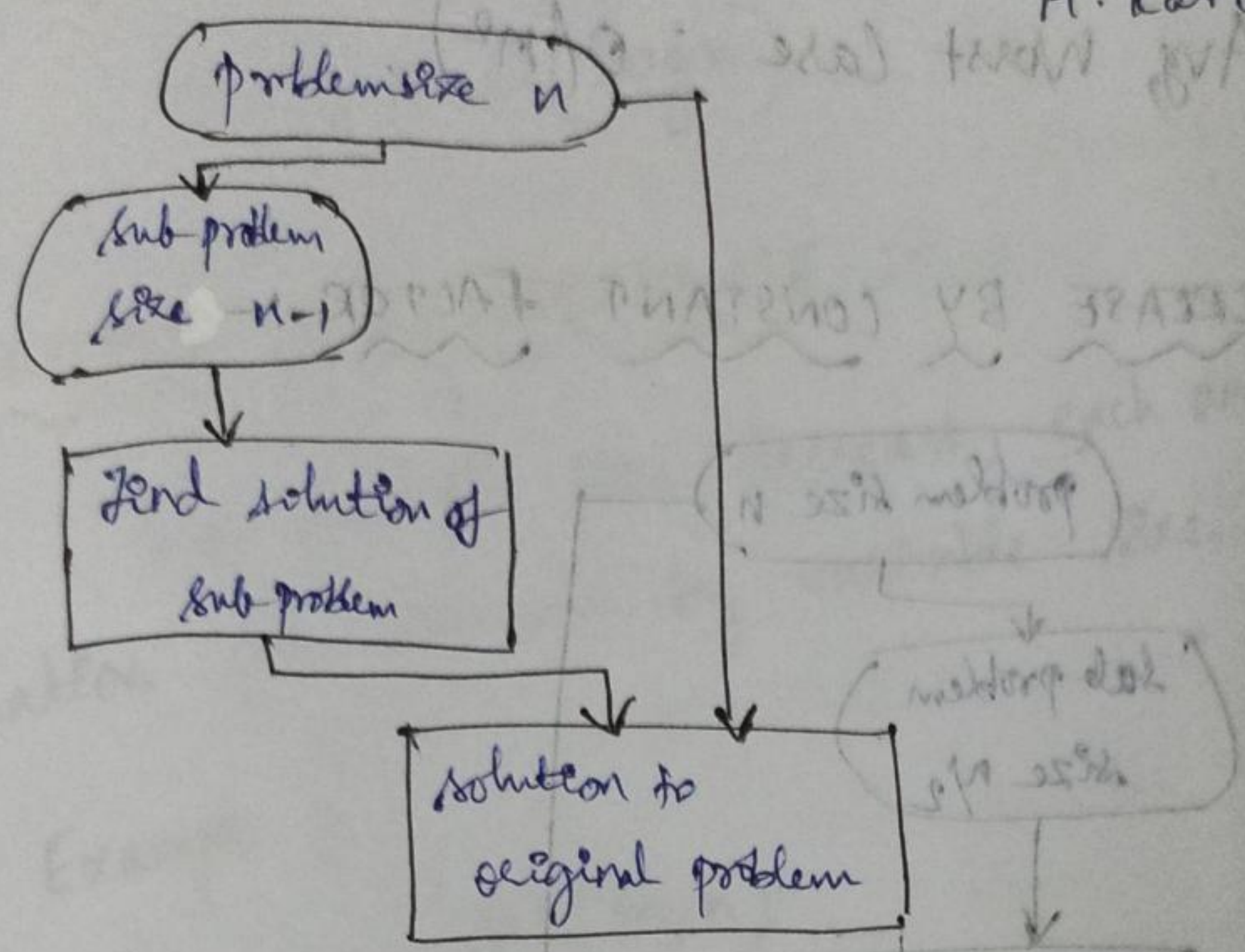


DECREASE BY CONSTANT :- 16 CSR 89
M. Karthik



Example :- Insertion sort :-

Alg Insertionsort ($A[0, \dots, n-1]$)

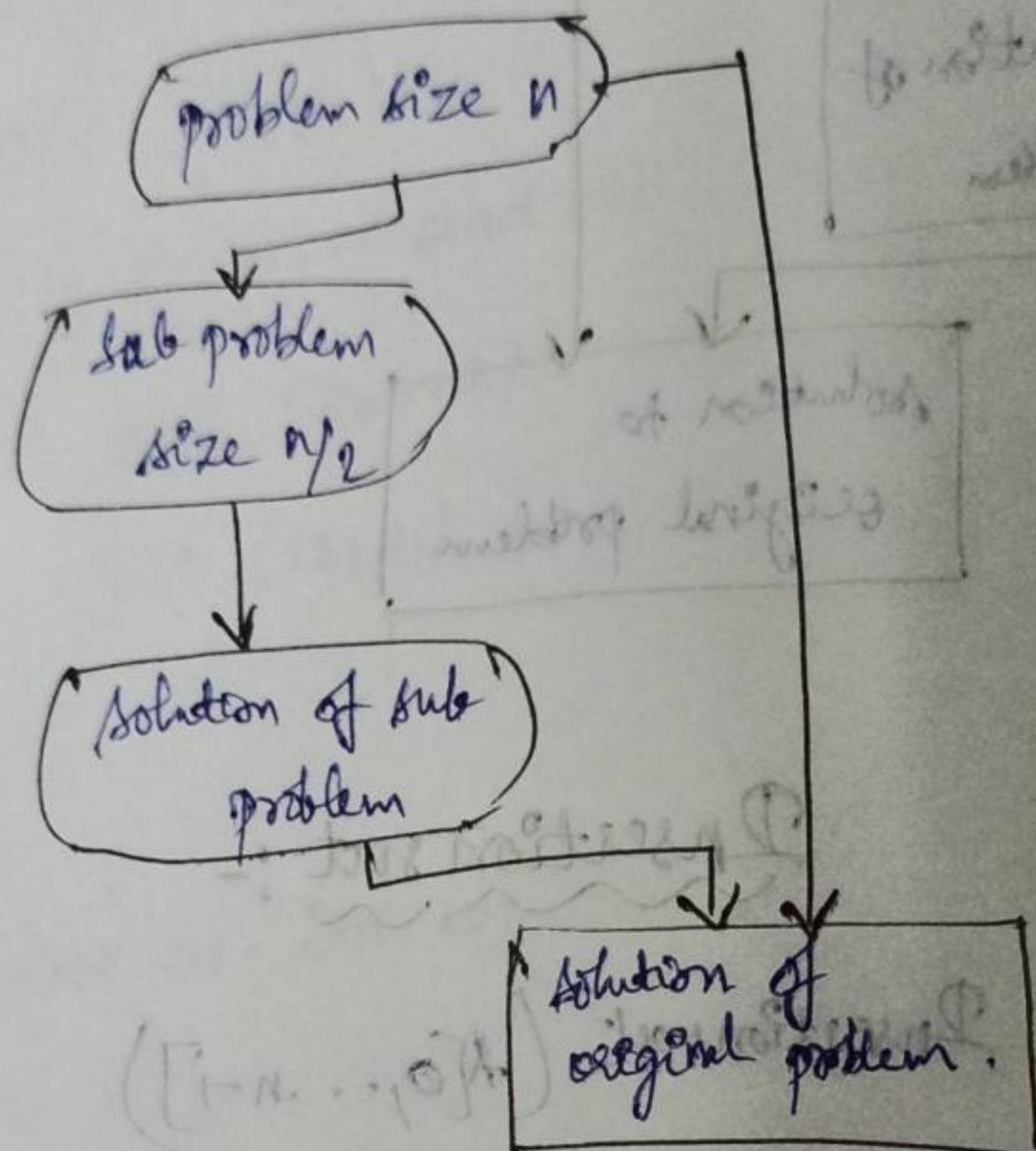
```

{
  for i = 1 to n-1
  {
     $V = A[i]$ ;  $j = i - 1$ ;
    while ( $j \geq 0$  and  $A[j] > V$ )
    {
       $A[j+1] = A[j]$ 
       $j = j - 1$ 
    }
     $A[j+1] = V$ 
  }
}
  
```

$$T(n) = \sum_{i=1}^{n-1} \left[\sum_{j=0}^{i-1} 1 \right] = \sum_{i=1}^{n-1} i = \frac{n(n-1)}{2} \Rightarrow O(n^2)$$

Best case : $O(n)$
Avg, Worst case : $O(n^2)$

DECREASE BY CONSTANT FACTOR :-



Example :-

Binary Search :-

Alg binsearch ($A[0, \dots, n-1], \text{key}$)

{

$l = 0$

$r = n - 1$

 while ($l \leq r$)

 {

$m = \frac{l+r}{2}$

 if ($A[m] == \text{key}$)

 return m

 else if $\text{key} < A[m]$

$r = m - 1$

 else

$l = m + 1$

 } return -1

Execution Time :-

$$T(n) \in O(\log n).$$

VARIABLE SIZE DECREASE :-

In variable size decrease, each and every iteration is decrease by variable size.

Example :

$\text{gcd}(m, n)$

$\text{gcd}(m, n)$

$\{ \text{if } (n == 0)$

$\text{return } m;$

else

$\{$

$t = m \% n;$

$\text{gcd}(n, t);$

$\}$

$\}$

$\text{gcd}(60, 24) = \text{gcd}(24, 12) = \text{gcd}(12, 0)$

TRANSFORM AND CONQUER :-

convert the problem into another type and solve

Example :-

Heap sort

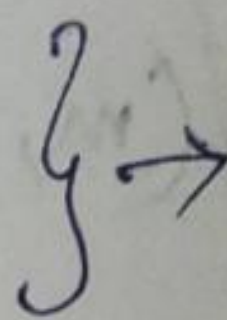
Types :-

* Instance Simplification.

- uniqueness

- mode

- binary search



These are all application of pre solving.

* representation change.

Ex: heap sort

* problem reduction.

mode :-

Repeated no's more times called as mode.

Algorithm :-

Alg-mode (A[...])

⌊

count = 0; Num = A[0]; count1 = 1;

for (i = 0 to n-1)

⌊

if (A[i] == A[i+1])

count1 ++;

else if (count1 > count)

⌊

count = count1;

Num = A[i];

count1 = 1; } else count1 = 1;

}
display(count, Num);
}

Example :-

Uniqueness :-

Alg unique ($A[0, \dots, n-1]$)

{

for $i = 0$ to $n-2$

{

if ($A[i] = A[i+1]$)

return false

}

return true

}

Kaur