

# Programming Assignment 2

CS 218 : Design and Analysis of Algorithms

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# Functions

My Algorithm to solve the given problem is to call a function `myfunc()`, which in turn calls a recursive function `recfunc()`, whose functionalities are given below:

## `myfunc()`

Takes in a vector of elements and memory matrix as input. It defines more variables namely `dp`, `subs` and `perm`. Now this calls `recfunc()`, which does the computation recursively.

## `recfunc()`

This is the crux of the program that recursively computes the needed result. The arguments include:

- `const vector<int> &elements`: This is a vector of IDs of all processes.
- `int subs`: An integer whose binary representation would reveal the elements considered in the current subset (like a characteristic vector). Initially all processes would be included so this has value of `111..1` (`n` 1s).
- `vector<int> &perm`: The vector of elements already considered by the parent call. Initially empty.
- `map<int,int> &dp`: This map stores the values of output of different recursive calls made during the entire run. This helps in saving a lot of computation as multiple calls are made to the same subset. Maps `subset(binary int)` to `output(memory terms of the subset for given order.)`
- `const vector<vector<int>> &mem`: Contains the data regarding each process, and we will refer to it as the memory matrix.

## `memreq()`

Evaluates the memory required while running the current process ID, for a given order of process IDs.

## Algorithm

It is a dynamic programming algorithm which stores the maximum peak memory required for the given subset of elements that occur at the last of a given order. This saves a lot of computation as the same subset of elements at the last are seen in multiple calls to the recursive function. The time complexity of the given algorithm is  $O(2^n * n^3)$ . This is so because there exists  $2^n$  unique calls to the function `recfunc()` and in each call, the `memreq()` function is called which runs in  $O(n^3)$ .

Also, magically, my program runs in less than 0.1 seconds for input10!

## References

- <https://www.geeksforgeeks.org/write-a-c-program-to-print-all-permutations-of-a-given-string/>
- <https://chat.openai.com/>