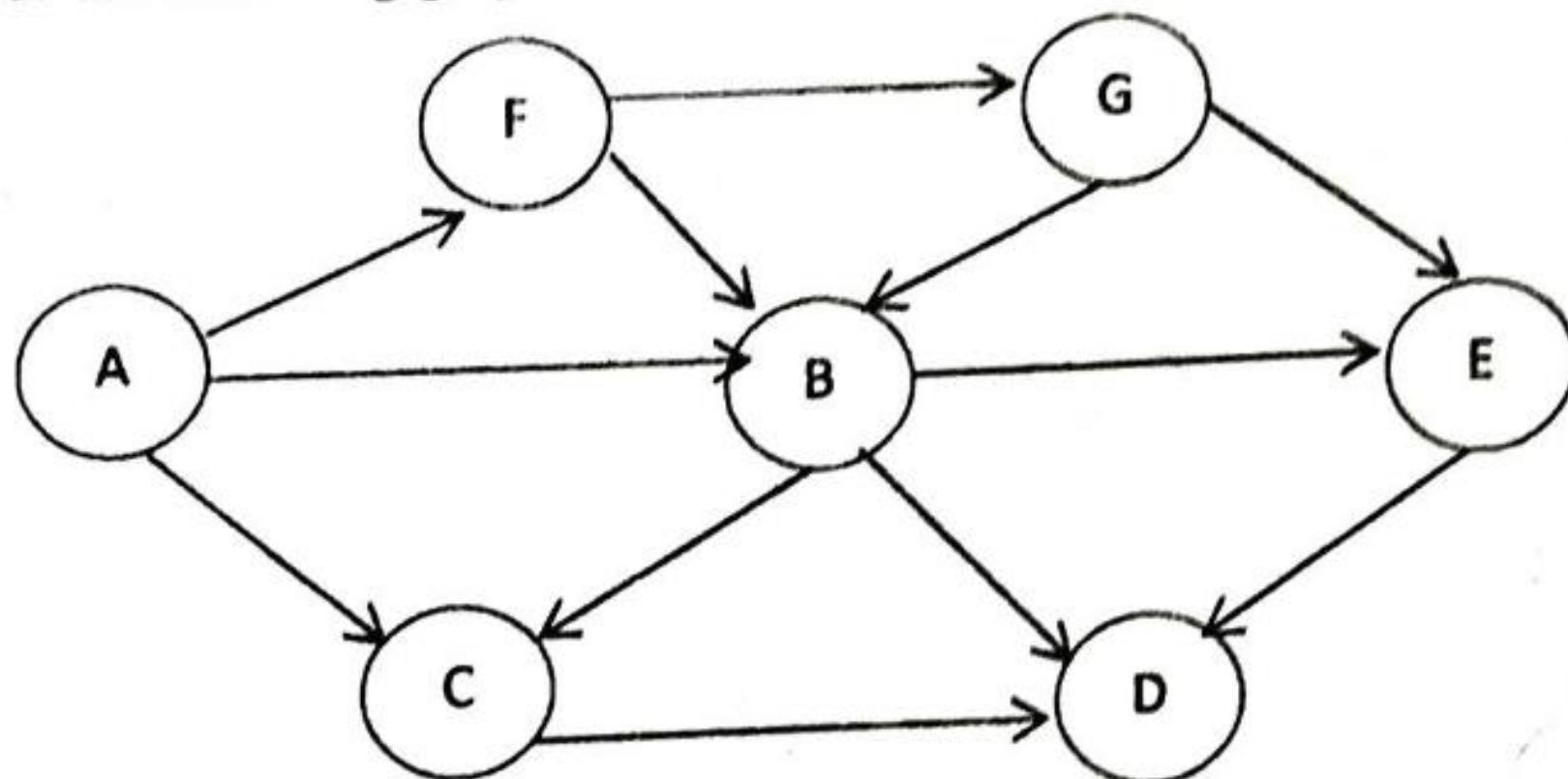


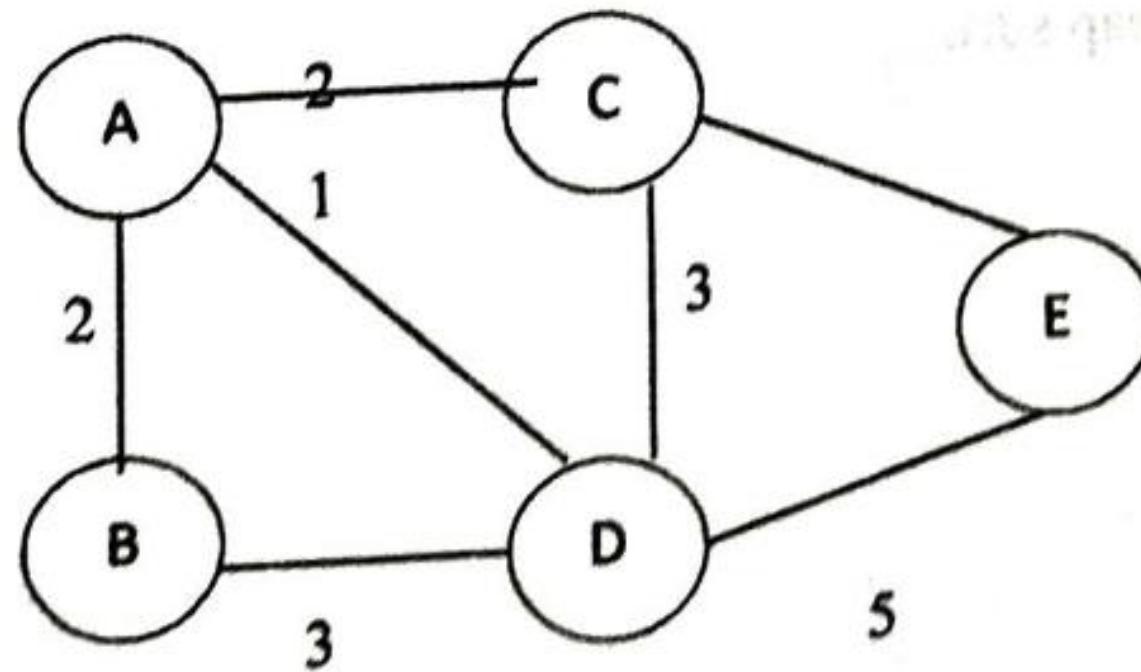
Programme : B.E	Date : 03.11.2016
Branch : CSE	Time : 2.30 pm to 4.00 pm
Semester : III	Duration : 1 1/2 Hours
Course Code : 14CST31	Max. Marks : 50
Course Name : Data Structure	

PART - A (10 X 2 = 20 Marks)
ANSWER ALL THE QUESTIONS

1. List the two properties of heap.
2. Mention any two collision resolution strategies in hashing.
3. Define graph.
4. For the following graph, draw the adjacency list representation



5. What is DAG?
6. Define articulation point.
7. Write the routine to perform DFS.
8. Find the MST for the following graph using kruskal's algorithm. Consider A as source.

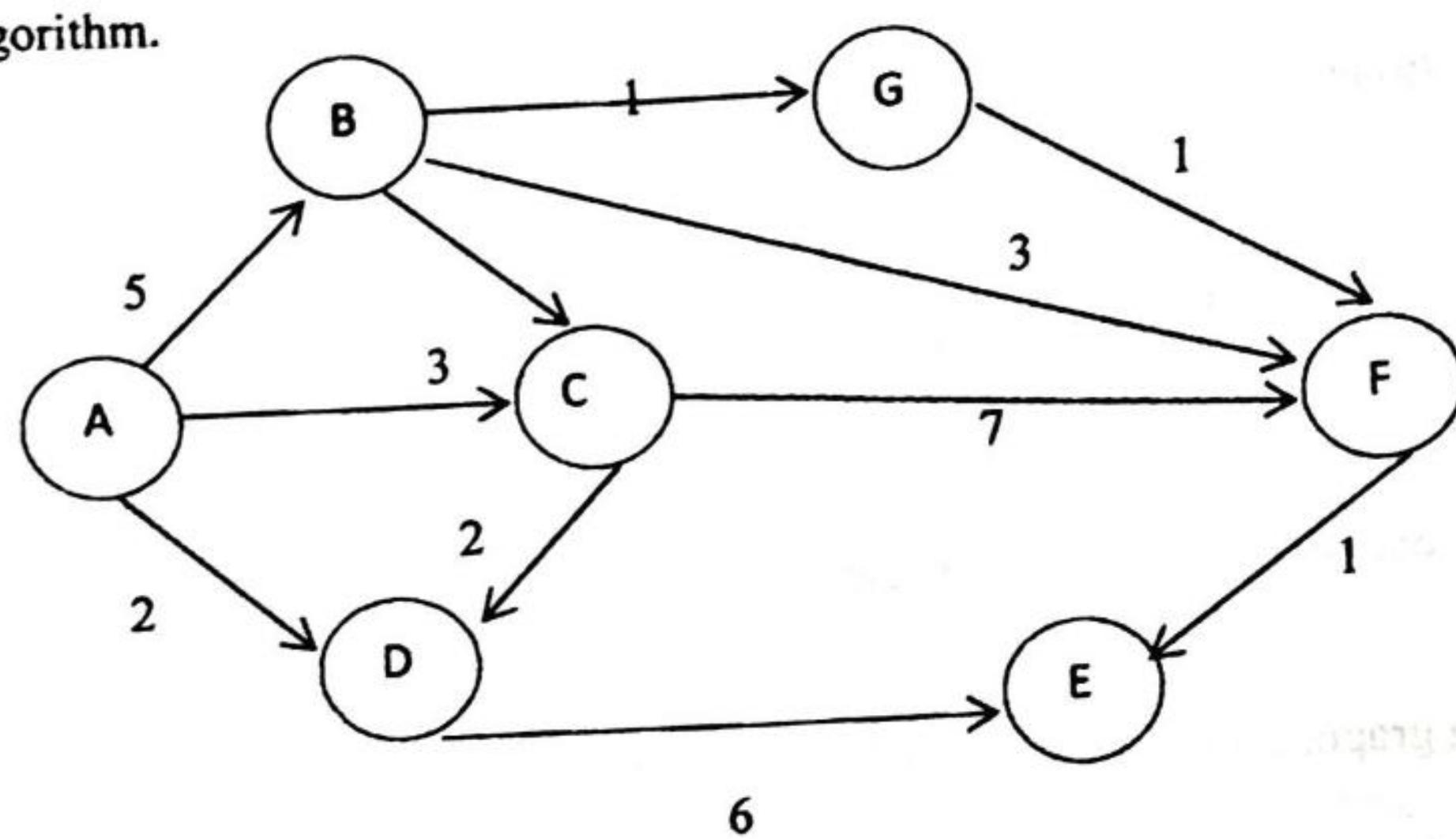


9. How will you sort the vertices in topological sorting?
10. List any four real time applications of graph.

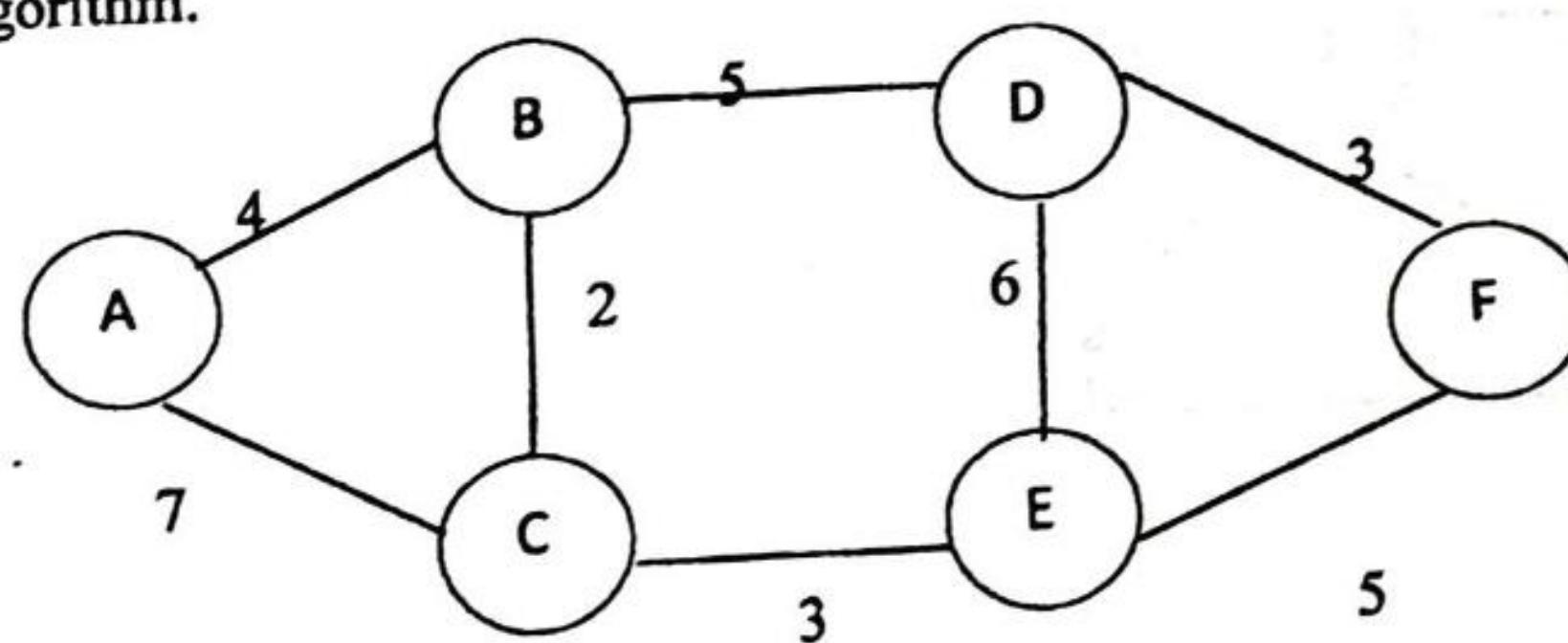
PART - B (3 X 10 = 30 Marks)
ANSWER ANY THREE QUESTIONS

11. Show the result of inserting 10,12,1,14,6,5,8,15,3,9,7 into an initially empty binary heap. (10)

12. Trace the shortest path from the vertex A to all other vertices using Dijkstra's algorithm. (10)



13. Construct a minimum spanning tree for the following graph using prime's algorithm. (10)



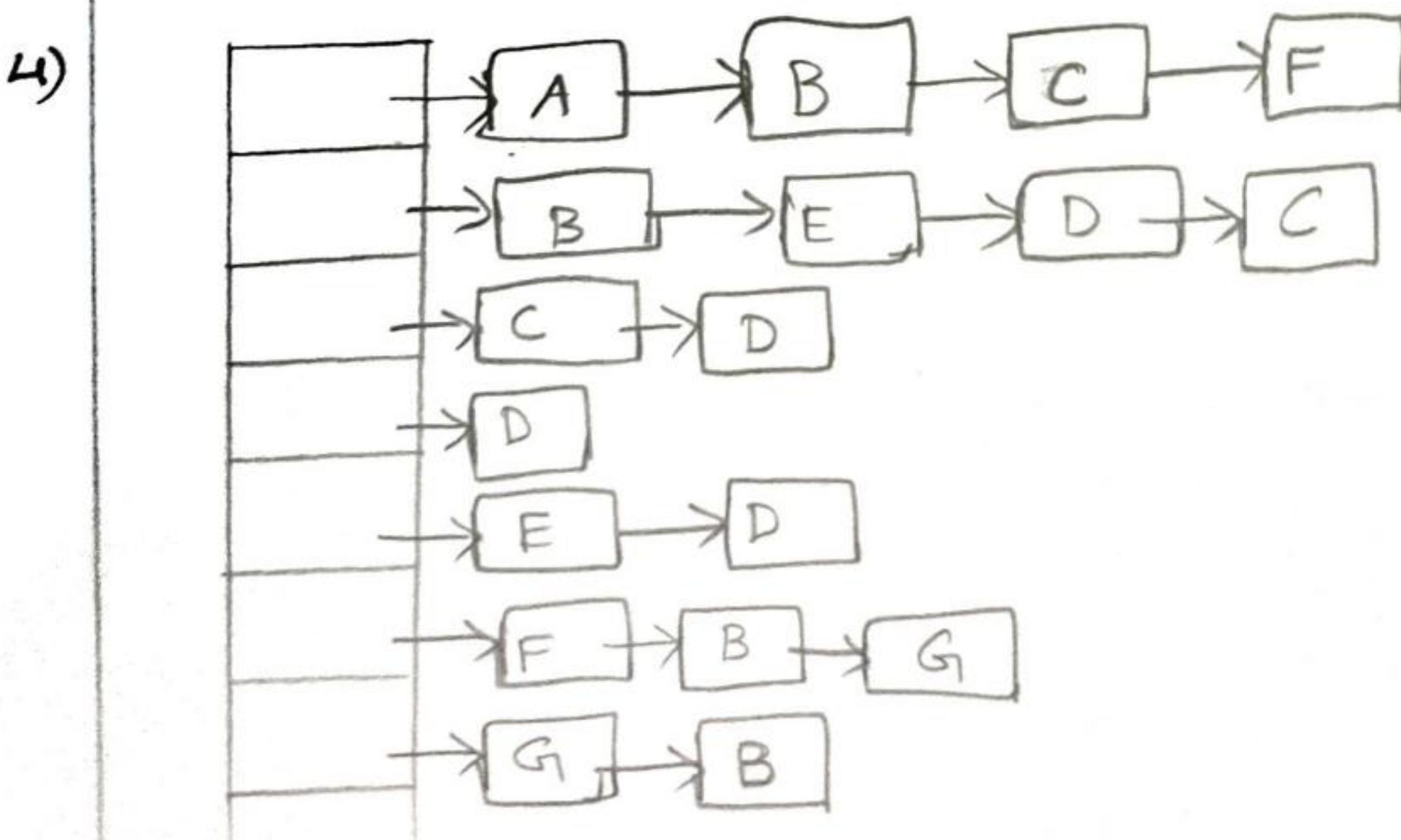
14. i) Given the input {4371, 1323, 6173, 4199, 4344, 9679} and a hash function $h(x) = x \bmod 10$. Show the result of applying separate chaining hash table. (5)
ii) Write the pseudo code to perform heap sort.

Ans. 15CS253 D

Module Test - 3 - Scheme

PART A

- 1) Properties of Heap
 - 1) Structural Property
 - 2) Heap Order Property
- 2) Collision resolution strategies
 - 1) Separate Chaining
 - 2) Open Addressing
 - 1) Linear Probing
 - 2) Quadratic Probing
 - 3) Double hashing
- 3) Graph - Data Structure
Collection of vertices v and edges e
- 5) DAG
 - 1) Directed Acyclic Graph
 - 2) NO cycle (or) loop



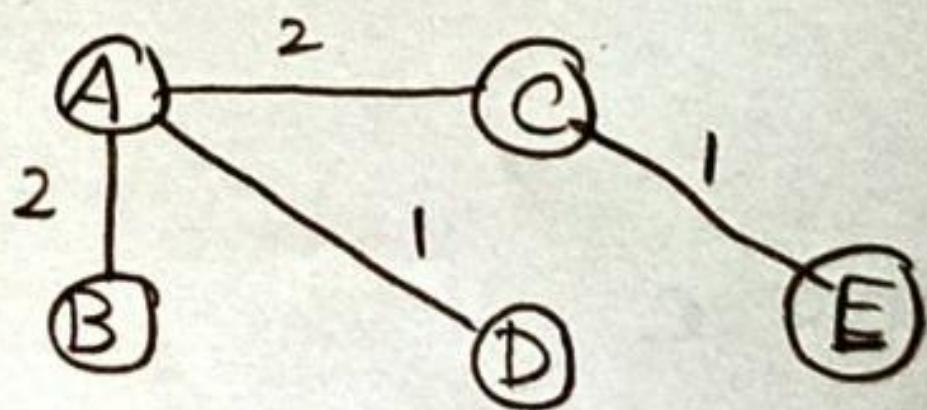
6) Articulation Point

- 1) Graph is bi-connected
- 2) Removal of vertex, disconnects the graph

7) DFS

```
dfs(1);  
void dfs (int v, int a[10][10], int visited [10], int  
{  
    visited [v] = 1;  
    for (i=1; i<=n; i++)  
        for (j=1; j<=n; j++)  
            if (cost [i][j] << !visited [i])  
                printf ("%d → %d ← %d", v, i);  
    dfs (i);  
}
```

8)



Minimum cost = 6

9)

- 1) Indegree
- 2) Outdegree

10)

- 1) Airport system
- 2) Wiring connection in home
- 3) Course pre requisite
- 4) Roads & Railways

Part B

O

(10)

(10)
12

(10)
12
1

Heap order
→

1
12
10

1
12
10
14

1
12
10
14
6

Heap order
→

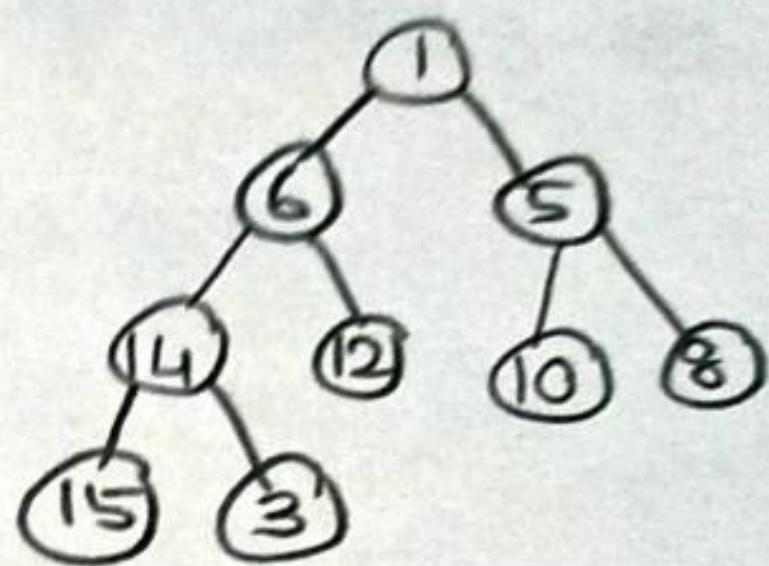
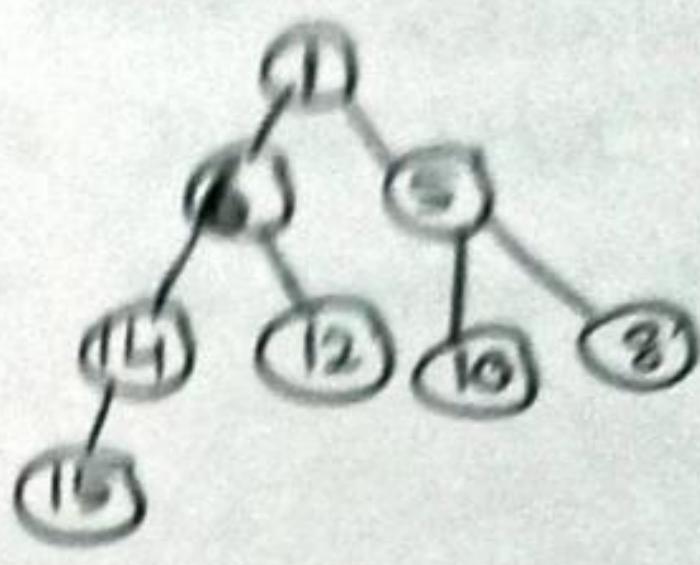
1
6
10
14
12

1
6
13
14
12
5

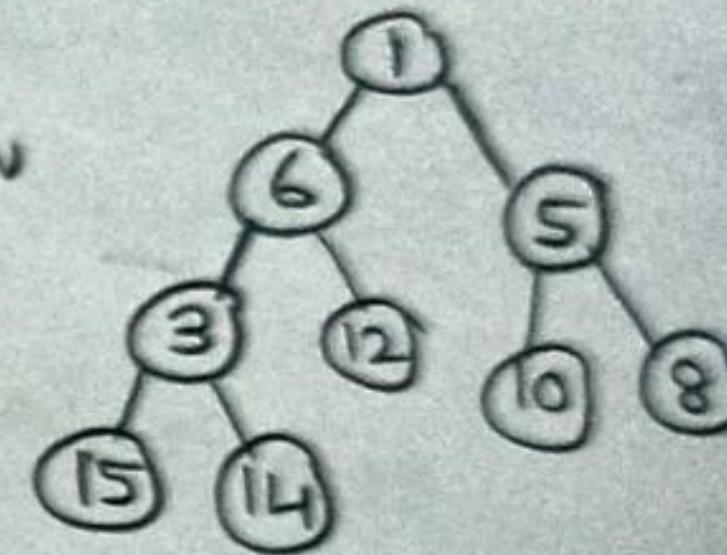
→

1
6
5
14
12
10

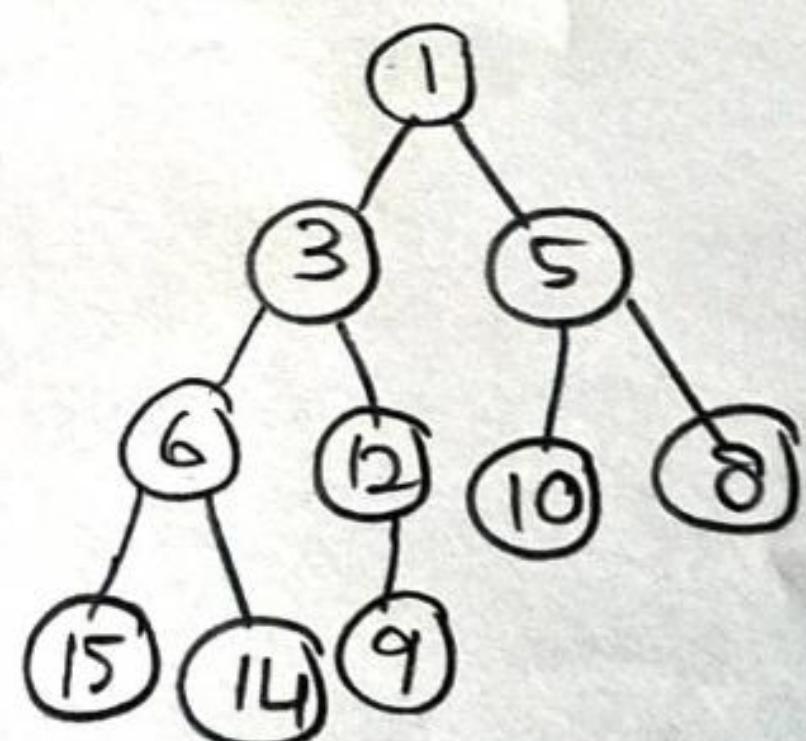
1
6
5
14
12
10
8



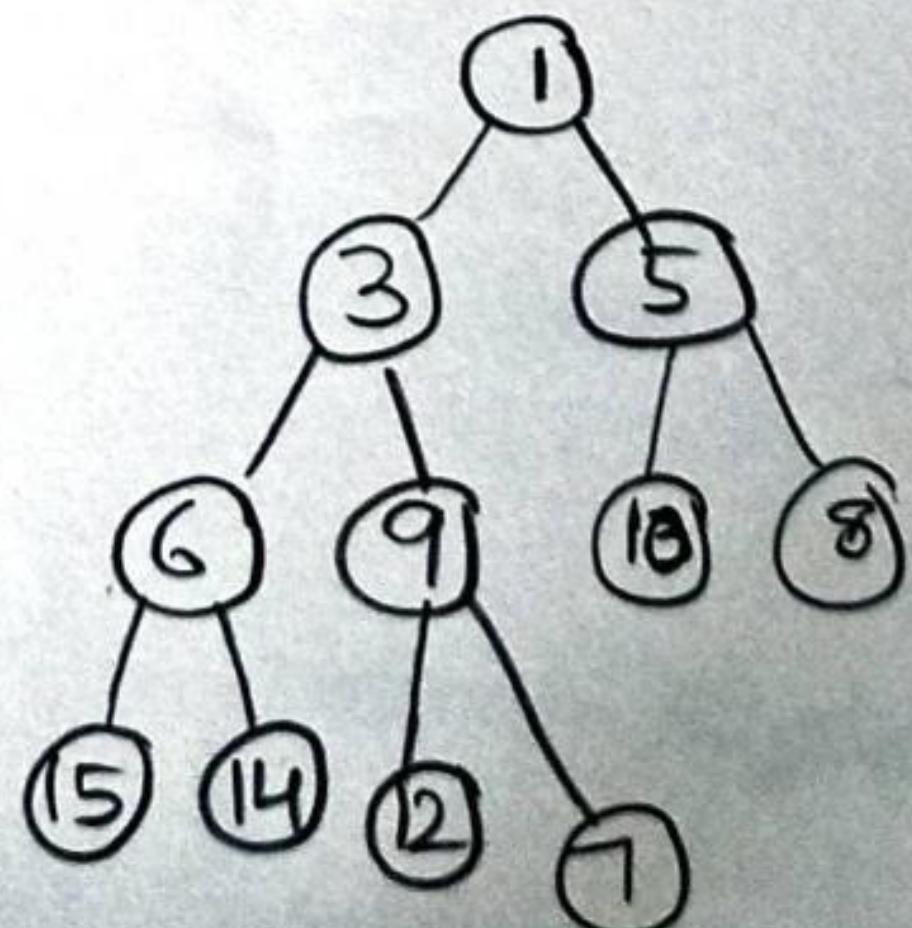
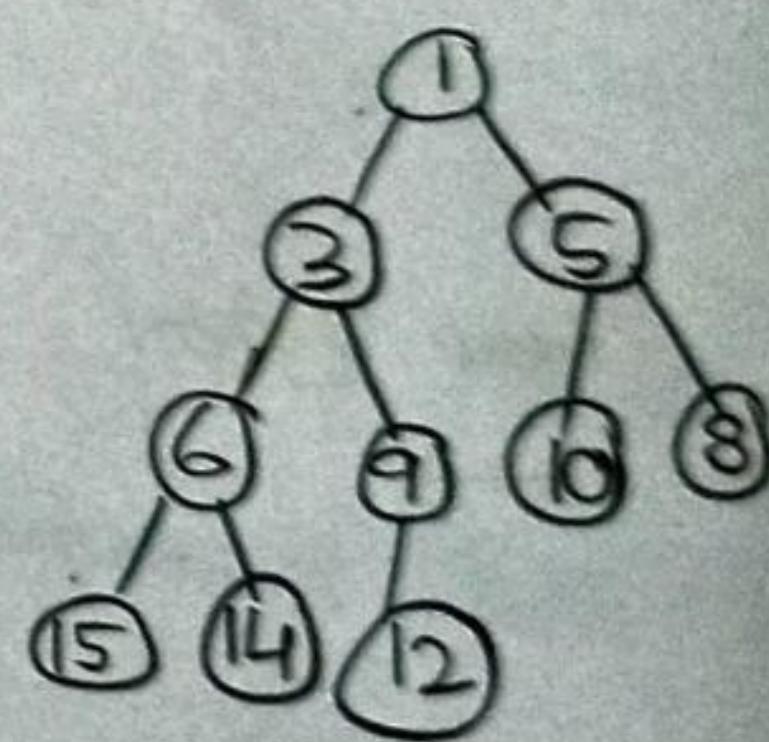
Heap order



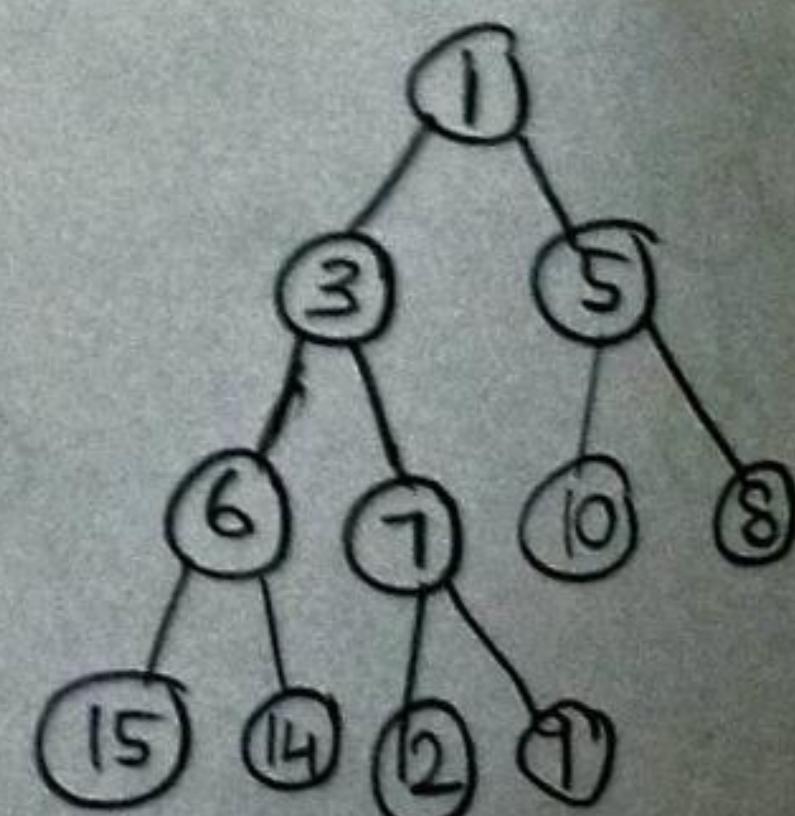
Heap order



Heap
order



Heap
order



Initial

V	K	d_V	P_V
A	0	0	0
B	0	∞	0
C	0	∞	0
D	0	∞	0
E	0	∞	0
F	0	∞	0
G ₁	0	∞	0

C

V	K	d_V	P_V
A	1	0	0
B	0	5	A
C	1	3	A
D	1	2	A
E	0	8	D
F	0	10	C
G ₁	0	2	0

A

V	K	d_V	P_V
A	1	0	0
B	0	5	A
C	0	3	A
D	0	2	A
E	0	∞	0
F	0	∞	0
G ₁	0	∞	0

B

V	K	d_V	P_V
A	1	0	0
B	1	5	A
C	1	3	A
D	1	2	A
E	0	8	D
F	0	8	B
G ₁	0	6	B

D

V	K	d_V	P_V
A	1	0	0
B	0	5	A
C	0	3	A
D	1	2	A
E	0	8	D
F	0	∞	0
G ₁	0	∞	0

G₁

V	K	d_V	P_V
A	1	0	0
B	1	5	A
C	1	3	A
D	1	2	A
E	0	8	D
F	0	7	G ₁
G ₁	1	6	B

F	K	d_v	P_v
V	I	0	O
A	I	5	A
B	I	3	A
C	I	2	A
D	O	8	D
E	I	7	G ₁
F	I	6	B

E

V	K	d_v	P_v
A	I	0	O
B	I	5	A
C	I	3	A
D	I	2	A
E	I	8	D
F	I	7	G ₁
G	I	6	B

$A \rightarrow B$, Cost = 5

$A \rightarrow C$, Cost = 3

$A \rightarrow D$, Cost = 2

$A \rightarrow E$, Cost = 8

$A \rightarrow F$, Cost = 7

$A \rightarrow G_1$, Cost = 6

Initial

V	K	d _v	P _v
A	0	0	0
B	0	∞	0
C	0	∞	0
D	0	∞	0
E	0	∞	0
F	0	∞	0

C	V	K	d _v	P _v
A	1	0	0	0
B	1	4	A	
C	1	2	B	
D	0	5	B	
E	0	3	C	
F	0	∞	0	

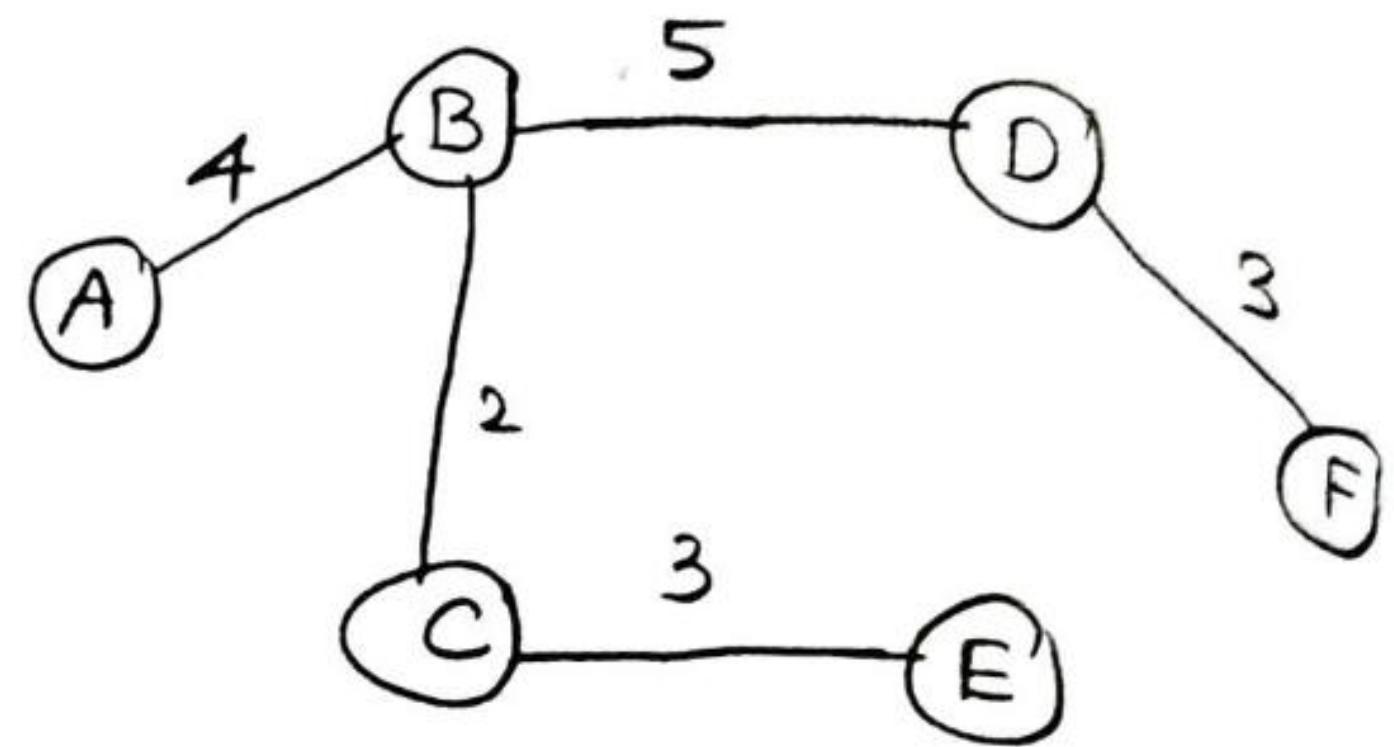
A	V	K	d _v	P _v
A	1	0	0	0
B	0	4	A	
C	0	7	A	
D	0	∞	0	
E	0	∞	0	
F	0	∞	0	

E	V	K	d _v	P _v
A	1	0	0	0
B	1	4	A	
C	1	2	B	
D	0	5	B	
E	1	3	C	
F	0	5	E	

B	V	K	d _v	P _v
A	1	0	0	0
B	1	4	A	
C	0	2	B	
D	0	5	B	
E	0	∞	0	
F	0	∞	0	

D	V	K	d _v	P _v
A	1	0	0	0
B	1	4	A	
C	1	2	B	
D	1	5	B	
E	1	3	C	
F	0	3	D	

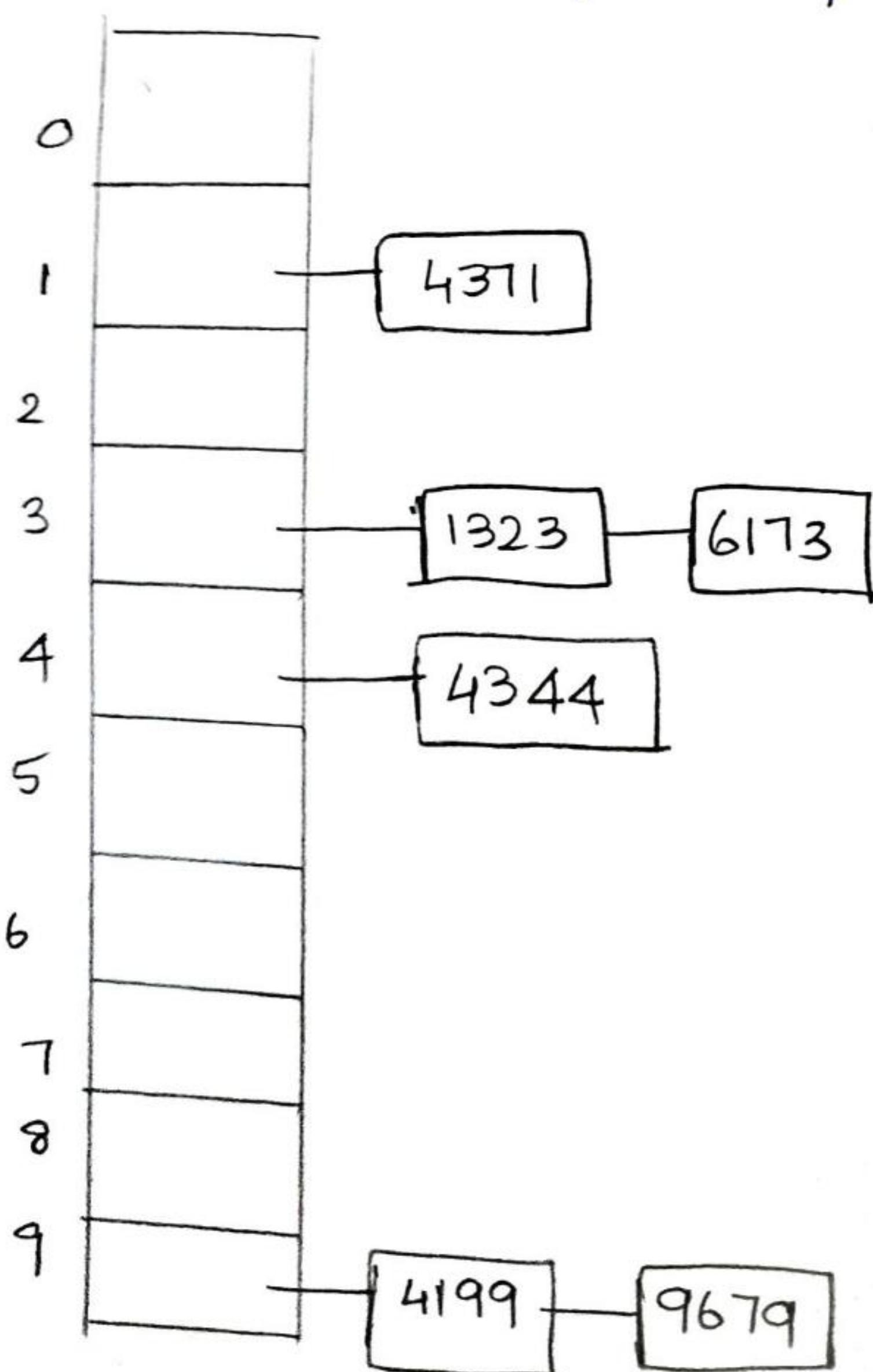
	v	κ	d_v	P_v
A	1	1	0	0
B	1	1	4	A
C	1	1	2	B
D	1	1	5	B
E	1	1	3	C
F	1	1	3	D



$$\text{Total Cost} = 4 + 2 + 5 + 3 + 3 = 17$$

4) i)

4371, 1323, 6173, 4199, 4344, 9679



$$4371 \div 10 = 1$$

$$6173 \div 10 = 3$$

$$1323 \div 10 = 3$$

$$4344 \div 10 = 4$$

$$4199 \div 10 = 9$$

$$9679 \div 10 = 9$$

```

#define leftchild(i) (2*i);

void heapsort (int A[], int N) {
    for (i=N/2; i>=0; i--)
        percdown (A,i,N);
    for (i=N; i>1; i++)
    {
        swap (&A[1], &A[i]);
        percdown (A,1,i);
    }
}

void percdown (int A[], int i, int N)
{
    int child, temp;
    for (temp = A[i]; leftchild(i) < N; i=child)
    {
        child = 2*i;
        if (child != N-1 && A[child+1] > A[child])
            child++;
        if (temp < A[child])
            A[i] = A[child];
        else
            break;
    }
    A[i] = temp;
}

```



ESTD 1984

SA	03/11/16
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Name and Signature of Hall Supdt. with Date

KONGU ENGINEERING COLLEGE

PERUNDURAI, ERODE - 638 052.

(Autonomous)



Name of the Student	SABARI GOVINDARAJAN.B	Register No.	1 5 C S R 1 7 4
Programme	BE	Branch & Semester	CSE & III
Course Code and Name	14CST31 Data Structures	Date	03.11.2016
		No. of Pages Used	12

Marks to be filled in by the Examiner

PART - A		PART - B		Grand Total Max. Marks : 50
Question No.	Max Marks : 2	Question No.	Max Marks : 10	
1	2	11	i) 10 Crore	
2	2	11	ii)	
3	2	12	i) 10	
4	2	12	ii)	
5	2	13	i) 10	
6	2	13	ii)	
7	2	14	i) —	
8	2	14	ii) —	
9	1			
10	2			
TOTAL	19	TOTAL	30	
Total Marks in words : FOUR NINE				

INSTRUCTION TO THE CANDIDATE

- Check the Question Paper, Programme, Course Code, Branch Name etc., before answering the questions.
- Use both sides of the paper for answering questions.
- POSSESSION OF ANY INCRIMINATING MATERIAL AND MALPRACTICE OF ANY NATURE IS PUNISHABLE AS PER RULES.

S.V.KOGILAVANI

Name of the Examiner

8/11/2016

Signature of the Examiner with Date

PART - A

- 1) Properties of Heap
 - structural property - The tree should be complete
 - Heap order property - Root element of the tree should contain the minimum among all the elements of tree.

2) Collision resolution strategies

- 1) Separate Chaining
- 2) Open Addressing
 - 1) Linear Probing
 - 2) Quadratic Probing
 - 3) Double hashing

3) Graph

A Graph is a set of vertices $v \in V$, and edges $e \in E$. It is a data structure which find many application in real life scenarios such as airport systems.

5) DAG

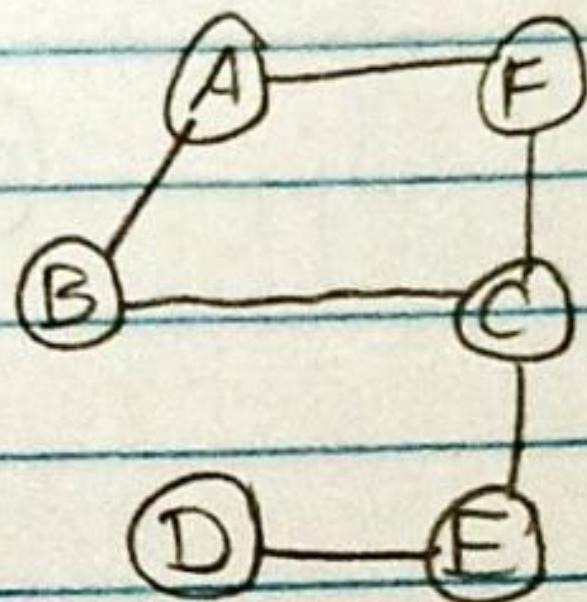
DAG - Directed Acyclic Graph

An acyclic graph is a graph in which the graph does not contain any loop, i.e. the starting ending vertices should be different. If this property is possessed by a directed graph then it is said to be Directed Acyclic graph.

6) Articulation Point

Articulation point in a graph refers to a vertex on whose removal, the rest of graph gets disconnected.

Eg:



Here E is the articulation point. If vertex E is removed the graph gets disconnected.

7) DFS

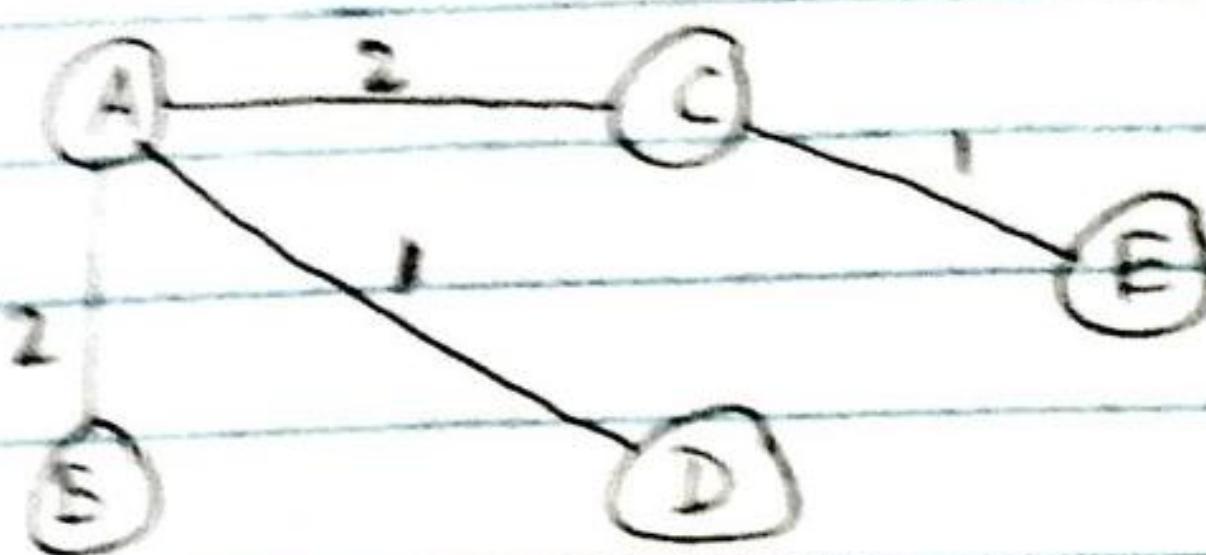
```

void dfs (int v, int a[10][10], int visited[10], int n)
{
    visited[v] = 1;
    for (int i = 0; i < n; i++)
        if (a[v][i]
            dfs(i);
    }
}
    
```

```

void dfs (int v, int a[10][10], int visited[10], int n)
{
    visited[v] = 1;
    for (int i = 0; i < n; i++)
        for (int j = 0; j < n; j++)
            if (a[v][j] && !visited[j])
                printf ("%d → %d ≠ %d", v, i);
    dfs(i);
}
    
```

5



A, D - Accepted

C, E - Accepted

A, B - Accepted

A, C - Accepted

A, D - Rejected

$$\text{Minimum cost} = 2+2+1+1$$

$$= 6$$

B, D - Rejected

D, E - Rejected

9) Topological sort

Topological sort in a DAG is used to sort the order of vertices in the visited order. A particular vertex can only be visited if the previous vertex is visited. Queue can be used to implement topological sort.

10) Real time applications of Graph

- 1) Airport System

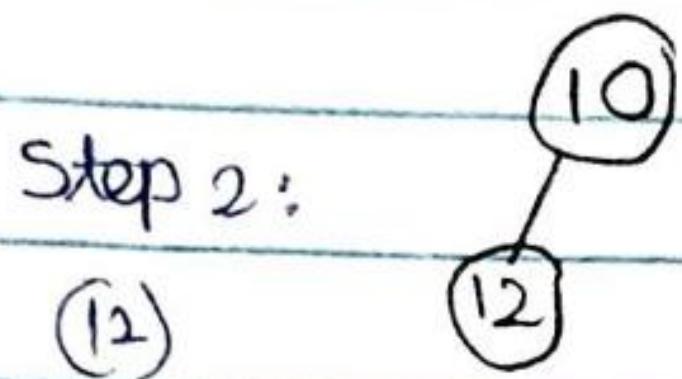
- 2) Wiring Connection in home

- 3) Course pre-requisite in a university

A

11) 10, 12, 1, 14, 6, 5, 8, 15, 3, 9, 7

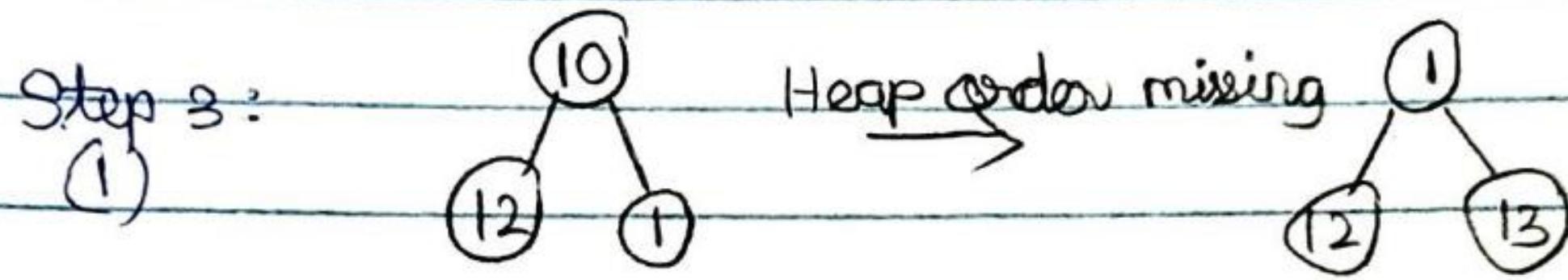
Step 1: (10)



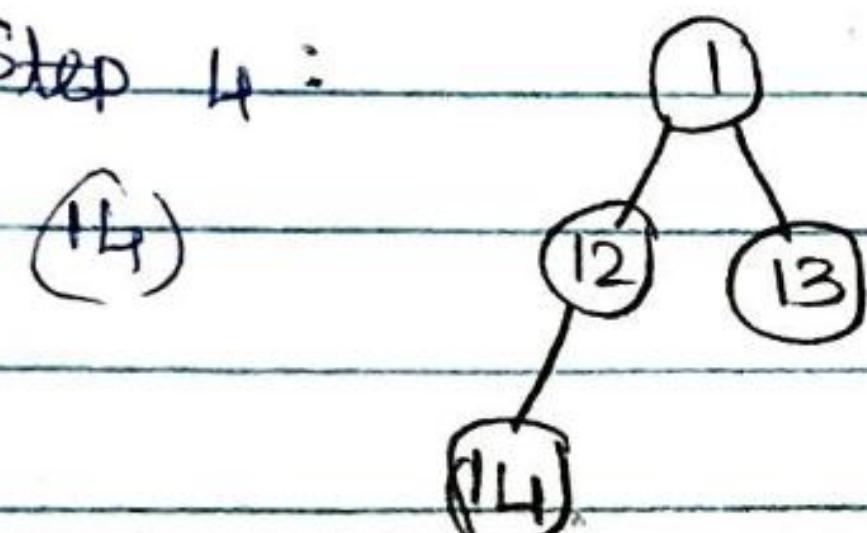
Step 2:



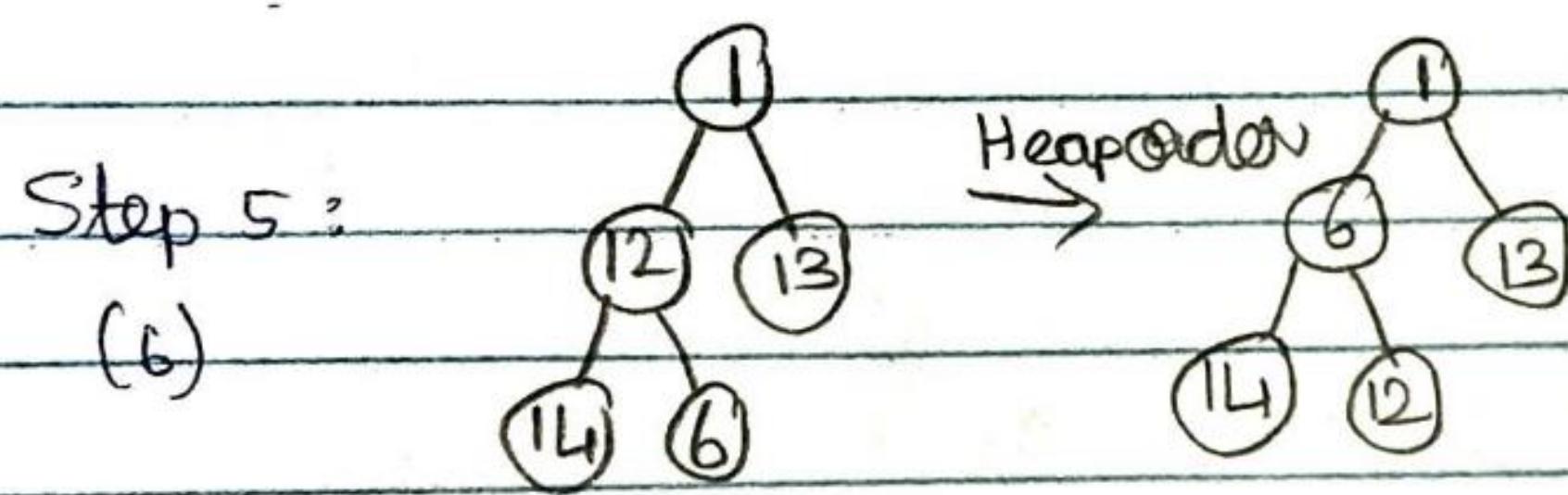
Step 3:



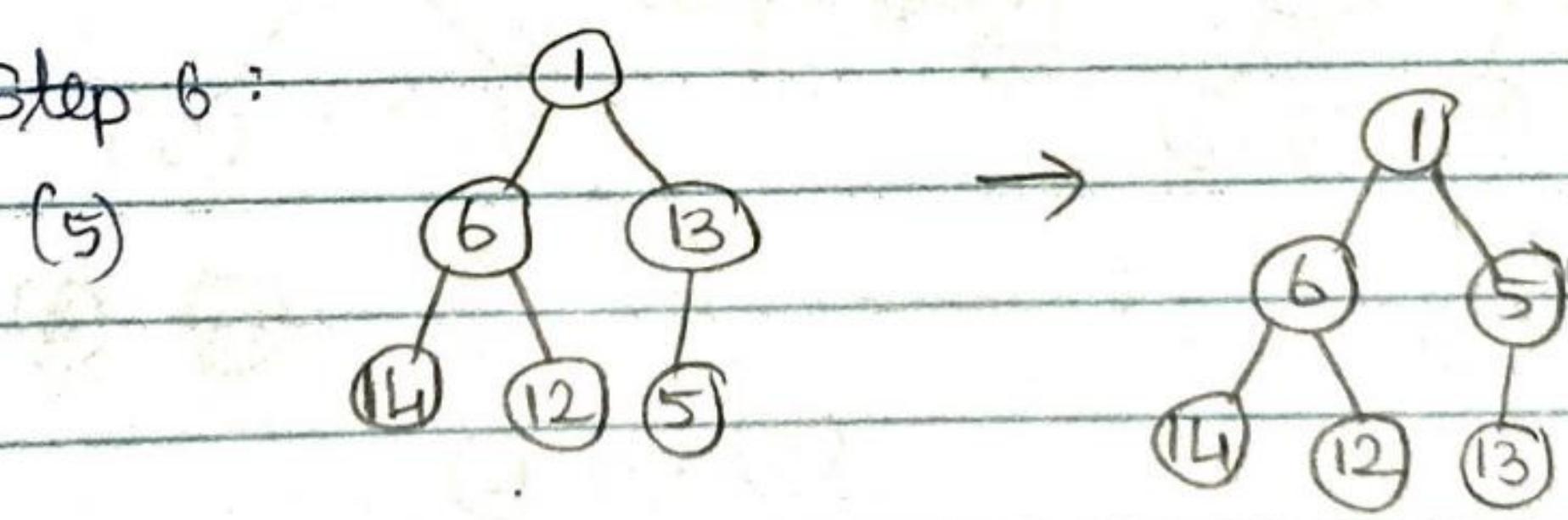
Step 4:



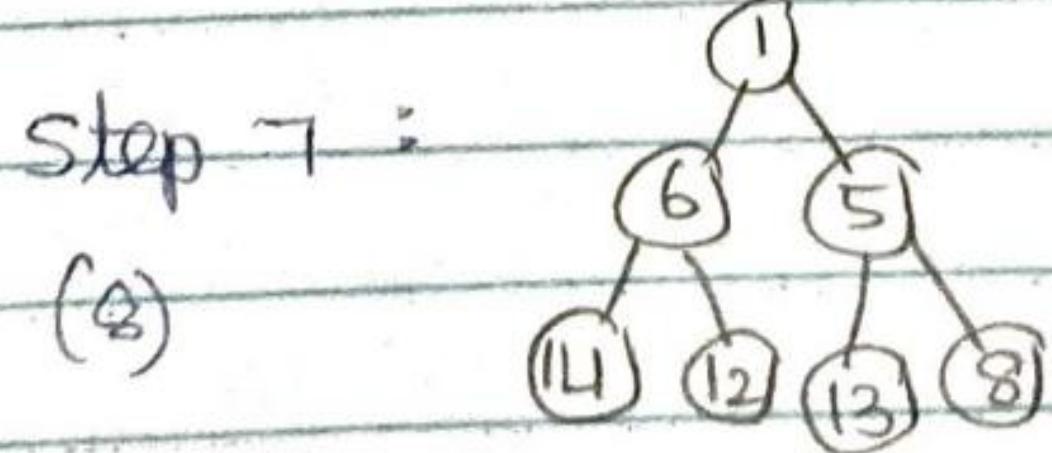
Step 5:



Step 6:

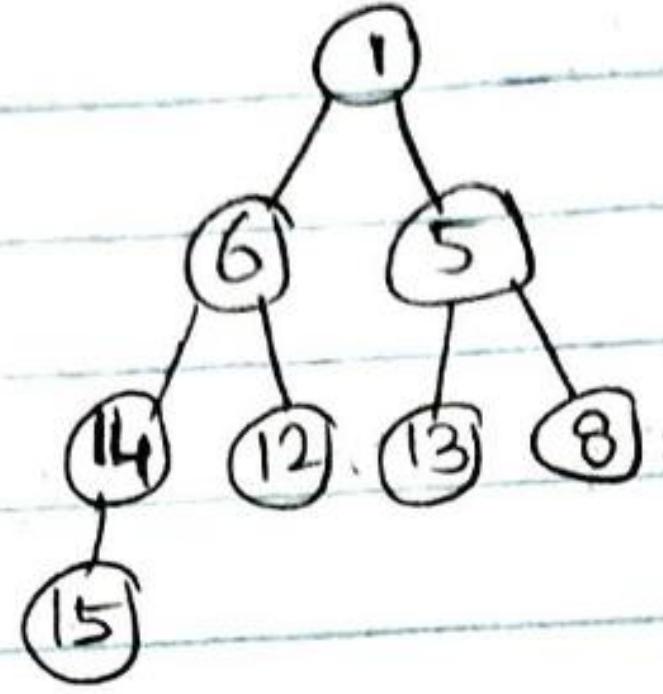


Step 7:



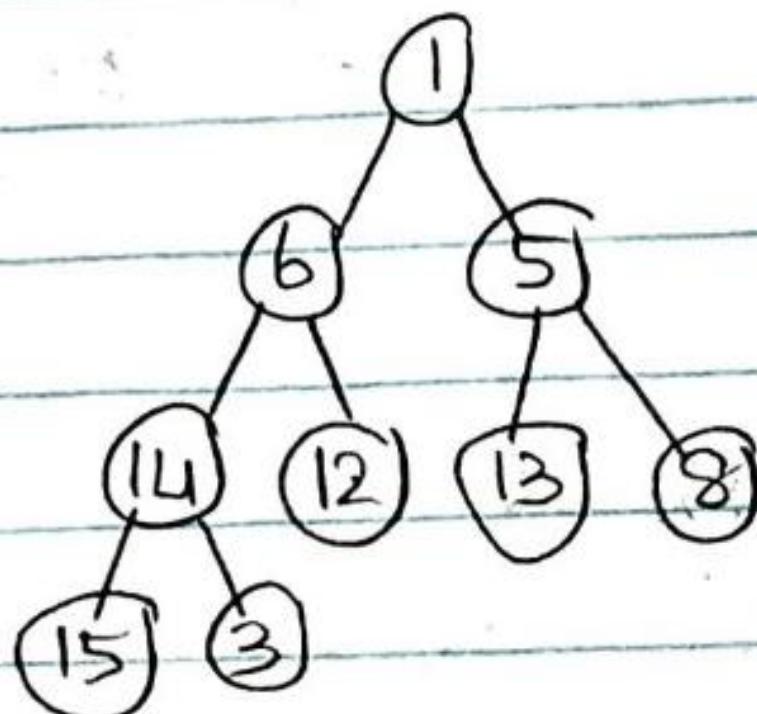
Step 8:

(15)

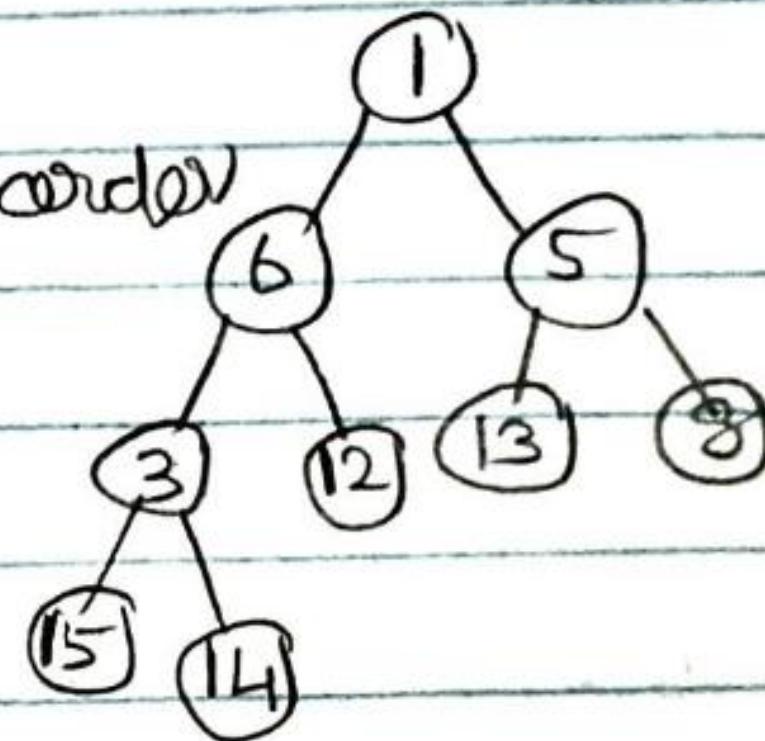


Step 9:

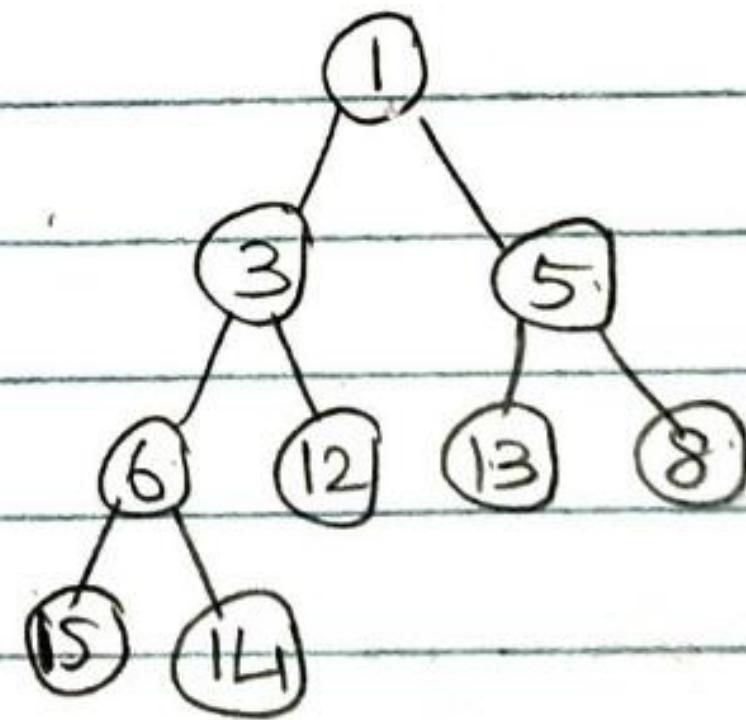
(3)



Heap order
→

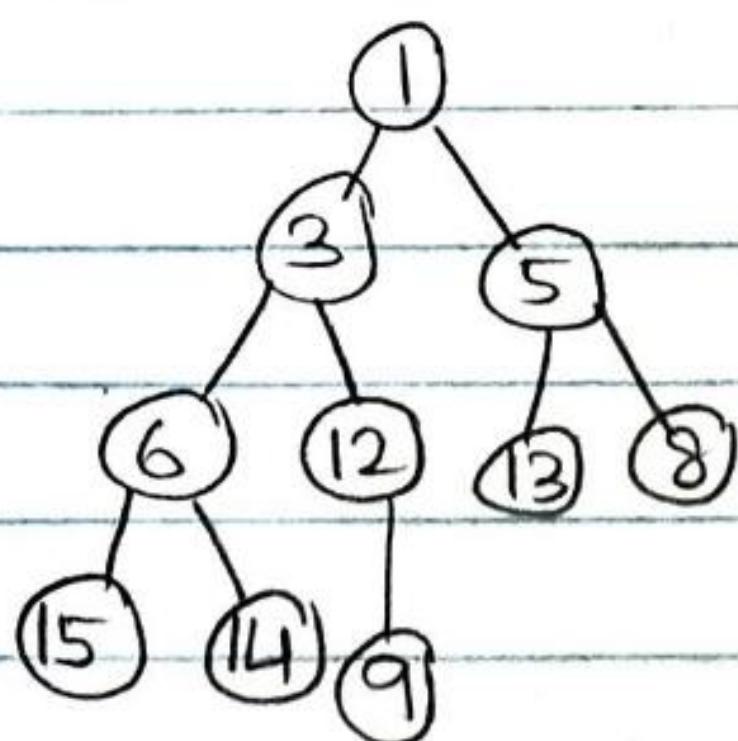


↓ Heap order

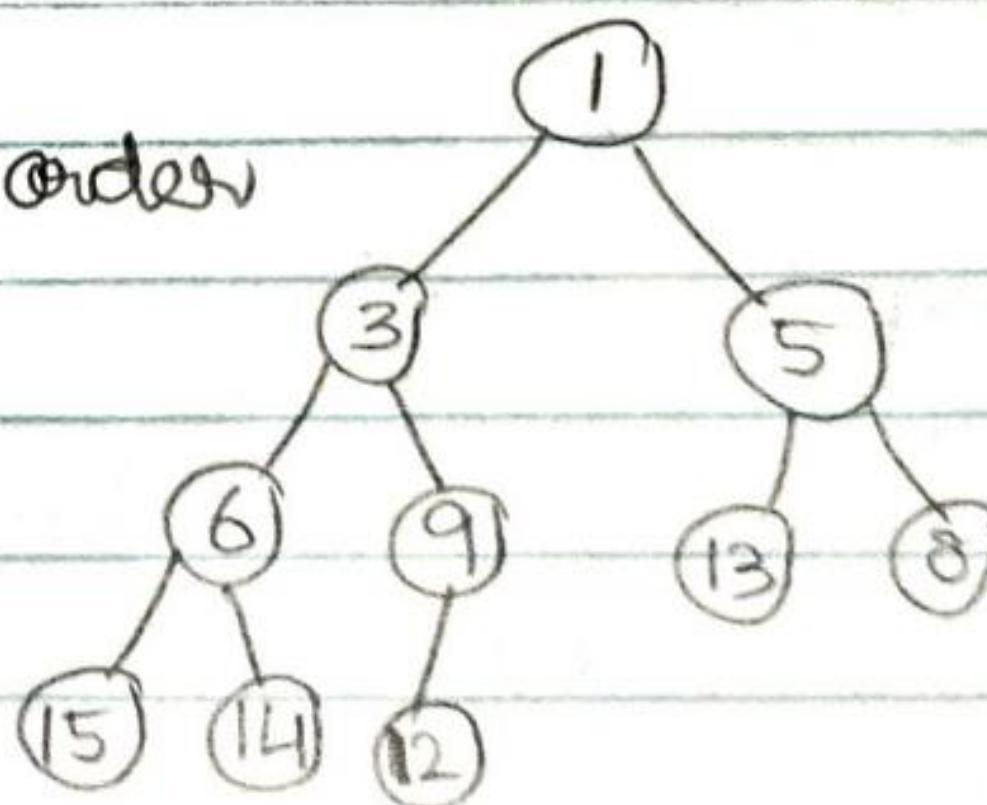


Step 10:

(9)

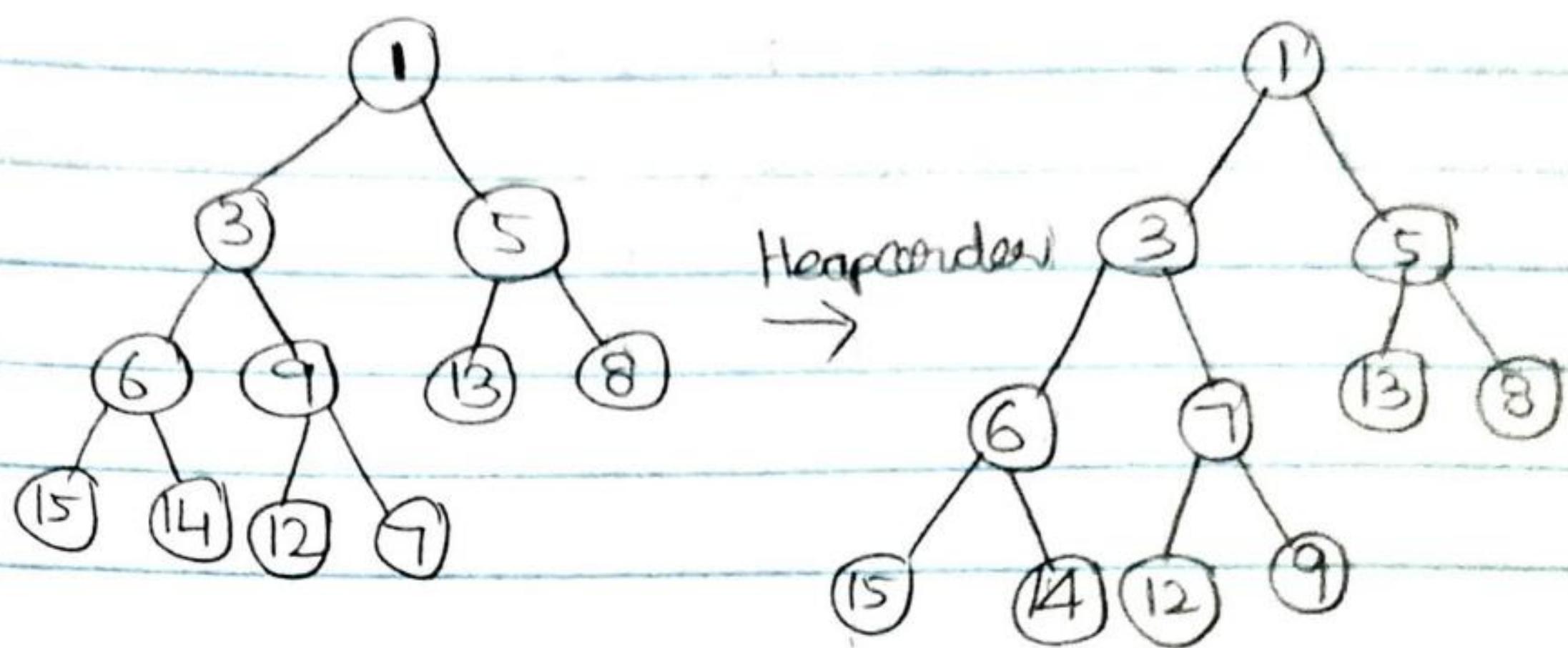


Heap order
→

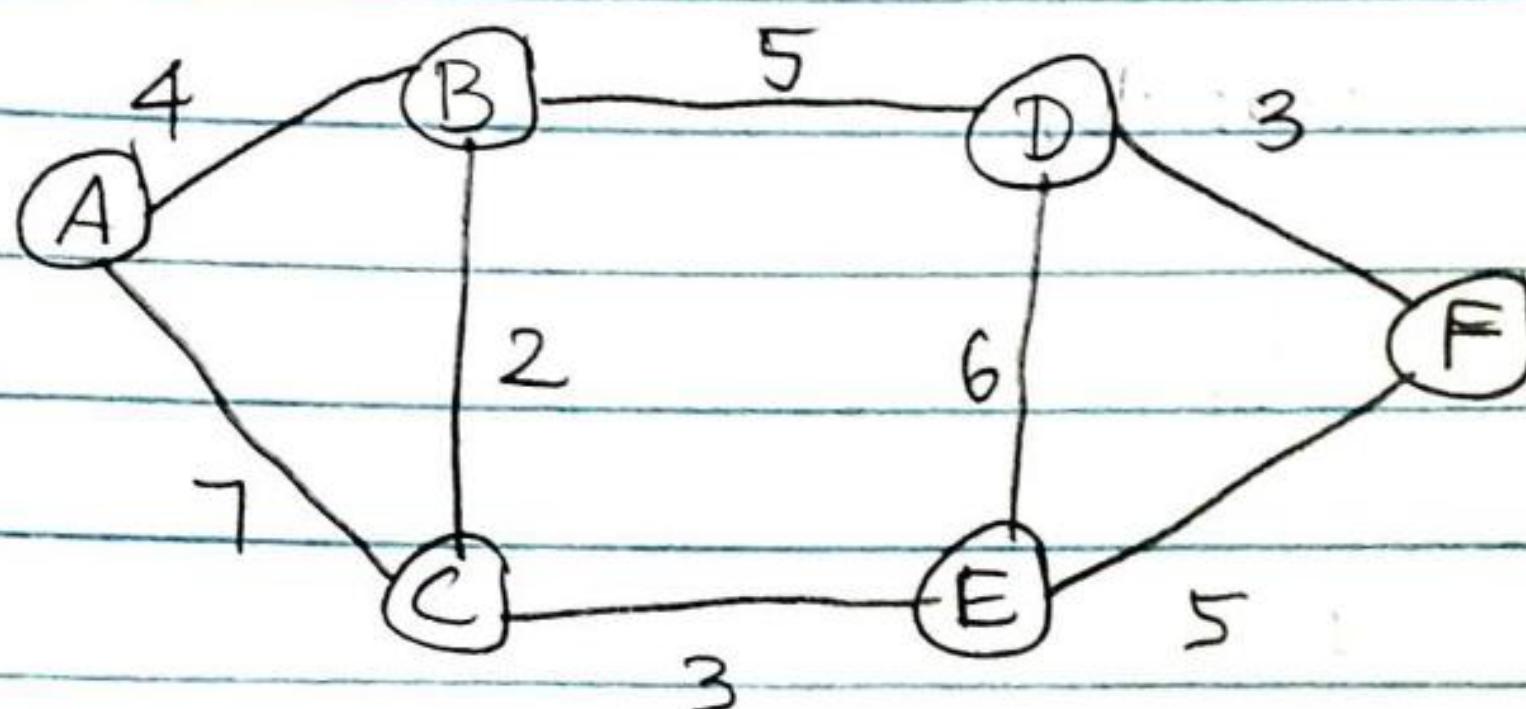


6

Step 11 :
(7)



(13)

Initial Configuration

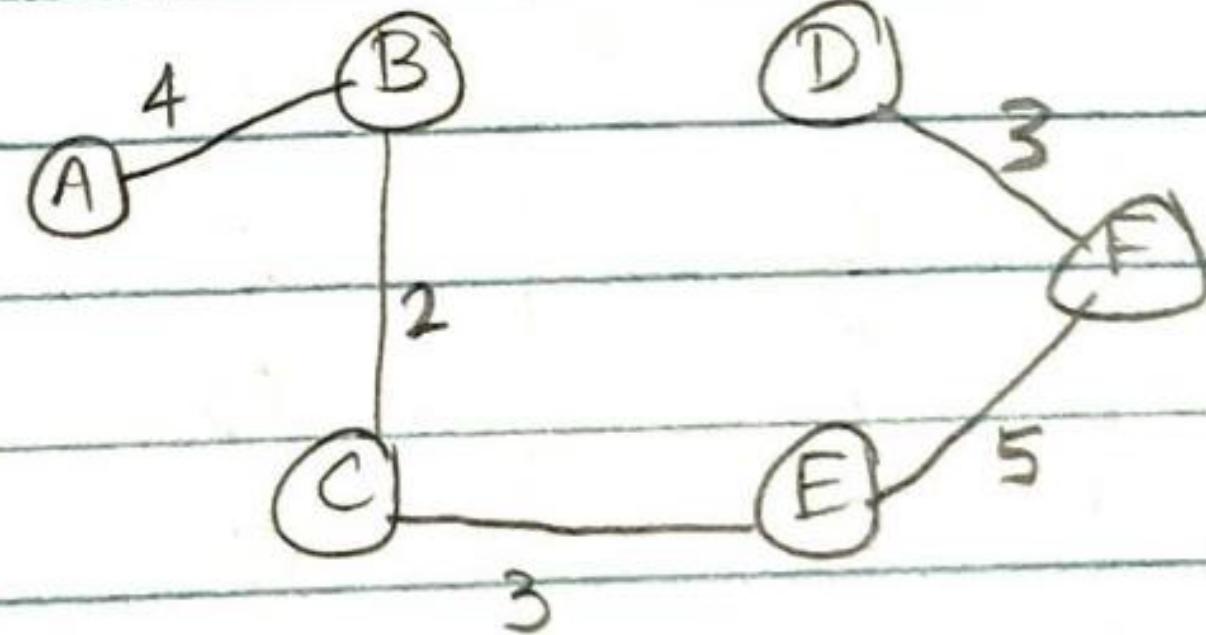
Vertices	Known	d_V	P_V
A	0	0	0
B	0	∞	0
C	0	∞	0
D	0	∞	0
E	0	∞	0
F	0	∞	0

After A is selected

Vertices	Known	d_V	P_V
A	1	0	0
B	0	4	A
C	0	7	A
D	0	∞	0
E	0	∞	0
F	0	∞	0

After B is selected

Vertices	Known	d_V	P_V
A	1	0	0
B	1	4	A
C	0	2	B
D	0	5	B
E	0	∞	0
F	0	∞	0



After C is selected

Vertices	Known	d_V	P_V
A	1	0	0
B	1	4	A
C	1	2	B
D	0	5	B
E	0	3	C
F	0	∞	0

8

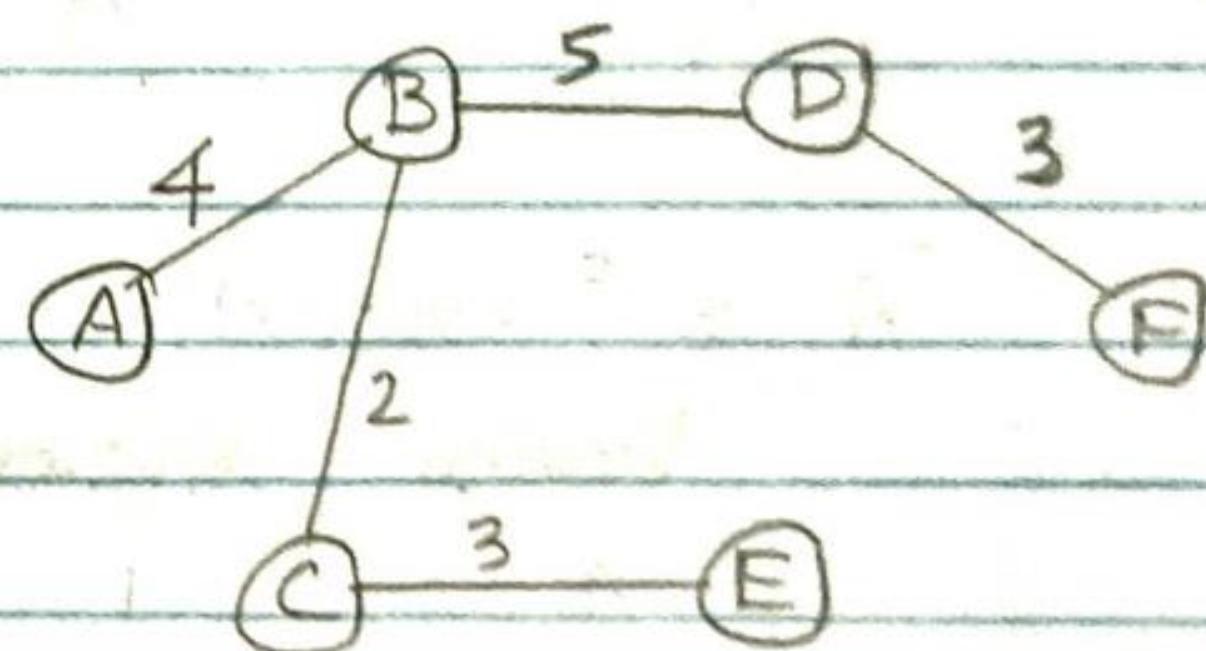
After F is selected

Vertices	Known	d_V	P_V
A	1	0	O
B	1	4	A
C	1	2	B
D	0	5	B
E	1	3	C
F	0	5	E

After D is selected

Vertices	Known	d_V	P_V
A	1	0	O
B	1	4	A
C	1	2	B
D	1	5	B
E	1	3	C
F	0	3	D

Output

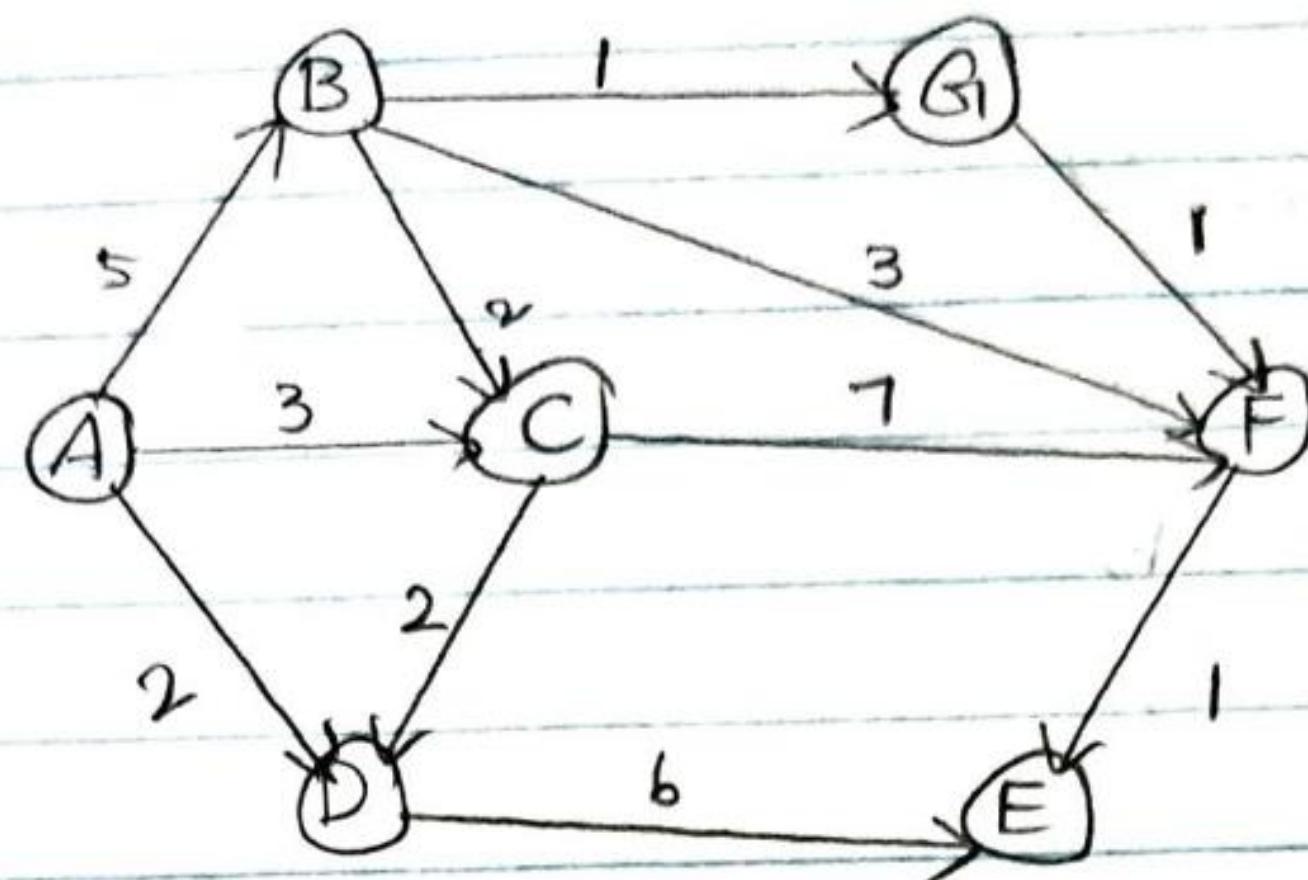


After F is selected

Vertices	Known	d_V	P_V
A	1	0	O
B	1	4	A
C	1	2	B
D	1	5	B
E	1	3	C
F	1	3	D

$$\text{Total Cost} = 4+2+5+3+3 = 17$$

(12)



Initial Configuration

Vertices	Known	d_v	P_v
A	0	0	0
B	0	∞	0
C	0	∞	0
D	0	∞	0
E	0	∞	0
F	0	∞	0
G	0	∞	0

A is Selected

Vertices	Known	d_v	P_v
A	1	0	0
B	0	5	A
C	0	3	A
D	0	2	A
E	0	∞	0
F	0	∞	0
G	0	∞	0

D is selected

Vertices	Known	d_V	P_V
A	1	0	O
B	0	5	A
C	0	3	A
D	1	2	A
E	0	8	D
F	0	∞	O
G	0	∞	O

C is selected

Vertices	Known	d_V	P_V
A	1	0	O
B	0	5	A
C	1	3	A
D	1	2	A
E	0	8	D
F	0	10	C
G	0	∞	O

B is selected

Vertices	Known	d_V	P_V
A	1	0	O
B	1	5	A
C	1	3	A
D	1	2	A
E	0	8	D
F	0	8	B
G	0	6	B

After G₁ is selected

Known	Known	d _v	P _v
A	1	0	0
B	1	5	A
C	1	3	A
D	1	2	A
E	0	8	D
F	0	7	G ₁
G	1	6	B

After F is selected

Vertices	Known	d _v	P _v
A	1	0	0
B	1	5	A
C	1	3	A
D	1	2	A
E	0	8	D
F	1	7	G
G	1	6	B

After E is selected

Vertices	Known	d _v	P _v
A	1	0	0
B	1	5	A
C	1	3	A
D	1	2	A
E	1	8	D
F	1	7	G ₁
G	1	6	B

12

$A \rightarrow B$, cost = 5

$A \rightarrow C$, cost = 3

$A \rightarrow D$, cost = 2

$A \rightarrow E$, cost = 8

$A \rightarrow F$, cost = 7

$A \rightarrow G_1$, cost = 6

A)

