Question: 12.10.5.11

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Nikam Pratik Balasaheb (EE21BTECH11037)

1 Problem

Show that direction cosines of a vector equally

inclined to axes **OX**, **OY** and **OZ** are
$$\pm \begin{pmatrix} \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \end{pmatrix}$$

2 Solution

The vector is equally inclined to the axes **OX**, **OY** and **OZ**. Let the angle be θ .

Direction cosines,

$$\mathbf{m} = \begin{pmatrix} \cos \theta_1 \\ \cos \theta_2 \\ \cos \theta_3 \end{pmatrix} = \begin{pmatrix} \cos \theta \\ \cos \theta \\ \cos \theta \end{pmatrix}$$
 (2.0.1)

we know that

$$||\mathbf{m}|| = 1 \tag{2.0.2}$$

$$\left|\sqrt{3}\cos\theta\right| = 1\tag{2.0.3}$$

$$\cos \theta = \pm \frac{1}{\sqrt{3}} \tag{2.0.4}$$

$$\left| \sqrt{3} \cos \theta \right| = 1 \qquad (2.0.3)$$

$$\cos \theta = \pm \frac{1}{\sqrt{3}} \qquad (2.0.4)$$

$$\mathbf{m} = \pm \begin{pmatrix} \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \end{pmatrix} \qquad (2.0.5)$$

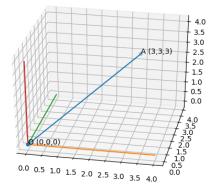


Fig. 0: vector OA, that makes equal angles with axes