

Time Complexity

##Worst case consider korte hbe.....

Write the time complexity of each of the code segments shown below.

```
1. int k=1;
   while(k<=n){
       cout<<k<<endl;
       k=k*2;
   }
```

Answer:

Time Complexity: $O(n)$

Space Complexity: $O(1)$

```
2. for (int i = 0; i < n; i++)
    for (int j = i; j > 0; j--)
        cout << i << j;
```

Answer:

Time Complexity: $O(n^2)$

Space Complexity: $O(1)$

$i=0, j=0, \dots \rightarrow 0$

$i=1, j=1; \dots \rightarrow 1$

$i=2, j=2; \dots \rightarrow 2$

.....

$i=n, j=n; \dots \rightarrow n*n \rightarrow n^2$

```

3.  for (int i = 0; i < n; i++)
      for (int j = i; j > 0; j--)
          for(int k=j; k > 0; k--)
              cout << i << j << k;

```

Answer:

Time Complexity: $O(n^3)$

Space Complexity: $O(1)$

$i=0, j=0, k=0 \rightarrow 0$

$i=1, j=1; k=1 \rightarrow 1$

$i=2, j=2; k=2 \rightarrow 2$

.....

$i=n, j=n; k=n \rightarrow n*n*n \rightarrow n^3$

```

4.  for(int i=n/2;i<=n;i++){
        for(int j=1;j<=n;j=j*2){
            cout<<i<<j<<endl;
        }
    }

```

Answer:

Time Complexity: $O((n/2) * \log n) = O(n \log n)$

Space Complexity: $O(1)$

$i=5, j=1, \rightarrow 6$

$i=6, j=1; \rightarrow 6$

$i=7, j=1; \rightarrow 6$

n ber er jnne vitor er loop ta logn ber
Ghurbe..... jmn... 8 er jnne vitor er loop
ta 3 ber ghurbe... $8 = \log_2^3 = 3$

```

5. for(int i=n/2;i<=n;i++){-----n/2
    for(int j=1;j<=n;j=j+i){-----n
        cout<<i<<j<<endl;
    }
}

```

Answer:

Time Complexity: $O\left(\frac{n}{2} * n\right) = O(n^2)$

Space Complexity: $O(1)$

$i=5, j=1, \rightarrow 1$

$i=6, j=1; \rightarrow 1$

$i=7, j=1; \rightarrow 1$

```

6. for(int i=1;i<=n;i++)
{
    if(builtin_popcount(i) == 1)
    {
        for(int j=1;j<=n;j++)
            cout<<i<<j<<endl;
    }
}

```

Answer:

Time Complexity: $O(n^2)$

Space Complexity: $O(1)$

$i=1, j=1, \rightarrow n \rightarrow n^2$

$i=2, j=1; \rightarrow n \rightarrow n^2$

$i=3, j=1; \rightarrow 0 \rightarrow n$

$i=4, j=1; \rightarrow n \rightarrow n^2$

$i=5, j=1; \rightarrow 0 \rightarrow n$