

EE2802: Assignment5

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1 PROBLEM

For the vectors $\mathbf{a} = \begin{pmatrix} 2 \\ -1 \\ 2 \end{pmatrix}$ and $\mathbf{b} = \begin{pmatrix} -1 \\ 1 \\ -1 \end{pmatrix}$, find the unit vector along the direction of $\mathbf{a} + \mathbf{b}$.

2 SOLUTION

$$\mathbf{a} = \begin{pmatrix} 2 \\ -1 \\ 2 \end{pmatrix} \quad \mathbf{b} = \begin{pmatrix} -1 \\ 1 \\ -1 \end{pmatrix}$$

$$\begin{aligned} \mathbf{a} + \mathbf{b} = \mathbf{u} &= \begin{pmatrix} 2 \\ -1 \\ 2 \end{pmatrix} + \begin{pmatrix} -1 \\ 1 \\ -1 \end{pmatrix} \\ &= \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \end{aligned}$$

Unit vector in direction of \mathbf{u} ,

$$\begin{aligned} \hat{u} &= \frac{\mathbf{u}}{\|\mathbf{u}\|} \\ &= \frac{1}{\sqrt{2}} \mathbf{u} \\ &= \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} \\ \hat{u} &= \begin{pmatrix} \frac{1}{\sqrt{2}} \\ 0 \\ \frac{1}{\sqrt{2}} \end{pmatrix} \end{aligned}$$