

Week 4

Logistic Regression

- I. Odds
 - a. A way to express likelihood event will take place
 - b. Written as X/Y, X:Y, or X to Y
 - c. Gambling odds called odds against
 - i. Probability event will not happen
 - ii. 10 to 1 odds == bet \$1 and win get \$10 + \$1 (initial bet)
 - iii. Probability an event will not happen > probability that it will happen
 - d. Probability an event will happen > probability that it will not happen
 - e. Also called odds for or odds on
 - f. 2 to 1 odds means event twice as likely to happen than not
 - g. Get back your initial bet + stake of \$2??
- II. Statistical Odds
 - a. Viewed as ratio of probabilities
 - b. Odds used in favor that event will happen over the probability that it will not happen
 - c. If Odds for is 2:1 then:
 - i. Odds(for) = $2/1 = p/(1-p)$ thus, $2(1-p) = p$, $2-2p = p$, $2=3p$, $2/3 = p = 0.6667$ or 66.67%
 - ii. P is probability
 - iii. $P = \text{Odds(for)} / (1 + \text{Odds(for)})$
 - iv. Odds(for) = $p / (1-p)$
 - v. $P = 12.5\%$ or 0.125 so odds for is $.125 / (1-.125) = 1/7$

Logistic Regression

- I. Linear regression can produce models with predicted values below 0 and above 1 making it unsuitable for binary responses
- II. Use logistic regression to predict binary responses
- III. Y is categorical (Yes/No), (Approve/Reject), (Pass/Fail) etc
- IV. Result expressed as probability of being in a group
 - a. Implying predicted value always between 0 and 1
- V.