$Final_Project_64060$

Contents

Data Preparation	1
Problem Statement	4
Understand3, the complexity of FDI decision factors by analysing their effects and using them to make FDI prediction	4
***	7
We now use Naive Bayes on select variables to predict Foreign Direct Investment Inflows.	7
we divide data set into 80% training and 20% testing	7
ROC Curves	13
Box-Cox Transformation	15
Hypertuning	16
Data Preparation	
getwd()	
## [1] "C:/Users/Mukht/OneDrive/Desktop/Kent State University/College of Business Admir	n-Bus. Analytics
<pre>setwd("C:\\Users\\Mukht\\OneDrive\\Desktop\\Kent State University\\College of Business</pre>	Admin-Bus. Analy
FinalProject<-read.csv("MukhtarMLProject.csv") str(FinalProject)	
## 'data.frame': 250 obs. of 5 variables: ## \$ \(\tilde{\	

```
head(FinalProject)
##
    i..FDIInflow
                   Security EaseOfDoingBus InvestFacilitation Corruption
## 1
             7 0.08251019 -1.0681966
                                                       2.8 3.142857
## 2
            12 1.44839773
                              -0.7473753
                                                       4.2 3.857143
            12 1.18841274
                                                       4.8 3.714286
## 3
                               0.4951372
             2 -0.69644101
## 4
                               -0.8701858
                                                       5.0 2.571429
                                                       4.2 3.857143
## 5
             1 0.32278869
                              0.1220579
## 6
             13 0.54041487
                               0.2062462
                                                        5.0 3.571429
library(class)
library(caret)
## Loading required package: ggplot2
## Loading required package: lattice
library(lattice)
library(ggplot2)
library(ISLR)
library(pROC)
## Type 'citation("pROC")' for a citation.
##
## Attaching package: 'pROC'
## The following objects are masked from 'package:stats':
##
##
      cov, smooth, var
library(tidyr)
library(dplyr)
##
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
      filter, lag
## The following objects are masked from 'package:base':
##
##
      intersect, setdiff, setequal, union
library(tidyverse)
## -- Attaching packages ------ tidyverse 1.3.1 --
```

```
## v tibble 3.1.4 v stringr 1.4.0
## v readr 2.0.1 v forcats 0.5.1
## v purrr 0.3.4
## -- Conflicts ------ tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag() masks stats::lag()
## x purrr::lift() masks caret::lift()
library(e1071)
library(rattle)
## Warning: package 'rattle' was built under R version 4.1.2
## Loading required package: bitops
## Rattle: A free graphical interface for data science with R.
## Version 5.4.0 Copyright (c) 2006-2020 Togaware Pty Ltd.
## Type 'rattle()' to shake, rattle, and roll your data.
library(esquisse)
## Warning: package 'esquisse' was built under R version 4.1.2
#Plot correlation headmap
library(GGally)
## Warning: package 'GGally' was built under R version 4.1.2
## Registered S3 method overwritten by 'GGally':
    method from
##
##
    +.gg ggplot2
ggcorr(FinalProject, label = TRUE, palette = "RdBu", name = "Correlation", hjust = 0.75, label_size =3,
```



Problem Statement

Understand3, the complexity of FDI decision factors by analysing their effects and using them to make FDI prediction

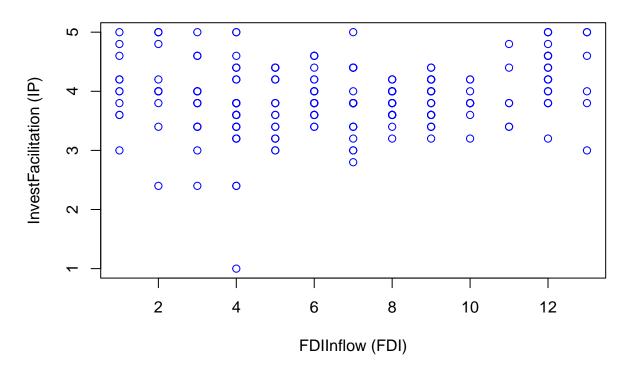
```
FinalProject_normalized<-preProcess (FinalProject, method = "range")
FinalProject_normalized = predict(FinalProject_normalized, FinalProject)
summary(FinalProject_normalized)</pre>
```

```
##
    i..FDIInflow
                       Security
                                     EaseOfDoingBus
                                                      InvestFacilitation
##
  Min.
          :0.0000
                    Min.
                           :0.0000
                                     Min.
                                            :0.0000
                                                      Min.
                                                             :0.000
  1st Qu.:0.2500
                    1st Qu.:0.4761
                                     1st Qu.:0.5139
                                                      1st Qu.:0.650
## Median :0.5000
                    Median :0.6806
                                     Median :0.6980
                                                      Median : 0.700
## Mean
          :0.4703
                    Mean
                           :0.6442
                                     Mean
                                            :0.6674
                                                      Mean
                                                             :0.723
                                     3rd Qu.:0.7588
##
  3rd Qu.:0.6667
                    3rd Qu.:0.8369
                                                      3rd Qu.:0.800
  Max.
          :1.0000
                    Max.
                           :1.0000
                                     Max.
                                            :1.0000
                                                      Max.
                                                             :1.000
##
     Corruption
## Min.
          :0.0000
## 1st Qu.:0.4286
## Median :0.5714
## Mean :0.5460
```

```
## 3rd Qu.:0.6429
## Max.
         :1.0000
#Linear Regression
# Creates a linear model for all the variables vs FDI Inflow and displays a plot of the points
Modela = lm("i...FDIInflow ~ EaseOfDoingBus + InvestFacilitation + FinalProject$Corruption + Security, da
summary(Modela)
##
## Call:
## lm(formula = i..FDIInflow ~ EaseOfDoingBus + InvestFacilitation +
       FinalProject$Corruption + Security, data = FinalProject)
##
## Residuals:
       Min
                1Q Median
                               30
                                      Max
## -6.4034 -2.3982 0.0278 2.1127 7.0927
##
## Coefficients:
##
                          Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                       2.7276 0.180
                            0.4920
                                                         0.857
## EaseOfDoingBus
                            0.2119
                                       0.2161
                                                0.981
                                                         0.328
## InvestFacilitation
                            0.8768
                                       0.3774 2.323
                                                         0.021 *
## FinalProject$Corruption
                            0.7494
                                       0.5775 1.298
                                                         0.196
## Security
                            -0.1548
                                       0.1997 -0.775
                                                         0.439
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
## Residual standard error: 3.182 on 245 degrees of freedom
## Multiple R-squared: 0.03244,
                                   Adjusted R-squared:
## F-statistic: 2.053 on 4 and 245 DF, p-value: 0.08759
```

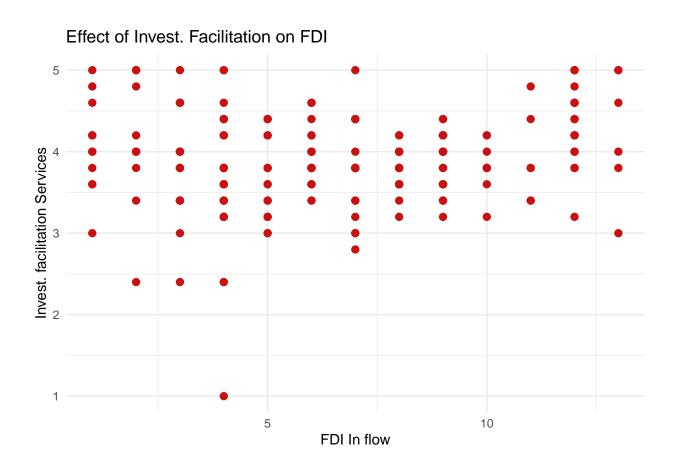
plot(FinalProject\$I..FDIInflow, FinalProject\$InvestFacilitation, xlab = "FDIInflow (FDI)", ylab = "Inve

InvestFacilitation against FDIInflow



esquisser(FinalProject)

```
ggplot(FinalProject) +
aes(x = \(\tilde{x}\) = InvestFacilitation) + geom_point(shape = "circle", size = 2.25, colour = "#
```



We now use Naive Bayes on select variables to predict Foreign Direct Investment Inflows.

We will use the e1070 package.

library(caret)
library(ISLR)
library(e1071)

we divide data set into 80% training and 20% testing

```
#Divide data into test and train
FinalProject_Index_Train<-createDataPartition(FinalProject$\text{\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\text{$\tex
```

```
Min. : 1.000
                           :-3.04528
                                            :-3.13918
                                                         Min.
                                                                :1.00
##
                    Min.
                                      Min.
                                                         1st Qu.:3.60
  1st Qu.: 4.000
                    1st Qu.:-0.76467
                                      1st Qu.:-0.72391
## Median : 7.000
                    Median : 0.15293
                                      Median : 0.11871
                                                         Median:3.80
## Mean
         : 6.663
                    Mean
                          :-0.03277
                                      Mean
                                            :-0.01463
                                                         Mean
                                                                :3.87
   3rd Qu.: 9.000
                    3rd Qu.: 0.85501
                                      3rd Qu.: 0.41935
                                                         3rd Qu.:4.20
##
                    Max. : 1.66035
                                      Max. : 1.50753
                                                         Max. :5.00
##
   Max.
          :13.000
##
     Corruption
##
  Min.
          :2.571
##
  1st Qu.:3.464
## Median :3.714
## Mean
         :3.673
## 3rd Qu.:3.857
## Max.
         :4.571
summary(Test)
                                      EaseOfDoingBus
    i..FDIInflow
                       Security
                                                        InvestFacilitation
##
## Min. : 1.000
                           :-2.2252
                                            :-2.96839
                    Min.
                                      Min.
                                                        Min.
                                                               :3.000
## 1st Qu.: 4.000
                    1st Qu.:-0.8293
                                      1st Qu.:-0.80094
                                                        1st Qu.:3.600
## Median : 7.000
                    Median : 0.1625
                                      Median : -0.02989
                                                        Median :4.000
                    Mean : 0.0648
                                     Mean :-0.13573
## Mean : 6.562
                                                        Mean
                                                               :3.983
                                      3rd Qu.: 0.31326
                                                        3rd Qu.:4.200
##
  3rd Qu.: 8.250
                    3rd Qu.: 1.0043
##
  Max.
          :12.000
                    Max. : 1.5852
                                     Max.
                                            : 1.27770
                                                        Max. :5.000
##
     Corruption
## Min.
          :2.571
## 1st Qu.:3.429
## Median :3.714
## Mean :3.625
## 3rd Qu.:3.857
## Max. :4.143
#Now, run the Naive Bayes classifier model, and predict FDI status on the test set
# Build a naïve Bayes classifier
FinalProject_nb_model <-naiveBayes(i..FDIInflow ~ EaseOfDoingBus + InvestFacilitation + Corruption + Se
FinalProject nb model
```

EaseOfDoingBus

InvestFacilitation

Security

##

i..FDIInflow

```
## Naive Bayes Classifier for Discrete Predictors
##
## naiveBayes.default(x = X, y = Y, laplace = laplace)
## A-priori probabilities:
## Y
                       2
##
                                   3
                                              4
                                                         5
                                                                     6
            1
## 0.04950495 0.03960396 0.07920792 0.14851485 0.06930693 0.10891089 0.09405941
                       9
                                  10
                                             11
                                                         12
## 0.10891089 0.12376238 0.03960396 0.02970297 0.07920792 0.02970297
##
## Conditional probabilities:
       EaseOfDoingBus
##
```

```
[,1]
                         [,2]
## Y
     1 -0.30027024 0.7135320
##
     2 -0.20558517 1.4438026
##
       -0.16639186 1.0450017
##
##
        -0.07188945 1.0075543
##
     5
        0.40838988 0.9238494
##
        0.26496896 0.6553708
     6
     7
       -0.29008117 0.9012087
##
##
     8
        -0.28828079 1.1568248
         0.19200974 0.8718009
##
     9
##
     10 0.22611897 0.6518544
##
     11 0.43386962 0.8237663
     12 -0.05021067 1.0790939
##
##
     13 -0.26504840 0.5961266
##
##
       InvestFacilitation
## Y
            [,1]
                       [,2]
##
     1 4.000000 0.5249339
##
     2 4.000000 0.7782765
##
        3.837500 0.6031860
##
     4 3.653333 0.7912161
##
     5 3.771429 0.4889999
     6 3.945455 0.3608552
##
##
        3.694737 0.4636494
     8 3.781818 0.2538023
##
##
     9 3.888000 0.3320643
##
     10 3.800000 0.3207135
     11 3.933333 0.5609516
##
     12 4.325000 0.5208967
##
     13 4.233333 0.7840068
##
##
##
       Corruption
                       [,2]
## Y
            [,1]
     1 3.800000 0.2446711
##
##
        3.410714 0.6363045
##
     3 3.696429 0.4201555
##
     4 3.614286 0.3542245
##
     5 3.775510 0.2949831
##
        3.720779 0.3648216
     7 3.503759 0.3242589
##
##
     8 3.746753 0.4180844
##
     9 3.731429 0.2745435
     10 3.607143 0.3030458
##
     11 3.690476 0.2102800
##
     12 3.696429 0.3720690
     13 3.642857 0.2347382
##
##
##
       Security
## Y
               [,1]
                          [,2]
         0.23072050 0.7155632
##
##
     2
         0.21890802 1.0884330
##
     3
       -0.42054470 1.3128653
##
     4
        0.19391240 1.0111003
        0.18806906 1.1063097
##
     5
```

```
##
       -0.08549680 0.7974383
##
     7
       -0.22843763 1.1563954
##
         0.06919476 0.9855971
##
     9 -0.23728942 1.0662863
##
     10 0.10035228 0.6081962
     11 -0.70653062 0.8054158
##
     12 0.02937670 1.2257045
##
     13 0.19957601 0.8441008
##
```

summary(FinalProject_nb_model)

```
## Length Class Mode
## apriori 13 table numeric
## tables 4 -none- list
## levels 13 -none- character
## isnumeric 4 -none- logical
## call 4 -none- call
```

#The first part of the output above shows the ratios of default (yes) and default (no) in the training set (called a priori probabilities), followed by a table giving for each target class, mean and standard deviation of the (sub-)variable. Also, note that the Naive Bayes algorithm assumes a Normal distribution for the independent variables. In accordance with the rule of the use of categorical predictors (the independent variables have been converted to categorical), we now have the conditional probabilities p(X|Y) for each attribute level given the default status.

Now, use the model on the test set

N / Row Total |

N / Col Total |

N / Table Total |

| ## |

##

##

```
set.seed(123)
# Predict the default status of test data set
FinalProject_Predicted_Test_labels <-predict(FinalProject_nb_model, Test)
library(gmodels)
##
## Attaching package: 'gmodels'
## The following object is masked from 'package:pROC':
##
##
       ci
# Show the confusion matrix of the classifier
CrossTable(x=Test$i..FDIInflow, y=FinalProject_Predicted_Test_labels, prop.chisq = FALSE)
##
##
##
      Cell Contents
##
##
                           N
```

##
Total Observations in Table: 48

##

##								
##								
	Test\$ïFDIInflow	2	4	5	6	7	8	1
##			,	!	,			
##	1	1	0	0	0	0	0	
##	!	0.500		0.000	0.000	0.000	0.000	
##	ļ	0.333		0.000	0.000	0.000	0.000	
## ##		0.021	0.000	0.000	0.000	0.000	0.000	0.02
##	2	1	 1	1	1	0	0	
##	!	0.200				0.000	0.000	0.000
##	ı	0.333					0.000	
##	ı	0.021				0.000	0.000	
##	!		(('	I		·
##	3	0	1	0 1	0 1	0	0	1
##	!	0.000				0.000	0.000	
##	!	0.000			0.000	0.000	0.000	
##	!	0.000	0.021	0.000	0.000	0.000	0.000	0.02
##			,J	[]	,			
##	4	0	0	0	1	1 1	1	
##	!	0.000		0.000		0.200	0.200	
##	·	0.000		0.000	0.125		0.167	
## ##		0.000	0.000 	0.000	0.021	0.021	0.021	0.04: -
##	5	1	2	0	 0	1	1	1
##	!	0.200				•		0.000
##	I	0.333					0.167	
##	1	0.021						
##	!		(11	('	I		·
##	6	0	0	0 1	1	1 1	0	1
##	!	0.000						
##	!	0.000					0.000	
##	,	0.000	0.000	0.000	0.021	0.021	0.000	0.000
##	7		, 	'	, ₁	₁	·	
## ##	7	0	1 0 167	0 0 0 0 1	0 000 1	1 0 167	0	1 0 33
## ##	ı	0.000 0.000					0.000	
##	1	0.000					1 0.000	0.14
##		1						.
##	8	0	, , , ,	. 0 1	1	0	3	i
##	· •	0.000				•	•	•
##		0.000						
##	!	0.000	0.000	0.000	0.021	0.000	0.062	
##	·							·
##		0						-
##		0.000						
##		0.000						
##	•	0.000						
## ##	10		 0		 1	•	•	•
## ##		0.000						-
##	ı	0.000 1	0.000 1	, 0.000 1	0.500 1	1 0.000	0.000	1 0.50

##	1	0.000	0.000	0.000	0.125	0.000	0.000	0.07
##	1	0.000	0.000	0.000	0.021	0.000	0.000	0.02
##		,	,'		·	-	.	-
##	12	0 1	. 1	0	1	1 0	1	
##	1	0.000	0.143	0.000	0.143	0.000	0.143	0.28
##	1	0.000	0.167	0.000	0.125	0.000	0.167	0.14
##	1	0.000	0.021	0.000	0.021	0.000	0.021	0.043
##		,	,		·	-	.	-
##	Column Total	3	6	1	1 8	1 4	1 6	1
##	1	0.062	0.125	0.021	0.167	0.083	0.125	0.29
##		,	,'		·	-	.	-
##								

#Our results indicate that we mis-classified a total of X cases. X as False Positives, and X as False Negatives.

##

#It is sometimes useful to output the raw prediction probabilities rather than the predicted class. To do that, we use the raw option in the model.

FinalProject_nb_model <- naiveBayes(i..FDIInflow ~ EaseOfDoingBus + InvestFacilitation + Corruption + S

```
#Make predictions and return probability of each class
FinalProject_Predicted_Test_labels <-predict(FinalProject_nb_model,Test, type = "raw")
#show the first few values
head(FinalProject_Predicted_Test_labels)</pre>
```

```
##
                                         3
                                                                              6
## [1,] 1.521914e-05 0.69414227 0.09052915 0.09353182 0.0001582876 0.003030543
## [2,] 3.035470e-02 0.04461605 0.07335099 0.13092896 0.1978481926 0.123562523
## [3,] 3.509910e-02 0.01504716 0.03584012 0.10058550 0.0909301362 0.219344713
## [4,] 3.563917e-02 0.02250682 0.04785579 0.10258168 0.1809680922 0.159132145
## [5,] 4.498815e-03 0.06978865 0.06364104 0.18657268 0.0556801454 0.181261108
  [6,] 2.295755e-04 0.42008221 0.10374540 0.17150416 0.0025488703 0.028874318
##
##
                                           9
                                                       10
                              8
## [1,] 0.01612071 1.319611e-05 3.637884e-05 3.305501e-05 1.481988e-06 0.1021497
## [2,] 0.01324486 2.867580e-02 1.240216e-01 6.911072e-03 3.376322e-03 0.2205693
## [3,] 0.04387863 4.826621e-02 1.928601e-01 8.919988e-02 4.079269e-02 0.0756084
## [4,] 0.01950271 7.458167e-02 2.048791e-01 2.551990e-02 9.784032e-03 0.1136775
## [5,] 0.09115523 7.600574e-02 8.332303e-02 5.802816e-02 2.593149e-03 0.1231007
  [6,] 0.10593413 2.769379e-02 2.649594e-03 2.869177e-03 2.428194e-06 0.1327659
##
## [1,] 0.0002381556
## [2,] 0.0025396872
## [3,] 0.0125473759
## [4,] 0.0033713954
## [5,] 0.0043515765
## [6,] 0.0011004738
```

```
set.seed(123)
data <- data.frame(FinalProject = sample(c("True", "False"), 250, replace = TRUE),</pre>
                    FinalProject_Predicted_Test_labels = sample(c("True", "False"), 250, replace = TRUE)
table(data$FinalProject_Predicted_Test_labels, data$FinalProject)
##
##
           False True
##
     False
              58
                    54
              69
                    69
##
     True
#The confusionMatrix function is very helpful as not only does it display a confusion matrix, it calculates
many relevant statistics alongside:
set.seed(123)
data <- data.frame(FinalProject = sample(c("True", "False"), 250, replace = TRUE),</pre>
FinalProject_Predicted_Test_labels = sample(c("True", "False"), 250, replace = TRUE)
library(caret)
confusionMatrix(as.factor(data$FinalProject_Predicted_Test_labels), as.factor(data$FinalProject), posit
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction False True
##
        False
                 58
##
        True
                 69
                       69
##
##
                   Accuracy: 0.508
##
                     95% CI: (0.4443, 0.5716)
##
       No Information Rate: 0.508
       P-Value [Acc > NIR] : 0.5253
##
##
                      Kappa: 0.0176
##
##
##
    Mcnemar's Test P-Value: 0.2068
##
##
               Sensitivity: 0.5610
##
               Specificity: 0.4567
##
            Pos Pred Value: 0.5000
##
            Neg Pred Value: 0.5179
##
                Prevalence: 0.4920
##
            Detection Rate: 0.2760
##
      Detection Prevalence: 0.5520
##
         Balanced Accuracy: 0.5088
##
```

ROC Curves

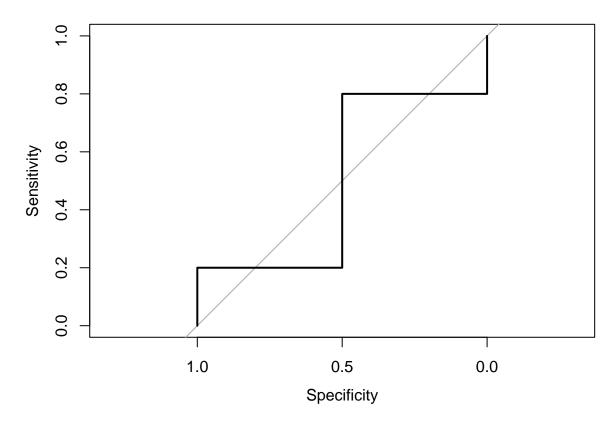
'Positive' Class : True

##

##

We can now output the ROC curves. we should emember that ROC curves plot sensitivity (true positive rate) versus (1 - specificity), which is (1 - TNR) or false positive rate. See here for more details

```
# install.packages("pROC") # install if necessary
library(pROC)
{\it \#Passing the column of the predicted probabilities}
#That column contains the probability associate to 'yes'
roc(Test$\(\text{\finalProject_Predicted_Test_labels[, 2]})
## Warning in roc.default(Test$i..FDIInflow, FinalProject_Predicted_Test_labels[, :
## 'response' has more than two levels. Consider setting 'levels' explicitly or
## using 'multiclass.roc' instead
## Setting levels: control = 1, case = 2
## Setting direction: controls > cases
##
## Call:
## roc.default(response = Test$i..FDIInflow, predictor = FinalProject_Predicted_Test_labels[,
                                                                                                     2])
## Data: FinalProject_Predicted_Test_labels[, 2] in 2 controls (Test$\"\"..FDIInflow 1) > 5 cases (Test$\"\".
## Area under the curve: 0.5
plot.roc(Test$\(\text{\textsiz}\)..FDIInflow, FinalProject_Predicted_Test_labels[, 2])
## Warning in roc.default(x, predictor, plot = TRUE, ...): 'response' has more
## than two levels. Consider setting 'levels' explicitly or using 'multiclass.roc'
## instead
## Setting levels: control = 1, case = 2
## Setting direction: controls > cases
```



The AUC is 1. The ROC curve is also plotted, though note that the X-Axis is Specificity (True Negative Rate), rather than 1-Specificity (False Positive Rate). This function can also be thought of as a plot of the FDI as a function of the Type I Error of the decision rule.

Box-Cox Transformation

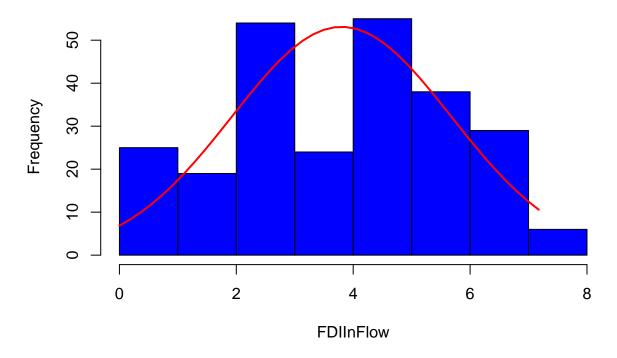
We first illustrate the transformation of data using the Box-Cox transformation approach

```
library(ISLR)
library(caret)
#Create a Box-Cox Transformation Model
FinalProject_Box_Cox_Transform<-preProcess(FinalProject,method = "BoxCox")
FinalProject_Box_Cox_Transform

## Created from 250 samples and 3 variables
##
## Pre-processing:
## - Box-Cox transformation (3)
## - ignored (0)
##
## Lambda estimates for Box-Cox transformation:
## 0.7, 1.8, 2</pre>
```

Now, we apply the transformation

Histogram before Transformation



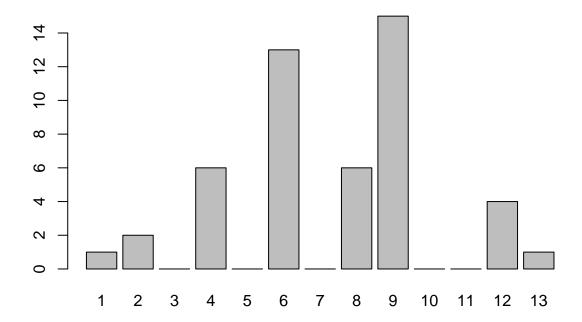
Hypertuning

```
library(caret)
library(ISLR)

set.seed(123)
#Divide data into test and train
Index_Train<-createDataPartition(FinalProject$\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{\tilde{
```

```
nb_model <-train(ï..FDIInflow ~ EaseOfDoingBus + InvestFacilitation + Corruption + Security, data = Tra
# Predict the default status of test dataset
Predicted_Test_labels <-predict(FinalProject_nb_model,Test)
summary(Predicted_Test_labels)

## 1 2 3 4 5 6 7 8 9 10 11 12 13
## 1 2 0 6 0 13 0 6 15 0 0 4 1</pre>
```



```
library(gmodels)
# Show the confusion matrix of the classifier
CrossTable(x=Test$:..FDIInflow,y=Predicted_Test_labels, prop.chisq = FALSE)
```

```
##
## Cell Contents
## |------|
## | N | N | N | N | N |
## | N | Col Total |
## | N | Table Total |
## |------|
```

plot(Predicted_Test_labels)

##		in Table. /	10							
##	Total Observations	in lable: 4	18							
##										
##										
	Test\$ïFDIInflow			4	l 6 l	8	9	1:		
##										
##	1	0	1	0	2	0	0	(
##		0.000	0.333	0.000	0.667	0.000	0.000	0.00		
##		0.000						0.00		
##		0.000	0.021	0.000	0.042	0.000	0.000	0.00		
##										
##		0						0.00		
##		0.000								
##		0.000						0.25		
## ##		0.000	0.000 	0.000	0.042	. 0.000	0.000	0.02		
##		l 0 l		1	 1	l 0	 1			
##		0.000					-	0.00		
##		0.000						0.00		
##		0.000						0.00		
##				,						
##	4	0 1	0	1	. 2	2	1 1			
##		0.000						0.00		
##		0.000						0.00		
##		0.000	0.000	0.021	0.042	0.042	0.021	0.00		
##										
##	5	1	1	1	0 1	0	1			
##		0.250		0.250				0.00		
##		1.000					0.067	0.00		
##		0.021	0.021	0.021	0.000	0.000	0.021	0.00		
##										
##		0						2 22		
##		0.000								
##		0.000						0.00		
## ##		0.000						0.00		
##	7	l 0 l		'	' '	1	1 1			
##		0.000						0.20		
##		0.000						0.25		
##		0.000					0.021	0.02		
##			 	,						
##		. 0 1	0	1	1	2	1	(
##		0.000						0.00		
##		0.000	0.000	0.167	0.077	0.333	0.067	0.00		
##		0.000	0.000	0.021	0.021	0.042	0.021	0.00		
##										
##	9	0						(
##		0 000 1	0 000 1	0 000	0 333 1	0 167	0 500 1	0.00		

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0.167 |

0.021 |

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##

##

##

##

##

##

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                      0.000 |
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                                                                        0.133 |
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                      0.000 |
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                                                     0.000 |
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                                                      13 |
                        1 l
                                    2 |
                                           6 |
                                                                 6 I
##
      Column Total |
                                                                          15 |
##
            0.021 |
                                0.042 |
                                          0.125 |
                                                    0.271 |
                                                               0.125 |
                                                                         0.312 |
                                                                                  0.08
      ##
```

```
set.seed(123)
data <- data.frame(FinalProject = sample(c("True", "False"), 250, replace = TRUE),
Predicted_Test_labels = sample(c("True", "False"), 250, replace = TRUE)
)
library(caret)
confusionMatrix(as.factor(data$Predicted_Test_labels), as.factor(data$FinalProject), positive = "True")</pre>
```

```
## Confusion Matrix and Statistics
##
           Reference
## Prediction False True
##
       False 58 54
       True
                69 69
##
##
                Accuracy: 0.508
                 95% CI : (0.4443, 0.5716)
##
      No Information Rate: 0.508
##
      P-Value [Acc > NIR] : 0.5253
##
##
                    Kappa: 0.0176
##
  Mcnemar's Test P-Value: 0.2068
##
##
##
              Sensitivity: 0.5610
##
              Specificity: 0.4567
```

Pos Pred Value: 0.5000

Neg Pred Value: 0.5179

Detection Rate: 0.2760

Detection Prevalence: 0.5520

Prevalence: 0.4920

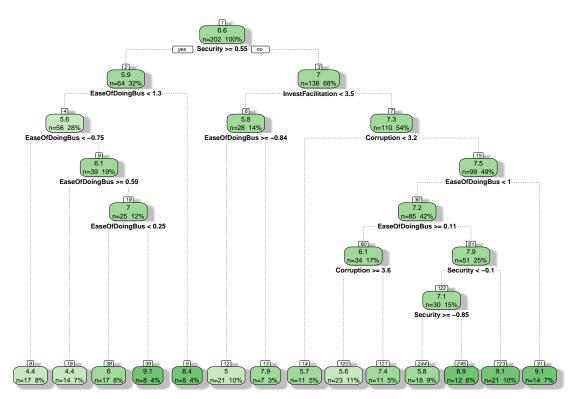
##

##

##

```
Balanced Accuracy: 0.5088
##
##
          'Positive' Class : True
##
##
#FDI Decision Tree
library(rpart)
library(ISLR)
library(rpart.plot)
## Warning: package 'rpart.plot' was built under R version 4.1.2
library(datasets)
library(caTools)
## Warning: package 'caTools' was built under R version 4.1.2
library(party)
## Warning: package 'party' was built under R version 4.1.2
## Loading required package: grid
## Loading required package: mvtnorm
## Loading required package: modeltools
## Loading required package: stats4
## Loading required package: strucchange
## Warning: package 'strucchange' was built under R version 4.1.2
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
       as.Date, as.Date.numeric
## Loading required package: sandwich
## Warning: package 'sandwich' was built under R version 4.1.2
## Attaching package: 'strucchange'
## The following object is masked from 'package:stringr':
##
##
       boundary
```

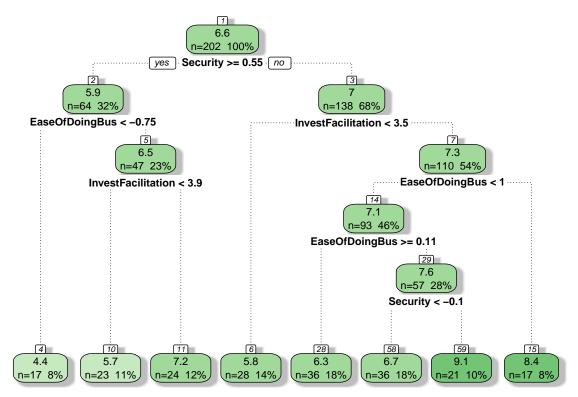
```
library(dplyr)
library(magrittr)
##
## Attaching package: 'magrittr'
## The following object is masked from 'package:purrr':
##
##
       set_names
## The following object is masked from 'package:tidyr':
##
##
       extract
# Decision Tree
library(rpart)
library(tidyverse)
library(rpart.plot)
# Tree plot
FDI<- rpart(i..FDIInflow ~ InvestFacilitation, data = Train) # only one independent variable
FDI<- rpart(i..FDIInflow ~ ., data = Train) # Except one dependent variable, others are all independent
# Predict Tree
PredictFDI<-predict(FDI, newdata = Test)</pre>
fancyRpartPlot(FDI)
```



Rattle 2021-Dec-14 19:56:20 Mukht

Tree with Minimum Observation

PredictFDI<-rpart(ï..FDIInflow ~ EaseOfDoingBus + InvestFacilitation + Corruption + Security, data = Tr fancyRpartPlot(PredictFDI)



Rattle 2021-Dec-14 19:56:21 Mukht

Make a prediction; Predict FDI In flow

table_FDI

```
library(rpart)
library(rpart.plot)
PredictFDIUnknown<-predict(PredictFDI, Test)
table_FDI <-table(Test$\cdots..FDIInflow, PredictFDIUnknown)
summary(table_FDI)

## Number of cases in table: 48
## Number of factors: 2
## Test for independence of all factors:
## Chisq = 82.96, df = 84, p-value = 0.5115
## Chi-squared approximation may be incorrect</pre>
```

##		PredictFDIUnknown				
##		4.41176470588235	5.65217391304348	5.75	6.305555555556	6.722222222222
##	1	1	0	0	2	0
##	2	0	0	0	0	1
##	3	0	0	1	0	1
##	4	0	0	1	2	3
##	5	1	0	1	1	0
##	6	0	0	0	2	1
##	7	0	1	1	0	1
##	8	0	0	1	0	0

```
##
     9
                                             0
                                                   0
                                                                       1
                                                                                          4
##
     10
                          0
                                             1
                                                   0
                                                                       1
                                                                                          0
                          0
                                             0
                                                                       0
                                                                                          0
##
     11
                                                   1
##
     12
                          0
                                                   0
                                                                       0
                                                                                          2
                                             1
##
     13
                          0
                                                   0
                                                                                          0
##
       PredictFDIUnknown
##
         7.25 8.35294117647059 9.09523809523809
##
     1
                                0
##
     2
            0
                                1
                                                   1
            0
                                0
                                                   1
##
     3
##
     4
            0
                                0
                                                   0
                                0
##
     5
            0
                                                   1
            0
                                                   0
##
     6
                                1
     7
            0
##
                                1
                                                   1
##
     8
            0
                                                   3
                                1
##
     9
            1
                                0
                                                   0
##
     10
            0
                                0
                                                   0
                                0
                                                   0
##
     11
            0
##
     12
            1
                                0
                                                   1
##
     13
            0
                                0
                                                   0
```

```
#accuracy test
accuracy_Test <- sum(diag(table_FDI)) / sum(table_FDI)
print(paste('Accuracy for test', accuracy_Test))</pre>
```

[1] "Accuracy for test 0.1666666666667"

CP nsplit rel error

#performance measurement- confusion matrix

##

```
accuracy_tune <- function(fit) {
    PredictFDIUnknown <- predict(FDI, Test, type = 'class')
    table_FDI <- table(FinalProject$:..FDIInflow, PredictFDIUnknown)
    accuracy_Test <- sum(diag(table_FDI)) / sum(table_FDI)
    accuracy_Test
}</pre>
```

#We tried to tune the parameters and see if we could improve the model over the default value. As a reminder, you need to get an accuracy higher than 0.78

```
control <- rpart.control(minsplit = 4,
    minbucket = round(5 / 3),
    maxdepth = 3,
    cp = 0)
tune_fit<-rpart(ï..FDIInflow ~., data = Train, method = "class", control = control)
summary(tune_fit)

## Call:
## rpart(formula = ï..FDIInflow ~ ., data = Train, method = "class",
## control = control)
## n= 202
##</pre>
```

xerror

xstd

```
## 1 0.02890173
                     0 1.0000000 1.000000 0.02880715
## 2 0.01445087
                     2 0.9421965 1.046243 0.02507420
## 3 0.01156069
                     4 0.9132948 1.046243 0.02507420
## 4 0.0000000
                     7 0.8786127 1.034682 0.02609568
##
  Variable importance
##
             Security
                          EaseOfDoingBus
                                                  Corruption InvestFacilitation
##
                   30
                                                          24
##
##
  Node number 1: 202 observations,
                                        complexity param=0.02890173
##
     predicted class=4
                         expected loss=0.8564356 P(node) =1
                                     16
                                           29
                                                                    25
                                                                          22
##
       class counts:
                              10
                                                 15
                                                       20
                                                                                             18
      probabilities: 0.045 0.050 0.079 0.144 0.074 0.099 0.099 0.124 0.109 0.040 0.025 0.089 0.025
##
##
     left son=2 (176 obs) right son=3 (26 obs)
##
     Primary splits:
##
         InvestFacilitation < 4.5
                                           to the left,
                                                         improve=2.545489, (0 missing)
##
         Security
                                           to the right, improve=2.141005, (0 missing)
                            < 0.5538103
##
                             < 2.785714
                                           to the left, improve=2.069528, (0 missing)
         Corruption
##
                            < 0.2855935
                                                         improve=1.768244, (0 missing)
         EaseOfDoingBus
                                           to the left,
##
     Surrogate splits:
##
         Corruption < 2.642857
                                  to the right, agree=0.881, adj=0.077, (0 split)
##
## Node number 2: 176 observations,
                                        complexity param=0.02890173
                         expected loss=0.8522727 P(node) =0.8712871
##
     predicted class=4
                                                                    25
##
       class counts:
                         7
                               7
                                     12
                                           26
                                                 15
                                                       17
                                                              19
                                                                          22
                                                                                 8
                                                                                             11
                                                                                                    3
##
      probabilities: 0.040 0.040 0.068 0.148 0.085 0.097 0.108 0.142 0.125 0.045 0.023 0.062 0.017
##
     left son=4 (20 obs) right son=5 (156 obs)
##
     Primary splits:
##
         InvestFacilitation < 3.3</pre>
                                           to the left, improve=2.066900, (0 missing)
##
                            < -0.01131459 to the right, improve=1.963858, (0 missing)
         EaseOfDoingBus
##
         Security
                             < 0.5538103
                                           to the right, improve=1.743861, (0 missing)
##
         Corruption
                            < 3.642857
                                           to the left, improve=1.188560, (0 missing)
##
##
  Node number 3: 26 observations,
                                       complexity param=0.01445087
##
     predicted class=12 expected loss=0.7307692 P(node) =0.1287129
##
       class counts:
                         2
                               3
                                      4
                                            3
                                                  0
                                                        3
                                                              1
                                                                     0
                                                                           0
                                                                                 0
                                                                                             7
##
      probabilities: 0.077 0.115 0.154 0.115 0.000 0.115 0.038 0.000 0.000 0.000 0.038 0.269 0.077
##
     left son=6 (9 obs) right son=7 (17 obs)
##
     Primary splits:
##
         EaseOfDoingBus
                            < -0.7376851 to the left, improve=2.233786, (0 missing)
                                                         improve=1.993590, (0 missing)
##
         Corruption
                             < 2.857143
                                           to the left,
                                                         improve=1.776923, (0 missing)
##
         Security
                             < 1.170145
                                           to the left,
                                           to the right, improve=1.082984, (0 missing)
##
         InvestFacilitation < 4.9
##
     Surrogate splits:
##
         Corruption < 3.214286
                                   to the left, agree=0.769, adj=0.333, (0 split)
##
                                  to the left, agree=0.692, adj=0.111, (0 split)
         Security < -1.164044
##
##
  Node number 4: 20 observations,
                                       complexity param=0.01156069
##
     predicted class=4
                         expected loss=0.65 P(node) =0.0990099
##
       class counts:
                               1
                                      1
                                            7
                                                  4
                                                                           1
                                                                                 1
##
      probabilities: 0.050 0.050 0.050 0.350 0.200 0.000 0.100 0.000 0.050 0.050 0.000 0.050 0.050
##
     left son=8 (13 obs) right son=9 (7 obs)
##
     Primary splits:
##
         Corruption
                            < 3.785714
                                           to the left, improve=1.870330, (0 missing)
```

```
##
                             < -0.9054582 to the left, improve=1.755556, (0 missing)
         Security
##
                            < 0.08610139 to the right, improve=1.331313, (0 missing)
         EaseOfDoingBus
         InvestFacilitation < 2.7</pre>
##
                                           to the left, improve=1.133333, (0 missing)
##
     Surrogate splits:
##
         Security
                        < 0.9845555
                                       to the left, agree=0.75, adj=0.286, (0 split)
         EaseOfDoingBus < -0.8286571 to the right, agree=0.70, adj=0.143, (0 split)
##
##
## Node number 5: 156 observations,
                                        complexity param=0.01156069
##
     predicted class=8
                         expected loss=0.8397436 P(node) =0.7722772
##
       class counts:
                         6
                                6
                                     11
                                           19
                                                 11
                                                       17
                                                              17
                                                                    25
                                                                          21
                                                                                             10
##
      probabilities: 0.038 0.038 0.071 0.122 0.071 0.109 0.109 0.160 0.135 0.045 0.026 0.064 0.013
##
     left son=10 (45 obs) right son=11 (111 obs)
##
     Primary splits:
##
         Security
                             < 0.5538103
                                           to the right, improve=2.125757, (0 missing)
##
         EaseOfDoingBus
                                           to the left, improve=1.844490, (0 missing)
                            < 0.2840279
##
         InvestFacilitation < 4.1</pre>
                                           to the left, improve=1.722112, (0 missing)
##
                                           to the left, improve=1.336114, (0 missing)
         Corruption
                             < 3.642857
     Surrogate splits:
##
##
                                       to the right, agree=0.731, adj=0.067, (0 split)
         EaseOfDoingBus < 1.235788
##
         Corruption
                        < 3.071429
                                       to the left, agree=0.724, adj=0.044, (0 split)
##
                                      complexity param=0.01445087
## Node number 6: 9 observations,
##
     predicted class=2
                         expected loss=0.6666667 P(node) =0.04455446
##
       class counts:
                         1
                               3
                                      0
                                            3
                                                  0
                                                        0
                                                              0
                                                                     0
                                                                           0
##
      probabilities: 0.111 0.333 0.000 0.333 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.111 0.111
##
     left son=12 (3 obs) right son=13 (6 obs)
##
     Primary splits:
         EaseOfDoingBus
                            < -0.8043081 to the right, improve=2.666667, (0 missing)
##
##
         Corruption
                                           to the left, improve=1.523810, (0 missing)
                             < 2.857143
                                           to the right, improve=1.366667, (0 missing)
##
         Security
                             < 0.3176438
##
         InvestFacilitation < 4.9
                                           to the right, improve=1.266667, (0 missing)
##
     Surrogate splits:
##
         Security
                    < 0.3176438
                                   to the right, agree=0.778, adj=0.333, (0 split)
##
                                   to the right, agree=0.778, adj=0.333, (0 split)
         Corruption < 3.642857
##
## Node number 7: 17 observations,
                                       complexity param=0.01156069
##
     predicted class=12 expected loss=0.6470588 P(node) =0.08415842
##
                               0
                                                  0
       class counts:
                         1
                                      4
                                            0
                                                        3
                                                              1
                                                                     0
                                                                           0
##
      probabilities: 0.059 0.000 0.235 0.000 0.000 0.176 0.059 0.000 0.000 0.000 0.059 0.353 0.059
##
     left son=14 (13 obs) right son=15 (4 obs)
##
     Primary splits:
##
         Security
                            < 1.112083
                                           to the left, improve=2.7149320, (0 missing)
##
         InvestFacilitation < 4.7</pre>
                                           to the left, improve=1.2320260, (0 missing)
##
         Corruption
                            < 4.071429
                                           to the left, improve=1.1764710, (0 missing)
##
         EaseOfDoingBus
                             < 0.1551669
                                           to the right, improve=0.7193277, (0 missing)
##
     Surrogate splits:
##
         Corruption < 4.071429
                                   to the left, agree=0.882, adj=0.5, (0 split)
##
##
  Node number 8: 13 observations
##
     predicted class=4
                         expected loss=0.4615385 P(node) =0.06435644
##
                                0
                                            7
                                                  2
                                                        0
                                                                     0
                                                                           0
       class counts:
                         1
                                      1
                                                               1
      probabilities: 0.077 0.000 0.077 0.538 0.154 0.000 0.077 0.000 0.000 0.000 0.000 0.077 0.000
##
##
## Node number 9: 7 observations
```

```
##
                      expected loss=0.7142857 P(node) =0.03465347
    predicted class=5
##
      class counts:
                      0 1 0 0
                                           2 0 1 0
                                                                 1
                                                                       1
##
     probabilities: 0.000 0.143 0.000 0.000 0.286 0.000 0.143 0.000 0.143 0.143 0.000 0.000 0.143
##
## Node number 10: 45 observations
    predicted class=4 expected loss=0.7777778 P(node) =0.2227723
##
      class counts: 1 4
##
                                 3 10
                                           7
     probabilities: 0.022 0.089 0.067 0.222 0.156 0.089 0.022 0.178 0.089 0.000 0.000 0.044 0.022
##
##
##
  Node number 11: 111 observations
    predicted class=8 expected loss=0.8468468 P(node) =0.549505
                      5 2 8 9 4 13
##
                                                     16
                                                                       7
      class counts:
                                                         17
                                                                 17
     probabilities: 0.045 0.018 0.072 0.081 0.036 0.117 0.144 0.153 0.153 0.063 0.036 0.072 0.009
##
##
##
  Node number 12: 3 observations
##
    predicted class=4 expected loss=0 P(node) =0.01485149
##
                      0 0
                              0 3 0 0 0
                                                            0
                                                                 Ω
                                                                       Ω
      class counts:
##
     probabilities: 0.000 0.000 0.000 1.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000
##
## Node number 13: 6 observations
    predicted class=2 expected loss=0.5 P(node) =0.02970297
##
##
                    1 3 0 0
                                         0
      class counts:
                                                0 0
##
     probabilities: 0.167 0.500 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.167 0.167
##
## Node number 14: 13 observations
##
    predicted class=3
                      expected loss=0.6923077 P(node) =0.06435644
##
                     1 0 4 0 0 3 1 0
                                                                 0
      class counts:
                                                                            1
     probabilities: 0.077 0.000 0.308 0.000 0.000 0.231 0.077 0.000 0.000 0.000 0.077 0.154 0.077
##
##
## Node number 15: 4 observations
##
    predicted class=12 expected loss=0 P(node) =0.01980198
##
      class counts:
                      0 0 0 0 0 0
                                                      Ω
                                                            0
                                                                 Ω
                                                                       0
##
     probabilities: 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 0.000 1.000 0.000
```