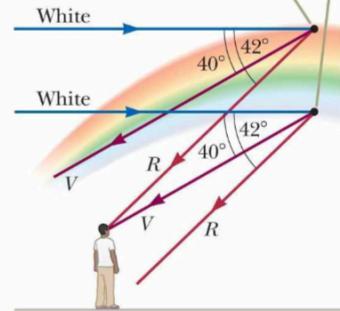
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Dispersion

Rainbows



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018
<https://en.wikipedia.org/wiki/Rainbow>

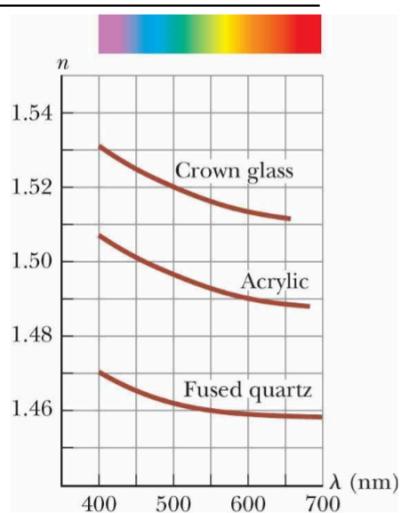
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Quick Quiz

Quick Quiz

In photography, lenses in a camera use refraction to form an image on a light-sensitive surface. Ideally, you want all the colors in the light from the object being photographed to be refracted by the same amount. Of the materials shown in the figure, which would you choose for a single-element camera lens?

- (a) crown glass
- (b) acrylic
- (c) fused quartz
- (d) impossible to determine



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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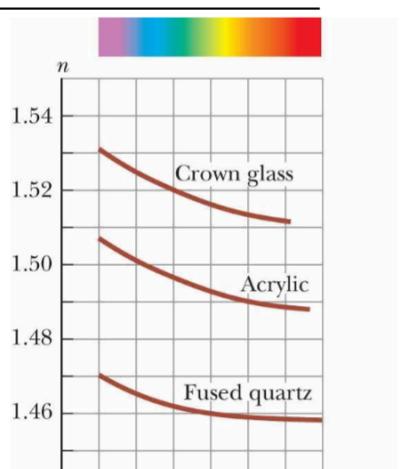
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- (a) crown glass
- (b) acrylic
- (c) fused quartz**
- (d) impossible to determine

An ideal camera lens would have an index of refraction that does not vary with wavelength so that all colors would be bent through the same angle by the lens. Of the three choices, fused quartz has the least variation in n across the visible spectrum. A lens designer can do even better by **stacking** two lenses of different materials together to make an **achromatic double**.





Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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→ Total Internal Reflection

Nature of Light and Ray Optics (Ch. 34)

Total Internal Reflection

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Total Internal Reflection

- **Total internal reflection:** can occur when light travels from a higher index of refraction medium to a lower index of refraction medium

As the angle of incidence θ_1 increases, the angle of refraction θ_2 increases until θ_2 is 90° (ray 4). The dashed line indicates that no energy actually propagates in this direction.

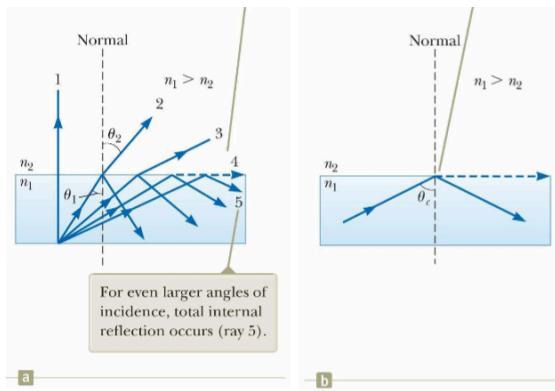
The angle of incidence producing an angle of refraction equal to 90° is the critical angle θ_c . For angles greater than θ_c , all the energy of the incident light is reflected.

- Figure (a): Labels 1 to 5 indicate various possible directions of ray consistent with wave under refraction model.

- As θ_1 increases $\rightarrow \theta_2$ becomes larger
- Refracted ray bends away from normal so much that it approaches direction parallel to interface

- At the particular angle of incidence θ_c (**critical angle**):

- Refracted light ray reaches this condition that it is parallel to the boundary $\rightarrow \theta_2 = 90^\circ$ (ray 4 figure (a), and figure (b))



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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Total Internal Reflection

- For angles of incidence $> \theta_c$:

- Rays cannot escape from the material and will be entirely reflected at boundary (ray 5 figure (a))

- Use Snell's law of refraction to find the **critical angle**

- When $\theta_1 = \theta_c$, $\theta_2 = 90^\circ$:

$$\sin \theta_c = \frac{n_2}{n_1}$$

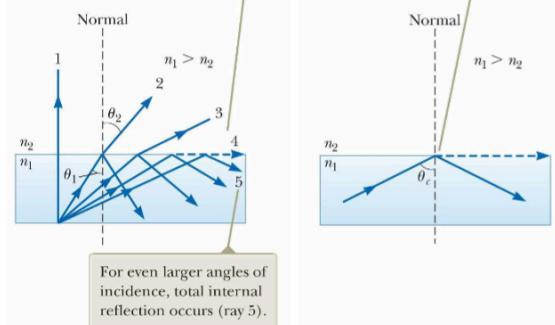
(for $n_1 > n_2$)

- Total internal reflection **occurs only when** light travels from a higher index of refraction medium to a lower index of refraction medium

- If $n_1 < n_2 \rightarrow$ equation gives $\sin \theta_c > 1$
 - impossible situation!

As the angle of incidence θ_1 increases, the angle of refraction θ_2 increases until $\theta_2 = 90^\circ$ (ray 4). The dashed line indicates that no energy actually propagates in this direction.

The angle of incidence producing an angle of refraction equal to 90° is the critical angle θ_c . For angles greater than θ_c , all the energy of the incident light is reflected.



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Total Internal Reflection

Diamonds

- Critical angle for a diamond in air = 24° ($n: \sim 2.4$)
 - Any ray inside the diamond that approaches surface at angle $> 24^\circ$ completely is reflected back into the crystal
 - This property, combined with proper faceting, causes diamonds to sparkle
- Angles of the facets cut so that light is “caught” inside the crystal through multiple internal reflections
 - Multiple reflections give light long path through medium
 - Substantial dispersion of colors occurs
- By the time light exits through the top surface of the crystal:
 - Rays associated with different colors widely separated from one another



Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.
<https://commons.wikimedia.org/wiki/File:6ABrillanten.jpg>
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Total Internal Reflection

Cubic Zirconia

- Cubic zirconia: high index of refraction ($n: \sim 2.2$)
 - Can be made to sparkle like diamond.
- If a suspect jewel is immersed in corn syrup →
 - Difference in n for cubic zirconia and that for corn syrup ($n: \sim 1.5$) is small.
 - Critical angle is great.
 - More rays escape sooner →
 - Sparkle completely disappears
- Real diamond does not lose all its sparkle when placed in corn syrup



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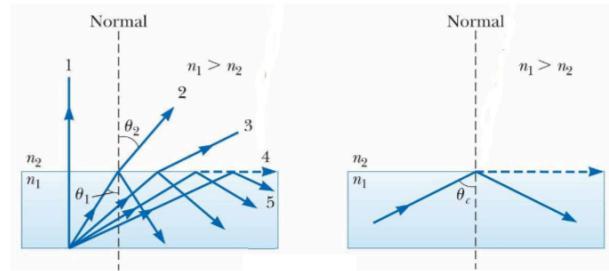
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Angle of Refraction for Glass

Example 34.6

Find the critical angle for an air–water boundary. (Assume the index of refraction of water is 1.33.)



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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018.

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Angle of Refraction for Glass

Example 34.6

Find the critical angle for an air–water boundary. (Assume the index of refraction of water is 1.33.)

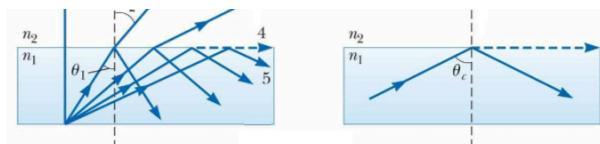
Solution

$$\sin \theta_c = \frac{n_2}{n_1} = \frac{1.00}{1.33} = 0.752$$



$$n_1 = 1.33$$

$$\theta_c = 48.8^\circ$$



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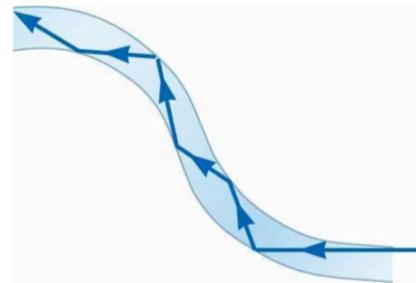
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Source: Serway, Raymond A., and John W. Jewett. *Physics for scientists and engineers*. 10th Edition. Cengage learning, 2018. 64

Total Internal Reflection

Optical Fibers

- A great application example of total internal reflection
- Use of glass or transparent plastic rods to “pipe” light from one place to another
- Figure: light is confined to travel within the rod (even around curves)
 - Result of successive total internal reflections
- Light pipe: flexible with thin fibers rather than thick rods
 - Flexible light pipe: **optical fiber**
- Part of the 2009 Nobel Prize in Physics was awarded to **Charles K. Kao** for his discovery of how to transmit light signals over long distances through thin glass fibers
 - Discovery led to the development of sizable industry known as **fiber optics**



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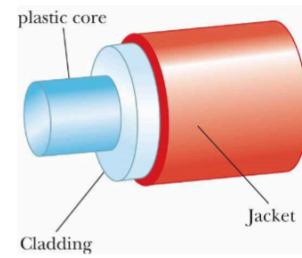
Total Internal Reflection

Optical Fibers

Glass or

Optical Fibers

- Figure: cutaway view of an optical fiber
- An optical fiber consists of a transparent core surrounded by a **cladding** (material that has lower index of refraction than the core)
 - Combination may be surrounded by plastic **jacket** to prevent mechanical damage
- Because index of refraction of the cladding < that of the core →
 - Light traveling in the core experiences total internal reflection if it arrives at interface between core and cladding at angle of incidence $> \theta_c$
 - Light “**bounces**” along the core of an optical fiber
- Optical fiber cables replacing copper wiring and coaxial cables for telecommunications →
 - Fibers can carry much greater volume of telephone calls or other forms of communication than electrical wires can



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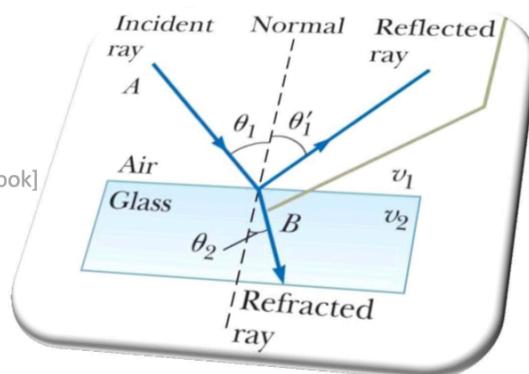
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Summary of Week 12, Class 10

- Reminder of the previous week
- Nature of Light and Ray Optics (Ch. 34)
 - The Nature of Light
 - The Ray Approximation in Ray Optics
 - Analysis Model: Wave Under Reflection
 - Analysis Model: Wave Under Refraction
 - Huygen’s Principle [Optional – Reading from Textbook]
 - Dispersion
 - Total Internal Reflection
- Examples
- Next week’s topic



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Reading / Preparation for Next Week

Topics for next week:

- Image Formation (Ch. 35)