

Work

May 13, 2020

```
[1]: import pywt
import numpy as np
import pandas as pd
import statsmodels.api as sm
import matplotlib.pyplot as plt

import warnings
warnings.filterwarnings('ignore')

np.random.seed(0)
```

```
[2]: X_range = np.arange(1000)

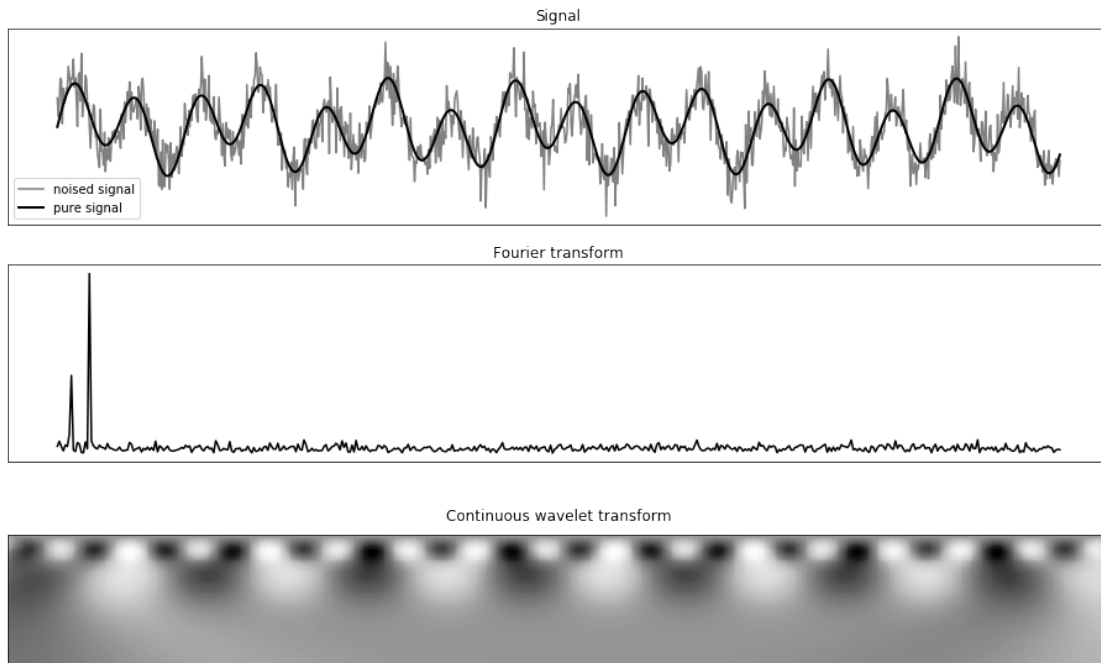
def describe(signal):
    plt.figure(figsize=(16, 10))
    signal_with_noise = signal + np.random.normal(0, 1, len(signal))

    plt.subplot(3, 1, 1)
    plt.plot(signal_with_noise, 'gray', label='noised signal')
    plt.plot(signal, 'black', label='pure signal', linewidth=2)
    plt.xticks((), plt.yticks(())
    plt.title('Signal')
    plt.legend()

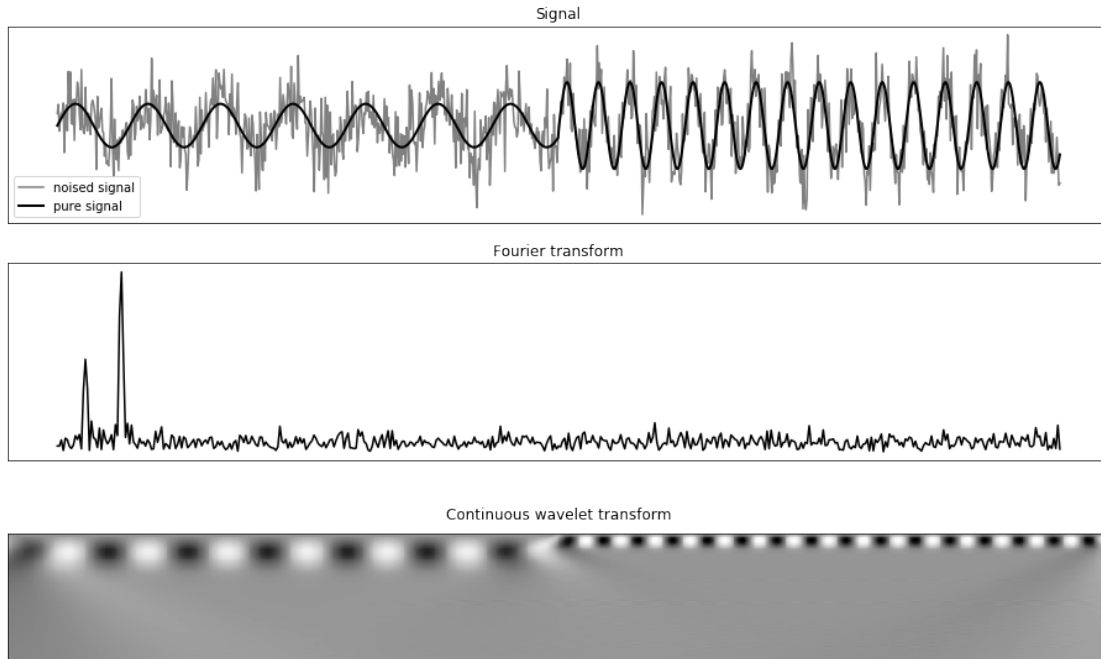
    plt.subplot(3, 1, 2)
    plt.plot(np.abs(np.fft.rfft(signal_with_noise)), 'black')
    plt.title('Fourier transform')
    plt.xticks((), plt.yticks(())

    ax = plt.subplot(3, 1, 3)
    coef, freqs=pywt.cwt(signal, np.arange(1, 120), 'mexh')
    ax.matshow(coef, cmap='Greys')
    plt.title('Discontinuous wavelet transform')
    plt.xticks((), plt.yticks(())
    plt.show()
```

```
[3]: describe(np.sin(X_range / 23) + 2 * np.sin(X_range / 10))
```



```
[4]: describe(np.append(np.sin(X_range[:,2] / 23), 2 * np.sin(X_range[:,2] / 10)))
```



```
[5]: from scipy import integrate

class wavelet_series:
    def __init__(self, g, levels=8):
        self.levels = levels
        mother_wavelet = lambda x: 0 if x < 0 else 1 if x < 0.5 else -1 if x < 1
        else 0

        self.scaling = lambda x: 1 if 0 <= x < 1 else 0

        self.basis = [[
            (lambda i, j: lambda x: 2 ** (i / 2) * mother_wavelet(2**i * x -
            j))(i, j)
            for j in range(2 ** i)] for i in range(levels)]

        self.coef = [[
            integrate.quad(lambda x: g(x) * self.basis[i][j](x), 0, 1)[0]
            for j in range(2 ** i)] for i in range(levels)]

        self.scaling_coef = integrate.quad(
            lambda x: g(x) * self.scaling(x), 0, 1)[0]

    def __call__(self, point):
        value = 0
        for i in range(self.levels):
            for j in range(2 ** i):
                value += self.coef[i][j] * self.basis[i][j](point)
        return value + self.scaling_coef * self.scaling(point)
```

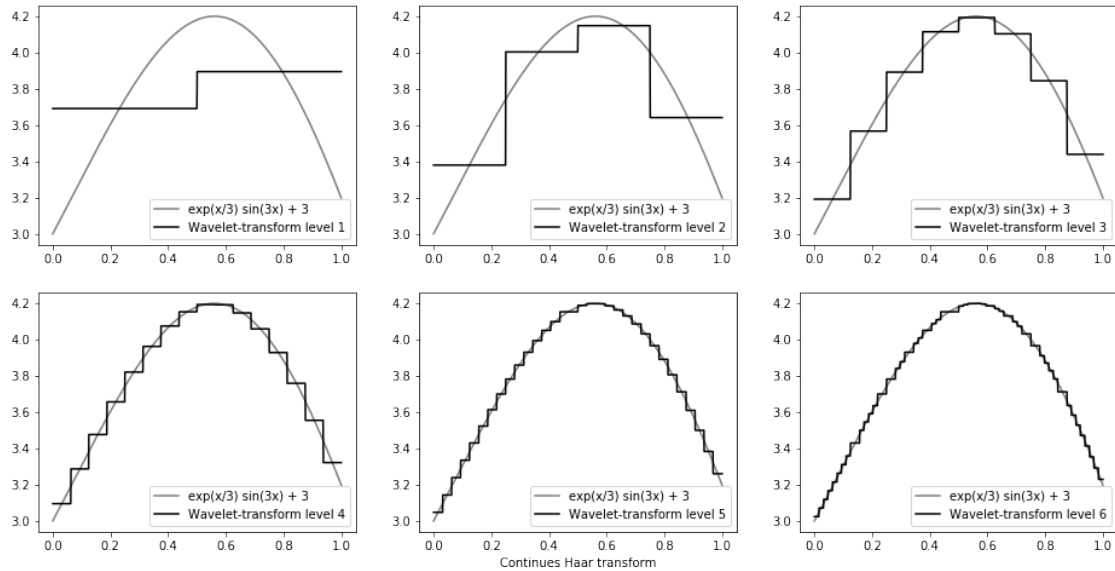
```
[6]: g = lambda x: np.exp(x / 3) * np.sin(3 * x) + 3
xs = np.linspace(1e-8, 1 - 1e-8, 1000)

plt.figure(figsize=(16, 8))

for i in range(1, 7):
    f = wavelet_series(g, i)
    plt.subplot(2, 3, i)
    plt.plot(xs, list(map(g, xs)), 'grey', label='exp(x/3) sin(3x) + 3')
    plt.plot(xs, list(map(f, xs)), 'black', label='Wavelet-transform level %d' %
    i)
    plt.legend()

    if i == 5:
        plt.xlabel('Continues Haar transform')

plt.show()
```



```
[7]: def decomposition(signal, wavelet='Haar'):
    wavelet = pywt.Wavelet(wavelet)
    signal_with_noise = signal + np.random.normal(0, 0.2, len(signal))

    plt.figure(figsize=(16, 8))
    plt.subplot(2, 2, 1)
    plt.plot(signal, 'black', label='pure signal')
    plt.plot(signal_with_noise, 'gray', label='noised signal', linewidth=0.5)
    plt.legend()

    coefs = pywt.wavedec(signal_with_noise, wavelet, level=8)

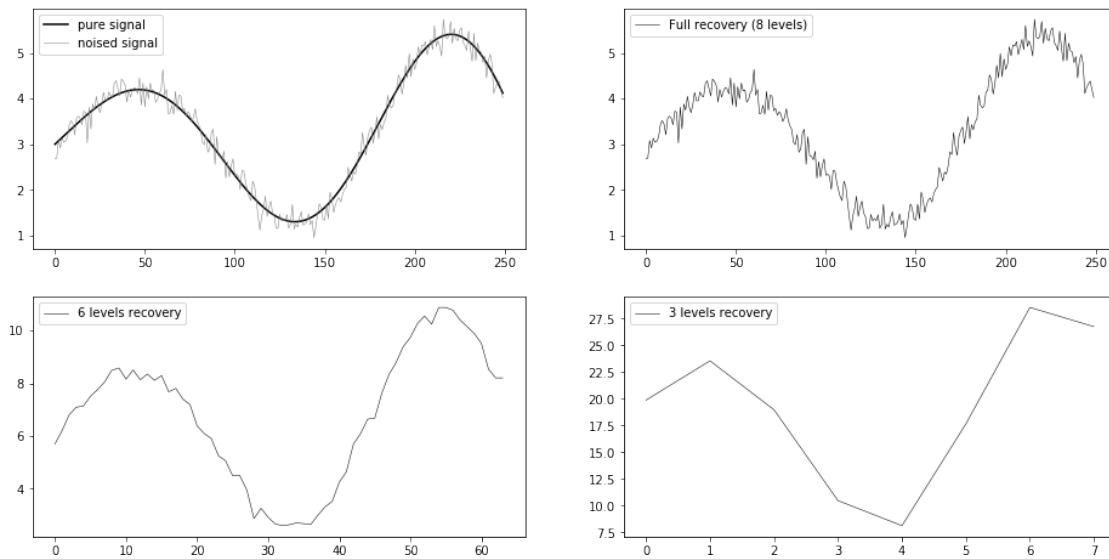
    plt.subplot(2, 2, 2)
    plt.plot(pywt.waverec(coefs, wavelet), 'black', label='Full recovery (8
    ↪levels)', linewidth=0.5)
    plt.legend()

    plt.subplot(2, 2, 3)
    plt.plot(pywt.waverec(coefs[:-2], wavelet), 'black', label='6 levels
    ↪recovery', linewidth=0.5)
    plt.legend()

    plt.subplot(2, 2, 4)
    plt.plot(pywt.waverec(coefs[:-5], wavelet), 'black', label='3 levels
    ↪recovery', linewidth=0.5)
    plt.legend()

    plt.show()
```

```
[8]: decomposition(g(np.linspace(0, 3, 250)))
```



```
[9]: def ShowSeries(series):
    test = sm.tsa.adfuller(series)

    plt.figure(figsize=(16, 3))
    plt.plot(series, 'Grey', linewidth=0.5)
    plt.xticks(())
    plt.yticks(())
    if test[0] > test[4]['5%']:
        plt.title('Non-stationary series by Dickey-Fuller test')
    else:
        plt.title('Stationary series by Dickey-Fuller test')

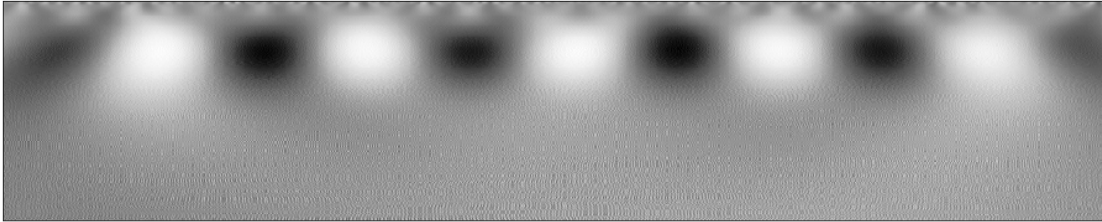
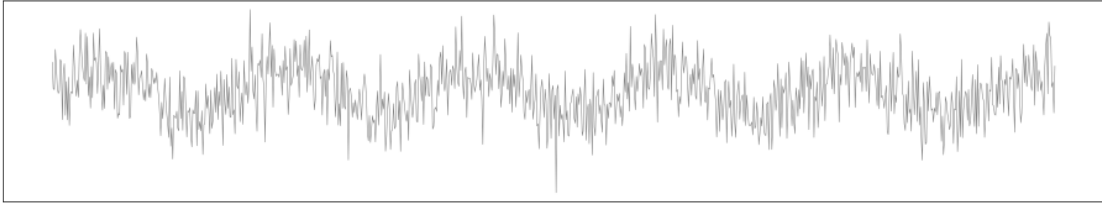
    coef, freqs = pywt.cwt(series, np.arange(1, 200), 'morl')
    plt.matshow(coef, cmap='Greys')
    plt.xticks(())
    plt.yticks(())
    plt.show()

    print('adf: ', test[0])
    print('p-value: ', test[1])
    print('Critical values: ', test[4])
```

```
[10]: noise = np.random.normal(0, 1, 1000)
x_range = np.arange(1000)

ShowSeries(np.sin(x_range / 30) + noise)
```

Stationary series by Dickey-Fuller test



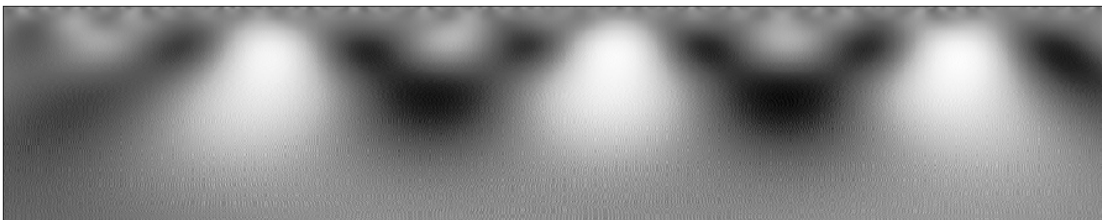
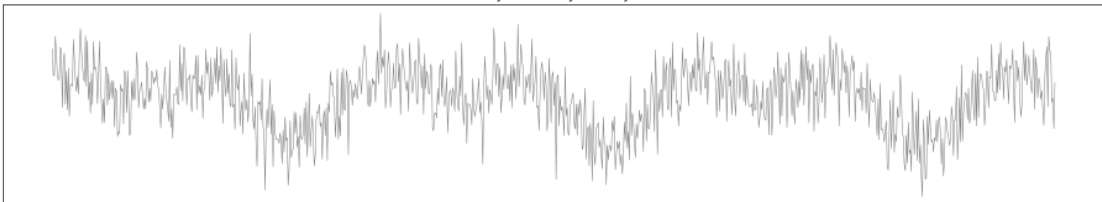
adf: -3.481848853184378

p-value: 0.008465675598229853

Critical values: {'1%': -3.4369860032923145, '5%': -2.8644697838498376, '10%': -2.5683299626694422}

```
[11]: ShowSeries(np.sin(x_range / 50) + np.sin(x_range / 25 - 5) + noise)
```

Non-stationary series by Dickey-Fuller test

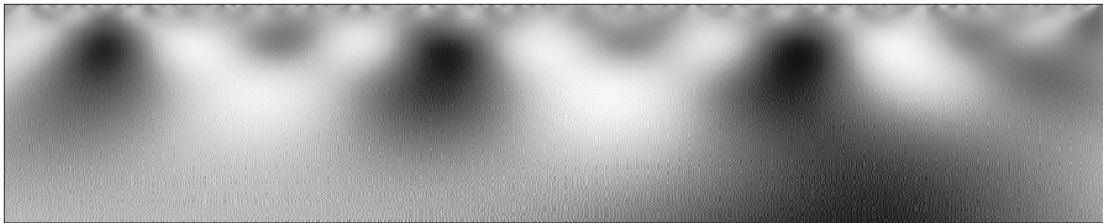
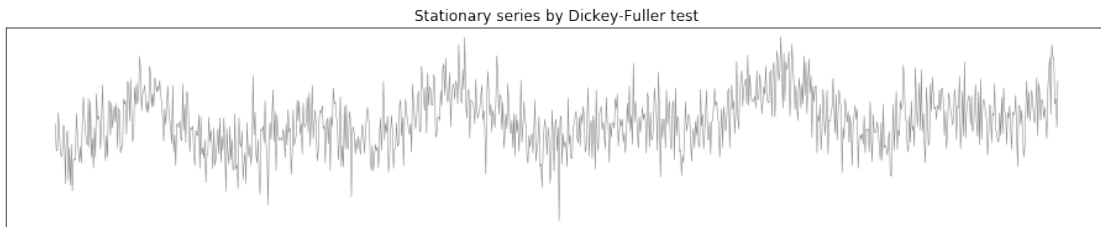


adf: -2.903023162949968

p-value: 0.0449975725101061

Critical values: {'1%': -3.4369860032923145, '5%': -2.8644697838498376, '10%': -2.5683299626694422}

```
[12]: ShowSeries(np.sin(x_range / 50) + np.sin(x_range / 25 - 2) + + x_range / 500 +  
→noise * 1.3)
```

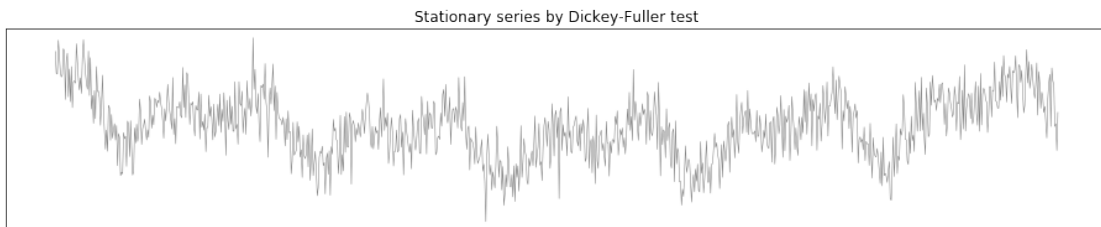


adf: -3.276199205944301

p-value: 0.015976475379125093

Critical values: {'1%': -3.4369860032923145, '5%': -2.8644697838498376, '10%': -2.5683299626694422}

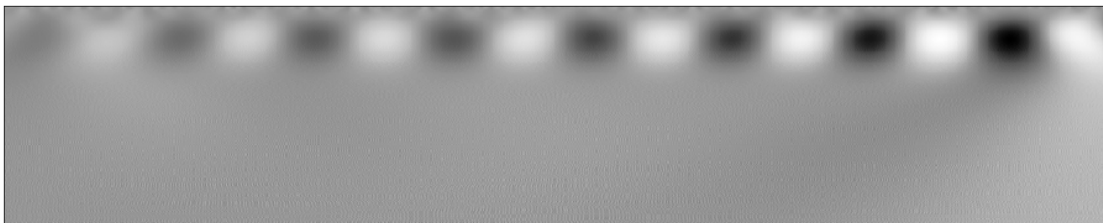
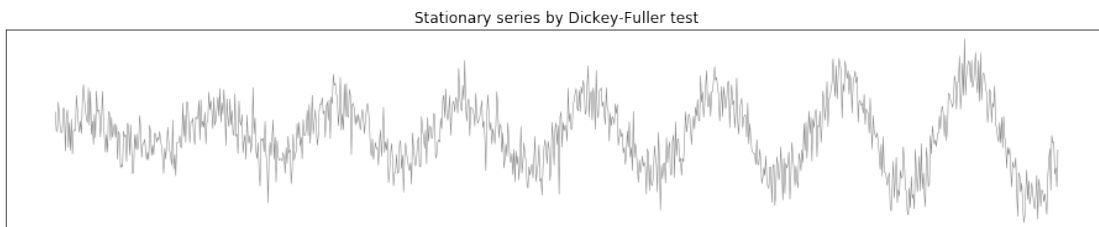
```
[13]: ShowSeries(np.sin(x_range / 30 + 2) + np.sin(x_range / 15) + ((x_range -  
→len(x_range) / 2) / 400)**2 + noise)
```





```
adf: -3.5973135357984862
p-value: 0.005812595366803051
Critical values: {'1%': -3.4369658620871286, '5%': -2.8644609013346485, '10%': -2.56832523159495}
```

```
[14]: ShowSeries((np.sin(x_range / 20)) * (x_range + len(x_range))**2 + noise * 1e6)
```



```
adf: -5.770885118947002
p-value: 5.39587787602044e-07
Critical values: {'1%': -3.4370471695043037, '5%': -2.8644967585264784, '10%': -2.5683443301882956}
```

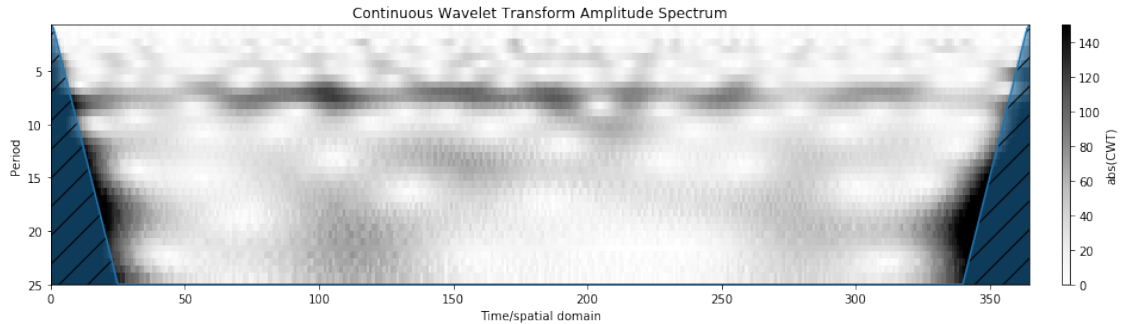
```
[15]: df = pd.read_csv('nss15.csv')

time = pd.to_datetime(df.treatmentDate, format='%m/%d/%Y')
timeseries = pd.Series(np.ones(len(time)), index=sorted(time), dtype=np.int64).
    →resample('D').sum()
```



```
[16]: from scaleogram import cws
```

```
cws(timeseries, cmap='Greys', clim=[0, 150], figsize=(16, 4))
plt.show()
```



```
[17]: timeseries.index = pd.Series(timeseries.index).apply(lambda day: day.weekday())
```

```
[18]: dayweeks = ['DŠD;D;DtDtDtDzNND;DyDž', 'DšNCD;NAD;DyDž', 'NANADtDtNČ',
    → 'NČDtNCDsDtNADs', 'DšNRNCD;DyNENČ', 'NANCDsDsD;NČNČ', 'DšD;NADzNADtNADtD;NNDt']

for i in range(7):
    print('DŠ { :12s}: {} NADzNČNČDřDtDš'.format(dayweeks[i], timeseries[i].
    → sum()))
```

```
DŠ DŠD;D;DtDtDtDzNND;DyDž : 49868 NADzNČNČDřDtDš
DŠ DšNCD;NAD;DyDž : 46629 NADzNČNČDřDtDš
DŠ NANADtDtNČ : 46727 NADzNČNČDřDtDš
DŠ NČDtNCDsDtNADs : 46798 NADzNČNČDřDtDš
DŠ DšNRNCD;DyNENČ : 45269 NADzNČNČDřDtDš
DŠ NANCDsDsD;NČNČ : 49408 NADzNČNČDřDtDš
DŠ DšD;NADzNADtNADtD;NNDt : 50140 NADzNČNČDřDtDš
```

```
[19]: plt.figure(figsize=(16, 16))
```

```
for i in range(6):
    ax = plt.subplot(3, 2, i + 1)
    cws(timeseries[i], cmap='Greys', ax=ax, clim=[0, 60], title='DřD;D;NNDt
    → NČNADřDsD;DřNČDyDŮD;Dř Dš %s' % dayweeks[i])
plt.show()

plt.figure(figsize=(16, 4))
ax = plt.subplot(1, 1, 1)
cws(timeseries[6], cmap='Greys', ax=ax, clim=[0, 60], title='DřD;D;NNDt
    → NČNADřDsD;DřNČDyDŮD;Dř Dš %s' % dayweeks[i])
plt.show()
```

