### String processing

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30 januari 2016

Ad hoc

Tries

String matching

Naive

Rabin-Karp

Z-algorithm

Knuth-Morris-Pratt

### Ad hoc

- Straightforward solution
- See CP3, section 6.3 (pages 236 240)
- ightharpoonup If you know regular expressions, C++ 11 has those as well

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### Trie Properties

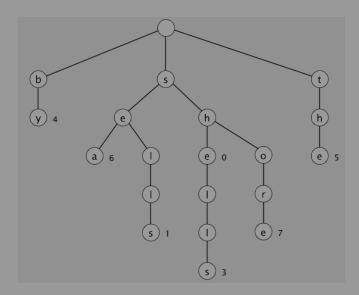
- <Retrieval (but can be pronounce as either tree or try)</p>
- Store a set of words (with or without associated values)
- $\triangleright$  insert/retrieve in O(S), with S the length of the string
- Allows for non-exact matches (<> set/map)

### Trie Structure

- Tree structure
- Stores the *path* for the string instead of the string
- Edges labeled with single characters
- ► If the last character of a stored word, marked (+ associated value)
- Can vary in type of character (bits/ints/...)
- ► Can be compressed by eliminating successive single-edge nodes

#### Trie

### Structure



Trie Usage

- Spelling suggestions
- Autocompletion
- Bioinformatics (DNA/RNA)
- Alphabetical ordering / sorting
- (Similar to structure for Aho-Corasick)
- ► (Basis for *suffix tree*)

# Trie Code

```
#include <map>
using namespace std;

struct Trie
{
    //Can be map/unordered_map/direct adressing table/implicit edge/...
    map<char, Trie*> children;
    bool marked;
};
```

# Trie Code

```
void insert(Trie* t, string s)
{
  for (int index = 0; index < s.length(); index++)
    {
      if (t->children.find(s[index]) == t->children.end())
        {
            t->children[s[index]] = new Trie();
      }
      t = t->children[s[index]];
   }
} t = t->marked = true;
}
```

# Trie Code

```
bool contains(Trie* t, string s)
{
    for (auto c : s)
    {
        if (t->children.find(c) == t->children.end())
            return false;
        t = t->children[c];
    }
    return t->marked;
}
```

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 $Z\hbox{-} algorithm$ 

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# Naive matching principle

- Straightforward
- Check for match at each index
- Usually, use the one in the standard library, don't write your own
- $\triangleright O(s * p)$  (s = length of string, p = length of pattern)

### Naive matching

#### Code

```
#include <string>
using namespace std;
int match (string s, string pat)
    if (s.length() < pat.length())</pre>
    for (int i = 0; i \le s.length() - pat.length(); i++)
        bool found = true;
        for (int j = 0; j < pat.length(); j++)
             if (s[i+j] != pat[j])
                 found = false:
                 break;
        if (found) return i;
    return -1;
```

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Idea

 $\triangleright$  Checking for a match with the pattern: O(n)

- Faster possible?
- $\triangleright$  What about hashes, integer comparison = O(n)
- $\triangleright$  We still need a O(1) way to generate the hashes.
- Useful for multiple same-length patterns (check all hashes)

Polynomial hashing

- Generate successive hashes of the same length as the pattern (and hash the pattern)
- Polynomial hashing: the string is an integer in some base B
   (usually prime)
- $\triangleright s_i, s_{i+1}, \dots, s_{i+k-1} = s_i \times B^{k-1} + s_{i+1} \times B^{k-2} + \dots + s_{i+k-1} \times B^0$
- ► Too big  $\Rightarrow$  modulo H (usually prime)
- Watch out for false positives

Rolling hashes

- Once we have a hash, it's easy to compute the next
- $\succ s_{i+1}, s_{i+2}, \ldots, s_{i+k} = ((s_i, \ldots, s_{i+k-1}) s_i \times B^{k-1}) \times B) + s_{i+k}$
- ▶ A rolling hash frame
- ► O(1)

Collision strategies

- ▶ If equal hashes ⇒ compare the strings explicitely
- $\triangleright$  Worst case, still  $O(n^2)$
- ightharpoonup Gambling: keep 2 hashes (with distinct B and H)
- Collision chance is low, if the two hashes match, guess it's correct
- ⇒ triple hashing, . . .

```
const int B = 17;
const int H = 12632251;
int hash_pattern(string pat, int start, int end)
{
    int h = 0;
    for (int i = start; i <= end; i++)
    {
        h = ((h * B) % H + pat[i]) % H;
    }
    return h;
}</pre>
```

```
bool check(string s, string pat, int start)
{
    for (int i = 0; i < pat.length(); i++)
    {
        if (s[start + i] != pat[i])
            return false;
    }
    return true;
}
int modpow(int exp) { //This can be done in O(log N)
    int result = 1;
    for (int i = 0; i < exp; i++)
    {
        result = (result * B) % H;
    }
    return result;
}</pre>
```

```
int match(string s, string pat)
{
    if (pat.length() > s.length()) return -1;
    int k = pat.length();
    int Hp = hash.pattern(pat, 0, k - 1);
    int Hs = hash.pattern(s, 0, k - 1);
    int Hs = modpow(k-1);
    for (int i = 0; i <= s.length() - k; i++)
    {
        if (Hs == Hp && check(s, pat, i))
        {
            return i;
        }
        Hs = ((B * (Hs - (s[i] * Bk) % H)) % H + s[i+k]) % H;
        if (Hs < 0) Hs += H;
    }
    return -1;
}</pre>
```

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### String matching

Naive

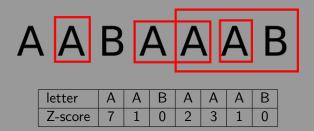
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terminology

- Z-box = substring that matches with a prefix from the string
- $\triangleright$  Z-score  $Z_i(S)$  = length of Z-box starting at index i



## Z-algorithm

Matching

- $\triangleright P = pattern$
- $\triangleright$  S = search string
- \$ = sentinel (not part of alphabet)
- return *i* for each i > 0 where  $Z_i(P$S) = |P|$

#### Calculating Z-scores

- Naive  $\Rightarrow O(n^2)$ , possible in O(n)
- ► Keep track of the Z-box with right end furthest to the right (bounds: [I, r])
- $\vdash$  if current character in [I, r]: look at corresponding character in prefix (computed previously)
- $\triangleright$  expand if grows beyond r, update [l, r]
- $\triangleright$  else: calculate explicitely, update [I, r]
- Nicely illustrated: https://www.cs.umd.edu/class/fall2011/cmsc858s/Lec02zalg.pdf)

```
int match(string s, string pat)
    string S = pat + "\$" + s;
    vector < int > Z(S.length());
    int l = -1, r = -1;
   for (int i = 1; i < S.length(); i++)
        if (i > r) //Outside furthest Z-box
            int len = 0:
            for (int j = i; j < S.length() && S[j] == S[j-i]; j++)
                len++;
            Z[i] = len;
            if (len > 0)
                I = i:
                r = i + len - 1;
```

```
else
        int inside = r - i + 1:
        int corresponding = i - I;
        if (Z[corresponding] < inside)</pre>
            Z[i] = Z[corresponding];
        else //Need to grow beyond r
            int len = 0;
            for (int j = r + 1; j < S.length() && S[j] == S[j - i]; j++)
                len++;
            Z[i] = inside + len;
            I = i;
            r = i + len - 1;
for (int i = 1; i < S.length(); i++)
    if (Z[i] == pat.length())
        return i - pat.length() - 1; //Don't forget to subtract the sentinel
return -1;
```

Ad hoo

Tries

### String matching

Rabin-Karp

Z-algorithm

Knuth-Morris-Pratt

- Don't inspect substring starting at each index
- ▶ Fail smart
- ▶ Jump ahead to the next possible index, given what we've seen so far
- Precompute the failure jumps

- ▶ How to choose the jump?
- Next possible partially matched pattern = longest proper suffix (of the partial match) that is a prefix
- Precompute and keep the length of this suffix/prefix in an array (call this L)
- $\triangleright$  L[i] = length of that prefix for S[0..i-1] (inclusive)

Precomputation

- $\succ L[0] = L[1] = 0$  (it should be a *proper* suffix)
- ► Search for the next *parent* in *L* that can be expanded with the current character
- $\triangleright$  L[i] = j + 1 (j is the length of the parent's match)
- ▶ If none can be found: L[i] = 0

# Knuth-Morris-Pratt Matching

- $\triangleright$  Precompute the failure jumps (L) of the pattern
- ► Skip characters using *L* while matching
- Very similar to the actual precomputation
- $\triangleright$  O(S+P)

```
vector<int> precompute(string pat)
    vector < int > L(pat.length() + 1);
   L[0] = L[1] = 0;
    for (int i = 2; i \le pat.length(); i++)
        for (int j = L[i-1]; ; j = L[j])
            if (pat[j] == pat[i - 1])
            }
if (j == 0)
                L[i] = 0;
   return L;
```

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### Exercises

Ad hoc

- UVa 10115 (Automatic Editing)
- ► UVa 10361 (Automatic Poetry)
- ► UVa 10082 (WERTYU)
- ► UVa 1368 (DNA Consensus String)

### Exercises

Tries

- ▶ UVa 902 (Password Search)
- ► UVa 755 (487–3279)
- Codechef Remember the recipe (https://www.codechef.com/problems/TWSTR/)

# Exercises String matching

- ▶ UVa 363 (Approximate matches)
- ▶ UVa 455 (Periodic strings)
- ▶ UVa 1223 (Editor)
- Codeforces 126, problem B (http://codeforces.com/contest/126/problem/B)
- ► UVa 11151 (Longest Palindrome)
- ▶ UVa 11475 (Extend to Palindrome)