

ASSIGNMENT 5

2. Write an algorithm for Successive-Over-Relaxation (SOR) method.

1. Input matrix $A = [a_{ij}]$, b , x_0 , ω , tolerance TOL , max no. of iterations

2. set $k = 1$

3. while $(k \leq N)$ do step 4-8

4. For $i = 1, 2, \dots, n$

$$x_i = \frac{1}{a_{ii}} \left[\sum_{j=1}^{i-1} (a_{ij} x_j) - \sum_{j=i+1}^n (a_{ij} x_{0j}) + b_i \right]$$

5. $x_i = (1 - \omega) * x_{0i} + \omega * x_i$;

6. If $\text{norm}(x_i - x_0, \text{inf}) < \text{tol}$
break

7. $k = k + 1$

8. For $i = 1, 2, \dots, n$
Set $x_{0i} = x_i$

9. OUTPUT (x_1, x_2, \dots, x_n)
STOP

3. Solve this system of equations by Gauss-Seidel starting with the initial vector $[0; 0; 0]$ and tolerance

10⁻³:

$$4.63x_1 - 1.21x_2 + 3.22x_3 = 2.22$$

$$-3.07x_1 + 5.48x_2 + 2.11x_3 = -3.17$$

$$1.26x_1 + 3.11x_2 + 4.57x_3 = 5.11$$

Sol.

```

clc;
clear all;
a=[4.63 -1.21 3.22; -3.07 5.48 2.11; 1.26 3.11 4.57];
b=[2.22; -3.17; 5.11];
tol = 0.001; N = 1000;
k=1;
[n,~]=size(a);
x0=zeros(n,1);
xi=zeros(n,1);
while k<=N
    for i=1:n
        x0(i,1)=xi(i,1);
        xi(i,1) = (b(i,1)-(a(i,1:i-1)*xi(1:i-1)+a(i,i+1:n)*x0(i+1:n)))/a(i,i);
        if norm(xi-x0,inf)<tol
            break;
        end
    end
    k=k+1;
end
xi
a\b

```

```

xi =

    -8.9807
    -9.4752
    10.0421

```

```

ans =

    -8.9893
    -9.4845
    10.0510

```

4. Use the SOR method with $\omega = 1.2$ to solve the linear system with an initial vector $[0; 0; 0; 0]$ a tolerance

10^{-3} in the k_1 norm.

$$4x_1 + x_2 + x_3 + x_4 = 2$$

$$x_1 + 4x_2 + x_3 + x_4 = 1$$

$$x_1 + x_2 + 5x_3 + x_4 = 0$$

$$x_1 + x_2 + x_3 + 3x_4 = 1$$

Sol.

```
clc;
clear all;
a=[4 1 -1 1; 1 4 -1 -1; -1 -1 5 1; 1 -1 1 3];
b=[-2; -1; 0; 1];
tol = 0.001; N = 1000; w = 1.2;
k=1;
[n,~]=size(a);
x0=zeros(n,1);
xi=zeros(n,1);
while k<=N
    for i=1:n
        x0(i,1)=xi(i,1);
        xi(i,1) = (b(i,1)-(a(i,1:i-1)*xi(1:i-1)+a(i,i+1:n)*x0(i+1:n)))/a(i,i);
        xi(i,1)=(1-w)*x0(i,1)+w*xi(i,1);
        if norm(xi-x0,inf)<tol
            break;
        end
    end
    k=k+1;
end
xi
a\b
```

xi =

```
-0.7537
 0.0408
-0.2806
 0.6913
```

ans =

```
-0.7534
 0.0411
-0.2808
 0.6918
```

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